

The comparison of the Seebeck coefficients between the experimental and theoretical values.

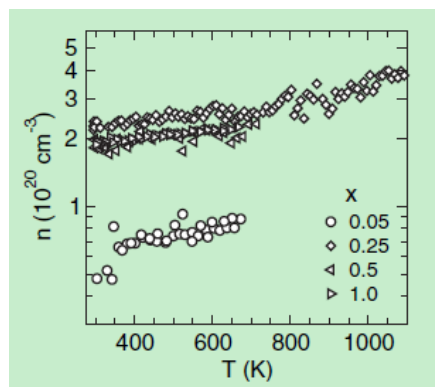


Fig. 1. The Hall Carrier concentration is constant with temperature for all  $\text{Ca}_{5-x}\text{Na}_x\text{Al}_2\text{Sb}_6$  compositions, suggesting the successful formation of heavily doped semiconductor.

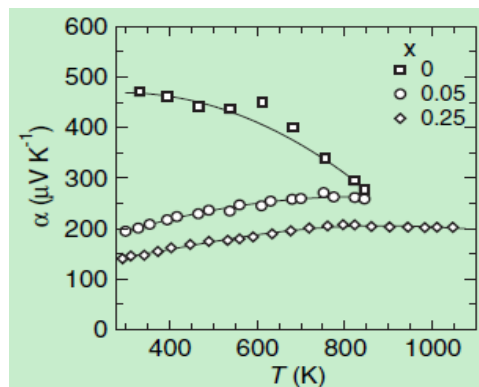


Fig. 2. High-temperature Seebeck coefficients of  $\text{Ca}_{5-x}\text{Na}_x\text{Al}_2\text{Sb}_6$  show decreasing magnitude with increasing carrier concentration.

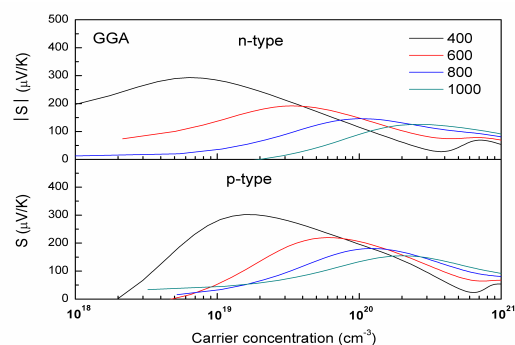


Fig. 3. Calculated Seebeck coefficients of  $\text{Ca}_5\text{Al}_2\text{Sb}_6$  with GGA.

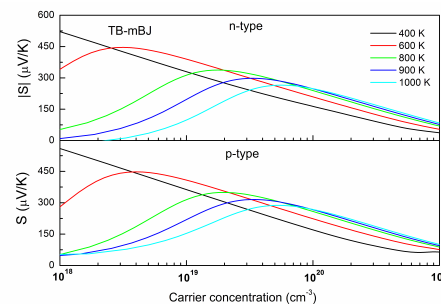


Fig. 4. Calculated Seebeck coefficients of  $\text{Ca}_5\text{Al}_2\text{Sb}_6$  with TB-mBJ.

Fig. 1 and Fig. 2 are the experimental data in Ref. 20 (Advanced Functional Materials 20 (2010) 4375), which corresponds to the p-type doping. Fig. 3 and Fig. 4 are the theoretical values calculated by different exchange-correlation potentials. We list them in below table for comparison. We can see that the theoretical Seebeck coefficients calculated by TB-mBJ are more consistent with the experimental results.

Temperature (K)	Carriers concentration ( $\text{cm}^{-3}$ )	Seebeck(experiment) ( $\mu\text{V/K}$ )	Seebeck (GGA) ( $\mu\text{V/K}$ ) p-type	Seebeck(TB-mBJ) ( $\mu\text{V/K}$ ) p-type
400	$x=0$	460	300(biggest)	566(biggest)
400	$6.6 \times 10^{19}$ ( $x=0.05$ )	210	230	207
400	$2.3 \times 10^{20}$ ( $x=0.25$ )	160	120	115

600	x=0	420	220(biggest)	440(biggest)
600	$7.2 \times 10^{19}$ (x=0.05)	245	215	248
600	$2.6 \times 10^{20}$ (x=0.25)	170	160	165
800	x=0	300	185(biggest)	345(biggest)
800	$2.8 \times 10^{20}$ (x=0.25)	180	150	178
1000	$3.2 \times 10^{20}$ (x=0.25)	175	146	180