

*Supplementary Information For*

**Examining the robustness of first-principles calculations for metal hydride reaction thermodynamics by detection of metastable reaction pathways**

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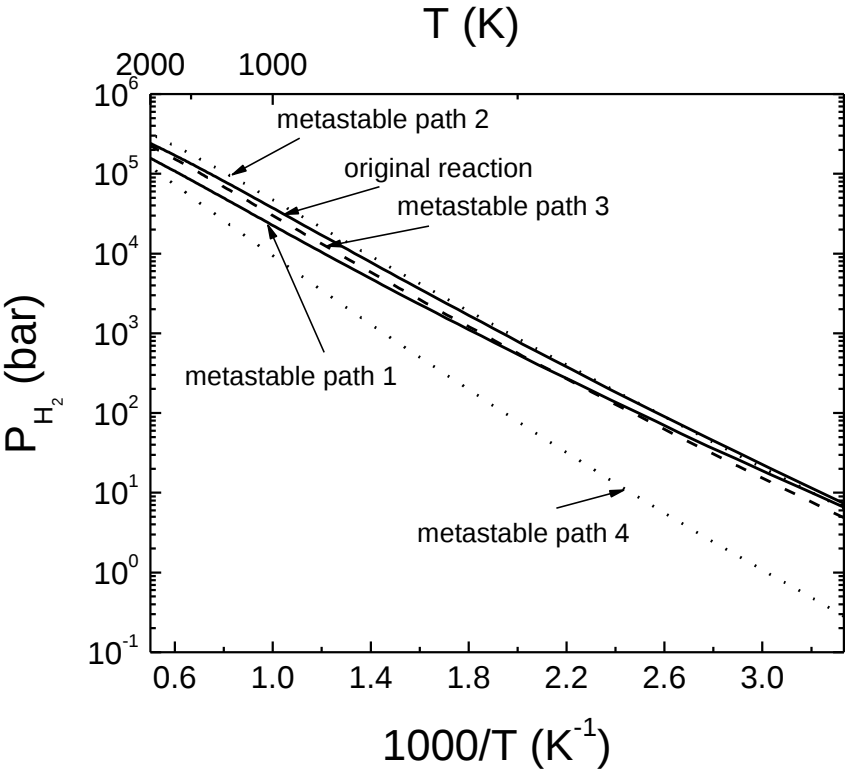
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The tables and figures below contain the ground state and metastable pathways for the seven single-step reactions involving B<sub>12</sub>H<sub>12</sub> species listed in Table 6 of the paper.

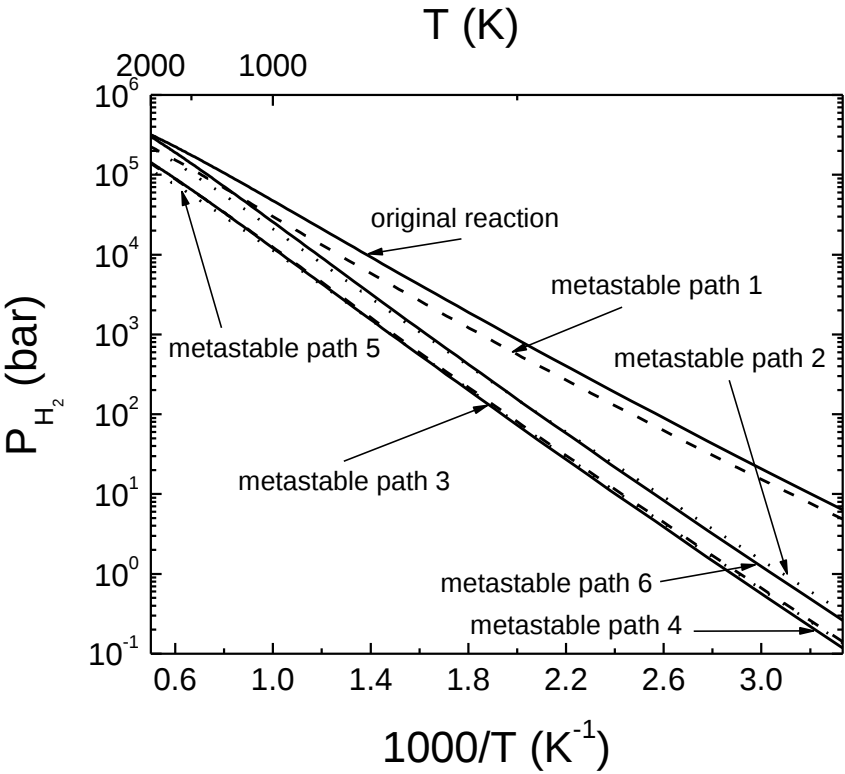
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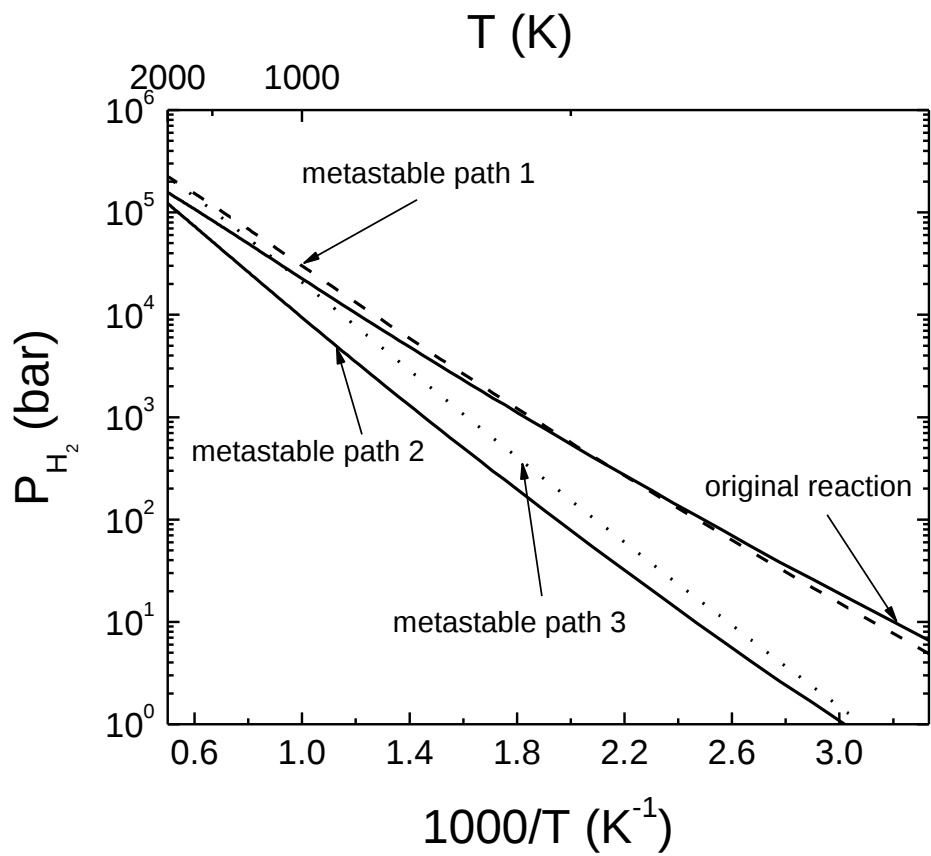
| Original path                                                                                                                                        |                                                                                                                                                                                                                                  | wt.<br>% | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) |
|------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------|---------------------------------------|
| $4\text{LiBH}_4 + 5\text{Si} + 10\text{Mg}(\text{BH}_4)_2 \rightarrow 5\text{Mg}_2\text{Si} + 2\text{Li}_2\text{B}_{12}\text{H}_{12} + 36\text{H}_2$ |                                                                                                                                                                                                                                  | 9.46     | 41                                    |
| No.                                                                                                                                                  | Metastable path                                                                                                                                                                                                                  | wt.<br>% | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) |
| 1                                                                                                                                                    | $4\text{LiBH}_4 + 5\text{Si} + 10\text{Mg}(\text{BH}_4)_2 \rightarrow 5\text{Si} + 10\text{MgH}_2 + 2\text{Li}_2\text{B}_{12}\text{H}_{12} + 26\text{H}_2$                                                                       | 6.83     | 43.1                                  |
