Supporting Information

Bulk ionic screening lengths from extremely large-scale molecular dynamics simulations

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S1 Simulated Systems

Table S1 below list	s the compositions of	all inv	vestigated	systems,	and	${\it ball-and-stick}$	models	with '	the
corresponding Lewi	s formulas are shown	in fig.	S1.						

$c({ m mol/l})$	$N_{\rm IP}$	$N_{ m S}$	$\bar{L}(\mathrm{nm})$	$t_{\rm sim}({\rm ns})$	$t_{\rm eq}({\rm ns})$
р	ure $[C_4C_1]$	$[m]^{+} [PF_6]^{-}$	(all-atom	ı)	
4.63	108,000	0	33.84	600	300
pure	$[C_4C_1Im]$	$+ [PF_6]^-$ (co	oarse-grai	ned)	
4.78	358,296	0	49.92	700	300
	NaCl in	n water (all-	-atom)		
4.43	216,000	$2,\!458,\!296$	43.25	200	50
1.16	3,750	$176,\!577$	17.53	537	50
2.43	3,750	81,814	13.68	5369	50
4.86	3,750	38,411	10.86	5369	50
5.19	3,750	$35,\!625$	10.63	5369	50
[C4	$[C_1Im]^+$ [N	$[VTf_2]^-$ in P	C (all-ator	m)	
0.00	0	1,000	5.19	1074	100
0.53	200	$3,\!800$	8.54	2147	200
0.97	500	4,500	9.51	2147	200
1.63	500	2,000	7.99	3221	200
2.10	500	1,167	7.34	4295	200
2.47	500	750	6.96	4295	200
2.75	500	500	6.71	4295	200
2.98	500	333	6.53	4295	200
3.17	500	214	6.40	4295	200
3.33	500	125	6.30	4295	200
3.46	500	56	6.21	4295	200
3.58	500	0	6.15	4295	200

Table S1: System compositions. Listed values are: molar ion pair concentration c (mol/l), number of ion pairs $N_{\rm IP}$, the number of solvent molecules $N_{\rm S}$, average simulation box edge length \bar{L} (nm), total simulation time $t_{\rm sim}$ (ns) after equilibration, and equilibration time $t_{\rm eq}$ (ns). Further details with corresponding error estimates can be found in section S2.1.



Figure S1: Ball-and-stick models (top row, produced with VMD^{S1}) and corresponding Lewis formulas (bottom row) of the investigated substances. **a**: 1-butyl-3-methylimidazolium ($[C_4C_1Im]^+$) cation (all-atom (left) and coarse-grained (right)). **b**: hexafluorophosphate ($[PF_6]^-$) anion (all-atom (left) coarse-grained (right)). **c**: bis(trifluoromethylsulfonyl)imide ($[NTf_2]^-$) anion. **d**: (R)-propylene carbonate (left) and (S)-propylene carbonate (right).

S2 Additional Results

S2.1 Volumetric system properties

pure $[C_4C_1Im]^+ [PF_6]^-$ (all-atom)								
$c({ m mol/l})$	$\bar{V} (\mathrm{nm}^3)$	$\overline{arrho}(\mathrm{kg}/\mathrm{m}^3)$	$arrho_{ m exp}(m kg/m^3)$	$\Delta \varrho (\%)$				
4.62987(4)	38,735.0(3)	1,315.735(10)	1,360.47	-3.29				

pure $[C_4C_1Im]^+ [PF_6]^-$ (coarse-grained)

$c({ m mol/l})$	$\bar{V} ({ m nm}^3)$	$ar{arrho}(\mathrm{kg}/\mathrm{m}^3)$	$arrho_{ m exp}(m kg/m^3)$	$\Delta \varrho (\%)$
4.78280(2)	124,396.7(5)	1,359.223(6)	1,360.47	-0.09

 $[C_4C_1Im]^+$ $[NTf_2]^-$ in PC (all-atom)

