

Supporting information for:

**Effects of the first hydration sphere and the bulk
solvent on the spectra of the f^2 isoelectronic
actinide compounds: U^{4+} , NpO_2^+ , and PuO_2^{2+}**

Cécile Danilo,[†] Jean-Pierre Flament,[†] Valérie Vallet,^{*,†} and Ulf Wahlgren[‡]

Université des Sciences et Technologies de Lille 1, Laboratoire PhLAM, CNRS UMR 8523, CERLA, CNRS FR 2416, Bât P5, 59655 Villeneuve d'Ascq Cedex, France, and Department of Physics, Stockholm University, AlbaNova University Centre, 106 91 Stockholm, Sweden and NORDITA, AlbaNova University Centre, 106 91 Stockholm, Sweden

E-mail: valerie.vallet@univ-lille1.fr

*To whom correspondence should be addressed

[†]Université des Sciences et Technologies de Lille 1, Laboratoire PhLAM, CNRS UMR 8523, CERLA, CNRS FR 2416, Bât P5, 59655 Villeneuve d'Ascq Cedex, France

[‡]Department of Physics, Stockholm University, AlbaNova University Centre, 106 91 Stockholm, Sweden and NORDITA, AlbaNova University Centre, 106 91 Stockholm, Sweden

List of Tables

1	Bond distances in Angstroms of hydrated $[\text{U}(\text{H}_2\text{O})_8]^{4+}$, $[\text{NpO}_2(\text{H}_2\text{O})_5]^+$, and $[\text{PuO}_2(\text{H}_2\text{O})_5]^{2+}$ complexes.	S-4
2	Cartesian coordinates of $[\text{U}(\text{H}_2\text{O})_8]^{4+}$ in Angstroms.	S-5
3	Cartesian coordinates of $[\text{NpO}_2(\text{H}_2\text{O})_5]^+$ in Angstroms.	S-6
4	Cartesian coordinates of $[\text{PuO}_2(\text{H}_2\text{O})_5]^{2+}$ in Angstroms.	S-7
5	Spectrum of $[\text{U}(\text{H}_2\text{O})_8]^{4+}$ in gas-phase computed at the SO-CASPT2 level. Energies are in cm^{-1}	S-8
6	Absorption spectrum of $[\text{U}(\text{H}_2\text{O})_8]^{4+}$ in PCM computed at the SO-CASPT2 level (PCM equilibrated on the ground-state). Energies are in cm^{-1}	S-11
7	Emission spectrum of $[\text{U}(\text{H}_2\text{O})_8]^{4+}$ in PCM computed at the SO-CASPT2 level (PCM equilibrated on the highest singlet state). Energies are in cm^{-1}	S-15

Tables

Table 1: Bond distances in Angstroms of hydrated $[\text{U}(\text{H}_2\text{O})_8]^{4+}$, $[\text{NpO}_2(\text{H}_2\text{O})_5]^+$, and $[\text{PuO}_2(\text{H}_2\text{O})_5]^{2+}$ complexes.

Complex	$R(\text{An}-\text{O}_{\text{yl}})$	$R(\text{An}-\text{OH}_2)$
$[\text{U}(\text{H}_2\text{O})_8]^{4+}$	...	2.475
$[\text{NpO}_2(\text{H}_2\text{O})_5]^+$	1.790	2.590
$[\text{PuO}_2(\text{H}_2\text{O})_5]^{2+}$	1.719	2.490 ± 0.005

Table 2: Cartesian coordinates of $[\text{U}(\text{H}_2\text{O})_8]^{4+}$ in Angstroms.

Atom	x	y	z
U	0.000000	0.000000	0.000000
O	0.000000	2.003970	1.452183
O	0.000000	-2.003970	-1.452183
O	-2.003970	0.000000	1.452183
O	2.003970	0.000000	-1.452183
O	0.000000	-2.003970	1.452183
O	0.000000	2.003970	-1.452183
O	2.003970	0.000000	1.452183
O	-2.003970	0.000000	-1.452183
H	-0.762458	2.515692	1.787052
H	0.762458	-2.515692	-1.787052
H	0.762458	2.515692	1.787052
H	-0.762458	-2.515692	-1.787052
H	-2.515692	-0.762458	1.787052
H	2.515692	0.762458	-1.787052
H	-2.515692	0.762458	1.787052
H	2.515692	-0.762458	-1.787052
H	0.762458	-2.515692	1.787052
H	-0.762458	2.515692	-1.787052
H	-0.762458	-2.515692	1.787052
H	0.762458	2.515692	-1.787052
H	2.515692	0.762458	1.787052
H	-2.515692	-0.762458	-1.787052
H	2.515692	-0.762458	1.787052
H	-2.515692	0.762458	-1.787052

Table 3: Cartesian coordinates of $[\text{NpO}_2(\text{H}_2\text{O})_5]^+$ in Angstroms.

