

# Depletion NO<sub>x</sub> Made Easy by Nitrogen Doped Graphene

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Received: 19 November 2013 / Accepted: 28 February 2014 / Published online: 16 March 2014  
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**Abstract** The integrated mechanism of the catalytic oxidation of NO by N<sub>2</sub>O on the metal-free support of nitrogen doped graphene (NG) is investigated using density function theory calculations. The results indicate that the N<sub>2</sub>O can be intensively adsorbed on NG support, while the NO, N<sub>2</sub>, NO<sub>2</sub> are all weakly adsorbed. In the oxidation process, a two-step mechanism is identified: the dissociation of N<sub>2</sub>O followed by the oxidation of NO with the dissociative O-atom. The present work suggests that the NG support, as a high-efficient and metal-free catalyst, is one of the promising candidates for removing the nitrogen oxides gases exhaust.

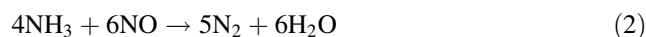
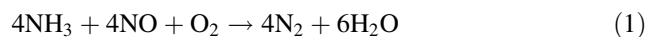
**Keywords** Metal-free · Nitrogen doped graphene · Depletion NO<sub>x</sub>

## 1 Introduction

The production of poisonous gases from the combustion of fuel, vehicles, and industrial processes is considered to be one of the big environmental issues to be solved. Among the poisonous gases, nitrogen oxides (NO<sub>x</sub>) are considered to be the most toxic gases emitted into the atmosphere. For example, the NO, a major atmospheric pollutant, has aroused wide public concern experimentally and theoretically [1–3]. N<sub>2</sub>O

has been recognized as one of the contributors to global warming and also a cause of ozone depletion [4]. So effective strategy to reduce NO and N<sub>2</sub>O is necessary for the protection of the ozone layer and control of global warming effects.

The conventional method used to reduce the NO<sub>x</sub> emissions is the selective catalytic reduction (SCR) with ammonia as the reduction agent [5–7]. The SCR processes for denoxing with ammonia as the reduction agent are:



However, the use of ammonia causes additional problems, e.g., the ammonia slip [8], which brings about additional environment problem. In the NO<sub>x</sub> depletion process using the metal-free nitrogen doped graphene (NG) catalyst, the poisonous ammonia is not needed. Additionally, the metal-free NG catalyst avoids the high costs of the traditional noble metal catalysts. Another efficient method to deplete NO is the oxidation of NO into NO<sub>2</sub>, which is then captured by water [9–12]. Moreover, given the decisive role of the NO<sub>2</sub> in exhaust gas after treatment techniques, efforts made by a number of researchers in the past decade have resulted in a wide number of catalysts for this reaction [2, 13–16].

Because of the damage of N<sub>2</sub>O to the environment, as of today, decomposition of the N<sub>2</sub>O molecule has been considered to be an efficacious method to remove it [17]. For instance, Zhao et al. [18] found that Rh/ALHT catalyst is stable for decomposition of N<sub>2</sub>O, but needs a higher start temperature. Lv et al. [19] revealed that N<sub>2</sub>O molecule decomposes easily on Al- and Ga-embedded graphene, but needs an appropriate external electric field.

As mentioned above, the poisonous NO and N<sub>2</sub>O are harmful to the environment and difficult to be eliminated.

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Therefore, finding appropriate low temperature and base metal catalysts, even metal-free catalysts, to accelerate the reactions for the abatement of NO and N<sub>2</sub>O has become a key challenge. Recently, Wang and Pantelides [20] suggested that NO can be removed easily with adsorbed O on NG based on first-principles molecular dynamics simulations. Besides, Chen et al. [1] found that NO can be easily converted into N<sub>2</sub>O through a dimer mechanism on Si-doped graphene. Zhao et al. [21] illustrated that N<sub>2</sub>O decomposition occurs easily on the same support. Although segments about the reaction of NO<sub>x</sub> (NO and N<sub>2</sub>O) are studied and described, the reaction mechanism is not well addressed. With nitrogen doping in the monolayer graphene, the spin density and charge distribution of carbon atoms will be influenced by the neighbor nitrogen dopant [22, 23], which induce the “activation region” on the graphene surface. This kind of activated region can participate in catalytic reaction directly, such as the oxygen reduction reaction [23, 24]. Whether or not the NG catalyst can catalyze the decomposition of N<sub>2</sub>O? Whether or not the NG can eliminate the NO<sub>x</sub> simultaneously? Motivated by this, we apply the first-principles calculation to study the adsorption and reaction of the poisonous gases (NO<sub>x</sub>) on NG. The reaction mechanism and the integrated reaction process are investigated. Our results demonstrate that NG, a metal-free catalyst, would be a promising candidate for eliminating the toxic NO<sub>x</sub> gases and plays an important role in the protection of the environment and resources.