$c({ m mol}/{ m l})$	$\bar{V} ({\rm nm^3})$	$ar{arrho}({ m kg/m^3})$	$arrho_{ m exp}(m kg/m^3)$	$\Delta \varrho (\%)$
0.00000(0)	139.46(5)	1,215.5(4)	1,197.30	1.52
0.53340(1)	622.628(5)	1,258.31(1)	1,229.92	2.31
0.96600(1)	859.490(1)	1,292.67(1)	1,262.49	2.39
1.62504(1)	510.922(1)	1,345.08(1)	1,307.08	2.91
2.10316(1)	394.772(3)	1,383.12(1)	1,339.01	3.29
2.46649(2)	336.619(3)	1,412.06(1)	1,363.58	3.56
2.75140(2)	301.763(3)	1,434.72(1)	1,382.19	3.80
2.98136(3)	278.487(3)	1,452.98(2)	$1,\!396.75$	4.03
3.17022(4)	261.896(3)	1,467.99(2)	1,408.63	4.21
3.32780(4)	249.495(3)	1,480.49(2)	1,418.32	4.38
3.46103(7)	239.891(5)	1,491.00(3)	$1,\!426.15$	4.55
3.57732(5)	232.092(3)	1,500.20(2)	$1,\!432.52$	4.72

NaCl in SPC/E water (all-atom)

$c({ m mol/l})$	$\bar{V} ({ m nm^3})$	$ar{arrho}({ m kg/m^3})$	$arrho_{ m exp}(m kg/m^3)$	$\Delta \varrho \left(\%\right)$
1.155534(2)	5,388.87(1)	1,047.766(2)	1,042.34	0.52
2.432431(8)	2,559.999(8)	1,098.209(4)	1,090.56	0.70
4.433304(9)	80,905.0(2)	1,168.069(2)	1,162.79	0.45
4.86353(2)	1,280.349(5)	1,181.711(5)	$1,\!178.07$	0.31
5.19117(3)	1,199.541(7)	1,191.838(7)	1,189.70	0.18

Table S2: Volumetric system properties. The listed values are molar ion pair concentration c (mol/l), average simulation box volume $\overline{V} \text{(nm}^3)$, average mass density $\overline{\varrho} \text{(kg/m}^3)$, experimental mass density $\varrho_{\exp} \text{(kg/m}^3)$, and relative deviation $\Delta \varrho = \frac{\overline{\varrho} - \varrho_{\exp}}{\varrho_{\exp}} (\%)$. The experimental value of ϱ_{\exp} for $[C_4C_1\text{Im}]^+ [PF_6]^-$ at 300 K is a linear extrapolation of temperature-dependent mass density measurements taken from Machida *et al.*, ^{S2} whereas the values of ϱ_{\exp} for $[C_4C_1\text{Im}]^+ [NTf_2]^-$ in PC are linear interpolations of temperature- and concentration-dependent measurements obtained from Vraneš *et al.* ^{S3} For aqueous NaCl, the values of ϱ_{\exp} are linear inter- and extrapolations of temperature- and concentration-dependent data from ref. S4.

S2.2 Static relative dielectric permittivities

			,	
x	$c ({ m mol}/{ m l})$	ε_r	$\lambda_{\rm D} ({\rm nm})$	$\lambda_{\rm S} ({\rm nm})$
0.00	0.00	59.3(6)		
0.05	0.53	46(3)	0.32(1)	0.67(3)
0.10	0.97	39(5)	0.22(1)	0.65(4)
0.20	1.63	28(3)	0.144(8)	0.496(8)
0.30	2.10	23(3)	0.114(8)	0.465(6)
0.40	2.47	20(3)	0.099(7)	0.584(9)
0.50	2.75	15(2)	0.081(6)	0.607(4)
0.60	2.98	13(2)	0.073(4)	0.686(4)
0.70	3.17	12(1)	0.068(3)	0.753(6)
0.80	3.33	10.0(8)	0.060(2)	0.846(8)
0.90	3.46	10.5(7)	0.060(2)	0.95(1)
1.00	3.58	9.1(5)	0.055(1)	1.07(1)
	1			

$[C_4C_1Im]^+$ $[NTf_2]^-$ in PC

aqueous NaCl

_	x	$c({ m mol/l})$	ε_r	$\lambda_{\rm D}({\rm nm})$	$\lambda_{\rm S}({\rm nm})$
-	0.02	1.16	53(2)	0.233(3)	0.25(1)
	0.04	2.43	47(4)	0.151(6)	0.197(8)
	0.09	4.86	35(3)	0.093(4)	0.32(2)
	0.10	5.19	33(3)	0.087(4)	0.33(1)

Table S3: Static relative permittivities ε_r , Debye lengths λ_D , and effective screening lengths λ_S for solutions of $[C_4C_1Im]^+ [NTf_2]^-$ in PC (top) and NaCl in water (bottom) at different concentrations. The numbers in parentheses represent the uncertainty of the last digit.