| 2                                                                                                                                                    | $4\text{LiBH}_4 + 5\text{Si} + 10\text{Mg}(\text{BH}_4)_2 \rightarrow 4\text{LiBH}_4 + \frac{5}{6}\text{Si} + \frac{25}{6}\text{Mg}_2\text{Si} + \frac{5}{3}\text{MgB}_{12}\text{H}_{12} + 30\text{H}_2$                         | 7.88     | 43.62                                 |
| 3                                                                                                                                                    | $4\text{LiBH}_4 + 5\text{Si} + 10\text{Mg}(\text{BH}_4)_2 \rightarrow 4\text{LiBH}_4 + 5\text{Si} + \frac{25}{3}\text{MgH}_2 + \frac{5}{3}\text{MgB}_{12}\text{H}_{12} + \frac{65}{3}\text{H}_2$                                 | 5.69     | 47.06                                 |
| 4                                                                                                                                                    | $4\text{LiBH}_4 + 5\text{Si} + 10\text{Mg}(\text{BH}_4)_2 \rightarrow 5\text{Si} + \frac{15}{2}\text{Mg}(\text{BH}_4)_2 + \frac{5}{2}\text{LiMgH}_3 + \frac{3}{4}\text{Li}_2\text{B}_{12}\text{H}_{12} + \frac{39}{4}\text{H}_2$ | 2.56     | 50.64                                 |



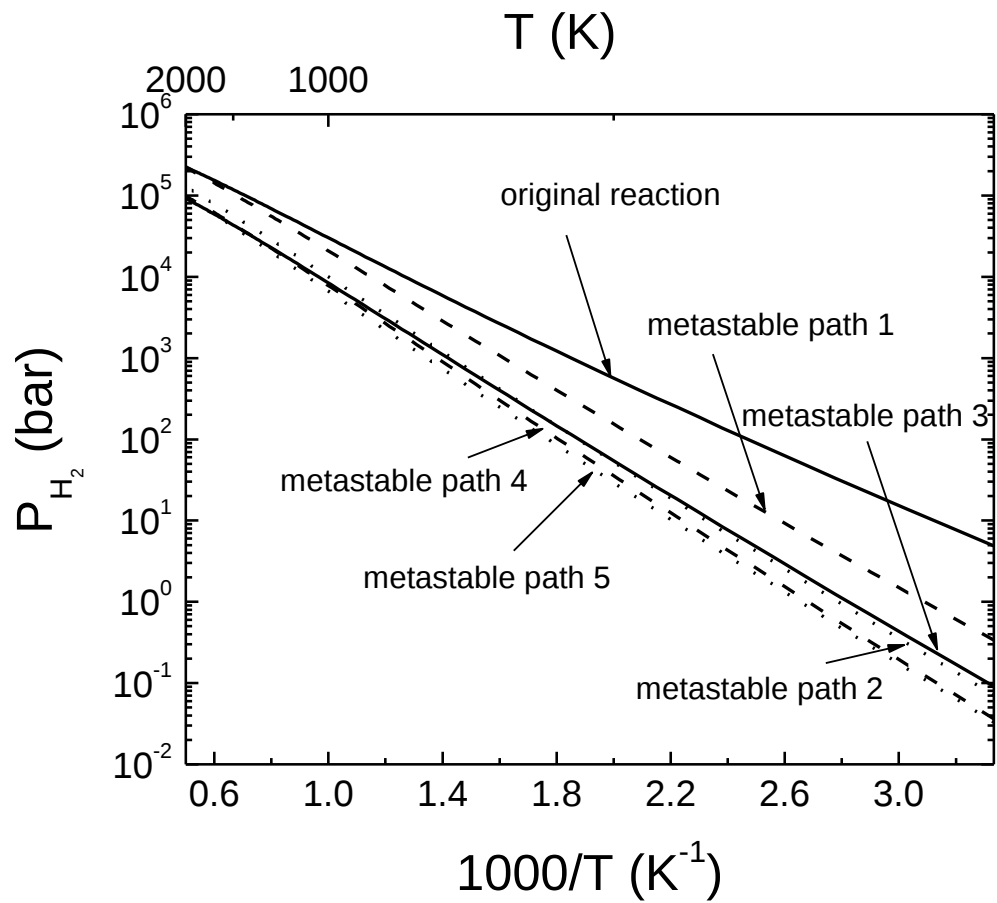
| Original path                                                                                                              |                                                                                                                                                                                                 | wt. % | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) |
|----------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|---------------------------------------|
| $5\text{Si} + 12\text{Mg}(\text{BH}_4)_2 \rightarrow 5\text{Mg}_2\text{Si} + 2\text{MgB}_{12}\text{H}_{12} + 36\text{H}_2$ |                                                                                                                                                                                                 | 9.21  | 43.6                                  |
| No.                                                                                                                        | Metastable path                                                                                                                                                                                 | wt. % | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) |
| 1                                                                                                                          | $5\text{Si} + 12\text{Mg}(\text{BH}_4)_2 \rightarrow 5\text{Si} + 10\text{MgH}_2 + 2\text{MgB}_{12}\text{H}_{12} + 26\text{H}_2$                                                                | 6.65  | 47.06                                 |