## 2 Calculation Method and Model

Periodic density function theory calculations are performed using the Vienna Ab-initio Simulation Package (VASP) [25]. For improving the calculation efficiency, core electrons are replaced by the projector augmented wave pseudo-potentials [26] and the generalized gradient approximation of the Perdew, Burke, and Ernzerhof (PBE) functional [27] is used for the exchange and correlation. The wave functions are expanded in plane waves with a cut off energy of 450 eV and the convergence criterion for the electronic self-consistent iteration is set to 10<sup>-5</sup> eV. The NG layer and the adsorbates are free to relax until the self-consistent force drop to below 0.02 eV Å<sup>-1</sup>. With the purpose of avoiding the interactions due to the artificial periodicity, a vacuum layer of 15 Å is used to separate the periodic images in the direction perpendicular to the surface. The Brillouin zone integration is performed with a 3 × 3 × 1  $\Gamma$ -centered Monkhorst–Pack (MP) grid. We also make a comparison test with a 5 × 5 × 1 MP grid and find only tiny changes in energy (0.01 eV).

The climbing image nudged elastic band method (CI-NEB) [28–30] is employed to investigate the saddle points

and minimum energy paths (MEP). The spring force between adjacent images is set to 5.0 eV Å<sup>-1</sup>. Images are optimized until the forces on each atom drop to below 0.02 eV Å<sup>-1</sup>. The energy barriers are calculated using the initial state (IS) as a reference.

The Bader’s “atoms in molecules” theory [31] is used to assign charges to atoms and fragments. These charges provided useful clues to how the charge transfers between different atoms or fragments. One major issue with the normal charge density from the VASP code is that they only contain the valence charge density, which would give an unreal charge transfer of N dopant by Bader charge analysis in the NG systems. Considering this point, the core charge is included for Bader charge analysis in the current study, by which a real charge transfer could be obtained.

The adsorption energy is defined by the formula.

$$E_{\text{ad}} = E_{\text{NG}} + E_{\text{X}} - E_{(\text{X}/\text{NG})} \quad (3)$$

where  $E_{(\text{X}/\text{NG})}$  and  $E_{\text{NG}}$  are the spin-polarized total energies for the optimized equilibrium configurations of NG with and without gas adsorbate (X), respectively, and  $E_{\text{X}}$  is the spin-polarized total energy of the corresponding isolated gas molecule in its ground state. With this definition, a higher  $E_{\text{ad}}$  value means a stronger adsorption.