S2.3 PMF behavior over time

As stated in the main article, when analyzing simulations of concentrated ionic liquid systems, it is cruicial that enough simulation time has been allowed for such systems to reach thermal equilibrium. The following plots show how the PMFs of the largest investigated systems (pure $[C_4C_1Im]^+$ $[PF_6]^-$, AA and CG models) change over time.



Figure S2: Absolute value of the potential of mean force $|w_{+-}|(r)$ between anions and cations in neat $[C_4C_1Im]^+[PF_6]^-$ (AA model) for 250 analyzed frames (corresponding to a time span $\Delta t = 0.5 \text{ ns}$) taken at different time steps t during the simulation. The first PMF at t = -200 ns (dashed gray line) was computed from trajectory data during system equilibration. Even though its short-range behavior is similar to the remaining PMF curves, this PMF exhibits comparatively large-amplitude, regular oscillations in its tail, showing that the system is not properly equilibrated at this point in time. The remaining PMFs were computed for the same number of frames but at times $t \in \{0, 200, 400, 599.5\}$ ns after equilibration. After equilibration, all PMFs show the same qualitative behavior with rather noisy tails of similar amplitude, demonstrating that the system has reached an equilibrium state.



Figure S3: Absolute value of the potential of mean force $|w_{+-}|(r)$ between anions and cations in neat $[C_4C_1Im]^+[PF_6]^-$ (CG model) for 100 analyzed frames (corresponding to a time span $\Delta t = 0.5 \text{ ns}$) taken at different time steps t during the simulation. The first PMF at t = -100 ns (dashed gray line) was computed from trajectory data during system equilibration. It is clearly visible that there are small structural artifacts in the PMF tail at $r \approx 24 \text{ nm}$ and for r > 29 nm, showing that the system is not yet equilibrated at this point in time. The remaining PMFs were computed for the same number of frames but at times $t \in \{0, 300, 500, 699.5\}$ ns after equilibration. Obviously, the structural artifacts have vanished after equilibration, and all PMFs show the same qualitative behavior, demonstrating that the system is indeed equilibrated.

The PMFs shown in the above figs. S2 and S3 demonstrate that the systems are properly equilibrated, however, they do not yield implications about the relaxation of the *cumulative* PMF behavior over time. Therefore, the following figs. S4 and S5 show the PMFs' relaxation behavior depending on the number of analyzed frames after equilibration.



Figure S4: Absolute value of the potential of mean force $|w_{+-}|(r)$ between anions and cations in neat $[C_4C_1Im]^+$ $[PF_6]^-$ (AA model) for different numbers of analyzed frames (i.e., time spans). Regardless of the number of analyzed frames, the PMFs exhibit an exponentially damped oscillatory behavior, followed by rather noisy oscillations of almost constant amplitude. As the number of analyzed frames increases, the extent of the exponentially damped region increases to larger distances and the amplitude of the oscillatory tail decreases. However, there is no sign of any long-range monotonic decay.



Figure S5: Absolute value of the potential of mean force $|w_{+-}|(r)$ between anions and cations in neat $[C_4C_1Im]^+$ $[PF_6]^-$ (CG model) for different numbers of analyzed frames (i.e., time spans). As for the all-atom model, the PMFs exhibit an exponentially damped oscillatory behavior, followed by rather noisy oscillations of almost constant amplitude. Likewise, as the number of analyzed frames increases, the extent of the exponentially damped region increases to larger distances and the amplitude of the oscillatory tail decreases. Again, there is no sign of any long-range monotonic decay.

For both molecular models, the extent of the damped oscillatory region increases with simulation time but the qualitative PMF behavior remains unchanged and without any indication for a long-ranged, monotonic decay.



S2.4 Screening length scaling analysis of $[C_4C_1Im]^+$ $[NTf_2]^-$ in propylene carbonate

Figure S6: Panel a: Cation-anion radial distribution functions $g_{+-}(r)$ of $[C_4C_1Im]^+ [NTf_2]^-$ in propylene carbonate for different IL mole fractions x ranging from x = 0.05 (blue) to x = 1.0 (red). Panel b: Corresponding cation-anion potentials of mean force $w_{+-}(r)$ of the same systems (same color code). Arrows indicate increasing IL mole fraction.



