

Electronic Supplementary Information

The permittivity of thermodynamically ideal liquid mixtures and the excess relative permittivity of binary dielectrics

João Carlos R. Reis, T. P. Iglesias, Gérard Douhéret and Michael I. Davis

Table S1. Experimental density ρ and relative permittivity ϵ_r of the pure liquids at different temperatures

Compound	T/K	$\rho/\text{g cm}^{-3}$	ϵ_r	
Tetraglyme	283.15	1.02108	8.16	10
	288.15	1.01586	8.04	15
	298.15	1.00703	7.81	
	308.15	0.99743	7.53	20
	328.15	0.97930	7.08	
Hexane	288.15	0.66387	1.909	
	308.15	0.64572	1.879	25
	328.15	0.62685	1.850	
Cyclohexane	283.15	0.78787	2.056	
	288.15	0.78329	2.049	30
	308.15	0.76438	2.018	
Benzene	288.15	0.88424	2.316	
	298.15	0.87358	2.296	35

Table S2. Experimental values of relative permittivity ϵ_r , excess relative permittivity ϵ_r^E and inverse vertical asymptote $1/p$ for mixtures tetraglyme(A)-
40 hexane(B) as a function of mole fraction x_A and ideal volume fraction ϕ_A^{id} at different temperatures T

x_A	ϕ_A^{id}	ϵ_r	ϵ_r^E	$1/p$	x_A	ϕ_A^{id}	ϵ_r	ϵ_r^E	$1/p$
$T = 288.15 \text{ K}$									
0.0478	0.0782	2.167	-0.221	0.482	0.5988	0.7156	5.663	-0.633	0.372
0.0965	0.1526	2.453	-0.391	0.459	0.6935	0.7923	6.264	-0.502	0.357
0.1946	0.2894	3.051	-0.632	0.438	0.7974	0.8690	6.925	-0.312	0.322
0.2954	0.4141	3.701	-0.747	0.416	0.9000	0.9382	7.509	-0.152	0.305
0.3901	0.5188	4.313	-0.777	0.402	0.9520	0.9710	7.769	-0.093	0.353
0.4920	0.6201	4.990	-0.721	0.381					
$T = 308.15 \text{ K}$									
0.0480	0.0777	2.120	-0.197	0.469	0.5972	0.7123	5.423	-0.481	0.320
0.0999	0.1564	2.390	-0.373	0.464	0.6952	0.7920	5.988	-0.367	0.300
0.1942	0.2870	2.984	-0.516	0.396	0.7939	0.8655	6.534	-0.236	0.274
0.2970	0.4137	3.639	-0.578	0.359	0.9023	0.9391	7.097	-0.089	0.219
0.3958	0.5224	4.242	-0.589	0.343	0.9532	0.9714	7.349	-0.019	0.108
0.4897	0.6157	4.798	-0.560	0.333					
$T = 328.15 \text{ K}$									
0.0491	0.0786	2.113	-0.148	0.379	0.6000	0.7124	5.216	-0.360	0.271
0.1013	0.1569	2.402	-0.268	0.365	0.6943	0.7895	5.700	-0.279	0.256
0.1917	0.2814	2.900	-0.422	0.359	0.7995	0.8681	6.245	-0.145	0.200
0.2996	0.4139	3.518	-0.497	0.337	0.8941	0.9331	6.683	-0.047	0.127
0.3912	0.5148	4.047	-0.495	0.317	0.9523	0.9706	6.894	-0.032	0.177
0.4987	0.6216	4.664	-0.437	0.291					

Table S3. Experimental values of relative permittivity ε_r , excess relative permittivity ε_r^E and inverse vertical asymptote $1/p$ for mixtures tetraglyme(A)-cyclohexane(B) as a function of mole fraction x_A and ideal volume fraction ϕ_A^{id} at different temperatures T