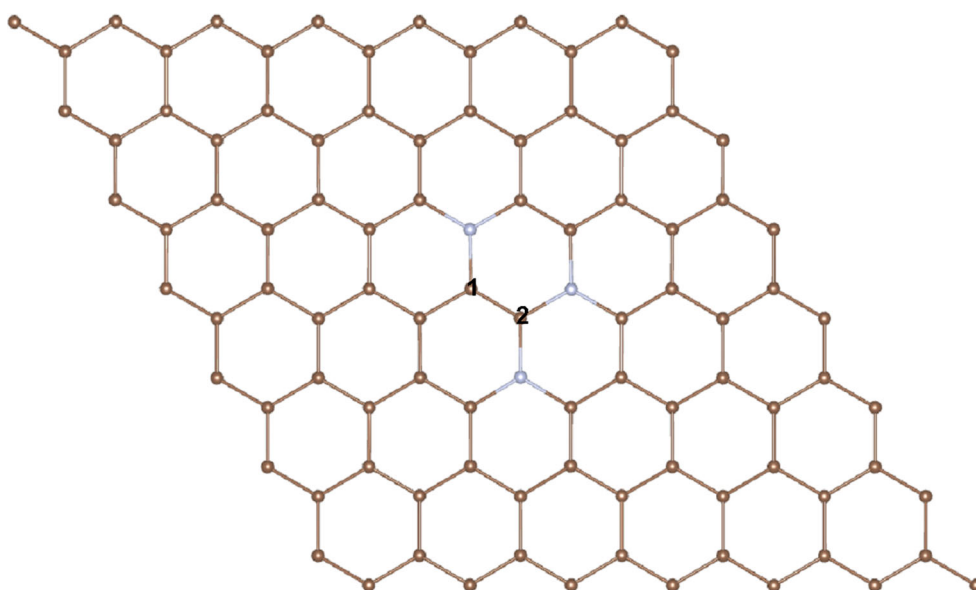
The NG system is modeled using a 6 × 6 hexagonal graphene supercell with three substitutional nitrogen dopant atoms as shown in Fig. 1 (all figures generated using the VESTA package) [32]. Our previous work [33] has proved that such a NG system has high catalytic activity for oxygen dissociation. Electrochemical tests also indicated that this catalyst had the highest activity for oxygen reduction via a four-electron pathway. Using first-principles calculation method, Feng et al. [34] revealed that nitrogen clusters other than the isolated one are the most efficient catalytic sites for oxygen reduction. In addition, Yang and colleague [35] also pointed out that this kind of nitrogen has a higher catalytic effect for oxygen dissociation than other types, such as pyridine-like nitrogen atoms. Based on these facts, we use the NG model as the substrate in all of our calculations. The calculated lattice constant of pristine graphene (PG) is 2.46 Å, which is consistent with the values of other groups [36–38]. The C–N bond length in the optimized NG is 1.41 Å, which is reduced by 0.1 Å compared with C–C bond length in the PG, 1.42 Å, in agreement with the results of Dai et al. [39].

## 3 Results and Discussion

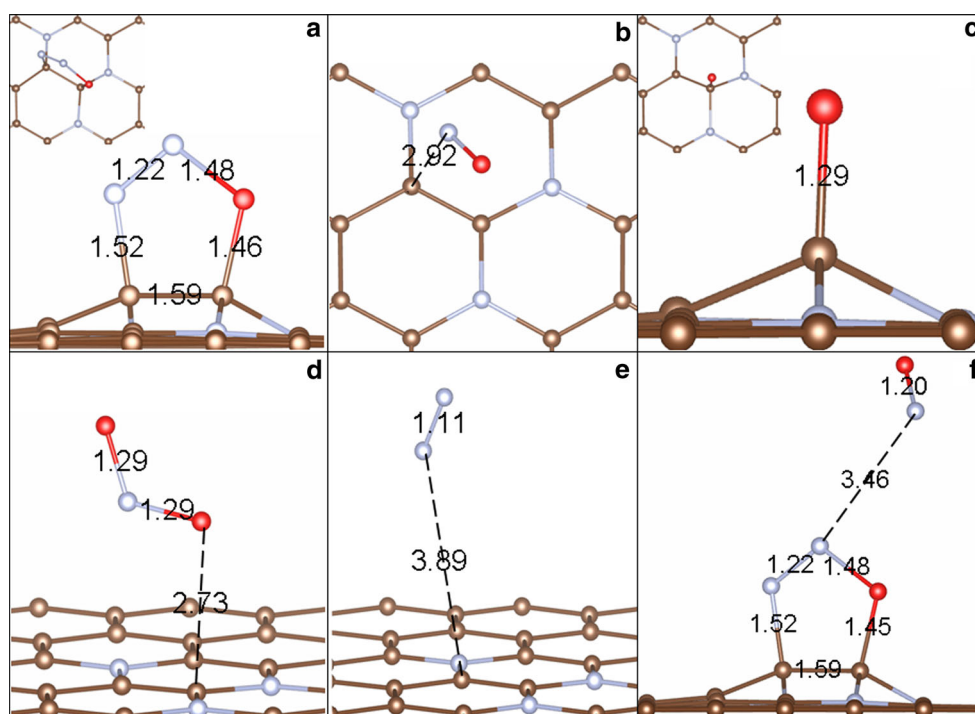
### 3.1 The Adsorption of Toxic Gases on NG

Before exploring the catalytic oxidation of NO by N<sub>2</sub>O, we start our study by investigating the geometric structure of

**Fig. 1** The top view of the nitrogen doped graphene model. Hereafter, the *brown* and *blue* spheres denote the C and N atoms, respectively



