

Supplementary Information

Chemical bonding in electron-deficient boron oxide clusters: core boronyl group, dual 3c-4e hypervalent bond, and rhombic 4c-4e bond[†]

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Full citation of ref 22.

Tables S1–S7 Natural charges, natural resonance theory (NRT) bond orders and atomic valencies for the global-minimum structures **3–9** of B_3O_2^+ , $\text{B}_3\text{O}_3^{-/0/+}$, and $\text{B}_3\text{O}_4^{-/0/+}$.

Table S8 Calculated vertical electron detachment energies (VDEs) at the TD-B3LYP level based on the global minimum structures $\text{D}_{\infty\text{h}} \text{B}_3\text{O}_2^-$ (**1**, ${}^3\Sigma_g^-$), $\text{C}_{2v} \text{B}_3\text{O}_3^-$ (**4**, ${}^1\text{A}_1$), and $\text{C}_{2v} \text{B}_3\text{O}_4^-$ (**7**, ${}^1\text{A}_1$).

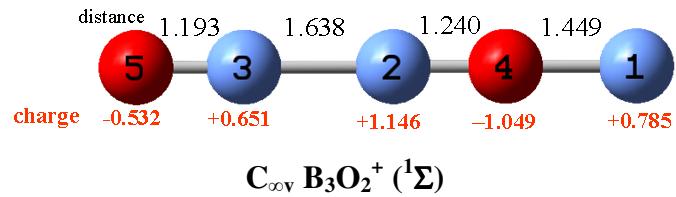
Figs. S1–S7 Alternative optimized structures for B_3O_2^+ , $\text{B}_3\text{O}_3^{-/0/+}$, and $\text{B}_3\text{O}_4^{-/0/+}$, along with their point group symmetries, electronic states, and minimum vibrational frequencies. Relative energies are given at B3LYP/aug-cc-pVTZ and CCSD(T)//B3LYP/aug-cc-pVTZ (in curly brackets). The structures were obtained initially using the Coalescence Kick and Basin Hopping global-minimum search programs at B3LYP/3-21G.

Figs. S8–S15 AdNDP bonding patterns and canonical molecular orbitals (CMOs) for the global-minimum structures **3–9** of B_3O_2^+ , $\text{B}_3\text{O}_3^{-/0/+}$, and $\text{B}_3\text{O}_4^{-/0/+}$. A low-lying $\text{D}_{\infty\text{h}} \text{B}_3\text{O}_2^+$ (${}^1\Sigma_g$) structure is also analyzed.

Full citation of ref 22.

22 Gaussian 09, Revision A.2, M. J. Frisch, G. W. Trucks, H. B. Schlegel, G. E. Scuseria, M. A. Robb, J. R. Cheeseman, G. Scalmani, V. Barone, B. Mennucci, G. A. Petersson, H. Nakatsuji, M. Caricato, X. Li, H. P. Hratchian, A. F. Izmaylov, J. Bloino, G. Zheng, J. L. Sonnenberg, M. Hada, M. Ehara, K. Toyota, R. Fukuda, J. Hasegawa, M. Ishida, T. Nakajima, Y. Honda, O. Kitao, H. Nakai, T. Vreven, J. A. Montgomery, Jr., J. E. Peralta, F. Ogliaro, M. Bearpark, J. J. Heyd, E. Brothers, K. N. Kudin, V. N. Staroverov, R. Kobayashi, J. Normand, K. Raghavachari, A. Rendell, J. C. Burant, S. S. Iyengar, J. Tomasi, M. Cossi, N. Rega, J. M. Millam, M. Klene, J. E. Knox, J. B. Cross, V. Bakken, C. Adamo, J. Jaramillo, R. Gomperts, R. E. Stratmann, O. Yazyev, A. J. Austin, R. Cammi, C. Pomelli, J. W. Ochterski, R. L. Martin, K. Morokuma, V. G. Zakrzewski, G. A. Voth, P. Salvador, J. J. Dannenberg, S. Dapprich, A. D. Daniels, Ö. Farkas, J. B. Foresman, J. V. Ortiz, J. Cioslowski, and D. J. Fox, Gaussian, Inc., Wallingford CT, 2009.

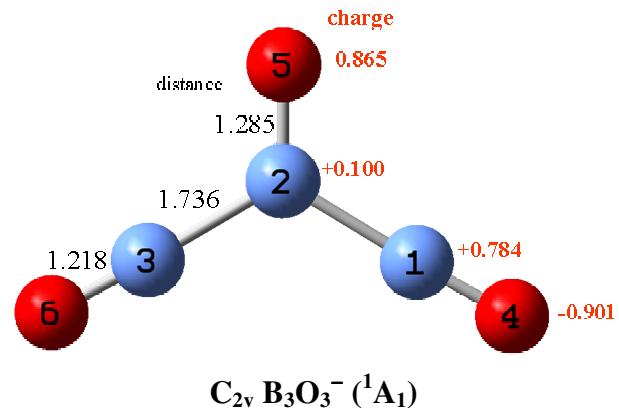
Table S1. Natural resonance theory (NRT) bond orders and atomic valencies of $C_{\infty v} B_3O_2^+ (\mathbf{3}, ^1\Sigma)$ at B3LYP/aug-cc- pVTZ. The bond lengths (in Å) and natural atomic charges (in lel) are also labeled.



		Natural Bond Order				Natural Atomic Valency				
		B ₁ -O ₄	B ₂ -B ₃	B ₂ -O ₄	B ₃ -O ₅	O ₅	B ₃	B ₂	O ₄	B ₁
NRT	t ^a	1.03	1.03	2.93	2.97	2.97	3.99	3.95	3.97	1.03
	c	0.17	0.93	0.72	1.39	1.39	2.32	1.65	0.89	0.17
	i	0.86	0.10	2.21	1.58	1.58	1.67	2.30	3.08	0.86

^a t, the total bond orders; c, the covalent bond orders of NRT; i, the ionic bond orders of NRT.

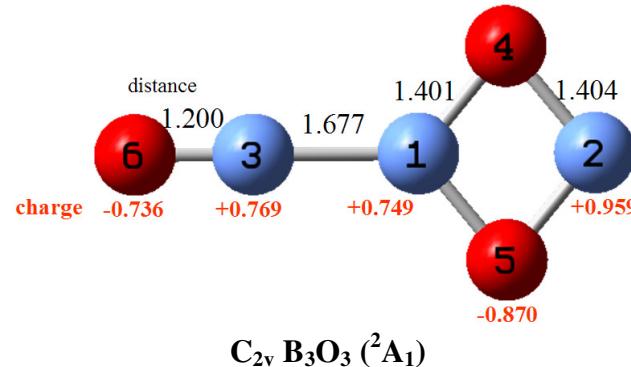
Table S2. Natural resonance theory (NRT) bond orders and atomic valencies of $C_{2v} B_3O_3^-$ (**4**, 1A_1) at B3LYP/aug-cc- pVTZ. The bond lengths (in Å) and natural atomic charges (in lel) are also labeled.



		Natural Bond Order					Natural Atomic Valencies			
		B ₁ -B ₂	B ₂ -B ₃	B ₁ -O ₄	B ₂ -O ₅	O ₃ -O ₆	O ₆	B ₃	B ₂	O ₅
NRT	t ^a	0.98	0.98	2.98	2.04	2.98	2.98	3.96	4.00	2.04
	c	0.90	0.90	1.08	0.95	1.08	1.08	1.98	2.75	0.95
	i	0.08	0.08	1.90	1.09	1.90	1.90	1.98	1.25	1.09

^a t, the total bond orders; c, the covalent bond orders of NRT; i, the ionic bond orders of NRT.

Table S3. Natural resonance theory (NRT) bond orders and atomic valencies of C_{2v} B_3O_3 (**5**, 2A_1) at B3LYP/aug-cc- pVTZ. The bond lengths (in Å) and natural atomic charges (in lel) are also labeled.



		Natural Bond Order						Natural Atomic Valency					
		B ₁ -B ₃	B ₁ -O ₄	B ₁ -O ₅	B ₂ -O ₄	B ₂ -O ₅	B ₃ -O ₆	O ₆	B ₃	B ₁	O ₄	O ₅	B ₂
NRT ^a	t	0.99	1.45	1.45	1.46	1.46	3.00	3.00	3.98	3.88	2.91	2.91	2.92
	c	0.95	0.49	0.49	0.42	0.42	1.23	1.23	2.18	1.93	0.91	0.91	0.84
	i	0.04	0.96	0.96	1.04	1.04	1.77	1.77	1.80	1.95	2.00	2.00	2.08

^a C_{2v} B_3O_3 (2A_1) possesses two leading NRT reference structures: NRT₁ and NRT₂.

