

Supporting Information

Theoretical formulation of $\text{Li}_{3a+b}\text{N}_a\text{X}_b$ ($\text{X} = \text{Halogen}$) as potential artificial solid electrolyte interphases (ASEI) to protect Li anode

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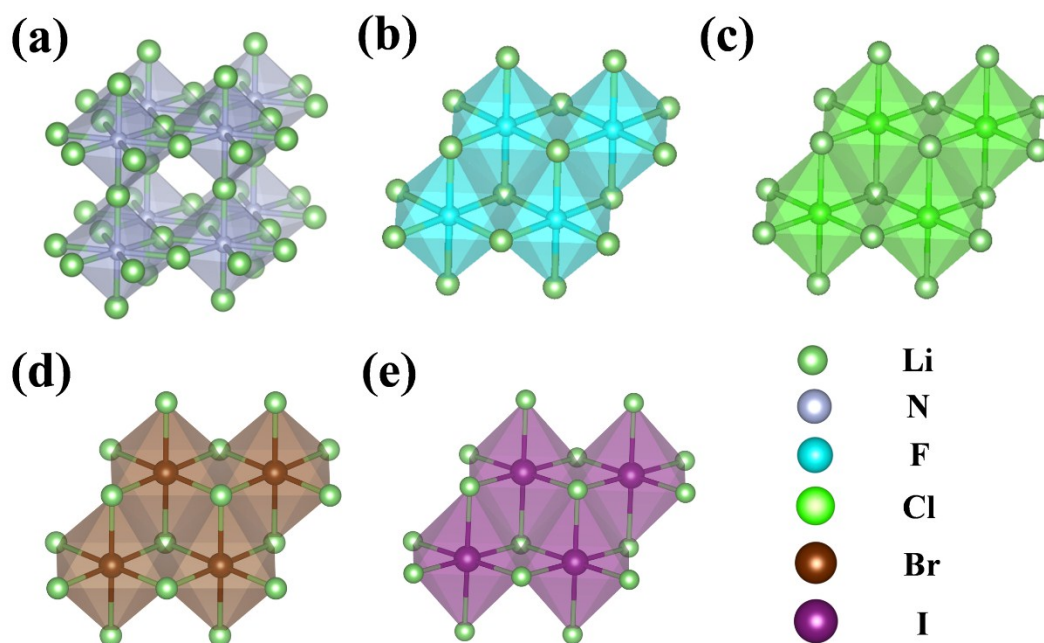


Fig. S1 Structural configurations of (a) Li_3N , (b) LiX ($\text{X} = \text{F}, \text{Cl}, \text{Br}, \text{I}$).

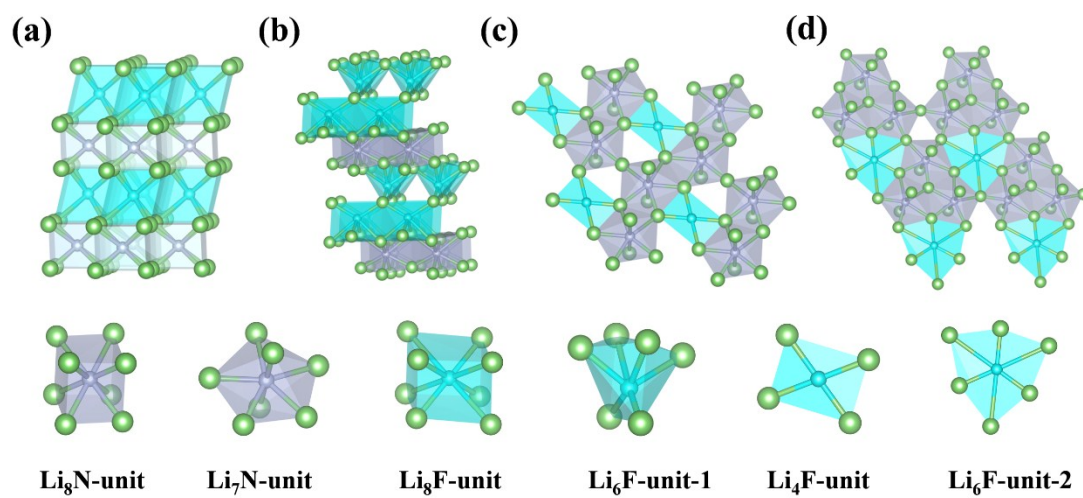


Fig. S2 Structures from USPEX energy minimization for (a) Li_4NF , (b) $\text{Li}_5\text{N}_2\text{F}$, (c) $\text{Li}_7\text{N}_2\text{F}$, and (d) $\text{Li}_{10}\text{N}_3\text{F}$.