Atom	x	y	z
Np	0.000000	0.000000	0.000000
O	0.000000	0.000000	1.789671
O	0.000000	0.000000	-1.789727
O	-2.462823	-0.800220	-0.000558
O	0.000000	-2.589565	-0.000558
O	-1.522109	2.095002	-0.000558
O	1.522108	2.095003	-0.000558
O	2.462823	-0.800219	-0.000558
H	-3.094226	-0.690458	-0.720272
H	-2.911034	-1.258452	0.719042
H	-0.299504	-3.156147	-0.720272
H	0.297300	-3.157441	0.719042
H	-1.612833	2.729421	-0.720272
H	-2.096418	2.379675	0.719042
H	2.909122	-1.260148	-0.720272
H	3.094775	-0.692954	0.719042
H	2.097440	2.377333	-0.720272
H	1.615376	2.729172	0.719042

Table 4: Cartesian coordinates of $[\text{PuO}_2(\text{H}_2\text{O})_5]^{2+}$ in Angstroms.

Atom	x	y	z
Pu	0.000000	0.000000	0.000000
O	0.000000	0.000000	-1.719712
O	-0.000957	0.003909	1.719066
O	1.438517	2.029018	0.004841
O	2.379105	-0.738238	-0.006265
O	-1.561727	1.938500	-0.004294
O	-2.309734	-0.924121	-0.004562
O	0.108563	-2.492715	-0.003283
H	1.492156	2.699449	0.702664
H	2.069504	2.289159	-0.683324
H	3.049829	-0.537295	0.663080
H	2.802650	-1.298773	-0.673232
H	-2.192985	2.169668	0.694006
H	-1.664317	2.601316	-0.704116
H	0.550419	-3.049073	0.654854
H	-0.276886	-3.086036	-0.664704
H	-2.692455	-1.507515	0.667668
H	-2.987847	-0.792107	-0.683952

Table 5: Spectrum of $[\text{U}(\text{H}_2\text{O})_8]^{4+}$ in gas-phase computed at the SO-CASPT2 level. Energies are in cm^{-1} .

Energy	Contributions of U^{4+} SO states
0	46% 3H_4
210	46% 3H_4
309	44% 3H_4
316	44% 3H_4
1277	43% 3H_4
1345	44% 3H_4
1464	45% 3H_4
5114	33% 3F_2 + 13% 3H_5
5286	20% 3F_2 + 29% 3H_5
5325	9% 3H_5 + 37% 3F_2
5428	30% 3F_2 + 16% 3H_5
6495	52% 3H_5
6678	45% 3H_5
6804	14% 3F_2 + 35% 3H_5
6808	45% 3H_5
7073	49% 3H_5
7452	21% 3H_5 + 23% 3F_2
7679	37% 3H_5
7909	45% 3H_5
9846	45% 3F_3
9942	30% 3F_3 + 17% 3H_6
10017	12% 3H_6 + 35% 3F_3
10734	35% 3F_3
10747	11% 3H_6 + 15% 3F_4 + 15% 1G_4
11092	30% 3F_3 + 10% 3H_6

