

**Supplementary Information:**

**Theoretical predictions of the spectroscopic parameters in  
noble-gas molecules: HXeOH and its complex with water**

Janusz Cukras and Joanna Sadlej

**Comments to Table II** Some methodological aspects of the calculations should be discussed: the comparison of the non-relativistic results (P3) versus ECP-relativistic results (aug-cc-pVTZ(-PP)) (Table II). The total SAPT energies for the latter are in agreement with the corresponding supermolecular interaction energies for P3 basis set. The slightly smaller values of  $E_{elst}$  and  $E_{exch}$  in comparison with P3 basis set may be attributed to a smaller basis set. There are, however, some differences in  $E_{ind}$  and  $E_{disp}$  that need a comment. The dispersion term doubles for the  $\alpha$  complex as compared to P3 results, similarly for  $\delta$  and  $\gamma$  structures, but to a lesser extent. Induction term essentially remains unchanged for  $\alpha$ , whereas it decreases ca. two and three times for  $\delta$  and  $\gamma$  structures, respectively. The overall relative contributions to total SAPT interaction energy are also changed. For instance, the relative contributions of  $E_{ind}$  and  $E_{disp}$  in the  $\alpha$  structure are 51% and 54% for aug-cc-pVTZ(-PP) basis set and make this structure induction-dispersion stabilized. The  $\delta$  structure is characterized by the induction/dispersion ratio of 66%:41% in P3 basis, while it becomes 35%:73% in aug-cc-pVTZ(-PP) basis set. These changes, however, cannot be attributed to any kind of relativistic effect because of the difference in the number of basis set functions applied in each calculation. Moreover, the ECP approximation, as applied and tested in SAPT software suite, may lead to inaccurate results in induction and exchange-induction terms and, thus, poorly reproduce the SCF level contribution [? ]. The total SAPT energy, however, is well reproduced when the  $\delta E_{int,resp}^{HF}$  is used. Indeed, this is the case, since the total SAPT values agree well with the corresponding P3 results. This is why we focus on P3 results when analyzing individual contributions. Applying Douglas-Kroll approximation to SAPT calculations does not qualitatively affect the results. The largest change in total SAPT interaction energy occurs for SAPT0 energy and it is not larger in absolute value than 3% of the non-relativistic result.

Table I: A comparison of frequencies [ $\text{cm}^{-1}$ ] and IR intensities [km/mol] calculated with P3 basis set obtained for  $\text{H}_2\text{O}$ ,  $(\text{H}_2\text{O})_2$ ,  $\text{HXeOH}$  and  $\alpha\text{-HXeOH}\cdots\text{H}_2\text{O}$

	$\text{H}_2\text{O}$			$\text{HXeOH}$			$(\text{H}_2\text{O})_2$			$\alpha\text{-HXeOH}\cdots\text{H}_2\text{O}$		
	Vibration	$\nu$	I	Vibration	$\nu$	I	Vibration	$\nu$	I	Vibration	$\nu$	I
Intramolecular												
				$\nu_{\text{O}3\text{Xe}7}$	425	119.9						
				$\nu_{\text{H}1\text{O}3\text{Xe}7} + \nu_{\text{O}3\text{Xe}7\text{H}2}$	568	3.0						
				$\nu_{\text{O}3\text{Xe}7\text{H}2}$	628	0.1						
				$\nu_{\text{H}1\text{O}3\text{Xe}7} - \nu_{\text{O}3\text{X}37\text{H}2}$	779	60.1						
							$\nu_{\text{H}4\text{O}5\text{H}6}$	1628	112.5	$\nu_{\text{H}4\text{O}5\text{H}6}$	1657	138.7
							$\nu_{\text{H}1\text{O}2\text{H}3}$	1675	110.1			
										$\nu_{\text{Xe}7\text{H}2}$	1895	830.6
										$\nu_{\text{O}5\text{H}4} + \nu_{\text{O}5\text{H}6}$	3494	296.3
										$\nu_{\text{O}3\text{H}1} + \nu_{\text{O}3\text{H}2}$	3632	0.2
										$\nu_{\text{O}5\text{H}4} - \nu_{\text{O}5\text{H}6}$	3754	107.7
										$\nu_{\text{O}3\text{H}1} - \nu_{\text{O}3\text{H}2}$	3807	73.5
Intermolecular												
										138	102.3	5.9
										213	35.2	156
										239	121.8	191
										243	315.2	292
										415	250.8	533
										840	272.4	592
											773	92.5
										871	170.4	

Table II: SAPT calculations of the interaction energy of the  $\alpha$ ,  $\delta$ ,  $\gamma$ -HXeOH $\cdots$ H<sub>2</sub>O complexes [kJ/mol] with different basis sets. (H<sub>2</sub>O)<sub>2</sub> data for comparison.