**Fig. 2** The most stable configuration of various reaction or intermediate gases adsorbed on the nitrogen doped graphene (NG): **a**  $\text{N}_2\text{O}$ , **b**  $\text{NO}$ , **c** atomic O, **d**  $\text{NO}_2$ , **e**  $\text{N}_2$ , **f**  $\text{N}_2\text{O}$  and  $\text{NO}$  coadsorption. The *inset* pictures in **a** and **c** are the top views. *Red* spheres denote O atoms



toxic gases adsorption on NG. For each adsorbate, we consider various adsorption sites and different adsorption patterns. In Fig. 2, we depict the most stable configurations for each adsorbate and intermediate products. The corresponding adsorption energies, the shortest distance between adsorbate and support and the bond lengths of the reaction gases before (after) adsorption are listed in Table 1. The corresponding quantitative effects of the van-der-Waals (vdW) correction [40] are examined. It is found that the vdW correction becomes important when the adsorption energy is small enough. The adsorption energies increase quite a lot,

while the adsorbate-NG distances ( $d_{\text{nn}}$ ) decrease accordingly, indicating that the calculations without the vdW corrections underestimate the strength of the adsorption. However, the adsorption can still be assigned as physisorption, which has relatively small adsorption energies, large adsorbate-NG distances ( $d_{\text{nn}}$ ) and almost unchanged intramolecular distances ( $d_{\text{N-N}}$  or  $d_{\text{N-O}}$ ). In the following, we will mainly present the results without the vdW corrections.

The calculated results indicate that  $\text{N}_2\text{O}$  is intensely adsorbed on NG and the most stable adsorption configuration is that the N- and O-atoms of  $\text{N}_2\text{O}$  bind with the C-C bond

**Table 1** Adsorption energy ( $E_{\text{ad}}$ ) of reactants and intermediate products adsorbed on NG, the shortest distance between the adsorbates and NG ( $d_{\text{nn}}$ ), the N–N ( $d_{\text{N–N}}$ ) and/or N–O ( $d_{\text{N–O}}$ ) bond lengths of the reaction gases before (after) adsorption

Adsorbate	$E_{\text{ad}}$ (eV)		$d_{\text{nn}}$ (Å)		$d_{\text{N–N}}$ (Å)		$d_{\text{N–O}}$ (Å)	
N <sub>2</sub> O	2.67 <sup>a</sup>	–	1.46 <sup>a</sup>	–	1.15 (1.22) <sup>a</sup>	–	1.23 (1.48) <sup>a</sup>	–
NO	0.23 <sup>a</sup>	0.65 <sup>b</sup>	2.92 <sup>a</sup>	2.37 <sup>b</sup>	–	–	1.19 (1.22) <sup>a</sup>	1.20 (1.23) <sup>b</sup>
O	5.06 <sup>a</sup>	5.22 <sup>b</sup>	1.29 <sup>a</sup>	1.29 <sup>b</sup>	–	–	–	–
N <sub>2</sub>	0.03 <sup>a</sup>	0.20 <sup>b</sup>	3.89 <sup>a</sup>	3.65 <sup>b</sup>	1.11 (1.11) <sup>a</sup>	1.11 (1.11) <sup>b</sup>	–	–
NO <sub>2</sub>	0.30 <sup>a</sup>	0.77 <sup>b</sup>	2.73 <sup>a</sup>	2.59 <sup>b</sup>	–	–	1.28 (1.29) <sup>a</sup>	1.28 (1.30) <sup>b</sup>

The superscripts “a” and “b” represent for the results without and with van-der-Waals correction, respectively

surrounded by three nitrogen atoms and form a five-member ring, which is similar to the N<sub>2</sub>O adsorbed on Si-embedded graphene [21]. In this most stable geometry, the adsorbate and the support are all distorted seriously, as shown in Fig. 2a, where the insert picture is a top view. The calculated adsorption energy is 2.67 eV with quite amount of electrons (0.50 e) transferred from NG to N<sub>2</sub>O.