| 2                                                                                                                          | $5\text{Si} + 12\text{Mg}(\text{BH}_4)_2 \rightarrow 5\text{Si} + 10\text{Mg} + 2\text{MgB}_{12}\text{H}_{12} + 36\text{H}_2$                                                                   | 9.21  | 51.16                                 |
| 3                                                                                                                          | $5\text{Si} + 12\text{Mg}(\text{BH}_4)_2 \rightarrow 4\text{Mg}(\text{BH}_4)_2 + 3\text{Mg}_2\text{Si} + \text{MgB}_4 + \text{MgB}_{12}\text{Si}_2 + 32\text{H}_2$                              | 8.19  | 52.11                                 |
| 4                                                                                                                          | $5\text{Si} + 12\text{Mg}(\text{BH}_4)_2 \rightarrow \frac{16}{3}\text{Mg}(\text{BH}_4)_2 + \frac{25}{9}\text{Mg}_2\text{Si} + \frac{10}{9}\text{MgB}_{12}\text{Si}_2 + \frac{80}{3}\text{H}_2$ | 6.82  | 52.38                                 |
| 5                                                                                                                          | $5\text{Si} + 12\text{Mg}(\text{BH}_4)_2 \rightarrow 2\text{Si} + 3\text{Mg}_2\text{Si} + 6\text{MgB}_4 + 48\text{H}_2$                                                                         | 12.28 | 52.73                                 |
| 6                                                                                                                          | $5\text{Si} + 12\text{Mg}(\text{BH}_4)_2 \rightarrow 7\text{Mg}(\text{BH}_4)_2 + \frac{5}{6}\text{Mg}_5\text{Si}_6 + \frac{5}{6}\text{MgB}_{12}\text{H}_{12} + 15\text{H}_2$                    | 3.84  | 52.94                                 |



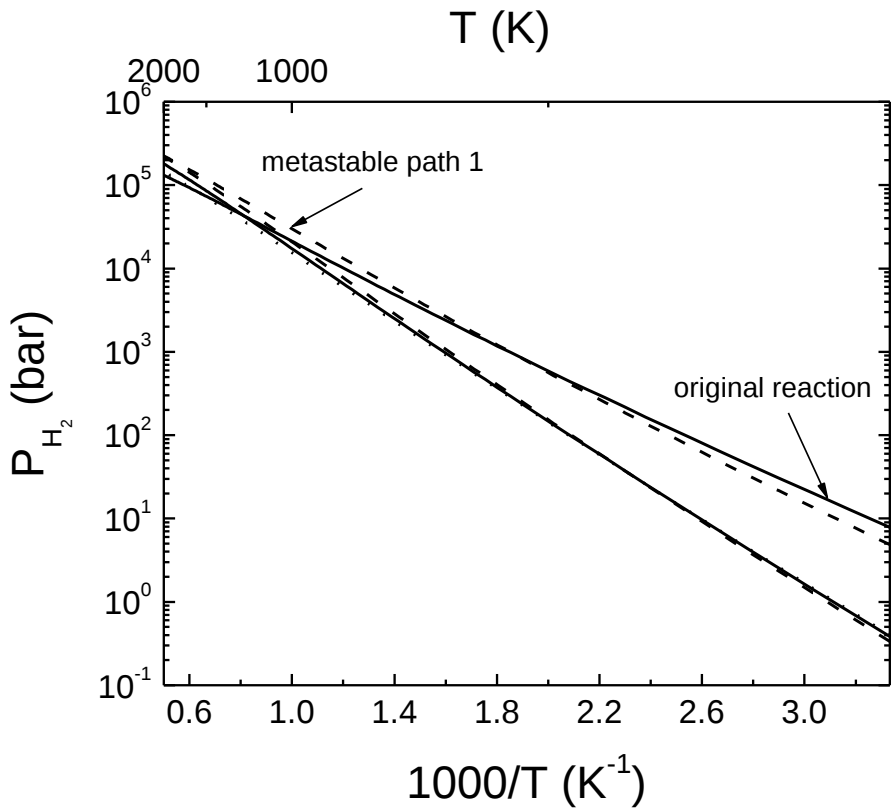
| Original path                                                                                                                 |                                                                                                                                                                                                       | wt. % | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) |
|-------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|---------------------------------------|
