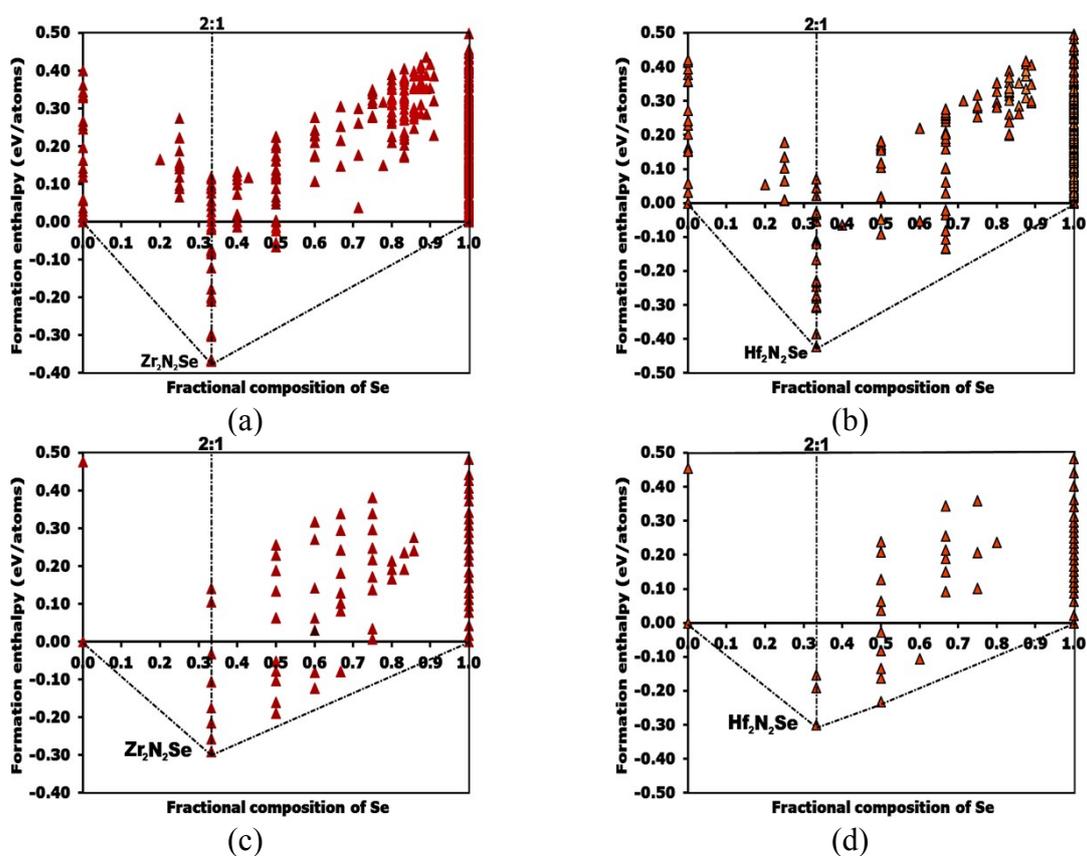
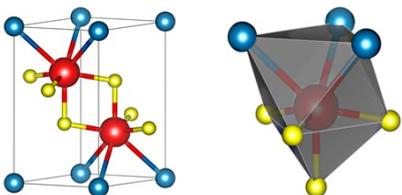
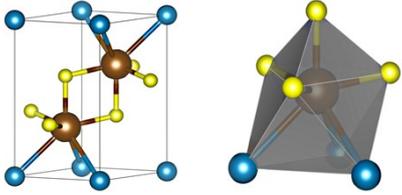