The adsorptions of NO and N<sub>2</sub> all can be assigned as physisorption both for the cases with and without the vdW correction. The end-on configuration is favored with the lowest  $E_{\text{ad}}$  values and large  $d$  values as shown in Fig. 2b and e, respectively. The weak physisorption is further verified by the negligible amounts of charge transfer, 0.09 and 0.02 e from NG for NO and N<sub>2</sub> adsorption, respectively. When the vdW force is considered, the adsorption is enhanced with the shortest distances between the adsorbates and NG shortened from 2.92 to 2.37 Å for NO and from 3.89 to 3.65 Å for N<sub>2</sub>, while the most stable adsorption configurations remain unchanged.

The atomic O, a kind of intermediate product, can be strongly bound to the top site of the carbon atom that directly connects with the two nitrogen dopant atoms as shown in Fig. 2c, with an  $E_{\text{ad}}$  of 5.06 eV and the C–O bond length of 1.29 Å. There are 0.80 electrons transferred from NG to O atom, which makes the C–C length elongated from 1.42 to 1.52 Å and the bonded carbon atom dragged by 0.04 Å away from the support surface. This observation indicates that the oxygen atom can strongly pull the charge back from the NG support due to its strong electronegativity and lead to an intense interaction.

The most energetically favorable adsorption configuration of NO<sub>2</sub> is shown in Fig. 2d. The adsorbed NO<sub>2</sub> has a quite large distance (2.73 Å) from the support. The calculated adsorption energy is 0.30 eV accompanied by a charge transfer of 0.60 e from NG to NO<sub>2</sub>, which leads to the N–O bond enlarged from 1.28 to 1.29 Å. Upon considering vdW correction, the shortest distance between NO<sub>2</sub> and the NG support is reduced to 2.59 Å and the adsorption energy is increased to 0.77 eV. Similar to NO and N<sub>2</sub>, the intramolecular configuration of NO<sub>2</sub> is kept its optimal configuration whatever the vdW correction is considered or not.

### 3.2 The Oxidation of NO by N<sub>2</sub>O on NG

According to the possible situation of two reactant gases (nitrous oxide and nitric oxide) completely mixed, the reaction mechanisms are divided into two pathways depending on the adsorption strength, i.e., the Eley–Rideal (ER) and Langmuir–Hinshelwood (LH) mechanisms. For the ER mechanism, the gas-phase NO molecule approaches and reacts with the already-activated N<sub>2</sub>O, while the LH mechanism involves the coadsorption of NO and N<sub>2</sub>O molecules before reaction.

Comparing the adsorption properties of NO on NG with that of N<sub>2</sub>O, we found that the N<sub>2</sub>O molecule is preferred to be attached to the NG support surface than NO. Therefore, when NO and N<sub>2</sub>O mixture is injected as the reaction gas, the NG support would be covered by the N<sub>2</sub>O molecule. To verify this, we make a test by exploring the coadsorption of NO and N<sub>2</sub>O. The most stable coadsorption configuration is exhibited in Fig. 2f, which shows clearly that the activity region of NG are completely occupied by N<sub>2</sub>O when NO and N<sub>2</sub>O are coadsorbed. The calculated coadsorption energy is 2.73 eV, which is slightly smaller than the sum of the respective adsorption energies of NO and N<sub>2</sub>O (2.67 + 0.25 = 2.92 eV) on NG, indicating that the cooperative adsorption of NO and N<sub>2</sub>O is weak. Our simulation results show that the shortest distance between NO and N<sub>2</sub>O is 3.45 Å, which is in line with the weak coadsorption effect. In short, all the results indicate that there is only a quite weak interaction between NO and N<sub>2</sub>O.

On the basis of these results, we conclude that it is quite hard for the NO and N<sub>2</sub>O reaction to occur on NG along the LH mechanism. So, we turn our attention to the ER mechanism.

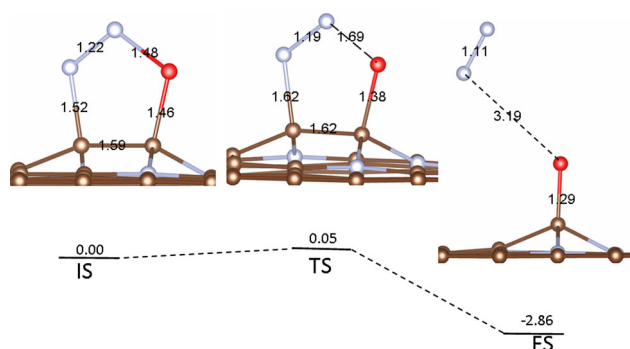
The reaction mechanism is proposed to occur in step-wise reactions, i.e., the decomposition of N<sub>2</sub>O followed by the oxidation of NO as presented in formulas (4) and (5).