| $2\text{LiBH}_4 + 5\text{Mg}(\text{BH}_4)_2 \rightarrow 5\text{MgH}_2 + \text{Li}_2\text{B}_{12}\text{H}_{12} + 13\text{H}_2$ |                                                                                                                                                                                                       | 8.36  | 43.1                                  |
| No.                                                                                                                           | Metastable path                                                                                                                                                                                       | wt. % | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) |
| 1                                                                                                                             | $2\text{LiBH}_4 + 5\text{Mg}(\text{BH}_4)_2 \rightarrow 2\text{LiBH}_4 + \frac{25}{6}\text{MgH}_2 + \frac{5}{6}\text{MgB}_{12}\text{H}_{12} + \frac{65}{6}\text{H}_2$                                 | 6.97  | 47.06                                 |
| 2                                                                                                                             | $2\text{LiBH}_4 + 5\text{Mg}(\text{BH}_4)_2 \rightarrow \frac{15}{4}\text{Mg}(\text{BH}_4)_2 + \frac{5}{4}\text{LiMgH}_3 + \frac{3}{8}\text{Li}_2\text{B}_{12}\text{H}_{12} + \frac{39}{8}\text{H}_2$ | 3.14  | 50.64                                 |
| 3                                                                                                                             | $2\text{LiBH}_4 + 5\text{Mg}(\text{BH}_4)_2 \rightarrow 2\text{LiBH}_4 + \frac{25}{6}\text{Mg} + \frac{5}{6}\text{MgB}_{12}\text{H}_{12} + 15\text{H}_2$                                              | 9.65  | 51.16                                 |



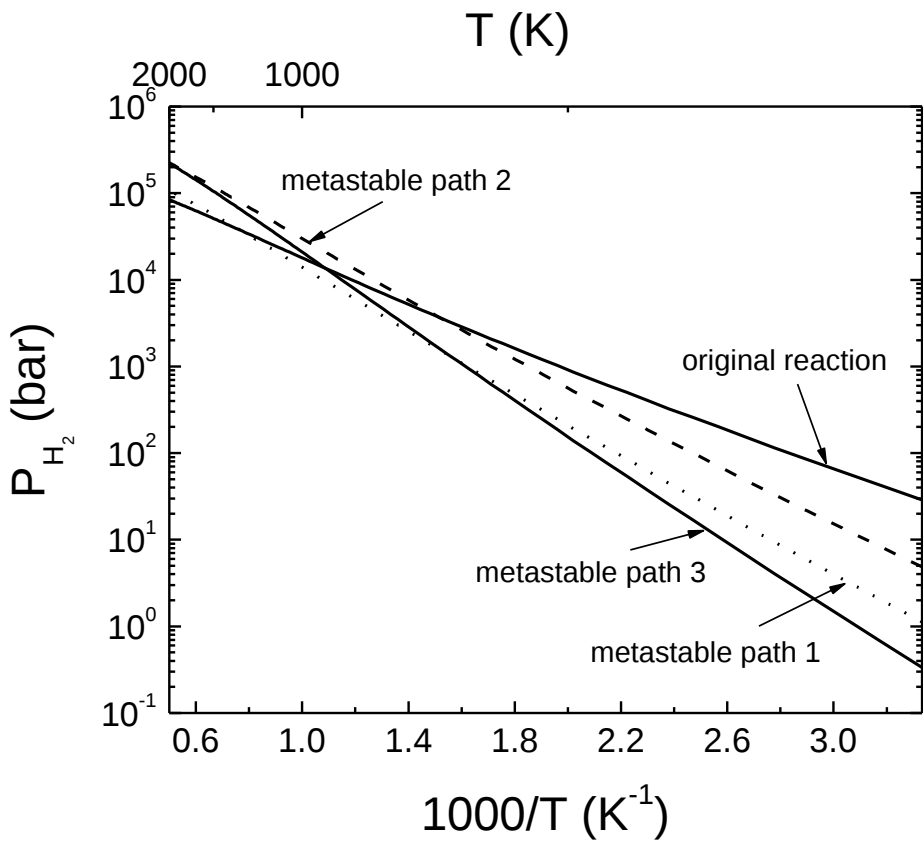
| Original path                                                                                       |                                                                                                  | wt. % | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) |
|-----------------------------------------------------------------------------------------------------|--------------------------------------------------------------------------------------------------|-------|---------------------------------------|
| $6\text{Mg}(\text{BH}_4)_2 \rightarrow 5\text{MgH}_2 + \text{MgB}_{12}\text{H}_{12} + 13\text{H}_2$ |                                                                                                  | 8.09  | 47.1                                  |