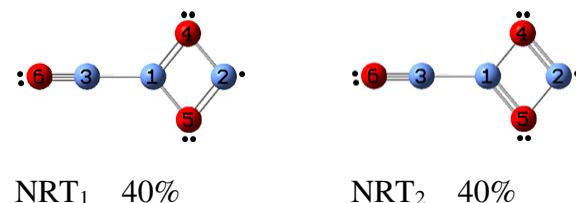
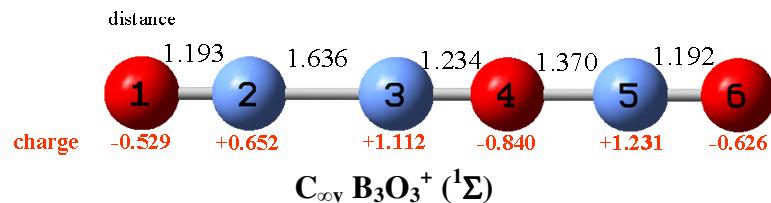


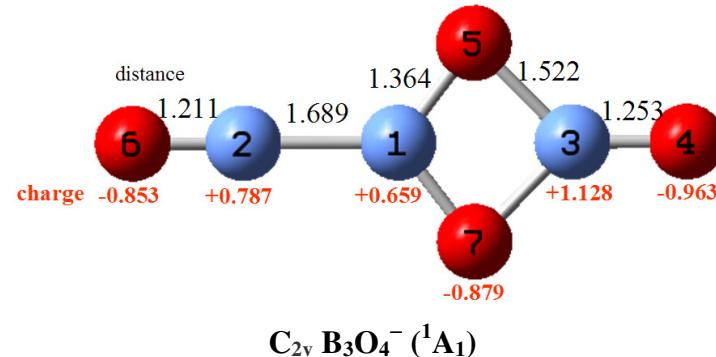
Table S4. Natural resonance theory (NRT) bond orders and atomic valencies of $C_{\infty v} B_3O_3^+ (\mathbf{6}, ^1\Sigma)$ at B3LYP/aug-cc- pVTZ. The bond lengths (in Å) and natural atomic charges (in lel) are also labeled.



		Natural Bond Order					Natural Atomic Valencies					
		B ₁ -B ₂	B ₂ -B ₃	B ₃ -O ₄	B ₄ -O ₅	B ₅ -O ₆	O ₁	B ₂	B ₃	O ₄	B ₅	O ₆
NRT	t ^a	2.97	1.02	2.91	1.04	2.95	2.97	3.99	3.93	3.95	4.00	2.95
	c	1.40	0.93	0.72	0.34	1.31	1.40	2.32	1.65	1.06	1.65	1.31
	i	1.57	0.09	2.19	0.70	1.64	1.57	1.67	2.28	2.89	2.35	1.64

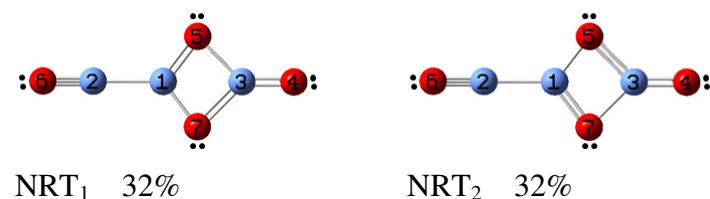
^a t, the total bond orders; c, the covalent bond orders of NRT; i, the ionic bond orders of NRT.

Table S5. Natural resonance theory (NRT) bond orders and atomic valencies of $C_{2v} B_3O_4^- ({}^1A_1)$ at B3LYP/aug-cc- pVTZ. The bond lengths (in Å) and natural atomic charges (in lel) are also labeled in the structure.



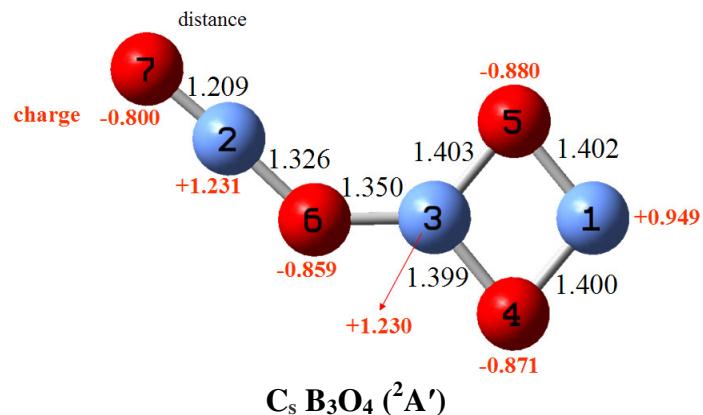
		Natural Bond Order							Natural Atomic Valency						
		B ₁ -B ₂	B ₁ -O ₅	B ₁ -O ₇	B ₂ -O ₆	B ₃ -O ₄	B ₃ -O ₅	B ₃ -O ₇	O ₆	B ₂	B ₁	O ₅	O ₇	B ₃	O ₄
NRT ^a	t ^b	0.99	1.47	1.47	2.99	2.04	1.38	1.38	2.99	3.98	3.93	2.86	2.86	4.81	2.04
	c	0.95	0.53	0.53	1.13	0.82	0.34	0.34	1.13	2.08	2.01	0.88	0.88	1.51	0.82
	i	0.04	0.94	0.94	1.86	1.22	1.04	1.04	1.86	1.90	1.92	1.98	1.98	3.30	1.22

^a $C_{2v} B_3O_4^- ({}^1A_1)$ possesses two significant NRT reference structures: NRT₁ and NRT₂.



^b t, the total bond orders; c, the covalent bond orders of NRT; i, the ionic bond orders of NRT.

Table S6. Natural resonance theory (NRT) bond orders and atomic valencies of $C_s B_3O_4$ (**8**, $^2A'$) at B3LYP/aug-cc-pVTZ. The bond lengths (in Å) and natural atomic charges (in lel) are also labeled.



		Natural Bond Order							Natural Atomic Valencies						
		B ₁ -O ₄	B ₁ -O ₅	B ₂ -O ₆	B ₂ -O ₇	B ₃ -O ₄	B ₃ -O ₅	B ₃ -O ₆	O ₇	B ₂	O ₆	B ₃	O ₄	O ₅	B ₁
NRT ^a	t	1.47	1.47	1.08	2.91	1.42	1.42	1.04	2.91	3.99	2.12	3.88	2.89	2.89	2.93
	c	0.43	0.43	0.39	1.16	0.48	0.48	0.40	1.16	1.56	0.79	1.36	0.91	0.90	0.85
	i	1.04	1.04	0.69	1.75	0.94	0.94	0.64	1.75	2.43	1.33	2.52	1.98	1.98	2.08

^a $C_s B_3O_4$ ($^2A'$) possesses two leading NRT reference structures: NRT₁ and NRT₂.

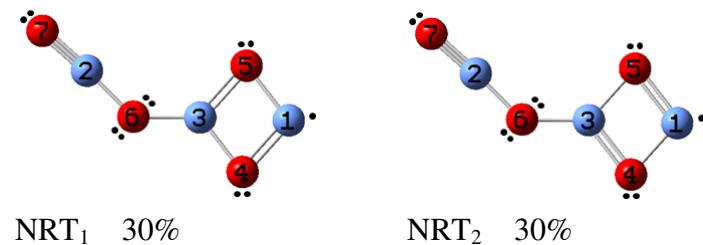
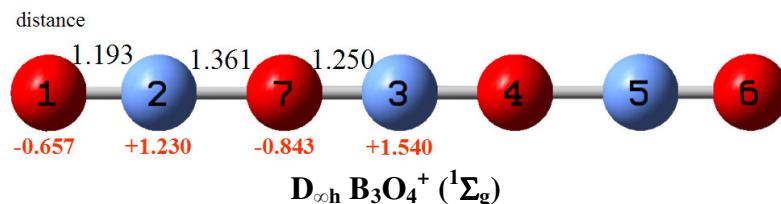
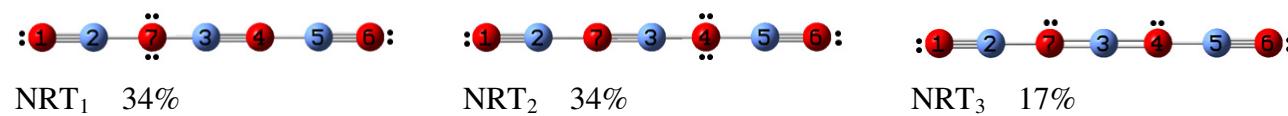


Table S7. Natural resonance theory (NRT) bond orders and atomic valencies of $D_{\infty h}$ $B_3O_4^+$ (**9**, ${}^1\Sigma_g$) at B3LYP/aug-cc- pVTZ. The bond lengths (in Å) and natural atomic charges (in lel) are also labeled.