SAPT term	aug-cc-pVTZ(PP)			P3			P3+mbf <sup>c)</sup>			DK-P3		
	$\alpha$	$\delta$	$\gamma$ (H <sub>2</sub> O) <sub>2</sub>	$\alpha$	$\delta$	$\gamma$ (H <sub>2</sub> O) <sub>2</sub>	$\alpha$	$\delta$	$\gamma$ (H <sub>2</sub> O) <sub>2</sub>	$\alpha$	$\delta$	$\gamma$ (H <sub>2</sub> O) <sub>2</sub>
$E_{int}^{HF}$	-33.40	-6.99	-5.90	-15.09	-54.87	-9.72	-17.4	-26.67	-41.87	-2.43	-8.87	-20.98
$E_{int}^{(10)}$	-82.29	-26.20	-18.39	-35.17	-104.12	-35.69	-44.82	-55.38	-89.88	-28.43	-38.85	-48.77
$E_{elst}^{(10)}$	77.26	25.75	19.32	29.73	83.72	37.58	46.87	43.83	82.75	36.58	47.87	42.94
$E_{exch}^{(20)}$	-42.13	-9.94	-9.17	-12.74	-46.04	-15.65	-24.89	-19.15	-45.52	-14.58	-23.78	-19.02
$E_{ind,resp}^{(20)}$	23.84	6.29	5.78	7.01	24.94	9.24	15.51	10.40	24.57	9.04	16.06	10.33
$E_{ex-ind,r}^{(20)}$	-59.58	-12.45	-15.21	-11.86	-61.43	-20.13	-45.03	-19.28			-18.94	-60.61
$E_{ex-ind}^{(30)b}$	48.86	11.43	14.25	10.72	56.55	18.85	43.19	17.44			17.03	55.71
$E_{ex-ind}^{(30)d}$	-23.33	-4.09	-2.45	-11.18	-41.50	-4.51	-7.33	-20.30	-28.06	2.6	1.30	-14.53
$\delta_{int,r}^{HF}$	-10.08	-2.90	-3.45	-3.91	-13.37	-5.21	-10.08	6.37	-13.80	-5.03	-10.17	-6.46
$E_{elst,resp}^{(12)}$	3.69	-1.62	1.61	0.38	6.09	-4.76	0.67	-0.07	5.94	-2.84	1.51	0.24
$E_{elst,resp}^{(13)}$	0.00	1.59	0.24	0.63	-1.43	3.3	0.92	1.23	-1.67	2.33	0.83	0.72
$E_{exch}^{(11)}$	0.95	0.16	0.52	0.39	-1.61	-1.24	-0.21	-0.79	0.39	-0.2	1.11	-0.17
$E_{exch}^{(12)}$	12.88	5.80	2.71	4.18	17.19	10.22	8.65	8.41	16.38	9.64	8.23	8.43
$\epsilon_{exch}^{(1)}(CCSD)$	13.01	5.42	3.27	4.79	16.45	9.26	11.29	9.24	16.55	9.22	11.74	9.71
$tE_{exch}^{(22)}$	-7.84	-2.67	-1.41	-1.86	-8.88	-4.53	-5.09	-3.40	-8.65	-4.39	-4.84	-3.42
$tE_{ex-ind}^{(22)*}$	4.44	1.69	0.89	1.02	4.81	2.67	3.17	1.84	4.67	2.72	3.27	1.86
$E_{disp}^{(20)}$	-28.66	-11.90	-10.24	-10.77	-14.02	-6.66	-8.45	-6.16	-26.93	-13.93	-17.79	-10.9
$E_{disp}^{(21)}$	3.21	0.45	1.07	0.2	1.48	-0.08	0.92	-0.09	2.33	0.17	1.50	-0.15
$E_{disp}^{(22)}$	-6.86	-2.87	-2.39	-1.96	-4.66	-1.95	-2.37	-1.43	-7.48	-3.88	-4.60	-2.48
$E_{exch-disp}^{(20)}$	5.72	2.17	1.84	1.97	3.32	1.56	2.03	1.34	5.51	2.76	3.76	2.18
$E_{ind-disp}^{(30)}$	-8.37	-2.67	-2.19	-2.71	-5.74	-2.57	-4.13	-2.48			-2.89	-5.70
$E_{ex-ind-disp}^{(30)}$	7.61	2.39	2.24	2.27	5.51	2.32	3.75	2.15			2.52	5.48
$E_{disp}^{(30)}$	0.87	0.40	0.33	0.4	-0.16	-0.07	-0.1	-0.05			0.21	-0.16
$E_{exch-disp}^{(30)}$	-0.43	-0.19	-0.18	-0.17	0.13	0.05	0.04	0.04			-0.1	0.13
$SAPT_{corr,resp}$	-13.29	-7.73	-5.12	-5.6	3.16	-1.18	3.09	2.51	-9.73	-7.83	-4.62	-2.25
$E_{elst}$	-78.61	-27.82	-16.77	-34.78	-98.03	-40.45	-44.15	-55.45	-83.94	-31.27	-37.34	-48.53
$E_{exch}$	91.09	31.71	22.55	34.29	99.3	46.57	55.31	51.45	99.53	46.01	57.21	51.2
$E_{ind}$	-21.7	-4.63	-3.91	-6.57	-25.17	-8.26	-11.3	-10.31	-24.92	-7.21	-9.29	-10.26
$E_{disp}$	-22.93	-9.73	-8.4	-8.8	-10.7	-5.1	-6.42	-4.82	-21.42	-11.16	-14.03	-8.73
<sup>a)</sup> SAPT0	-46.26	-13.82	-10.85	-19.98	-52.2	-9.61	-13.75	-25.11	-49.48	-8.56	-12.72	-23.25
<sup>b)</sup> SAPT2	-42.22	-13.36	-9.98	-19.78	-47.97	-12.46	-16.64	-25.49	-44.55	-8.67	-13.61	-22.77
<sup>c)</sup> SAPT	-46.69	-14.73	-11.02	-20.69	-51.71	-10.9	-14.31	-24.15	-51.60	-10.26	-13.48	-23.23
<sup>d)</sup> SAPT3	-47.65	-12.92	-8.33	-18.14	-43.48	-7.23	-6.52	-19.96			-18.95	-44.74
											-6.79	-6.00
											-19.87	