Figure S7: Panel a: Anion-anion radial distribution functions $g_{--}(r)$ of $[C_4C_1Im]^+ [NTf_2]^-$ in propylene carbonate for different IL mole fractions x ranging from x = 0.05 (blue) to x = 1.0 (red). Panel b: Corresponding anion-anion potentials of mean force $w_{--}(r)$ of the same systems (same color code). Arrows indicate increasing IL mole fraction.



Figure S8: Panel a: Cation-cation radial distribution functions $g_{++}(r)$ of $[C_4C_1Im]^+ [NTf_2]^-$ in propylene carbonate for different IL mole fractions x ranging from x = 0.05 (blue) to x = 1.0 (red). Panel b: Corresponding cation-cation potentials of mean force $w_{++}(r)$ of the same systems (same color code). Arrows indicate increasing IL mole fraction.

Listed below in tables S4 to S6 are the parameters resulting from fits of a superposition of k = 2 oscillatory, exponentially damped hyperbolas of the form

$$f(r) = \sum_{n=1}^{k} \frac{A_n}{r} \cos\left(\omega_n r - \phi_n\right) \exp\left(-\frac{r}{\lambda_n}\right)$$
(S1)

to the PMFs in solutions of $[C_4C_1Im]^+$ $[NTf_2]^-$ in propylene carbonate at different IL mole fractions x.

x	$c_{ m IL}~(m mol/l)$	$A_1 \left(k_{\rm B} T \right)$	$\lambda_1 (\text{nm})$	$2\pi/\omega_1 (\mathrm{nm})$	ϕ_1	$A_2 \left(k_{\rm B} T \right)$	$\lambda_2 (\mathrm{nm})$	$2\pi/\omega_2 ({ m nm})$	ϕ_2	R^2
0.05	0.53	1.11(4)	0.444(5)	0.477(1)	5.83(5)	-15(2)	0.222(3)	00		0.9955
0.10	0.97	1.13(7)	0.404(6)	0.458(1)	0.38(7)	9534(5496)	0.158(7)	116(1)	2(44)	0.9948
0.20	1.63	0.39(2)	0.496(8)	0.465(3)	5.87(5)	2.8(2)	0.309(5)	0.799(3)	6.04(6)	0.9980
0.30	2.10	0.79(8)	0.41(1)	0.468(6)	5.6(1)	1.6(1)	0.395(7)	0.729(3)	1.37(7)	0.9966
0.40	2.47	1.16(9)	0.373(7)	0.465(5)	5.6(1)	1.42(5)	0.462(4)	0.731(1)	1.56(3)	0.9990
0.50	2.75	1.5(1)	0.348(6)	0.461(5)	5.84(9)	1.14(2)	0.555(3)	0.7383(8)	1.50(2)	0.9996
0.60	2.98	1.7(1)	0.339(6)	0.464(5)	5.73(9)	1.02(1)	0.636(3)	0.7409(6)	1.45(1)	0.9997
0.70	3.17	1.5(1)	0.351(6)	0.467(5)	5.55(9)	0.99(1)	0.700(3)	0.7446(5)	1.35(1)	0.9998
0.80	3.33	1.6(2)	0.343(8)	0.468(7)	5.5(1)	0.90(1)	0.786(4)	0.7457(5)	1.32(1)	0.9998
0.90	3.46	1.6(2)	0.34(1)	0.468(8)	5.53(1)	0.83(1)	0.871(5)	0.7471(5)	1.28(1)	0.9997
1.00	3.58	2.0(3)	0.33(1)	0.48(1)	5.1(2)	0.81(1)	0.941(7)	0.7457(5)	1.28(1)	0.9997

Table S4: Fit parameters of eq. (S1) to cation-anion PMFs $w_{+-}(r)$ in solutions of $[C_4C_1Im]^+ [NTf_2]^-$ in propylene carbonate for different mole fractions x in the fit range $1.2 \le r \le 3.0$ nm. The values (units) are IL mole fraction x, concentration c (mol/l), amplitudes A_n (k_BT), wavelengths $2\pi/\omega_n$ (nm), phase shifts ϕ_n , and the coefficient of determination R^2 . The numbers in parentheses represent the uncertainty of the last digit.