		Natural Bond Order					Natural Atomic Valencies				
		O ₁ -B ₂	B ₂ -O ₇	B ₃ -O ₇	B ₃ -O ₄	O ₄ -B ₅	B ₅ -O ₆	O ₁	B ₂	O ₇	B ₃
NRT ^a	T ^b	2.96	1.04	1.97	1.97	1.04	2.95	2.96	3.99	3.00	3.93
	c	1.30	0.34	0.55	0.55	0.34	1.30	1.30	1.64	0.89	1.10
	i	1.66	0.70	1.42	1.42	0.70	1.65	1.66	2.35	2.11	2.83

^a $D_{\infty h}$ $B_3O_4^+$ (${}^1\Sigma_g$) possesses three significant NRT reference structures: NRT₁, NRT₂ and NRT₃.



^b t, the total bond orders; c, the covalent bond orders of NRT; i, the ionic bond orders of NRT.

Table S8. Calculated vertical electron detachment energies (VDEs) at the TD-B3LYP level based on the global minimum structures $D_{\infty h}$ $B_3O_2^-$ (**1**, $^3\Sigma_g^-$), C_{2v} $B_3O_3^-$ (**4**, 1A_1), and C_{2v} $B_3O_4^-$ (**7**, 1A_1).

Species	Feature	Final State	VDE (eV)
$B_3O_2^- D_{\infty h}$ (1 , $^3\Sigma_g^-$)	X	$^2\Pi_u$	3.07
	A	$^2\Pi_u$	6.43
$B_3O_3^- C_{2v}$ (4 , 1A_1)	X	2B_2	4.06
	A	2B_2	6.40
$B_3O_4^- C_{2v}$ (7 , 1A_1)	X	2B_2	5.10
	A	2A_2	6.10

Figure S1. Alternative optimized structures for B_3O_2^+ , along with their point group symmetries, electronic states, and minimum vibrational frequencies. Relative energies are given at B3LYP/aug-cc-pVTZ and CCSD(T)//B3LYP/aug-cc-pVTZ (in curly brackets). The structures were obtained initially using the Coalescence Kick and Basin Hopping global-minimum search programs at B3LYP/3-21G.

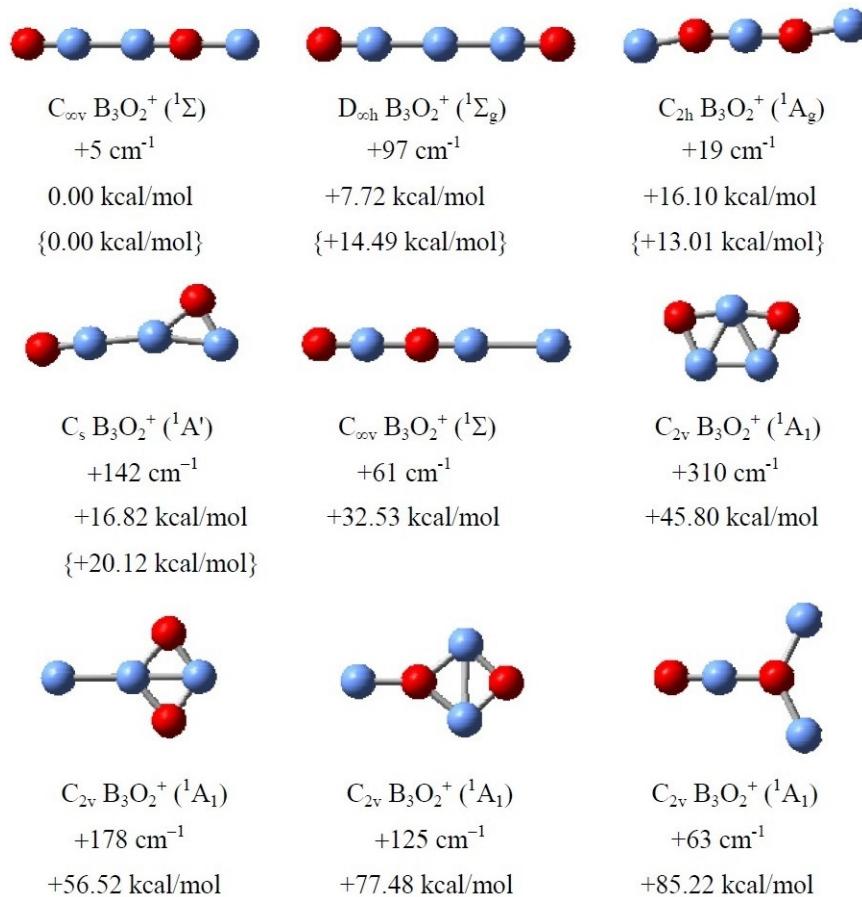


Figure S2. Alternative optimized structures for B_3O_3^- , along with their point group symmetries, electronic states, and minimum vibrational frequencies. Relative energies are given at B3LYP/aug-cc-pVTZ and CCSD(T)//B3LYP/aug-cc-pVTZ (in curly brackets). The structures were obtained initially using the Coalescence Kick and Basin Hopping global-minimum search programs at B3LYP/3-21G.

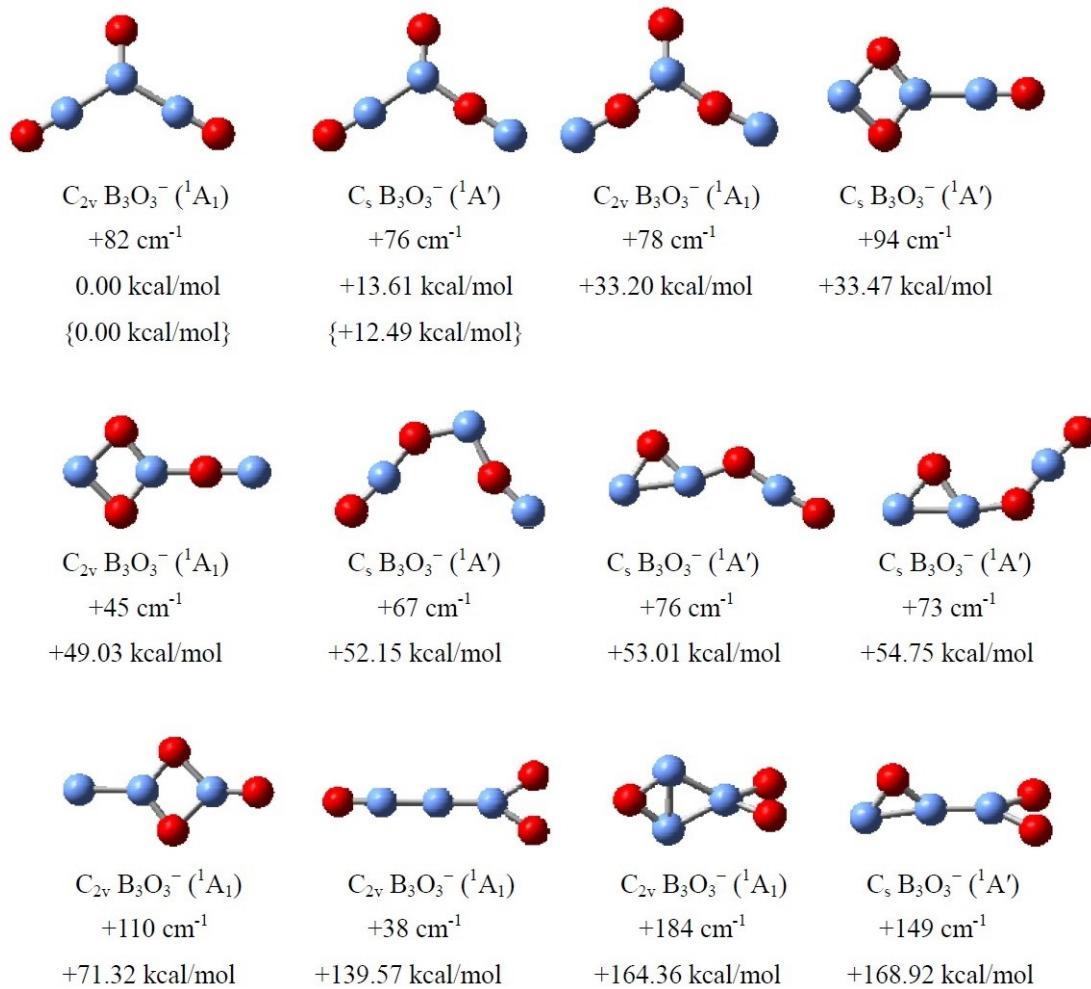


Figure S3. Alternative optimized structures for B_3O_3 , along with their point group symmetries, electronic states, and minimum vibrational frequencies. Relative energies are given at B3LYP/aug-cc-pVTZ and CCSD(T)//B3LYP/aug-cc-pVTZ (in curly brackets). The structures were obtained initially using the Coalescence Kick and Basin Hopping global-minimum search programs at B3LYP/3-21G.