x_A	ϕ_A^{id}	ε_r	ε_r^E	$1/p$	x_A	ϕ_A^{id}	ε_r	ε_r^E	$1/p$
$T = 283.15\text{ K}$									
0.0505	0.0978	2.393	-0.260	0.461	0.6000	0.7535	6.119	-0.536	0.349
0.0985	0.1821	2.727	-0.441	0.446	0.6986	0.8253	6.679	-0.414	0.339
0.1945	0.3298	3.422	-0.655	0.418	0.8018	0.8918	7.210	-0.290	0.342
0.2999	0.4661	4.160	-0.741	0.397	0.9004	0.9485	7.720	-0.126	0.302
0.3980	0.5740	4.826	-0.734	0.384	0.9505	0.9751	7.960	-0.048	0.246
0.4990	0.6699	5.498	-0.647	0.363					
$T = 288.15\text{ K}$									
0.0496	0.0961	2.375	-0.250	0.459	0.6041	0.7565	6.040	-0.541	0.358
0.1010	0.1862	2.722	-0.442	0.446	0.7039	0.8288	6.610	-0.404	0.341
0.1981	0.3347	3.408	-0.646	0.417	0.8061	0.8944	7.130	-0.277	0.340
0.3021	0.4685	4.140	-0.716	0.392	0.9018	0.9492	7.610	-0.136	0.333
0.4007	0.5766	4.789	-0.714	0.381	0.9542	0.9770	7.870	-0.032	0.193
0.4980	0.6689	5.410	-0.646	0.367					
$T = 308.15\text{ K}$									
0.0517	0.0994	2.330	-0.236	0.457	0.5982	0.7508	5.650	-0.507	0.359
0.0981	0.1804	2.620	-0.392	0.442	0.7001	0.8253	6.170	-0.397	0.354
0.1973	0.3322	3.260	-0.589	0.415	0.8024	0.8915	6.670	-0.262	0.342
0.2941	0.4575	3.870	-0.669	0.400	0.9009	0.9485	7.120	-0.126	0.324
0.3975	0.5718	4.510	-0.660	0.382	0.9537	0.9766	7.340	-0.061	0.329
0.4946	0.6645	5.080	-0.601	0.369					

⁴⁵ **Table S4.** Experimental values of relative permittivity ε_r , excess relative permittivity ε_r^E and inverse vertical asymptote $1/p$ for mixtures tetraglyme(A)-benzene(B) as a function of mole fraction x_A and ideal volume fraction ϕ_A^{id} at different temperatures T

x_A	ϕ_A^{id}	ε_r	ε_r^E	$1/p$	x_A	ϕ_A^{id}	ε_r	ε_r^E	$1/p$
$T = 288.15\text{ K}$									
0.0479	0.1108	2.724	-0.227	0.385	0.6072	0.7929	6.492	-0.363	0.296
0.1025	0.2205	3.177	-0.402	0.375	0.7031	0.8543	6.970	-0.236	0.258
0.2044	0.3889	3.959	-0.583	0.367	0.7904	0.9033	7.360	-0.126	0.205
0.3053	0.5212	4.685	-0.614	0.351	0.9012	0.9576	7.843	0.046	-0.244
0.4045	0.6272	5.330	-0.576	0.339	0.9492	0.9789	7.999	0.080	-1.993
0.5047	0.7162	5.940	-0.476	0.316	0.9507	0.9795	8.011	0.088	-3.098
$T = 298.15\text{ K}$									
0.0499	0.1148	2.702	-0.227	0.387	0.6041	0.7902	6.279	-0.374	0.309
0.1024	0.2197	3.134	-0.374	0.364	0.7059	0.8556	6.761	-0.253	0.282
0.2000	0.3816	3.870	-0.530	0.352	0.8065	0.9114	7.229	-0.093	0.176
0.3089	0.5246	4.620	-0.568	0.339	0.8935	0.9539	7.515	-0.041	0.146
0.4045	0.6264	5.190	-0.560	0.341	0.9512	0.9796	7.730	0.032	-0.408
0.5048	0.7156	5.770	-0.472	0.323					

⁵⁰ **Table S5.** Values of inverse vertical asymptote $1/p$ for Wiener's lower bound, $(r_{A/B} - 1)/r_{A/B}$, and Hashin-Shtrikman's lower, $(r_{A/B} - 1)/(r_{A/B} + 2)$, and upper, $(r_{A/B} - 1)/3r_{A/B}$, bounds of the experimental systems

	tetraglyme(A)-hexane(B) at			tetraglyme(A)-cyclohexane(B) at			tetraglyme(A)-benzene(B) at		
$1/p$	288.15 K	308.15 K	328.15 K	283.15 K	288.15 K	308.15 K	288.15 K	298.15 K	
$(r_{A/B} - 1)/r_{A/B}$	0.763	0.750	0.739	0.748	0.745	0.732	0.712	0.706	
$(r_{A/B} - 1)/(r_{A/B} + 2)$	0.517	0.501	0.485	0.497	0.494	0.477	0.452	0.445	
$(r_{A/B} - 1)/3r_{A/B}$	0.254	0.250	0.246	0.249	0.248	0.244	0.237	0.253	