| No.                                                                                                 | Metastable path                                                                                  | wt. % | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) |
| 1                                                                                                   | $6\text{Mg}(\text{BH}_4)_2 \rightarrow 5\text{Mg} + \text{MgB}_{12}\text{H}_{12} + 18\text{H}_2$ | 11.2  | 51.16                                 |
| 2                                                                                                   | $\text{Mg}(\text{BH}_4)_2 \rightarrow \text{MgB}_2 + 4\text{H}_2$                                | 14.94 | 53.97                                 |
| 3                                                                                                   | $2\text{Mg}(\text{BH}_4)_2 \rightarrow \text{MgH}_2 + \text{MgB}_4 + 7\text{H}_2$                | 13.07 | 54.68                                 |
| 4                                                                                                   | $\text{Mg}(\text{BH}_4)_2 \rightarrow \text{Mg} + \text{MgB}_4 + 8\text{H}_2$                    | 14.94 | 56.12                                 |
| 5                                                                                                   | $7\text{Mg}(\text{BH}_4)_2 \rightarrow 5\text{MgH}_2 + 2\text{MgB}_7 + 23\text{H}_2$             | 12.27 | 56.98                                 |



| Original path                                                                                                                  |                                                                                                                                                                                           | wt. % | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) |
|--------------------------------------------------------------------------------------------------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|---------------------------------------|
| $5\text{Mg}(\text{BH}_4)_2 + \text{Ca}(\text{BH}_4)_2 \rightarrow 5\text{MgH}_2 + \text{CaB}_{12}\text{H}_{12} + 13\text{H}_2$ |                                                                                                                                                                                           | 7.72  | 43.1                                  |
| No.                                                                                                                            | Metastable path                                                                                                                                                                           | wt. % | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) |