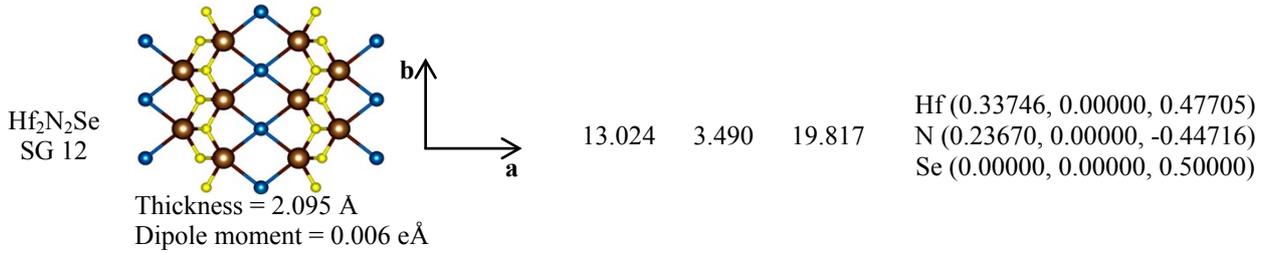
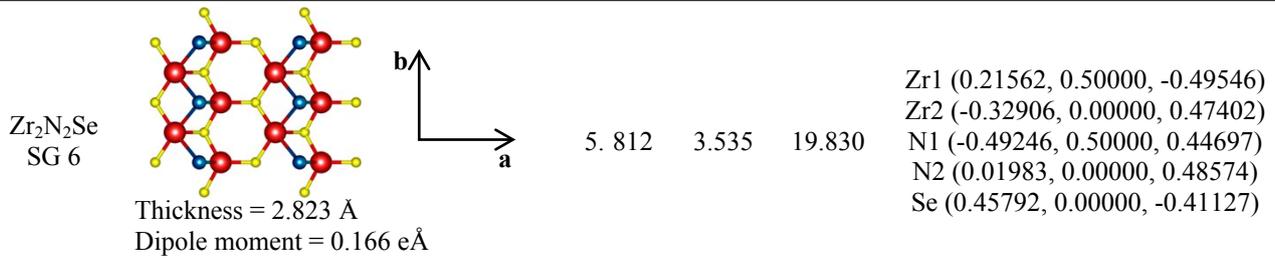
Supplementary file



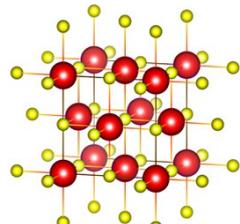
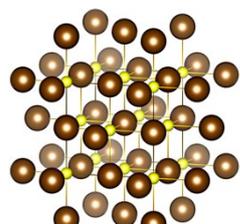
**S1** Convex hull plot for (a)  $P\bar{3}m1$ - $Zr_2N_2Se$  and (b)  $P\bar{3}m1$ - $Hf_2N_2Se$  phases, (c)  $P1m1$ - $Zr_2N_2Se$  and (d)  $C2/m$ - $Hf_2N_2Se$  monolayers.

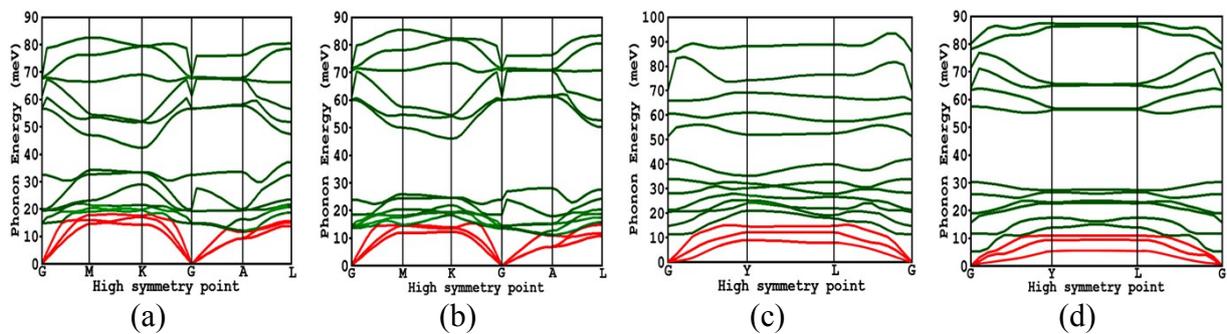
**T1** Calculated structural data for energetically stable (a)  $\alpha$ - $Zr_2N_2Se$  and (b)  $\alpha$ - $Hf_2N_2Se$  phases. Top view of (c)  $P1m1$ - $Zr_2N_2Se$  and (d)  $C2/m$ - $Hf_2N_2Se$  monolayers. Red, brown, blue and yellow spheres indicate Zr, Hf, Se and N atoms, respectively.