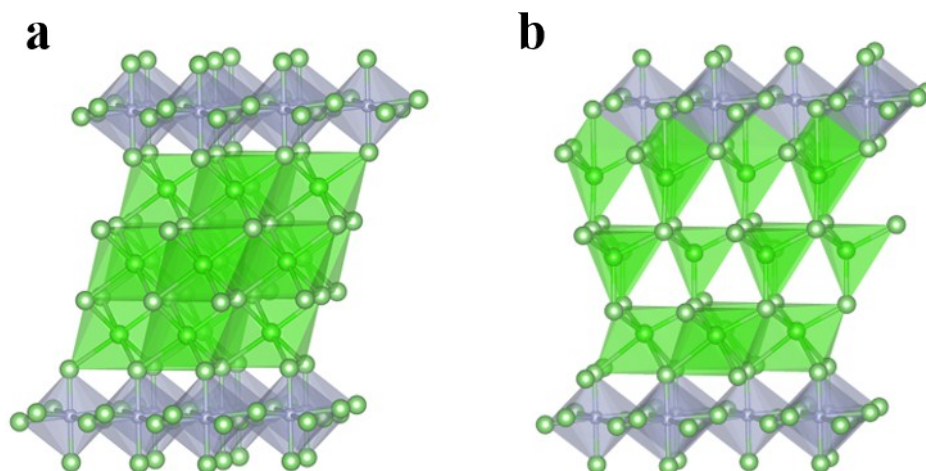


Fig. S3 Structural configuration of (a) Li_6NCl_3 predicted by USPEX with the symmetry of $\text{P}\bar{3}\text{m1}$ (164), (b) Li_6NCl_3 from Materials Project webpage with the symmetry of Cm (8).

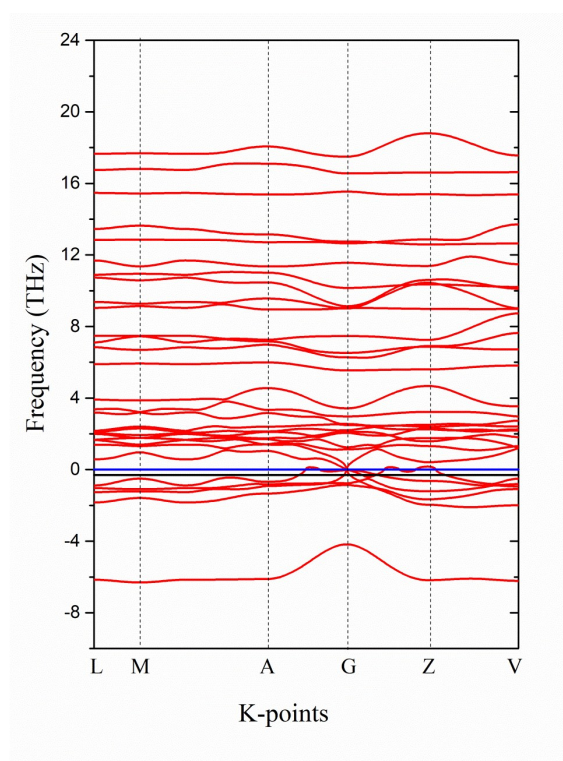


Fig. S4 Phonon band structure of Li_6Ni_3 . (blue line: 0 THz, black line: -0.3 THz)