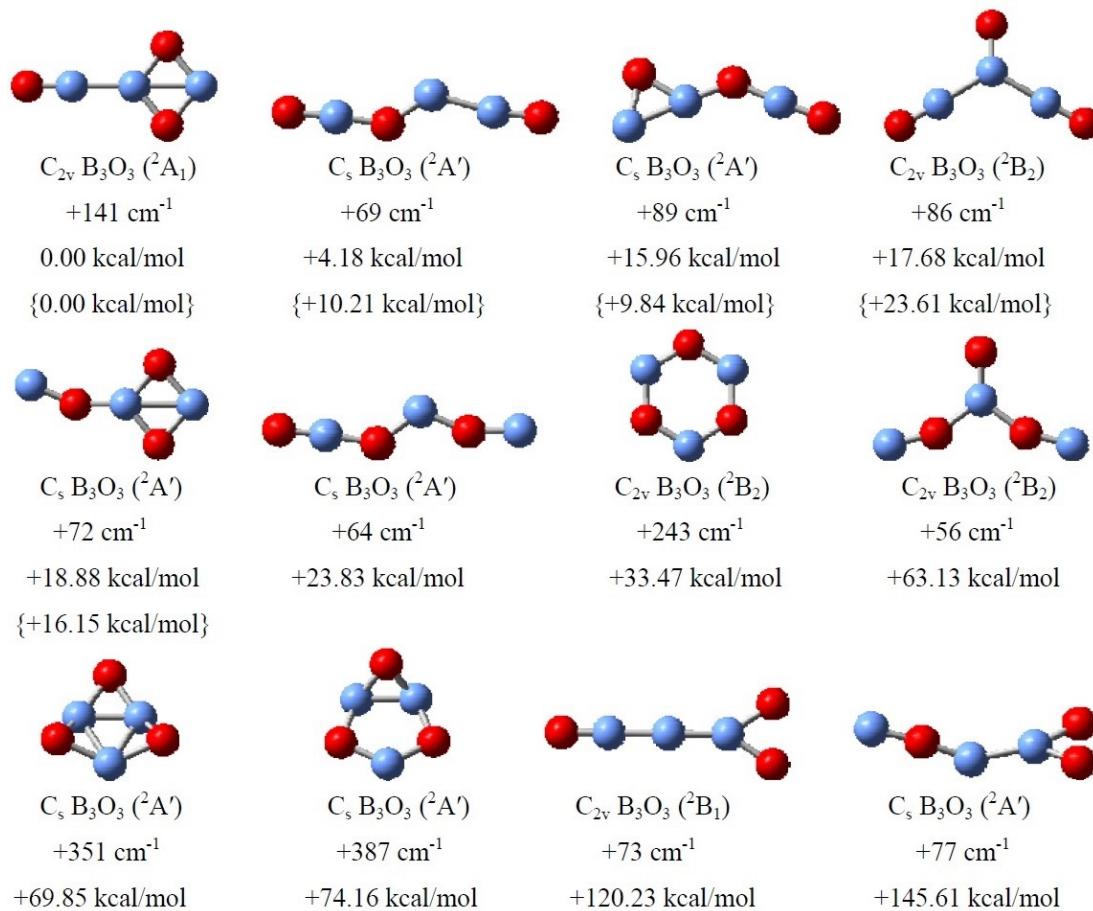


Figure S4. Alternative optimized structures for B_3O_3^+ , along with their point group symmetries, electronic states, and minimum vibrational frequencies. Relative energies are given at B3LYP/aug-cc-pVTZ and CCSD(T)//B3LYP/aug-cc-pVTZ (in curly brackets). The structures were obtained initially using the Coalescence Kick and Basin Hopping global-minimum search programs at B3LYP/3-21G.

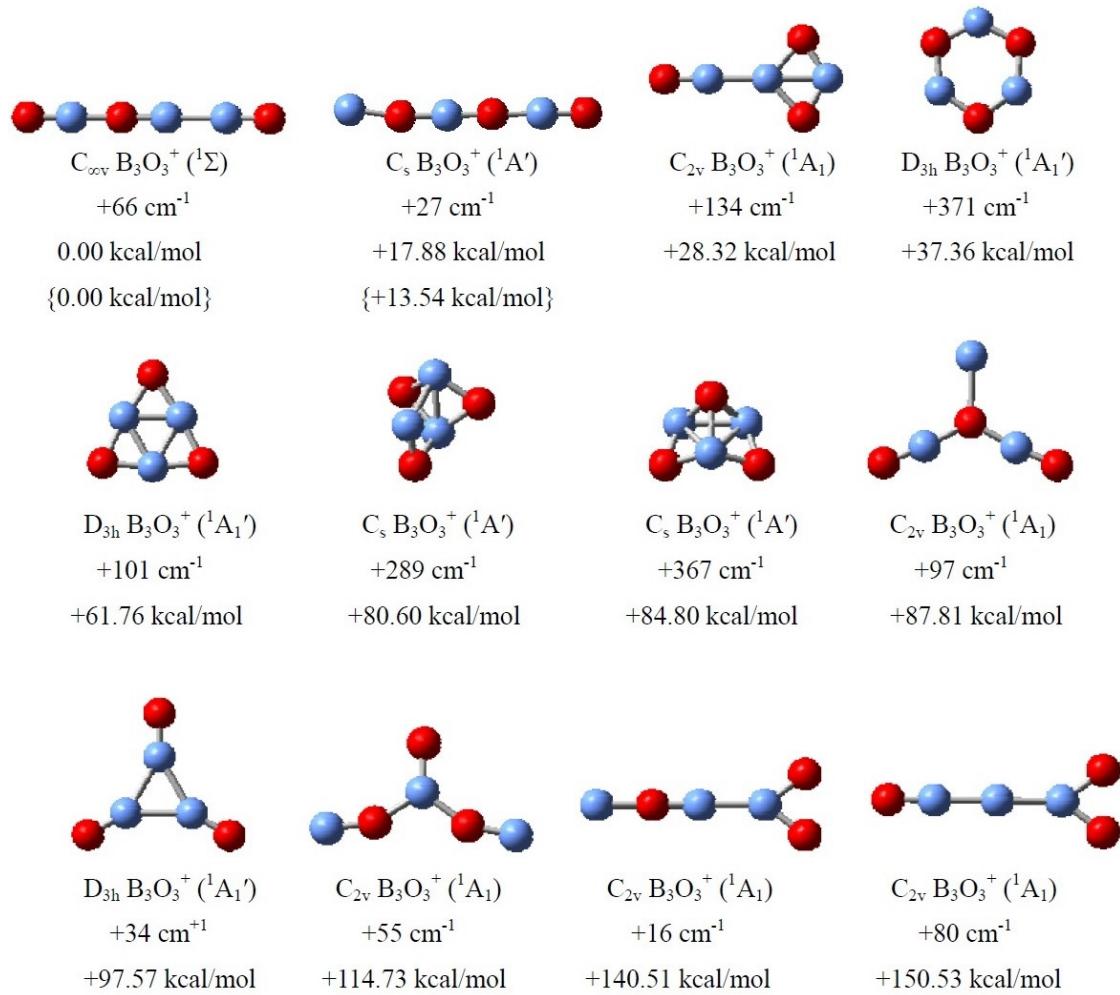


Figure S5. Alternative optimized structures for B_3O_4^- , along with their point group symmetries, electronic states, and minimum vibrational frequencies. Relative energies are given at B3LYP/aug-cc-pVTZ and CCSD(T)//B3LYP/aug-cc-pVTZ (in curly brackets). The structures were obtained initially using the Coalescence Kick and Basin Hopping global-minimum search programs at B3LYP/3-21G.