The adsorption and decomposition of N<sub>2</sub>O:



The adsorption and oxidation of NO:



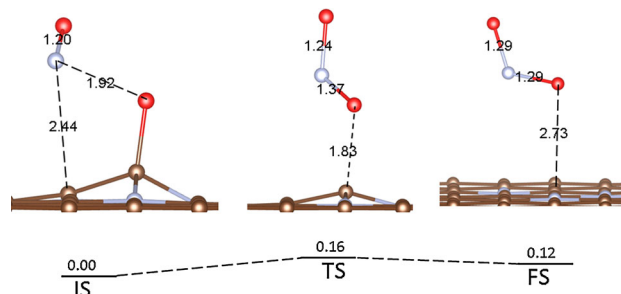


**Fig. 3** The MEP for the decomposition of the  $\text{N}_2\text{O}$  on NG. All energies are reported in eV relative to the initial state and the distances are in angstrom

Firstly, we discuss the  $\text{N}_2\text{O}$  decomposition on NG. To search for the MEP for this reaction, we selected the configuration shown in Fig. 2a as the IS. The final state (FS) is that a  $\text{N}_2$  molecule physically adsorbed on NG with a chemisorbed atomic O at the top site of carbon atom. The corresponding MEP profile is summarized in Fig. 3. The energetic is schematically plotted with respect to the reference energy of the IS. The local configurations of the adsorbate on NG at various states along the MEP are also displayed in Fig. 3, which shows that the N–O and N–C bonds are elongated from 1.48 and 1.52 Å in the IS to 1.69 and 1.62 Å in the transition state (TS), respectively, with a rather small energy barrier of 0.05 eV along the reaction pathway. The C–C bond connected to the  $\text{N}_2\text{O}$  in the substrate is also elongated (from 1.59 to 1.62 Å). In contrast, the N–N and C–O bonds are shrunk from 1.22 and 1.46 Å to 1.19 and 1.38 Å, respectively. Finally, the C–N–N–O–C five-member ring is broken, resulting in the formation of a  $\text{N}_2$  molecule and an atomic O adsorbed on the C atom (denoted as O/NG, the NG with atomic O adsorbate) as shown in the FS.

Due to the weak interaction between the  $\text{N}_2$  molecule and the O/NG ( $E_{\text{ad}} = 0.03$  eV), the  $\text{N}_2$  molecule can be easily desorbed. The energy released in the dissociation of  $\text{N}_2\text{O}$  on NG is 2.86 eV. In light of the small barrier (0.05 eV) and large exothermicity (2.86 eV), it is expected that the dissociation of  $\text{N}_2\text{O}$  can be achieved easily on the metal-free NG support.

The decomposition process of  $\text{N}_2\text{O}$  found in this paper is similar to that on the Si-embedded graphene [21], but different from that on the Fe-embedded graphene [41], which indicated that the decomposition barriers of  $\text{N}_2\text{O}$  on Si-embedded graphene and Fe-embedded graphene is about 0.02 and 0.35 eV, respectively. Our calculated barrier (0.05 eV) is comparable with that on the Si-embedded graphene (0.02 eV) and much smaller than those on the transition metals [17], e.g., Fe (41 kJ mol<sup>-1</sup>), Co (28 kJ mol<sup>-1</sup>) and Rh (35 kJ mol<sup>-1</sup>). More importantly,



**Fig. 4** The MEP for the NO oxidation by the dissociative O

the NG support is metal-free. In addition, compared with the Rh/ALHT catalyst [18], the NG could work at low temperature and does not need external electric field [19]. It is therefore expected that the NG is an excellent metal-free catalyst for the abatement of  $\text{N}_2\text{O}$ .

Since an atomic O is left on the NG support in the process of  $\text{N}_2\text{O}$  dissociation, it is necessary to explore whether this atomic O can be further reduced by subsequent NO molecules via ER mechanism. It is expected that the NO molecule can be oxidized easily by the O/NG intermediate due to the strong negative charge on the O atom, which can attract the N atom of the NO. This has been verified by Wang and Pantelides [20].