x	$c_{ m IL}~(m mol/l)$	$A_1 \left(k_{\rm B} T \right)$	$\lambda_1 (nm)$	$2\pi/\omega_1 (\mathrm{nm})$	ϕ_1	$A_2 \left(k_{\rm B} T \right)$	$\lambda_2 (\mathrm{nm})$	$2\pi/\omega_2 (\mathrm{nm})$	ϕ_2	R^2
0.05	0.53	3.8(1)	0.421(4)	0.4843(7)	4.09(3)	4.3(4)	0.308(7)	∞		0.9976
0.10	0.97	0.9(1)	0.56(1)	0.463(2)	5.4(1)	88(10)	0.201(4)	0.489(4)	3.7(1)	0.9995
0.20	1.63	3.8(2)	0.389(5)	0.475(3)	4.61(7)	1.9(2)	0.36(1)	0.714(5)	4.8(1)	0.9991
0.30	2.10	3.5(2)	0.382(4)	0.469(3)	4.94(5)	1.75(5)	0.465(6)	0.720(2)	4.82(4)	0.9996
0.40	2.47	3.5(1)	0.373(4)	0.466(2)	5.16(5)	1.69(5)	0.522(4)	0.723(1)	4.79(2)	0.9998
0.50	2.75	3.8(2)	0.358(4)	0.466(3)	5.24(5)	1.40(3)	0.607(4)	0.7282(7)	4.70(2)	0.9998
0.60	2.98	4.0(2)	0.349(4)	0.464(3)	5.37(5)	1.23(2)	0.686(4)	0.7310(7)	4.63(1)	0.9998
0.70	3.17	5.0(4)	0.329(5)	0.464(4)	5.46(8)	1.13(2)	0.753(6)	0.7342(7)	4.54(2)	0.9997
0.80	3.33	6.3(6)	0.312(6)	0.468(6)	5.4(1)	0.98(2)	0.846(8)	0.7371(8)	4.46(1)	0.9996
0.90	3.46	7.5(9)	0.303(7)	0.476(7)	5.1(1)	0.85(2)	0.95(1)	0.7394(8)	4.40(2)	0.9995
1.00	3.58	8(1)	0.296(8)	0.479(8)	5.0(1)	0.76(2)	1.07(1)	0.7388(9)	4.38(2)	0.9994

Table S5: Fit parameters of eq. (S1) to anion-anion PMFs $w_{--}(r)$ in solutions of $[C_4C_1Im]^+ [NTf_2]^-$ in propylene carbonate for different mole fractions x in the fit range $1.2 \le r \le 3.0$ nm. The values (units) are IL mole fraction x, concentration c (mol/l), amplitudes A_n (k_BT), wavelengths $2\pi/\omega_n$ (nm), phase shifts ϕ_n , and the coefficient of determination R^2 . The numbers in parentheses represent the uncertainty of the last digit.

x	$ c_{ m IL} ({ m mol}/{ m l})$	$A_1 \left(k_{\rm B} T \right)$	$\lambda_1 (\mathrm{nm})$	$2\pi/\omega_1 (\mathrm{nm})$	ϕ_1	$A_2 \left(k_{\rm B} T \right)$	$\lambda_2 (\mathrm{nm})$	$2\pi/\omega_2 (\mathrm{nm})$	ϕ_2	R^2
0.05	0.53	0.09(1)	0.67(3)	0.47(1)	0.7(1)	2.8(2)	0.302(4)	∞		0.9853
0.10	0.97	0.07(1)	0.65(4)	0.46(2)	1.0(1)	0.21(6)	0.43(3)	1.11(2)	6.0(2)	0.8456
0.20	1.63	0.24(3)	0.46(1)	0.48(1)	5.5(1)	0.18(3)	0.44(2)	0.96(2)	0.3(2)	0.9868
0.30	2.10	56(25)	0.19(1)	0.53(2)	4.3(3)	0.3(1)	0.45(3)	0.86(1)	1.6(2)	0.9905
0.40	2.47	12(2)	0.226(6)	0.50(1)	5.0(2)	0.26(2)	0.58(1)	0.740(3)	4.77(7)	0.9990
0.50	2.75	92(34)	0.169(7)	0.45(2)	0.9(4)	0.50(2)	0.597(6)	0.734(2)	4.95(4)	0.9991
0.60	2.98	12(2)	0.227(6)	0.48(1)	5.3(3)	0.56(1)	0.668(3)	0.730(1)	5.12(3)	0.9997
0.70	3.17	24(4)	0.206(4)	0.47(1)	5.8(2)	0.584(7)	0.744(3)	0.7394(5)	4.89(1)	0.9999
0.80	3.33	40(7)	0.193(4)	0.46(1)	0.1(3)	0.606(6)	0.815(3)	0.7411(4)	4.82(1)	0.9999
0.90	3.46	84(16)	0.176(4)	0.43(2)	1.3(3)	0.604(5)	0.895(3)	0.7444(4)	4.72(1)	0.9999
1.00	3.58	104(22)	0.174(4)	0.43(2)	1.6(3)	0.594(4)	0.983(3)	0.7432(4)	4.71(1)	0.9999