Table 5: continue

Energy	Contributions of U ⁴⁺ SO states
11240	8% ³ F ₃ + 9% ¹ G ₄ + 9% ³ F ₄ + 23% ³ H ₆
11301	13% ³ F ₄ + 9% ³ F ₃ + 13% ¹ G ₄ + 13% ³ H ₆
11625	14% ³ F ₄ + 14% ¹ G ₄ + 19% ³ H ₆
11787	11% ¹ G ₄ + 22% ³ H ₆ + 11% ³ F ₄
11955	16% ³ H ₆ + 16% ³ F ₃ + 9% ³ F ₄ + 9% ¹ G ₄
12047	15% ³ F ₄ + 15% ¹ G ₄ + 18% ³ H ₆
12310	11% ³ F ₄ + 23% ³ H ₆ + 11% ¹ G ₄
12454	36% ³ H ₆ + 9% ³ F ₃
12501	32% ³ H ₆
13042	26% ³ H ₆ + 10% ³ F ₄ + 10% ¹ G ₄
13130	31% ³ H ₆
13626	10% ³ F ₄ + 10% ¹ G ₄ + 26% ³ H ₆
13717	34% ³ H ₆
14038	39% ³ H ₆
14625	37% ³ H ₆
15237	38% ³ H ₆
18727	21% ³ F ₄ + 17% ¹ G ₄
18935	11% ¹ D ₂ + 17% ³ F ₄ + 14% ¹ G ₄
19331	44% ³ P ₀
19411	17% ³ F ₄ + 13% ¹ G ₄ + 13% ¹ D ₂
19632	22% ³ F ₄ + 18% ¹ G ₄
19884	14% ¹ G ₄ + 11% ¹ D ₂ + 17% ³ F ₄
19891	26% ³ F ₄ + 22% ¹ G ₄
20117	10% ³ P ₂ + 21% ¹ D ₂
20322	16% ¹ G ₄ + 19% ³ F ₄
20431	9% ³ P ₂ + 18% ¹ D ₂ + 9% ¹ G ₄ + 11% ³ F ₄

Table 5: continue

Energy	Contributions of U ⁴⁺ SO states
20799	22% ¹ D ₂ + 11% ³ P ₂
21155	19% ¹ G ₄ + 23% ³ F ₄
22265	50% ³ P ₁
22632	51% ³ P ₁
26586	43% ¹ I ₆
26623	48% ¹ I ₆
26642	20% ³ P ₂ + 23% ¹ I ₆
27353	28% ³ P ₂ + 11% ¹ D ₂ + 12% ¹ I ₆
27638	46% ¹ I ₆
27828	50% ¹ I ₆
28012	11% ¹ D ₂ + 29% ³ P ₂ + 12% ¹ I ₆
28143	38% ¹ I ₆ + 9% ³ P ₂
28401	22% ¹ I ₆ + 21% ³ P ₂ + 8% ¹ D ₂
29409	50% ¹ I ₆
29589	43% ¹ I ₆
30731	46% ¹ I ₆
31217	12% ³ P ₂ + 30% ¹ I ₆
32342	30% ¹ I ₆ + 12% ³ P ₂
48323	48% ¹ S ₀

Table 6: Absorption spectrum of $[\text{U}(\text{H}_2\text{O})_8]^{4+}$ in PCM computed at the SO-CASPT2 level (PCM equilibrated on the ground-state). Energies are in cm^{-1} .

Energy	Contributions of U^{4+} SO states
0	47% 3H_4
150	47% 3H_4
157	47% 3H_4
468	45% 3H_4
504	45% 3H_4
1288	44% 3H_4
1301	45% 3H_4
1311	45% 3H_4
1446	46% 3H_4
5174	12% 3H_5 + 35% 3F_2
5184	11% 3H_5 + 35% 3F_2
5350	29% 3H_5 + 21% 3F_2
5389	37% 3F_2 + 9% 3H_5
5442	16% 3H_5 + 31% 3F_2
6377	53% 3H_5
6688	50% 3H_5
6703	50% 3H_5
6818	45% 3H_5
6826	45% 3H_5
6920	13% 3F_2 + 36% 3H_5
7112	49% 3H_5
7413	23% 3F_2 + 23% 3H_5
7732	38% 3H_5
7788	45% 3H_5
7797	45% 3H_5

Table 6: continue

Energy	Contributions of U ⁴⁺ SO states
9848	45% 3F_3
9853	45% 3F_3
9919	35% 3F_3 + 13% 3H_6
10168	38% 3F_3 + 11% 3H_6
10787	40% 3F_3
10900	13% 3H_6 + 16% 3F_4 + 16% 1G_4
11159	33% 3F_3 + 12% 3H_6
11163	12% 3H_6 + 33% 3F_3
11317	23% 3H_6 + 10% 1G_4 + 10% 3F_4
11321	11% 3H_6 + 15% 3F_4 + 15% 1G_4
11326	11% 3H_6 + 15% 3F_4 + 15% 1G_4
11748	14% 3F_4 + 14% 1G_4 + 20% 3H_6
11852	11% 3F_4 + 11% 1G_4 + 25% 3H_6
11872	10% 1G_4 + 26% 3H_6 + 10% 3F_4
11899	11% 1G_4 + 11% 3F_4 + 16% 3H_6 + 12% 3F_3
12081	23% 3H_6 + 13% 1G_4 + 13% 3F_4
12337	33% 3H_6
12346	24% 3H_6 + 10% 1G_4 + 10% 3F_4
12363	32% 3H_6
12371	31% 3H_6
12994	10% 3F_4 + 10% 1G_4 + 26% 3H_6
13116	29% 3H_6
13137	28% 3H_6
13676	27% 3H_6 + 11% 1G_4 + 11% 3F_4
13833	36% 3H_6
14013	38% 3H_6