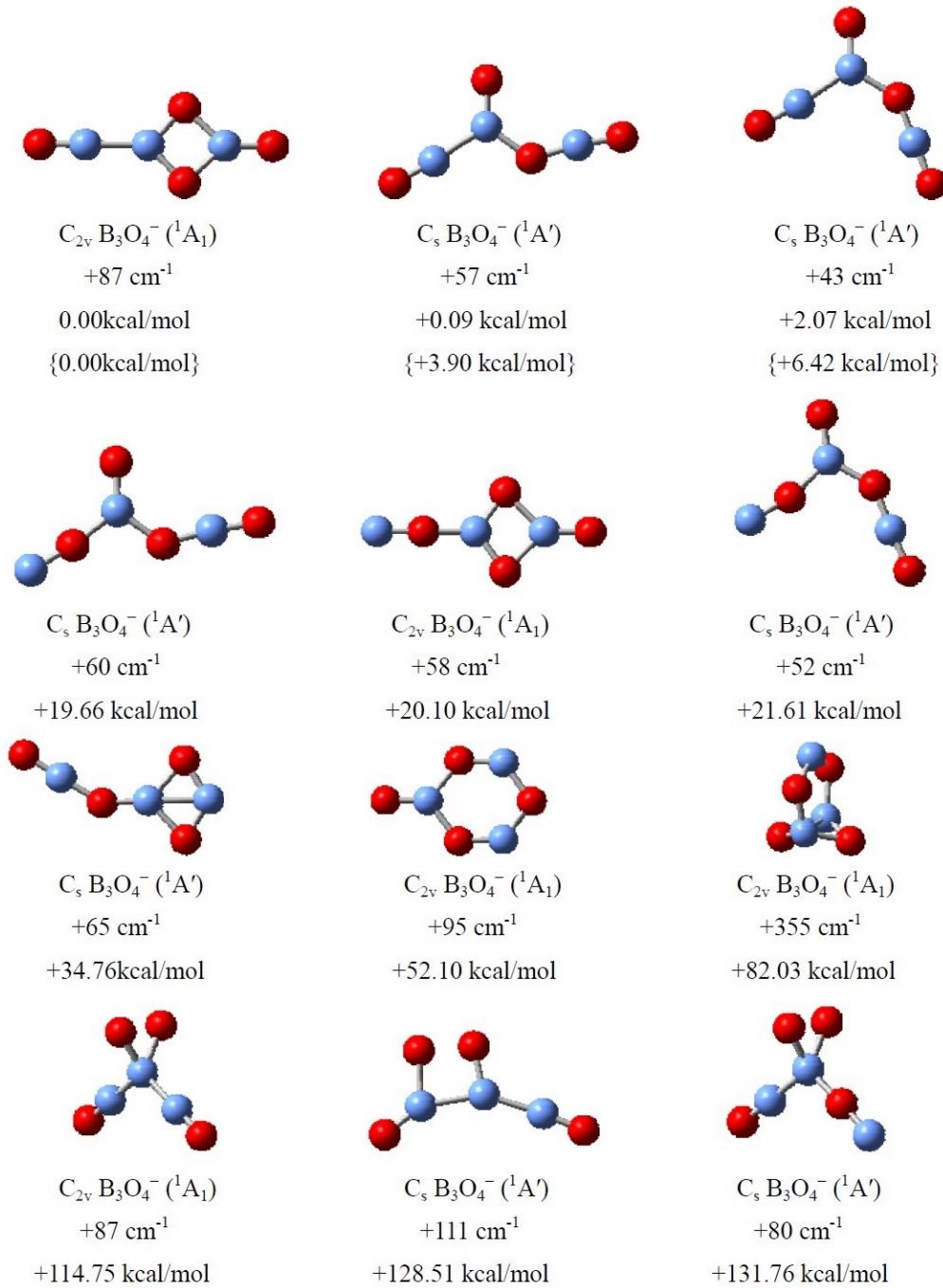


Figure S6. Alternative optimized structures for B_3O_4 , along with their point group symmetries, electronic states, and minimum vibrational frequencies. Relative energies are given at B3LYP/aug-cc-pVTZ and CCSD(T)//B3LYP/aug-cc-pVTZ (in curly brackets). The structures were obtained initially using the Coalescence Kick and Basin Hopping global-minimum search programs at B3LYP/3-21G.

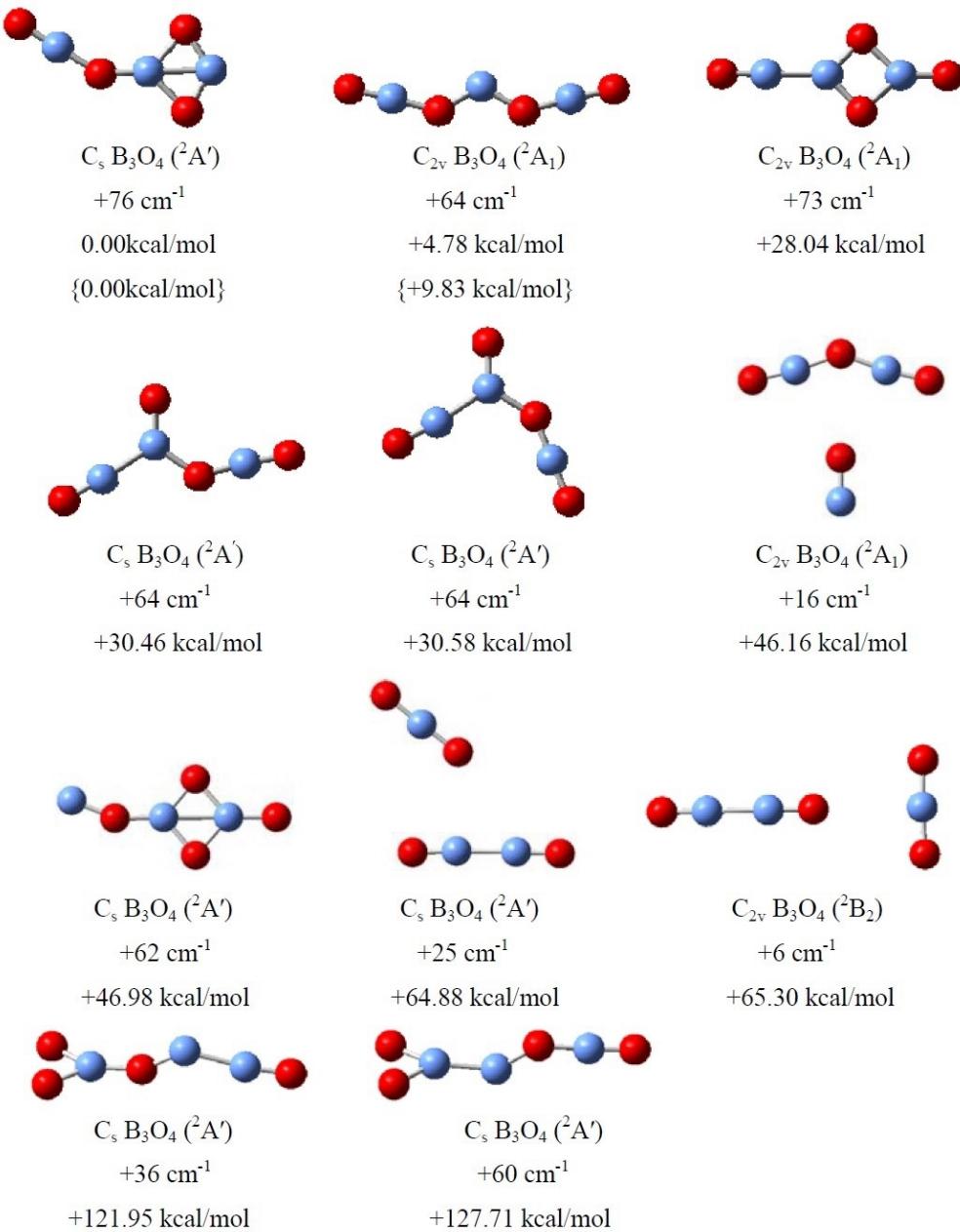


Figure S7. Alternative optimized structures for B_3O_4^+ , along with their point group symmetries, electronic states, and minimum vibrational frequencies. Relative energies are given at B3LYP/aug-cc-pVTZ and CCSD(T)//B3LYP/aug-cc-pVTZ (in curly brackets). The structures were obtained initially using the Coalescence Kick and Basin Hopping global-minimum search programs at B3LYP/3-21G.