Table S6: Fit parameters of eq. (S1) to cation-cation PMFs $w_{++}(r)$ in solutions of $[C_4C_1Im]^+ [NTf_2]^-$ in propylene carbonate for different mole fractions x in the fit range $1.2 \le r \le 3.0$ nm. The values (units) are IL mole fraction x, concentration c (mol/l), amplitudes A_n (k_BT), wavelengths $2\pi/\omega_n$ (nm), phase shifts ϕ_n , and the coefficient of determination R^2 . The numbers in parentheses represent the uncertainty of the last digit.

Fitting the data to eq. (S1) with k = 3 terms resulted in extremely unstable results under slight variation of initial fit parameters, while setting k = 1 lead to large fitting errors.

S2.5 Screening length scaling analysis of NaCl in water



Figure S9: Panel a: Cation-anion RDFs $g_{+-}(r)$ of aqueous NaCl solutions for different concentrations $c \in \{1.16, 2.43, 4.86, 5.19\}$ mol/l. Panel b: Corresponding cation-anion potentials of mean force $w_{+-}(r)$ of the same systems (same color code). Arrows indicate increasing NaCl concentration.



Figure S10: Panel a: Anion-anion RDFs $g_{--}(r)$ of aqueous NaCl solutions for different concentrations $c \in \{1.16, 2.43, 4.86, 5.19\}$ mol/l. Panel b: Corresponding cation-anion potentials of mean force $w_{--}(r)$ of the same systems (same color code). Arrows indicate increasing NaCl concentration.



Figure S11: Panel a: Cation-cation RDFs $g_{++}(r)$ of aqueous NaCl solutions for different concentrations $c \in \{1.16, 2.43, 4.86, 5.19\}$ mol/l. Panel b: Corresponding cation-cation potentials of mean force $w_{++}(r)$ of the same systems (same color code). Arrows indicate increasing NaCl concentration.

Listed below in table S7 are the parameters resulting from fits of a superposition of k = 3 oscillatory, exponentially damped hyperbolas of the form

$$f(r) = \sum_{n=1}^{k} \frac{A_n}{r} \cos\left(\omega_n r - \phi_n\right) \exp\left(-\frac{r}{\lambda_n}\right)$$
(S2)

to the PMFs $w_{+-}(r)$ in aqueous NaCl solutions at different concentrations.

$c({ m mol}/{ m l})$	$A_1 \left(k_{\rm B} T \right)$	$\lambda_1 (\mathrm{nm})$	$2\pi/\omega_1 \ (nm)$	ϕ_1	$A_2 \left(k_{\rm B} T \right)$	$\lambda_2 (\mathrm{nm})$	$2\pi/\omega_2 (\mathrm{nm})$	ϕ_2
1.16	3.9(3)	0.200(2)	2.372(3)	4.8(3)	30(4)	0.126(2)	0.209(3)	5.6(2)
2.43	4.2(5)	0.185(4)	1.096(1)	0.0(1)	1.1(3)	0.197(8)	0.289(3)	3.9(3)
4.86	1.4(1)	0.202(3)	0.9379(7)	5.5(1)	0.09(2)	0.32(2)	0.222(1)	5.7(2)
5.19	3.5(3)	0.170(2)	0.990(1)	4.9(1)	0.08(1)	0.33(1)	0.225(1)	5.0(2)
$c({ m mol/l})$	$A_3 \left(k_{\rm B} T \right)$	$\lambda_3 (\mathrm{nm})$	$2\pi/\omega_3 (\mathrm{nm})$	ϕ_3	R^2			
1.16	0.3(1)	0.25(1)	0.303(3)	3.0(2)	0.9986			
2.43	22408(11276)	0.069(9)	0.226(0)	4 4 (5)	0 0000			
2.40	32408(11370)	0.002(2)	0.220(9)	4.4(0)	0.9900			
4.86	32408(11570) 3203(1159)	0.002(2) 0.071(2)	0.220(9) 0.188(3)	2.4(3)	0.9988			