a) The notation - see the text.

b) The new implementation of the SAPT2008 code contains some third-order terms. We introduce them denoting this level of SAPT calculations as  $E_{int}^{SAPT3}$ :

$$E_{int}^{SAPT3} = E_{int}^{SAPT} + E_{ind}^{(30)} + E_{ind-disp}^{(30)} + E_{disp}^{(30)} + E_{exch-ind}^{(30)} + E_{exch-ind-disp}^{(30)} + E_{exch-disp}^{(30)} - \delta E_{int,resp}^{HF}. \quad (1)$$

It is important to note that this level does not include  $\delta E_{int,resp}^{HF}$  because the terms  $E_{ind}^{(30)}$  and  $E_{exch-ind}^{(30)}$  are part of it [? ? ?].

c) Due to high cost, third-order terms of SAPT were not calculated for complexes with midbond functions.

Table III: NMR shielding constants [ppm] for the  $^1\text{H}$ ,  $^{17}\text{O}$  and  $^{129}\text{Xe}$  nuclei in  $\text{H}_2\text{O}$ ,  $\text{HXeOH}$  and  $\alpha, \delta, \gamma\text{-HXeOH}\cdots\text{H}_2\text{O}$  complexes (at MP2/aug-cc-pVTZ(-PP) geometry) by different methods

SCF/aug-cc-PVTZ(-PP)											
at.	Xe	$\text{H}_2\text{O}$	$\text{HXeOH}$	$\Delta w$	$(\text{H}_2\text{O})_2$	$\alpha$	$\Delta c$	$\delta$	$\Delta c$	$\gamma$	$\Delta c$
H1		31	31	1	30	31	1	30	0	30	0
H2		31	27	-4	30	27	-3	30	0	30	0
O3 (in O3…H4)		327	147	-180	320	168	-152	318	-2	320	0
H4 (in O3…H4)					27	24	-4	28	1	26	-2
O5					326	318	-8	137	-189	152	-174
H6					31	31	0	27	-4	32	1
Xe7	515		458			461		457		457	

  

MP2/aug-cc-PVTZ(-PP)											
at.	Xe	$\text{H}_2\text{O}$	$\text{HXeOH}$	$\Delta w$	$(\text{H}_2\text{O})_2$	$\alpha$	$\Delta c$	$\delta$	$\Delta c$	$\gamma$	$\Delta c$
H1		31	29	-2	30	29	-1	30	0	30	0
H2		31	25	-5	30	26	-4	30	0	30	0
O3 (in O3…H4)		345	155	-189	337	171	-166	336	-1	338	1
H4 (in O3…H4)					28	24	-3	26	-1	24	-3
O5					340	330	-10	138	-202	164	-176
H6					31	31	0	25	-6	29	-2
Xe7	515		459			461		458		456	