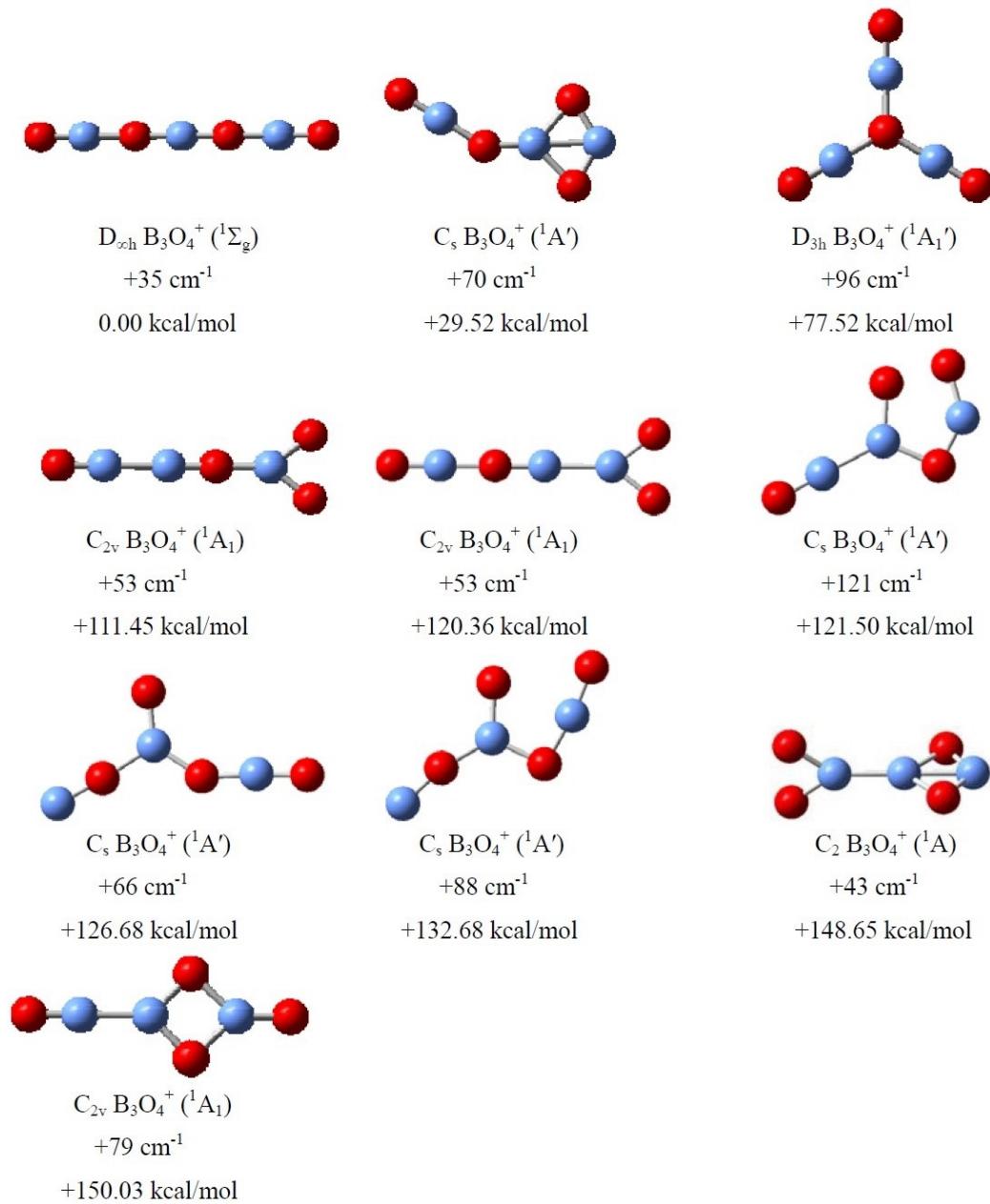
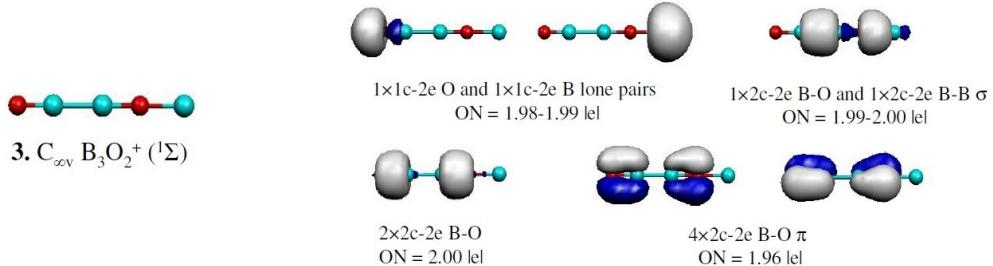


Figure S8. (a) AdNDP bonding pattern for the $C_{\infty v} B_3O_2^+ (\mathbf{3}, ^1\Sigma)$ global-minimum structure and (b) its canonical molecular orbitals (CMOs).

(a)



(b)

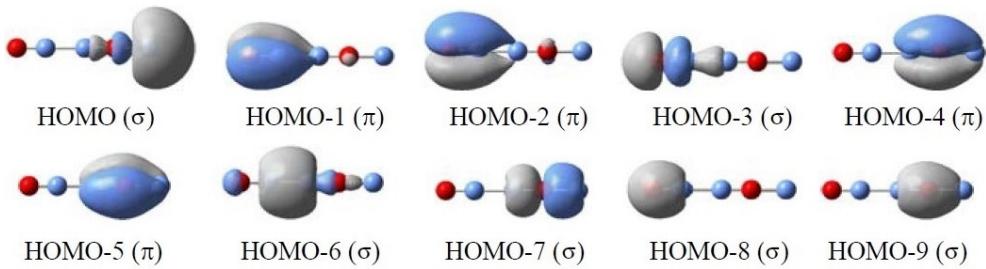
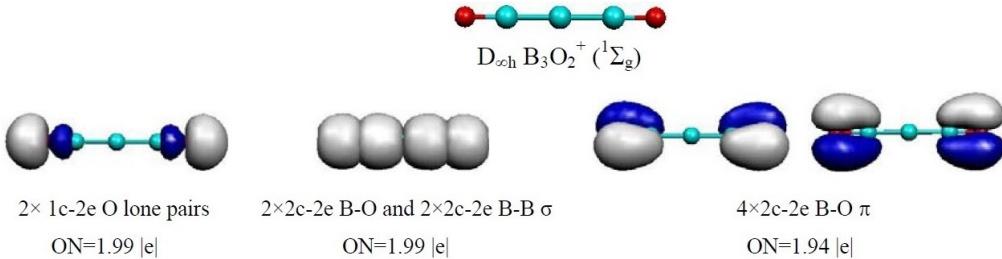


Figure S9. (a) AdNDP bonding pattern for $D_{\infty h}$ $B_3O_2^+$ (${}^1\Sigma_g$) and (b) its canonical molecular orbitals (CMOs).

(a)



(b)

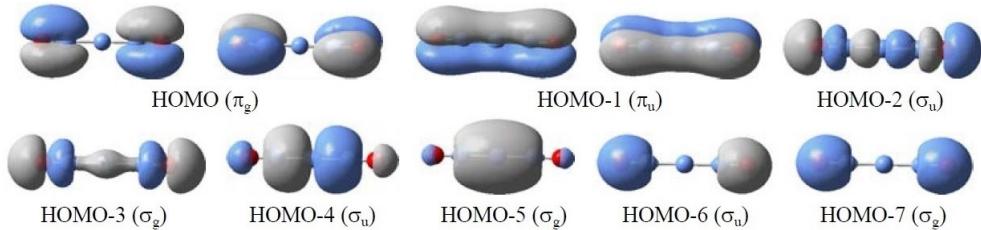
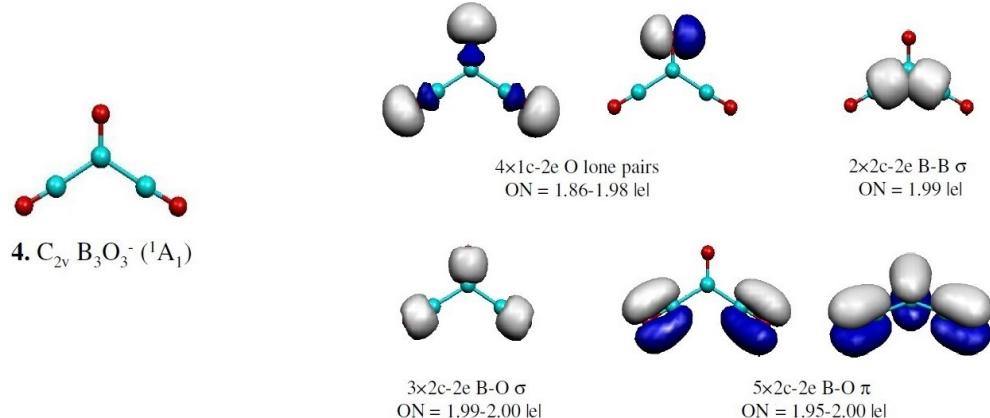


Figure S10. (a) AdNDP bonding pattern for the C_{2v} $B_3O_3^-$ (**4**, 1A_1) global-minimum structure and (b) its canonical molecular orbitals (CMOs).

