## Refractive properties of the α-BaGeO<sub>3</sub> crystal and their origins: a density function theory study

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| <i>k</i> -point       | total energy (eV) |
|-----------------------|-------------------|
| $1 \times 1 \times 1$ | -12465.43013      |
| $1 \times 1 \times 2$ | -12465.56520      |
| $2 \times 2 \times 3$ | -12465.37235      |
| $3 \times 3 \times 4$ | -12465.37167      |

**Table S1** Convergence test for the total energy of  $Ba_2MgGe_2O_7$  with respect to the  $\Gamma$ -centered k-point grid



(The energy cutoff is fixed at 900 eV)

Fig. S1 Convergence test for the total energy of  $Ba_2MgGe_2O_7$  with respect to the energy cutoff (The  $\Gamma$ -centered *k*-point grid is fixed at  $2 \times 2 \times 3$ ).

Table S1 and Fig. S1 present the results of convergence tests for the total energy of  $Ba_2MgGe_2O_7$  with respect to the  $\Gamma$ -centered k-point grid and the energy cutoff, respectively. The results show that an energy cutoff of 900 eV and a  $\Gamma$ -centered k-point grid of  $2 \times 2 \times 3$  are sufficient to yield a converged total energy.

| <i>k</i> -point       | total energy (eV) |
|-----------------------|-------------------|
| $1 \times 1 \times 1$ | -12600.76069      |
| $2 \times 2 \times 2$ | -12600.97733      |
| $3 \times 3 \times 3$ | -12600.97682      |

**Table S2** Convergence test for the total energy of  $\alpha$ -BaGeO<sub>3</sub> with respect to the  $\Gamma$ -centered *k*-point grid (The energy cutoff is fixed at 800 eV)



Fig. S2 Convergence test for the total energy of  $\alpha$ -BaGeO<sub>3</sub> with respect to the energy cutoff (The  $\Gamma$ -centered *k*-point grid is fixed at 2 × 2 × 2).

Table S2 and Fig. S2 present the results of convergence tests for the total energy of  $\alpha$ -BaGeO<sub>3</sub> with respect to the  $\Gamma$ -centered *k*-point grid and the energy cutoff, respectively. The results show that an energy cutoff of 800 eV and a  $\Gamma$ -centered *k*-point grid of 2 × 2 × 2 are sufficient to yield a converged total energy.



Fig. S3 Calculated band structure of Ba<sub>2</sub>MgGe<sub>2</sub>O<sub>7</sub>.

Fig. S3 presents the calculated band structure of  $Ba_2MgGe_2O_7$ . The crystal is an indirect band material with a calculated band gap of 3.678 eV. As compared with the experimental band gap of 5.124 eV, a scissors operator of 1.446 eV was used to compensate the underestimation of the band gap on the  $Ba_2MgGe_2O_7$  optical properties.



**Fig. S4** Calculated refractive dispersion curves of  $\alpha$ -BaGeO<sub>3</sub> when a light beam propagates along the crystallographic *a* axis with the polarized directions perpendicular/parallel to the *ac* crystallographic plane.

Fig. S4 presents  $n_0$  and  $n_e$  of  $\alpha$ -BaGeO<sub>3</sub> as a function of wavelength when a light beam propagates along the crystallographic *a* axis, which reveals that calculated refractive index and birefringence are almost invariable with the wavelength in the mid-IR region.