Phase	Unit cell	Lattice constants / $\text{\AA}$			Atomic Wyckoff positions
		<i>a</i>	<i>b</i>	<i>c</i>	
$Zr_2N_2Se$ SG 164		3.659	3.659	6.687	Zr (0.33333, 0.66667, 0.30472) N (0.33333, 0.66667, -0.36850) Se (0.00000, 0.00000, 0.00000)
$Hf_2N_2Se$ SG 164		3.623	3.623	6.655	Hf (0.33333, 0.66667, -0.30511) N (0.33333, 0.66667, 0.36841) Se (0.00000, 0.00000, 0.00000)

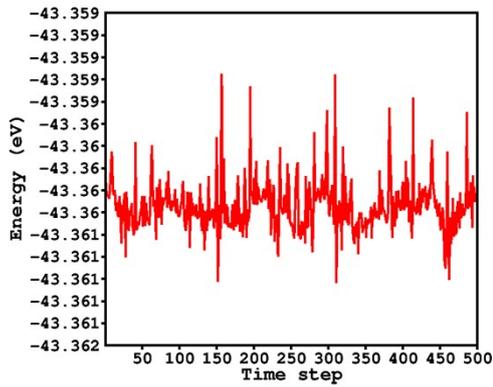


**T2** Crystallographic data of experimentally proven  $Zr_3N_3$  and  $Hf_4N_4$  phases. Red, brown and yellow spheres denote the Zr, Hf and N atoms, respectively. Refs [1-2] indicate their experimentally verified crystal class and lattice constants.

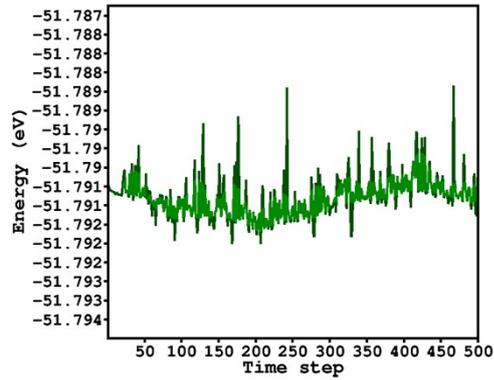
Phase	Unit cell structure	Lattice parameters / Å	Wyckoff position
$Fm\bar{3}m$ - $Zr_3N_3$ (SG 225)		$a = 4.59537$ $a = 4.56750$ [1]	Zr (0.00000, 0.00000, 0.00000) N (0.50000, 0.50000, 0.50000)
$Fm\bar{3}m$ - $Hf_4N_4$ (SG 225)		$a = 4.53684$ $a = 4.53000$ [2]	Hf (0.50000, 0.50000, 0.50000) N (0.00000, 0.00000, 0.00000)



**S2** Phonon dispersion curve for (a)  $P\bar{3}m1$ - $Zr_2N_2Se$ , (b)  $P\bar{3}m1$ - $Hf_2N_2Se$ , (c)  $P1m1$ - $Zr_2N_2Se$  and (d)  $C2/m$ - $Hf_2N_2Se$ .