(a)



(b)

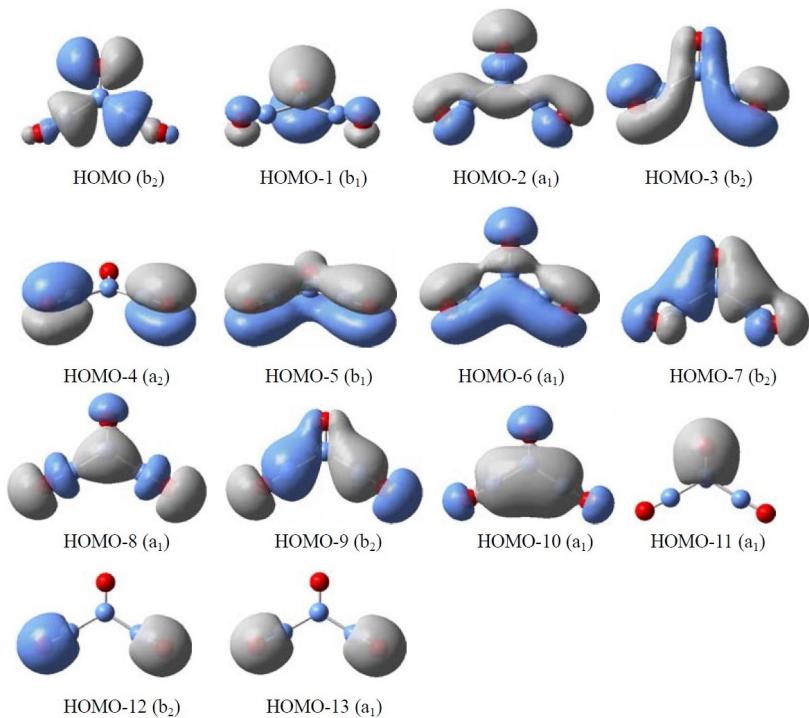


Figure S11. (a) AdNDP bonding pattern for the C_{2v} B_3O_3 (**5**, 2A_1) global-minimum structure and (b) its canonical molecular orbitals (CMOs).

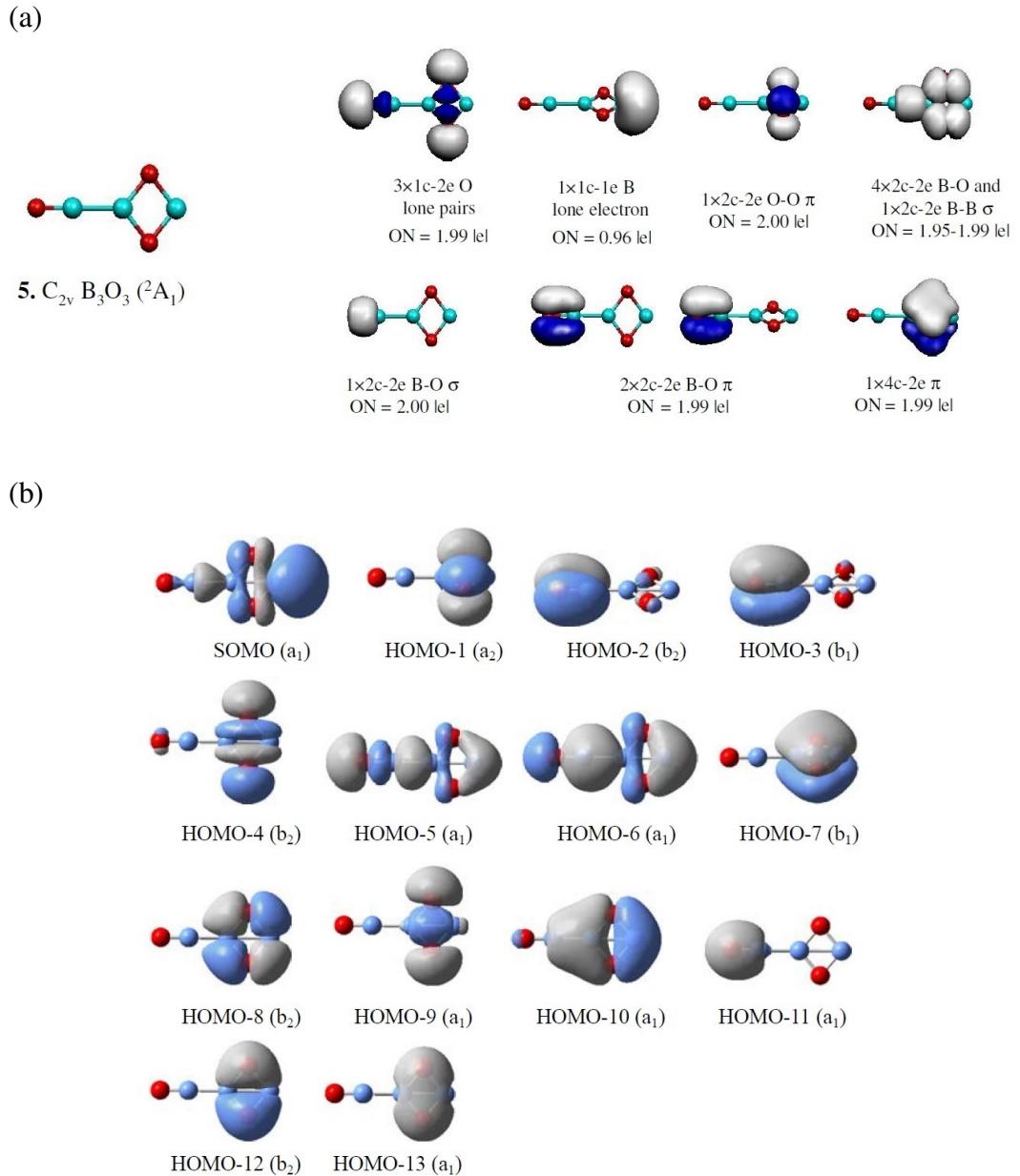
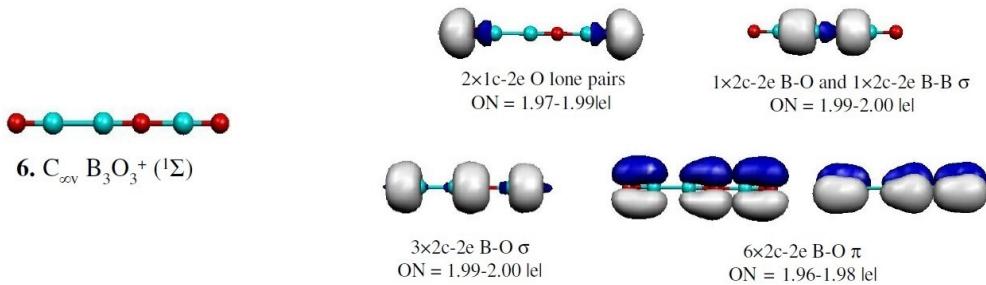


Figure S12. (a) AdNDP bonding pattern for the $C_{\infty v} B_3O_3^+ (\mathbf{6}, {}^1\Sigma)$ global-minimum structure and (b) its canonical molecular orbitals (CMOs).

(a)



(b)

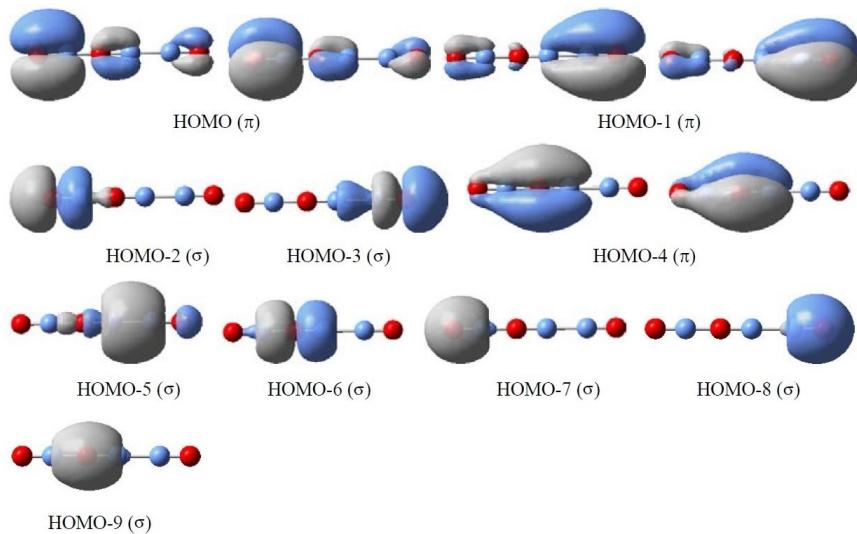


Figure S13. Canonical molecular orbitals (CMOs) for the C_{2v} $B_3O_4^-$ ($7, ^1A_1$) global-minimum structure. For its AdNDP bonding pattern, see Figure 4 in the text.