<sup>a)</sup> $\Delta w = \sigma(X, \text{HXeOH}) - \sigma(X, \text{H}_2\text{O})$ ,  $\Delta c = \sigma(X, \text{complex}) - \sigma(X, (\text{H}_2\text{O})_2)$

Table IV: NMR spin-spin coupling constants [Hz] for the  $^1\text{H}$  and  $^{17}\text{O}$  nuclei in  $(\text{H}_2\text{O})_2$  at MP2/aug-cc-pVTZ(-PP) geometry

	(H <sub>2</sub> O) <sub>2</sub>	constant SCF/P3			DHF/P3 B3LYP/P3			CCSD/P3									
		$J_{tot}$	$J^{FC}$	$J^{SD}$	$J^{PSO}$	$J^{DSO}$	$J^{tot}$	$J^{FC}$	$J^{SD}$	$J^{PSO}$	$J^{DSO}$	$J^{tot}$	$J^{FC}$	$J^{SD}$	$J^{PSO}$	$J^{DSO}$	
Intramolecular	$^1J_{\text{O}3\text{-H}1}$	-99.3	-88.9	0.4	-10.5	-0.2	-99.0	-66.9	-56.5	-0.1	-10.0	-0.2	-80.2	-70.6	-0.1	-9.3	-0.2
	$^1J_{\text{O}3\text{-H}2}$	-99.3	-88.9	0.4	-10.5	-0.2	-99.0	-66.8	-56.4	-0.1	-10.0	-0.2	-80.3	-70.6	-0.1	-9.3	-0.2
	$^1J_{\text{O}5\text{-H}4}$	-101.3	-92.9	0.4	-8.4	-0.3	-100.9	-66.4	-58.1	0.0	-8.0	-0.3	-80.6	-73.0	0.1	-7.4	-0.3
	$^1J_{\text{O}5\text{-H}6}$	-93.5	-81.6	0.4	-12.0	-0.3	-93.2	-61.9	-49.9	-0.2	-11.5	-0.3	-76.8	-65.9	-0.1	-10.6	-0.3
	$^2J_{\text{H}1\text{-H}2}$	-26.1	-25.7	1.6	4.3	-6.3	-26.1	-10.4	-9.9	1.2	4.5	-6.3	-14.0	-13.3	1.2	4.3	-6.2
	$^2J_{\text{H}6\text{-H}4}$	-25.3	-24.9	1.6	3.9	-5.9	-25.4	-10.0	-9.5	1.2	4.1	-5.8	-13.7	-13.0	1.2	3.8	-5.8
Intermolecular	$^{1\text{h}}J_{\text{O}3\text{-H}4}$	9.3	9.7	-0.4	0.4	-0.4	9.3	5.9	6.4	-0.4	0.3	-0.4	5.3	5.7	-0.3	0.4	-0.4
	$^{2\text{h}}J_{\text{H}4\text{-H}1}$	0.7	0.5	0.1	0.2	-0.1	0.6	0.2	0.0	0.1	0.2	-0.1	0.4	0.2	0.1	0.1	-0.1
	$^{2\text{h}}J_{\text{H}4\text{-H}2}$	0.7	0.5	0.1	0.1	-0.1	0.7	0.2	0.0	0.1	0.1	-0.1	0.3	0.2	0.1	0.2	-0.1
	$^{2\text{h}}J_{\text{O}5\text{-O}3}$	2.4	2.6	0.1	-0.4	0.0	2.4	-0.3	0.0	0.1	-0.4	0.0	1.2	1.4	0.1	-0.3	0.0
	$^{3\text{h}}J_{\text{O}3\text{-H}6}$	1.0	0.9	0.0	0.0	0.1	1.0	0.5	0.4	0.0	0.0	0.1	0.6	0.5	0.0	0.0	0.1
	$^{3\text{h}}J_{\text{O}5\text{-H}2}$	0.4	0.4	0.0	0.0	0.1	0.4	0.3	0.3	0.0	0.0	0.1	0.3	0.2	0.0	0.0	0.1
	$^{3\text{h}}J_{\text{O}5\text{-H}1}$	0.4	0.4	0.0	0.0	0.1	0.4	0.3	0.3	0.0	0.0	0.1	0.3	0.2	0.0	0.0	0.1
	$^{4\text{h}}J_{\text{H}6\text{-H}1}$	-0.9	0.0	0.0	0.8	-1.7	-0.9	-0.9	-0.1	0.0	0.8	-1.7	-0.9	0.0	0.0	0.8	-1.7
	$^{4\text{h}}J_{\text{H}6\text{-H}2}$	-0.9	0.0	0.0	0.8	-1.7	-0.9	-0.9	-0.1	0.0	0.8	-1.7	-0.9	0.0	0.0	0.8	-1.7