The adsorption and oxidation of NO on the O/NG are studied. The process is depicted in Fig. 4, where a NO is initially adsorbed with a configuration as shown Fig. 4a (IS) and the FS is set as the configuration with  $\text{NO}_2$  adsorbed on the NG (as shown Fig. 2d). The simulation results indicate that the N-atom of NO first approaches the adsorbed O-atom and reaches the TS. The distance between NO and the O atom is shortened from 1.92 Å of IS to 1.37 Å of TS in this endothermic process. At the same time, a  $\text{NO}_2$ -like molecule is formed and sits at the height of 1.83 Å above the NG. The transition barrier is 0.16 eV. Passing over the TS, a  $\text{NO}_2$  molecule is formed and desorbed, leading to the recovery of the NG. Once formed, the  $\text{NO}_2$  can be collected easily by water [9–12], resulting in the useful product, such as  $\text{H}_2\text{NO}_3$ . Our calculated barrier for NO oxidation on NG (0.16 eV) is much smaller than the result of Schneider et al. [15] for the NO oxidation on Pt(111) (1.28 eV), indicating that the NO oxidation is more moderate on the metal-free NG catalyst than on the noble metal Pt. Additionally, Oliver et al. [2] pointed out that  $\text{NO}_2$  as the product of NO oxidation on Pt/SiO<sub>2</sub> inhibits the further oxidation of NO. They also suspected that this catalyst would be deactivated because the formation of platinum oxide on the surface of the platinum particles. In contrast, the NG catalyst proposed here can conquer these obstacles completely.

The influence of vdW correction on the barrier energies is also considered. It is found that on the one hand, when

the vdW correction is considered, the interaction between N<sub>2</sub>O and the NG support is enhanced and the barrier of the N<sub>2</sub>O decomposition is changed to almost 0.00 eV, corresponding to the spontaneous decomposition of N<sub>2</sub>O, which is in agreement with the case for the results of the N<sub>2</sub>O decomposition (with a barrier of 0.05 eV) without the vdW correction.

On the other hand, when the vdW correction is considered, the NO oxidation process is the same and the geometric configuration is almost unchanged compared with the result without including the vdW correction, but the barrier increases to 0.26 from 0.16 eV.

In conclusion, the results testify again that the NG support is a high-efficient metal-free catalyst for the catalytic oxidation of NO by N<sub>2</sub>O.

It should be pointed out that, in the catalysis theory, the overall barrier is important rather than a particular barrier. Usually, if one of the intermediate reactions is endothermic, the overall barrier can be higher than all the particular ones. Then, the overall barrier should be equal to the highest particular one [21, 42]. For the stepwise oxidation process of NO by N<sub>2</sub>O on NG, the oxidation of NO by O adatom on NG is the rate-limiting step with a small barrier of 0.26 eV. The results indicate that the NG as a metal-free catalyst exhibits high catalytic activity for NO oxidation by N<sub>2</sub>O, and may be a promising candidate as a substitute for noble metal catalyst.

The high reaction activity of NG toward the NO catalytic oxidation by N<sub>2</sub>O can be further understood according to the Bader charge analysis. The results are shown in Table 2, which shows that the C<sub>1</sub> and C<sub>2</sub> atoms in the center of the N dopant cluster lose about 0.47 and 0.68 electrons, respectively. The carbon dimer, which loses 1.15 e in total, is just the most preferred adsorption site and the active center for the catalytic oxidation of NO by N<sub>2</sub>O. Compared with the pure the NG support, the C-dimer further loses electrons (1.45–1.69 vs 1.15) with the adsorption of N<sub>2</sub>O and O, respectively. The same phenomenon was observed when the NO, N<sub>2</sub> and NO<sub>2</sub> were adsorbed on the NG support as shown in Table 2, indicating that the electrons transferred from the NG support to the adsorbates are mainly from the carbon dimer. For example, upon the cleavage of the N–O bond of the N<sub>2</sub>O on the NG support (Fig. 3), the C-dimer loses about additional 0.53 electrons. Compared the situation of O adsorption with that of N<sub>2</sub> and O coadsorption, the same amount of charge transfer is found at the C-dimer, indicating that the N<sub>2</sub> molecule has almost no interaction with the NG support, which is in line with the weak adsorption as mentioned above. We also find that in this process the effect of C<sub>2</sub> atom is more important than the C<sub>1</sub> atom because of the more charge transfer of the C<sub>2</sub> atom. The same effect is observed in the process of NO oxidation by O atom.

