

Supplementary Information

Pyrochlore-type oxide solid solutions $(\text{Bi}_{1-x}\text{Ga}_x)_{2-d}\text{Ti}_2\text{O}_{7-3d/2}$

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Table S1 Compositions of the starting mixtures, heating times, compounds prepared at 1100 °C, and cubic cell parameters, a , for the pyrochlore phases.

Table S2 Results of EPMA of a $(\text{Bi}_{1.62}\text{Ga}_{0.14}\text{Ti}_2\text{O}_{6.64})$ single crystal prepared by slow cooling from 1250 °C.

Table S3 Anisotropic displacement parameters (Å^2) for $\text{Bi}_{1.62}\text{Ga}_{0.14}\text{Ti}_2\text{O}_{6.64}$.

Fig. S1 TG-DTA curves generated by $(\text{Bi}_{1-x}\text{Ga}_x)_{2-d}\text{Ti}_2\text{O}_{7-3d/2}$ ($x = 0.09$, $d = 0.08$, sample 35) on heating (red) and on cooling (blue).

Fig. S2 Temperature dependence of the dielectric constant ϵ_r , and loss $\tan\delta$ values determined for $(\text{Bi}_{1-x}\text{Ga}_x)_{2-d}\text{Ti}_2\text{O}_{7-3d/2}$ (sample 29 ($x = 0.06$, $d = 0.15$)) at 1 MHz.

Table S1 Composition of the starting mixture, heating time, compounds prepared at 1100 °C, and a cubic cell parameter a of a pyrochlore phase.

Sample	Composition (mol%)			Heating time (h)	Compounds	pyrochlore-phase a (Å)
	BiO _{1.5}	GaO _{1.5}	TiO ₂			
1	15.0	5.0	80.0	48 + 48	TiO ₂ , (Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , BiGaTi ₄ O ₁₁	
2	5.0	15.0	80.0	48 + 48	Ga ₂ O ₃ , TiO ₂ , BiGaTi ₄ O ₁₁	
3	17.2	10.3	72.4	48 + 48	TiO ₂ , (Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , BiGaTi ₄ O ₁₁	
4	33.3	0.0	66.7	12 + 12	Bi ₂ Ti ₄ O ₁₁	
5	30.0	3.3	66.7	12 + 12	TiO ₂ , (Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , Bi ₂ Ti ₄ O ₁₁	
6	16.7	16.7	66.7	48 + 48	BiGaTi ₄ O ₁₁ , TiO ₂	
7	31.7	3.3	65.0	12 + 12	TiO ₂ , (Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , Bi ₂ Ti ₄ O ₁₁	
8	32.7	5.8	61.5	48 + 48	TiO ₂ , (Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , BiGaTi ₄ O ₁₁	
9	5.8	32.7	61.5	48 + 48	Ga ₂ O ₃ , TiO ₂ , BiGaTi ₄ O ₁₁	
10	25.0	25.0	50.0	48 + 48	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , Ga ₂ O ₃ , BiGaTi ₄ O ₁₁	
11	35.0	20.0	45.0	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , Ga ₂ O ₃ , BiGaTi ₄ O ₁₁	
12	45.0	15.0	40.0	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , Bi ₄ Ti ₃ O ₁₂ , Ga ₂ O ₃	
13	33.3	33.3	33.3	48 + 48	(melt)	
14	14.3	52.4	33.3	48 + 48	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , Ga ₂ O ₃ , BiGaTi ₄ O ₁₁	
15	50.0	25.0	25.0	48 + 48	(melt)	
16	40.0	40.0	20.0	48 + 48	(melt)	
17	25.0	50.0	25.0	48 + 48	(melt)	
18	66.7	16.7	16.7	48 + 48	(melt)	
19	85.2	11.1	3.7	48 + 48	(melt)	
20	26.4	64.2	9.4	48 + 48	(melt)	
21	50.0	0.0	50.0	12 + 12	Bi ₄ Ti ₃ O ₁₂ , Bi ₂ Ti ₄ O ₁₁	
22	45.0	1.5	53.5	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , Bi ₂ Ti ₄ O ₁₁	
23	41.5	4.5	54.0	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , Bi ₂ Ti ₄ O ₁₁	
24	37.0	8.0	55.0	12 + 12	TiO ₂ , (Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , BiGaTi ₄ O ₁₁	
25	43.5	4.0	52.5	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , Bi ₂ Ti ₄ O ₁₁	
26	40.0	8.7	51.3	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , TiO ₂	
27	39.5	10.5	50.0	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} , Ga ₂ O ₃ , BiGaTi ₄ O ₁₁	
28	45.5	2.0	52.5	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} ($x = 0.04$, $d = 0.19$) >>Bi ₂ Ti ₄ O ₁₁ , Bi ₄ Ti ₃ O ₁₂	10.3522(2)
29	45.0	3.0	52.0	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} ($x = 0.06$, $d = 0.15$)	10.3508(3)
30	44.0	4.5	51.5	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} ($x = 0.09$, $d = 0.12$)	10.3471(2)
31	43.0	6.0	51.0	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} ($x = 0.12$, $d = 0.08$)	10.3444(2)
32	42.5	7.5	50.0	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} ($x = 0.15$, $d = 0.00$)	10.3451(2)
33	41.3	8.8	50.0	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} ($x \sim 0.18$, $d \sim 0.00$) >>BiGaTi ₄ O ₁₁ , TiO ₂	10.3416(2)
34	46.0	2.5	51.5	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} ($x \sim 0.05$, $d \sim 0.12$) >>Bi ₄ Ti ₃ O ₁₂	10.3550(2)
35	44.5	4.5	51.0	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} ($x = 0.09$, $d = 0.08$)	10.3541(6)
36	44.5	5.0	50.5	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti ₂ O _{7-3d/2} ($x = 0.10$, $d = 0.04$)	10.3508(2)
37	43.0	8.0	49.0	12 + 12	(Bi _{1-x} Ga _x) _{2-d} Ti _{1.96} Ga _{0.04} O _{7-3d/2} ($x = 0.16$, $d = 0.01$)	10.3459(2)