Table 6: continue

Energy	Contributions of U ⁴⁺ SO states
14544	38% ³ H ₆
14546	38% ³ H ₆
15146	8% ³ F ₃ + 40% ³ H ₆
18903	21% ³ F ₄ + 17% ¹ G ₄
19039	18% ³ F ₄ + 15% ¹ G ₄ + 10% ¹ D ₂
19042	10% ¹ D ₂ + 15% ¹ G ₄ + 18% ³ F ₄
19381	18% ³ F ₄ + 15% ¹ G ₄ + 11% ¹ D ₂
19399	45% ³ P ₀
19647	21% ³ F ₄ + 17% ¹ G ₄
19946	27% ³ F ₄ + 22% ¹ G ₄
20080	15% ³ F ₄ + 12% ¹ D ₂ + 13% ¹ G ₄
20109	14% ¹ D ₂ + 11% ¹ G ₄ + 14% ³ F ₄
20212	22% ¹ D ₂ + 11% ³ P ₂
20372	10% ³ F ₄ + 20% ¹ D ₂ + 10% ³ P ₂
20458	16% ¹ G ₄ + 20% ³ F ₄
20512	22% ³ F ₄ + 18% ¹ G ₄
20749	10% ³ P ₂ + 22% ¹ D ₂
21286	24% ³ F ₄ + 20% ¹ G ₄
22317	51% ³ P ₁
22329	51% ³ P ₁
22630	52% ³ P ₁
26828	20% ³ P ₂ + 24% ¹ I ₆
26838	20% ³ P ₂ + 24% ¹ I ₆
27057	10% ³ P ₂ + 38% ¹ I ₆
27070	47% ¹ I ₆
27424	16% ¹ I ₆ + 26% ³ P ₂ + 10% ¹ D ₂

Table 6: continue

Energy	Contributions of U^{4+} SO states
27654	50% 1I_6
27708	51% 1I_6
27733	51% 1I_6
28091	27% 3P_2 + 10% 1D_2 + 15% 1I_6
28223	12% 3P_2 + 35% 1I_6
28265	24% 1I_6 + 20% 3P_2
29337	50% 1I_6
29608	48% 1I_6
29659	47% 1I_6
30776	47% 1I_6
31069	15% 3P_2 + 27% 1I_6
31111	14% 3P_2 + 28% 1I_6
32195	12% 3P_2 + 31% 1I_6
48357	49% 1S_0

Table 7: Emission spectrum of $[\text{U}(\text{H}_2\text{O})_8]^{4+}$ in PCM computed at the SO-CASPT2 level (PCM equilibrated on the highest singlet state). Energies are in cm^{-1} .

Transition energy from the ground state	Emission ¹ from 1S_0	Contributions of U^{4+} SO states
0	37362	47% 3H_4
104	37257	47% 3H_4
106	37362	47% 3H_4
424	36938	45% 3H_4
539	36938	45% 3H_4
1078	36284	45% 3H_4
1154	36208	45% 3H_4
1166	36196	45% 3H_4
1259	36103	46% 3H_4
4923	32439	39% 3F_2
4928	32434	38% 3F_2
5093	32269	23% 3H_5 + 26% 3F_2
5143	32269	40% 3F_2
5194	32168	37% 3F_2 + 10% 3H_5
6476	30886	52% 3H_5
6808	30554	43% 3H_5
6850	30512	50% 3H_5
6858	30504	49% 3H_5
6910	30452	43% 3H_5
6911	30451	47% 3H_5
6958	30451	15% 3F_2 + 32% 3H_5
7008	30354	49% 3H_5
7725	29637	42% 3H_5
7899	29463	46% 3H_5