Table S7: Fit parameters of eq. (S2) to cation-anion PMFs $w_{+-}(r)$ in solutions for different NaCl concentrations c in the fit range $0.8 \le r \le 2.0$ nm. The values (units) are NaCl ion pair concentration c (mol/l), amplitudes A_n ($k_{\rm B}T$), wavelengths $2\pi/\omega_n$ (nm), phase shifts ϕ_n , and the coefficient of determination R^2 . The numbers in parentheses represent the uncertainty of the last digit.

The scaling plot of $\frac{\lambda_n}{\lambda_D}$ vs. $\frac{d}{\lambda_D}$ is shown in fig. S12 for fits to all concentration-dependent cation-anion PMFs $w_{+-}(r)$.



Figure S12: Scaling of the fitted screening lengths for all investigated cation-anion PMFs in aqueous NaCl solutions.

While the screening lengths λ_1 and λ_2 exhibit a polynomial scaling, the third term with corresponding screening length λ_3 , which was required to obtain a satisfactory fit, does not provide such a clear trend.

Setting k = 2 in eq. (S2) lead to much larger fit errors and no clearly identifyable scaling exponents. The corresponding plot is shown in fig. S13 below.



Figure S13: Scaling of the fitted screening lengths from eq. (S2) with k = 2 terms for all investigated cation-anion PMFs in aqueous NaCl solutions.

S3 GROMACS Simulation Parameters

All systems were simulated in the NpT ensemble in cubic boxes with periodic boundary conditions in all three dimensions, where temperature and pressure were maintained at T = 300 K and p = 1 bar using a Nosé-Hoover thermostat and Parrinello-Rahman barostat. Short-range van der Waals interactions were computed up to a system-dependent cut-off, and their long-range part was either computed using the smooth particle mesh Ewald (SPME) method with a relative accuracy of 10^{-3} , or taken into account via analytic dispersion corrections for energy and pressure. Long-range Coulomb interactions were computed using the SPME method with a short-range cut-off of at least 1.3 nm, a relative accuracy of 10^{-5} , and tin foil boundary conditions at infinity. The time step of the employed leapfrog integrator was 2 fs for the all-atom models and 5 fs for the coarse-grained IL model.

In the following, we list the **GROMACS** molecular dynamics parameters used in production runs for all investigated systems.

parameter	value	unit (note)
integrator	md	(leapfrog integrator)
dt	0.002	ps
nsteps	30000000	steps
comm-mode	linear	
nstcomm	50	steps
nstcalcenergy	50	steps
nstxout-compressed	1000	steps
compressed-x-precision	10000	(means 10^{-4} nm)
cutoff-scheme	verlet	
nstlist	40	steps
ns-type	grid	
pbc	xyz	
coulombtype	pme	
coulomb-modifier	potential-shift-verlet	
rcoulomb	1.3	nm
vdwtype	pme	
vdw-modifier	potential-shift-verlet	
rvdw	1.3	nm
tcoupl	nose-hoover	
nsttcouple	5	steps
nh-chain-length	1	
tau-t	2.0	ps
ref-t	300.0	K
pcoupl	parrinello-rahman	
pcoupltype	isotropic	
nstpcouple	5	steps
tau-p	3.0	ps
compressibility	4.5e-5	bar^{-1}
ref-p	1.0	bar
constraints	h-bonds	(fix length of bonds involving H atoms)
constraint-algorithm	lincs	

S3.1 $[C_4C_1Im]^+ [PF_6]^-$ (all-atom model)

Table S8: GROMACS molecular dynamics simulation parameters used for the simulation of $[C_4C_1Im]^+$ $[PF_6]^-$ (all-atom model). Only
parameters which differ from the default (or have no default) are listed.