38	45.0	5.0	50.0	12 + 12	$(\text{Bi}_{1-x}\text{Ga}_x)_{2-d}\text{Ti}_2\text{O}_{7-3d/2}, \text{Bi}_4\text{Ti}_3\text{O}_{12}$
39	43.5	8.5	48.0	12 + 12	$(\text{Bi}_{1-x}\text{Ga}_x)_{2-d}\text{Ti}_2\text{O}_{7-3d/2}, \text{Bi}_4\text{Ti}_3\text{O}_{12}$
40	47.5	2.5	50.0	12 + 12	$(\text{Bi}_{1-x}\text{Ga}_x)_{2-d}\text{Ti}_2\text{O}_{7-3d/2}, \text{Bi}_4\text{Ti}_3\text{O}_{12}$
41	50.0	2.5	47.5	12 + 12	$(\text{Bi}_{1-x}\text{Ga}_x)_{2-d}\text{Ti}_2\text{O}_{7-3d/2}, \text{Bi}_4\text{Ti}_3\text{O}_{12}$
42	50.0	5.0	45.0	12 + 12	$(\text{Bi}_{1-x}\text{Ga}_x)_{2-d}\text{Ti}_2\text{O}_{7-3d/2}, \text{Bi}_4\text{Ti}_3\text{O}_{12}$
43	48.8	2.5	48.8	12 + 12	$(\text{Bi}_{1-x}\text{Ga}_x)_{2-d}\text{Ti}_2\text{O}_{7-3d/2}, \text{Bi}_4\text{Ti}_3\text{O}_{12}$
44	47.5	5.0	47.5	12 + 12	$(\text{Bi}_{1-x}\text{Ga}_x)_{2-d}\text{Ti}_2\text{O}_{7-3d/2}, \text{Bi}_4\text{Ti}_3\text{O}_{12}$

Table S2 The results of EPMA for the single crystal $(\text{Bi}_{1.62}\text{Ga}_{0.14}\text{Ti}_2\text{O}_{6.64})$ prepared by slow cooling from 1250 °C

Point	Bi_2O_3 (mass%)	Ga_2O_3 (mass%)	TiO_2 (mass%)	Total (mass%)
1	69.2	2.2	29.2	100.5
2	69.3	2.6	29.7	101.5
3	68.6	2.6	29.2	100.4
4	69.4	2.6	28.6	100.6
5	68.9	2.8	28.6	100.3
6	67.0	2.0	28.9	98.0
7	68.0	2.4	28.3	98.7
8	68.0	2.3	29.5	99.7
9	68.7	1.9	28.9	99.6
10	69.6	2.0	29.0	100.6
avg.(dev.)	68.7(8)	2.3(3)	29.0(4)	100(1)

Table S3 Anisotropic displacement parameters (\AA^2) for $\text{Bi}_{1.62}\text{Ga}_{0.14}\text{Ti}_2\text{O}_{6.64}$.