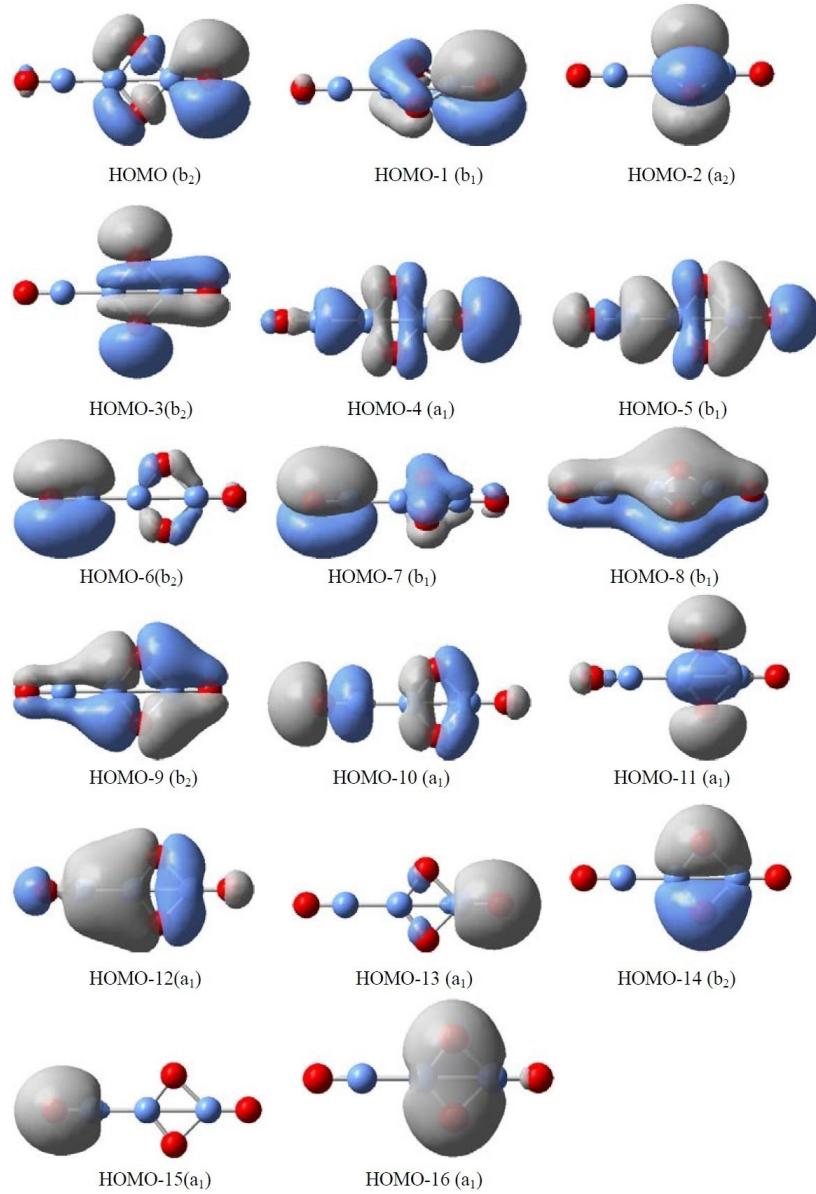


Figure S14. (a) AdNDP bonding pattern for the C_s B_3O_4 (**8**, $^2A'$) global-minimum structure and (b) its canonical molecular orbitals (CMOs).

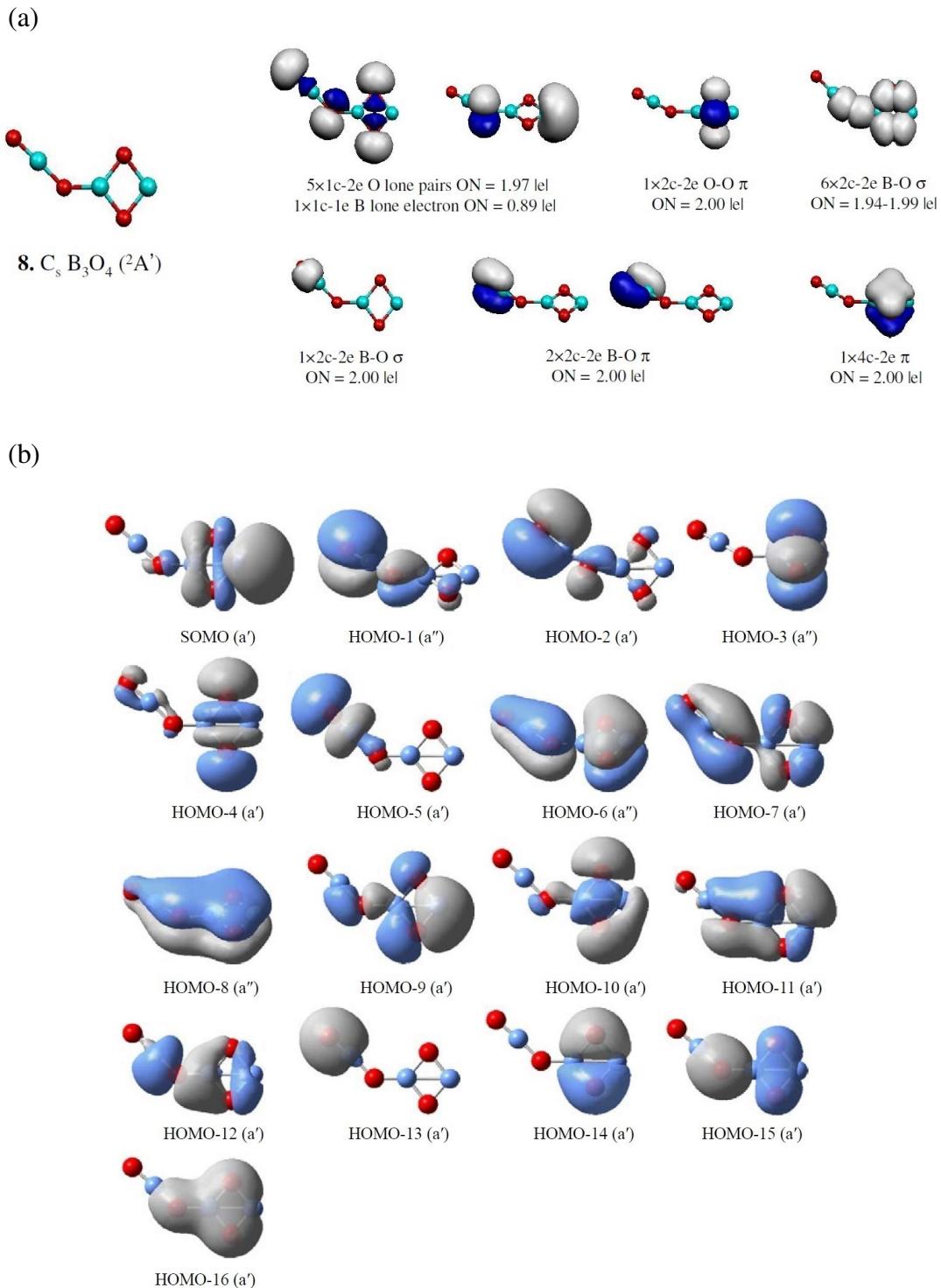
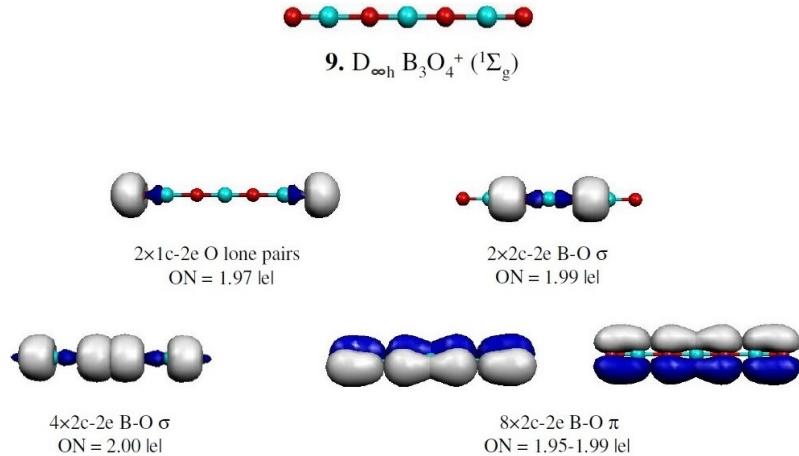


Figure S15. (a) AdNDP bonding pattern for the $D_{\infty h}$ $B_3O_4^+$ (**9**, ${}^1\Sigma_g$) global-minimum structure and (b) its canonical molecular orbitals (CMOs).

(a)



(b)