¹ S_0 shifted by -7687 cm^{-1} to match the 1S_0 experimental absorption energy

Table 7: continue

Transition energy from the ground state	Emission ¹ from 1S_0	Contributions of U^{4+} SO states
7901	29461	46% 3H_5
9569	27793	34% 3F_3
9573	27788	35% 3F_3
9750	27788	36% 3F_3 + 8% 3H_6
10036	27611	10% 3H_6 + 25% 3F_3
10070	27291	17% 1G_4 + 17% 3F_4 + 11% 3F_3
10078	27284	17% 1G_4 + 11% 3F_3 + 17% 3F_4
10133	27229	9% 3H_6 + 18% 1G_4 + 18% 3F_4
10262	27099	14% 1G_4 + 15% 3F_3 + 14% 3F_4
10574	26788	22% 3F_4 + 22% 1G_4
10775	26587	10% 1G_4 + 10% 3F_4 + 19% 3F_3 + 10% 3H_6
10789	26573	17% 3F_4 + 17% 1G_4 + 8% 3H_6
10855	26507	9% 3H_6 + 16% 3F_4 + 16% 1G_4
11083	26279	22% 1G_4 + 22% 3F_4
11183	26178	8% 3F_4 + 34% 3F_3
11204	26157	37% 3F_3
11215	26147	37% 3F_3
12070	25292	48% 3H_6
12118	25244	42% 3H_6
12137	25225	46% 3H_6
12151	25211	43% 3H_6
12457	24904	44% 3H_6
12778	24584	37% 3H_6
12828	24534	38% 3H_6
12841	24521	38% 3H_6

¹ S_0 shifted by -7687 cm^{-1} to match the 1S_0 experimental absorption energy

Table 7: continue

Transition energy from the ground state	Emission ¹ from 1S_0	Contributions of U^{4+} SO states
13371	23991	42% 3H_6
13545	23817	46% 3H_6
13886	23476	44% 3H_6
13901	23461	44% 3H_6
14641	22721	9% 3F_3 + 42% 3H_6
16978	20384	13% 3F_4 + 11% 1G_4 + 15% 1D_2
17069	20293	13% 1D_2 + 13% 1G_4 + 16% 3F_4
17301	20061	12% 1D_2 + 13% 1G_4 + 16% 3F_4
17627	19735	9% 3P_2 + 19% 1D_2 + 9% 3F_4
17684	19678	15% 1G_4 + 19% 3F_4 + 10% 1D_2
17826	19536	16% 1G_4 + 19% 3F_4
17911	19451	15% 1G_4 + 9% 1D_2 + 18% 3F_4
18009	19353	10% 1D_2 + 11% 1G_4 + 13% 3F_4 + 9% 3P_0
18171	19191	27% 3F_4 + 22% 1G_4
18385	18976	19% 3F_4 + 9% 1D_2 + 15% 1G_4
18553	18809	16% 3P_0 + 12% 1D_2
18647	18715	21% 3F_4 + 17% 1G_4
18724	18638	17% 1G_4 + 21% 3F_4
18735	18627	8% 3P_2 + 9% 3F_4 + 17% 1D_2
19304	18058	15% 3P_0 + 14% 1G_4 + 18% 3F_4
21391	15971	51% 3P_1
21488	15874	50% 3P_1
22021	15340	52% 3P_1
23831	13531	49% 1I_6
23892	13469	48% 1I_6

¹ S_0 shifted by -7687 cm^{-1} to match the 1S_0 experimental absorption energy

Table 7: continue

Transition energy from the ground state	Emission ¹ from 1S_0	Contributions of U^{4+} SO states
24249	13113	46% 1I_6
24265	13097	49% 1I_6
24326	13036	51% 1I_6
24508	12854	12% 3P_2 + 33% 1I_6
24519	12843	46% 1I_6
24688	12674	13% 3P_2 + 30% 1I_6
25468	11894	27% 1I_6 + 17% 3P_2
25802	11560	49% 1I_6
25821	11541	49% 1I_6
25938	11424	13% 1D_2 + 34% 3P_2
25992	11370	49% 1I_6
26419	10943	35% 3P_2 + 14% 1D_2
27434	9928	47% 1I_6
28554	8807	19% 1I_6 + 21% 3P_2 + 8% 1D_2
28689	8673	23% 3P_2 + 9% 1D_2 + 17% 1I_6
29320	8042	22% 1I_6 + 19% 3P_2
45048	0	48% 1S_0

1S_0 shifted by -7687 cm^{-1} to match the 1S_0 experimental absorption energy