Atom	U_{11}	U_{22}	U_{33}	U_{23}	U_{13}	U_{12}
Bi1	0.0096(13)	0.0103(9)	0.040(3)	-0.0023(9)	-0.0032(8)	-0.0013(8)
Ti1a	0.0039(4)	0.0039(4)	0.0039(4)	-0.0008(4)	-0.0008(4)	-0.0008(4)
O1a	0.015(2)	0.008(2)	0.022(3)	0.0076(15)	0	0

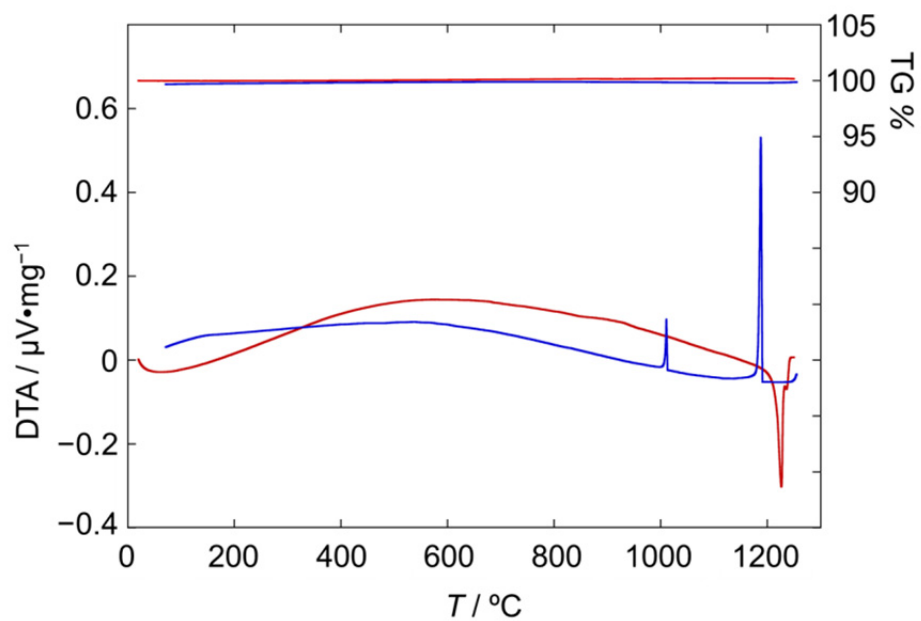


Fig. S1 TG-DTA curves generated by $(\text{Bi}_{1-x}\text{Ga}_x)_2-d\text{Ti}_2\text{O}_{7-3d/2}$ ($x = 0.09$, $d = 0.08$, sample 35) on heating (red) and on cooling (blue).

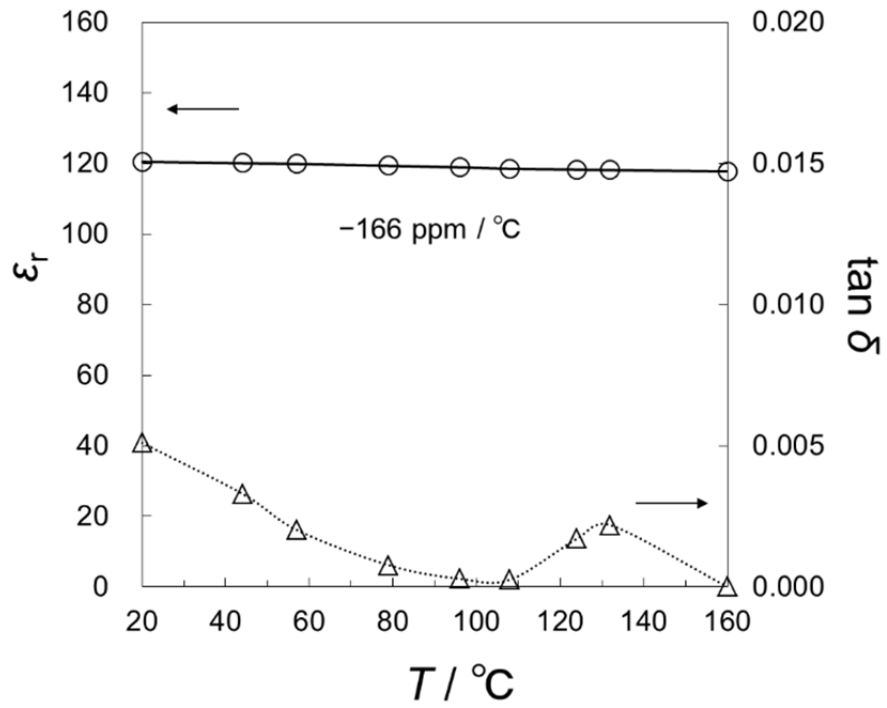


Fig. S2 Temperature dependence of the dielectric constant ϵ_r , and loss $\tan \delta$ values determined for $(\text{Bi}_{1-x}\text{Ga}_x)_2\text{-dTi}_2\text{O}_{7-3d/2}$ (sample 29 ($x = 0.06$, $d = 0.15$)) at 1 MHz.