S3.2 $[C_4C_1Im]^+ [PF_6]^-$ (coarse-grained model)

parameter	value	unit (note)
integrator	md	(leapfrog integrator)
dt	0.005	ps
nsteps	14000000	steps
comm-mode	linear	
nstcomm	200	steps
nstcalcenergy	200	steps
nstxout-compressed	1000	steps
compressed-x-precision	1000	$(\text{means } 10^{-3} \text{ nm})$
cutoff-scheme	verlet	
nstlist	40	steps
ns-type	grid	
pbc	xyz	
coulombtype	pme	
coulomb-modifier	potential-shift-verlet	
rcoulomb	1.6	nm
vdwtype	cut-off	
vdw-modifier	potential-shift-verlet	
dispcorr	enerpres	
rvdw	1.6	nm
tcoupl	nose-hoover	
nh-chain-length	1	
tau-t	5.0	ps
ref-t	300.0	K
pcoupl	parrinello-rahman	
pcoupltype	isotropic	
tau-p	10.0	ps
compressibility	4.5e-5	bar^{-1}
ref-p	1.0	bar
constraints	all-bonds	(rigid molecular geometry)
constraint-algorithm	lincs	

Table S9: GROMACS molecular dynamics simulation parameters used for the simulation of $[C_4C_1Im]^+$ $[PF_6]^-$ (coarse-grained model).Only parameters which differ from the default (or have no default) are listed.

S3.3 Aqueous NaCl solutions

parameter	value	unit (note)
integrator	md	(leapfrog integrator)
dt	0.002	ps
nsteps	10000000	steps
comm-mode	linear	
nstcomm	50	steps
nstcalcenergy	50	steps
nstxout-compressed	1000	steps
compressed-x-precision	10000	$(\text{means } 10^{-4} \text{ nm})$
cutoff-scheme	verlet	
nstlist	40	steps
ns-type	grid	
pbc	xyz	
coulombtype	p3m-ad	
coulomb-modifier	potential-shift-verlet	
rcoulomb	1.2	nm
vdwtype	cut-off	
vdw-modifier	potential-shift-verlet	
dispcorr	enerpres	
rvdw	1.2	nm
ewald-rtol	1.0e-6	
tcoupl	nose-hoover	
nsttcouple	5	steps
nh-chain-length	1	
tau-t	2.0	ps
ref-t	300.0	К
pcoupl	parrinello-rahman	
pcoupltype	isotropic	
nstpcouple	5	steps
tau-p	3.0	ps
compressibility	4.5e-5	bar^{-1}
ref-p	1.0	bar
constraints	all-bonds	(rigid water geometry)
$\operatorname{constraint-algorithm}$	lincs	

 Table S10: GROMACS molecular dynamics simulation parameters used for the simulation of aqueous NaCl solutions. Only parameters which differ from the default (or have no default) are listed.

S3.4 $[C_4C_1Im]^+ [NTf_2]^-$ in PC

parameter	value	unit (note)
integrator	md	(leapfrog integrator)
dt	0.002	ps
nsteps	1073741824	steps $(=2^{30})$
comm-mode	linear	
nstcomm	1	steps
nstcalcenergy	50	steps
nstxout-compressed	1000	steps
compressed-x-precision	10000	$(\text{means } 10^{-4} \text{ nm})$
cutoff-scheme	verlet	
nstlist	40	steps
ns-type	grid	
pbc	xyz	
coulombtype	pme	
coulomb-modifier	potential-shift-verlet	
rcoulomb	1.3	nm
vdwtype	cut-off	
vdw-modifier	potential-shift-verlet	
dispcorr	enerpres	
rvdw	1.3	nm
tcoupl	nose-hoover	
nsttcouple	5	steps
nh-chain-length	1	
tau-t	2.0	ps
ref-t	300.0	K
pcoupl	parrinello-rahman	
pcoupltype	isotropic	
nstpcouple	5	steps
tau-p	3.0	ps
compressibility	4.5e-5	bar^{-1}
ref-p	1.0	bar
constraints	h-bonds	(fix length of bonds involving H atoms)
constraint-algorithm	lincs	

Table S11: GROMACS molecular dynamics simulation parameters used for the simulation of $[C_4C_1Im]^+$ $[NTf_2]^-$ in propylene carbonate.Only parameters which differ from the default (or have no default) are listed.

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