**Table 2** The results of Bader charge analysis (in *e*)

adsorbate	q(adsorbate)	q(C <sub>1</sub> )	q(C <sub>2</sub> )	q(C-dimer)
pure	–	–0.47	–0.68	–1.15
N <sub>2</sub> O	0.50	–0.34	–1.11	–1.45
N <sub>2</sub>	0.02	–0.40	–0.85	–1.25
O	0.80	–0.39	–1.30	–1.69
NO <sub>2</sub>	0.60	–0.36	–1.00	–1.36
NO	0.09	–0.43	–1.00	–1.43
O+NO	0.68	–0.45	–1.18	–1.63
N <sub>2</sub> +O	0.55	–0.38	–1.30	–1.68

q(adsorbate) stands for the total charge on the adsorbate. q(C<sub>1</sub>) and q(C<sub>2</sub>) represent the charge of the C<sub>1</sub> and C<sub>2</sub> atoms as labeled in the Fig. 1 and the q(C-dimer) represent the total charge of C<sub>1</sub> and C<sub>2</sub>. The positive and negative numbers represent the electrons accumulation and depletion, respectively

According to the results above, the process of the NO<sub>x</sub> depletion process on NG could be summarized as N<sub>2</sub>O + NO → N<sub>2</sub> + NO<sub>2</sub>, and the best content of NO and N<sub>2</sub>O for the NO depletion on NG is 1:1 (mole ratio). If the content of NO is higher than N<sub>2</sub>O, in order to remove NO sufficiently, additional oxygen molecule would be needed. Fortunately, the dissociation of O<sub>2</sub> is very moderate on NG as mentioned above [23, 24, 33, 35]. So, when N<sub>2</sub>O is scanty, the O<sub>2</sub> could be used as oxidant. In this case, the best mole ratio of NO, N<sub>2</sub>O and O<sub>2</sub> is 4:2:1. This can be summarized as 4NO + 2N<sub>2</sub>O + O<sub>2</sub> → 2N<sub>2</sub> + 4NO<sub>2</sub>.

It is worth noting that the content of N<sub>2</sub>O is smaller than NO in exhaust gases practically. When O<sub>2</sub> is insufficient, the N<sub>2</sub>O could be dissociated completely; but the NO may be spillover. However, if the content of O<sub>2</sub> is enriched or is comparable with N<sub>2</sub>O, the NO could be removed completely; but it may result in a competition reaction and N<sub>2</sub>O spillover. Keeping this in mind, future experimental studies are greatly desired to probe the optimal ratio of N<sub>2</sub>O and O<sub>2</sub>.

## 4 Conclusion

The adsorption and reaction properties of NO<sub>x</sub> on NG are discussed. The reaction mechanism and the minimum energy path are addressed. It is found that the N<sub>2</sub>O molecule can be strongly adsorbed on the NG, while the NO, N<sub>2</sub> and NO<sub>2</sub> can only be weakly adsorbed. When the vdW correction is considered, the adsorption energies are enhanced by about 0.4 eV with the adsorbate-NG distances shortened for NO, N<sub>2</sub> and NO<sub>2</sub>. However, the adsorption configurations almost remain unchanged. The minimum energetic reaction path is evaluated. The results show that the N<sub>2</sub>O adsorbed on NG can be decomposed easily into atomic O and N<sub>2</sub> with a barrier of 0.05 eV. Then the adsorbed NO molecule can be oxidized readily by the

atomic O with a barrier of 0.16 eV. The present work suggests that NG is an efficient metal-free catalyst for NO catalytic oxidation by N<sub>2</sub>O and is one of the promising candidates for solving the environmentally harmful exhaust NO<sub>x</sub> from vehicles and industrial wastes.

**Acknowledgments** This work is supported by the National Natural Science Foundation of China (Grant No. 11174070 and 11147006). Z. Lu also acknowledges the support from the China Postdoctoral Science Foundation funded project (Grant No. 2012M521399) and Postdoctoral Research sponsorship in Henan Province (Grant No. 2011038), Foundation for the Key Young Teachers of Henan Normal University and Start-up Foundation for Doctors of Henan Normal University. Parts of the simulations are performed on resources provided by the high-performance computing center of College of Physics and Electronic Engineering in Henan Normal University.

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