| 1                                                                                                                              | $5\text{Mg}(\text{BH}_4)_2 + \text{Ca}(\text{BH}_4)_2 \rightarrow \text{Ca}(\text{BH}_4)_2 + \frac{25}{6}\text{MgH}_2 + \frac{5}{6}\text{MgB}_{12}\text{H}_{12} + \frac{65}{6}\text{H}_2$ | 6.43  | 47.06                                 |
| 2                                                                                                                              | $5\text{Mg}(\text{BH}_4)_2 + \text{Ca}(\text{BH}_4)_2 \rightarrow 5\text{Mg} + \text{CaB}_{12}\text{H}_{12} + 18\text{H}_2$                                                               | 10.69 | 48.72                                 |
| 3                                                                                                                              | $5\text{Mg}(\text{BH}_4)_2 + \text{Ca}(\text{BH}_4)_2 \rightarrow \text{Ca}(\text{BH}_4)_2 + \frac{25}{6}\text{Mg} + \frac{5}{6}\text{MgB}_{12}\text{H}_{12} + 15\text{H}_2$              | 8.91  | 51.16                                 |
| 4                                                                                                                              | $5\text{Mg}(\text{BH}_4)_2 + \text{Ca}(\text{BH}_4)_2 \rightarrow 3\text{Mg}(\text{BH}_4)_2 + 2\text{MgH}_2 + \text{CaB}_6 + 10\text{H}_2$                                                | 5.94  | 51.19                                 |



| Original path                                                                                                               |                                                                                                                                                                     | wt. % | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) | $T\Delta S_{\text{conf}}$<br>(kJ/mol H <sub>2</sub> ) |
|-----------------------------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------|-------|---------------------------------------|-------------------------------------------------------|
| $5\text{Mg}(\text{BH}_4)_2 + 2\text{KBH}_4 \rightarrow 5\text{MgH}_2 + \text{K}_2\text{B}_{12}\text{H}_{12} + 13\text{H}_2$ |                                                                                                                                                                     | 6.94  | 38                                    | -4.02<br>(T=567 K)                                    |