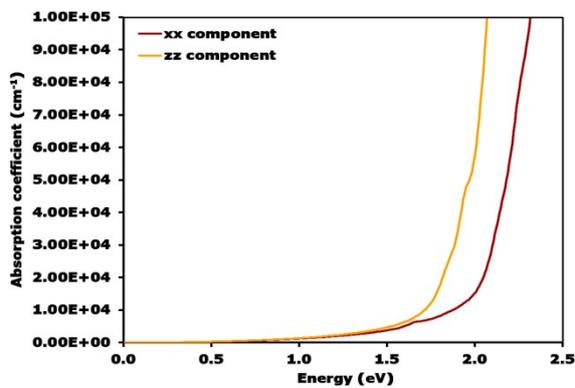


(a)

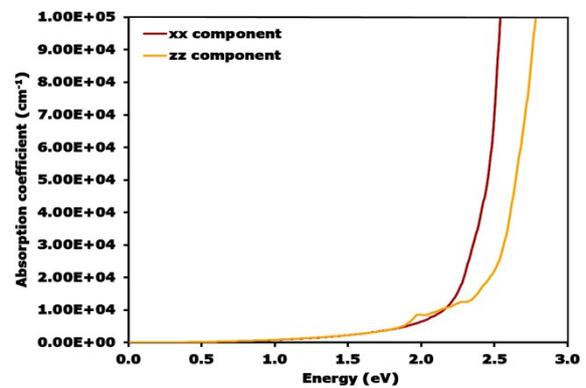


(b)

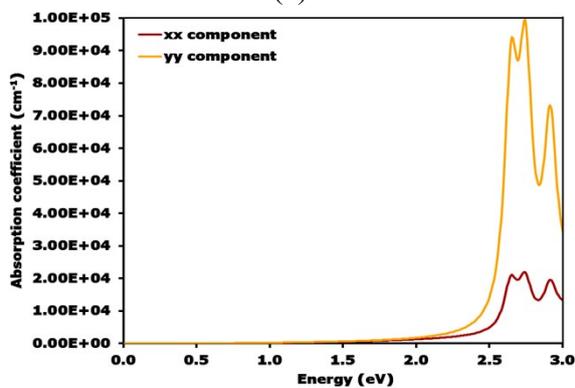
S3 Energy profiles for (a) P1m1-Zr<sub>2</sub>N<sub>2</sub>Se and (b) C2/m-Hf<sub>2</sub>N<sub>2</sub>Se during AIMD simulations at 300 K. Instability of structures is not observed.



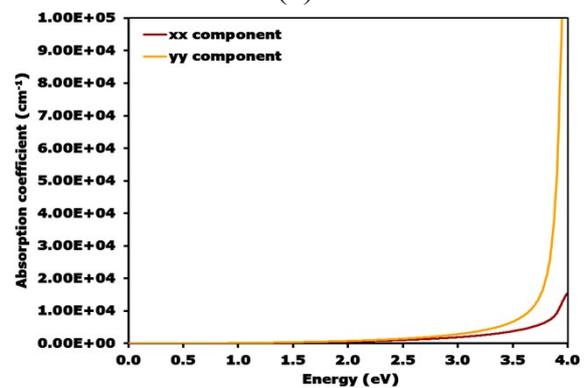
(a)



(b)



(c)



(d)

S4 Zoom-in features of absorption coefficient in the visible and infrared range for (a) P<sup>3</sup>m1-Zr<sub>2</sub>N<sub>2</sub>Se, (b) P<sup>3</sup>m1-Hf<sub>2</sub>N<sub>2</sub>Se, (c) P1m1-Zr<sub>2</sub>N<sub>2</sub>Se and (d) C2/m-Hf<sub>2</sub>N<sub>2</sub>Se.

## References

- 1) M.M.S. Sirajuddeena, I.B.S. Banu (2014). AIP Advances. 4(5), 057121.
- 2) A. Srivastava and B.D. Diwan (2014). Can. J. Phys. 92, 1058-1061.