| No.                                                                                                                         | Metastable path                                                                                                                                                     | wt. % | $\Delta U_0$ (kJ/mol H <sub>2</sub> ) | $T\Delta S_{\text{conf}}$<br>(kJ/mol H <sub>2</sub> ) |
| 1                                                                                                                           | $5\text{Mg}(\text{BH}_4)_2 + 2\text{KBH}_4 \rightarrow 5\text{Mg} + \text{K}_2\text{B}_{12}\text{H}_{12} + 18\text{H}_2$                                            | 9.61  | 44.84                                 | -3.12<br>(T=609 K)                                    |
| 2                                                                                                                           | $5\text{Mg}(\text{BH}_4)_2 + 2\text{KBH}_4 \rightarrow 2\text{KBH}_4 + \frac{25}{6}\text{MgH}_2 + \frac{5}{6}\text{MgB}_{12}\text{H}_{12} + \frac{65}{6}\text{H}_2$ | 5.78  | 47.06                                 | 0                                                     |
| 3                                                                                                                           | $5\text{Mg}(\text{BH}_4)_2 + 2\text{KBH}_4 \rightarrow 2\text{KBH}_4 + \frac{25}{6}\text{Mg} + \frac{5}{6}\text{MgB}_{12}\text{H}_{12} + 15\text{H}_2$              | 8.01  | 51.16                                 | 0                                                     |



| Original path                                                |                                                                 | wt. % | $\Delta U_0$ (kJ/mol $H_2$ ) |
|--------------------------------------------------------------|-----------------------------------------------------------------|-------|------------------------------|
| $2LiH+6Ca(BH_4)_2 \rightarrow 6CaH_2+Li_2B_{12}H_{12}+13H_2$ |                                                                 | 6.03  | 56.5                         |
| No.                                                          | Metastable path                                                 | wt. % | $\Delta U_0$ (kJ/mol $H_2$ ) |
| 1                                                            | $2LiH+6Ca(BH_4)_2 \rightarrow 2LiH+5CaH_2+CaB_{12}H_{12}+13H_2$ | 6.03  | 57.41                        |
| 2                                                            | $2LiH+6Ca(BH_4)_2 \rightarrow 2LiH+4CaH_2+2CaB_6+20H_2$         | 9.28  | 58.64                        |
| 3                                                            | $2LiH+6Ca(BH_4)_2 \rightarrow 2LiH+3CaH_2+3CaB_4+21H_2$         | 9.74  | 63.01                        |