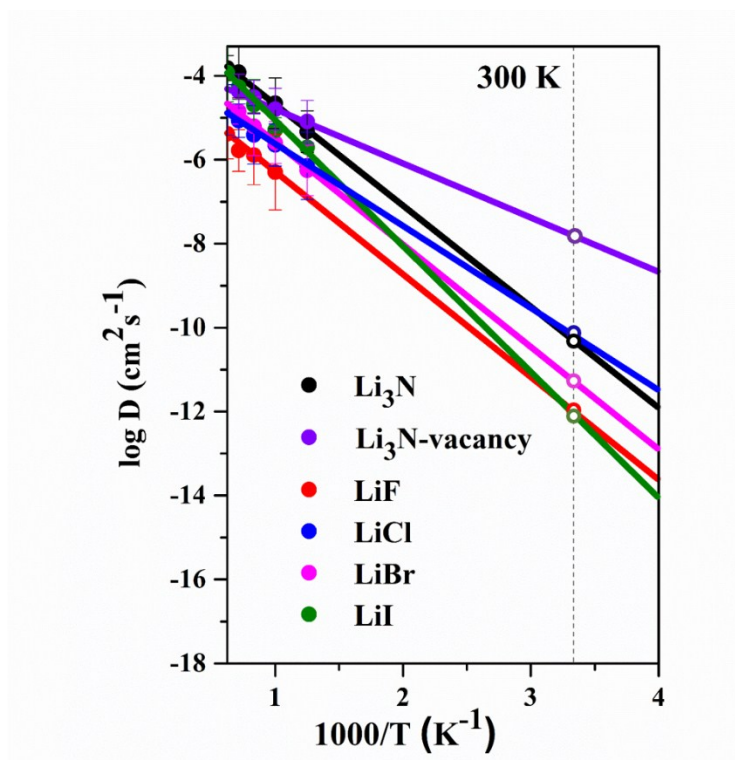


Fig. S5 Diffusion coefficients for lithium ions from AIMD simulation. The extrapolated D values at room temperature are presented by open patterns on the right.

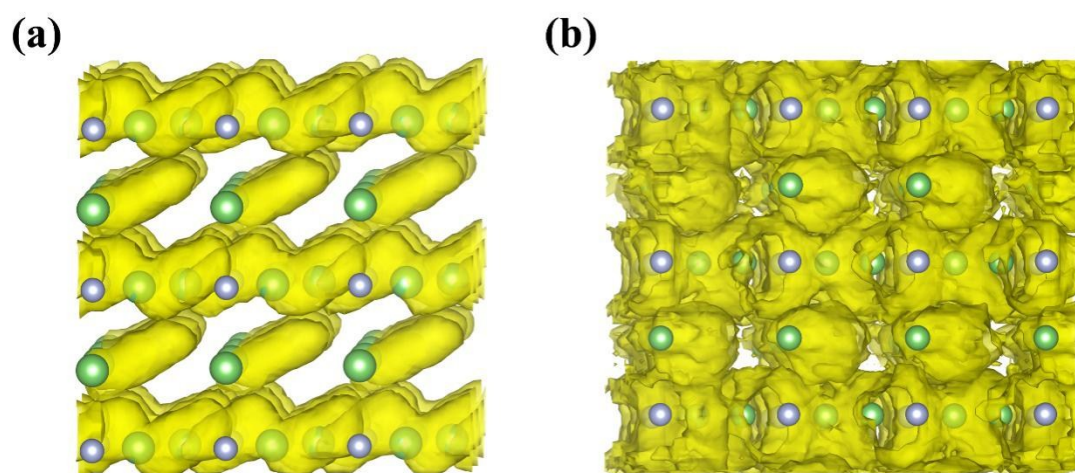


Fig. S6 Diffusion trajectories of Li^+ ions after 180 ps at 1000 K for (a) Li_3N and (b) Li_3N -vacancy. The yellow regions show the lithium ion diffusion path, with the Isosurface level being 2×10^{-6} .

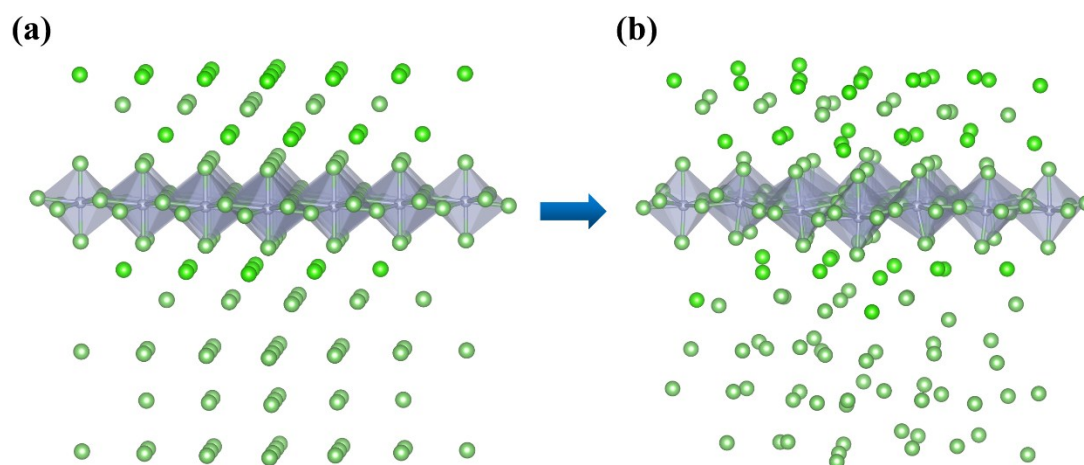
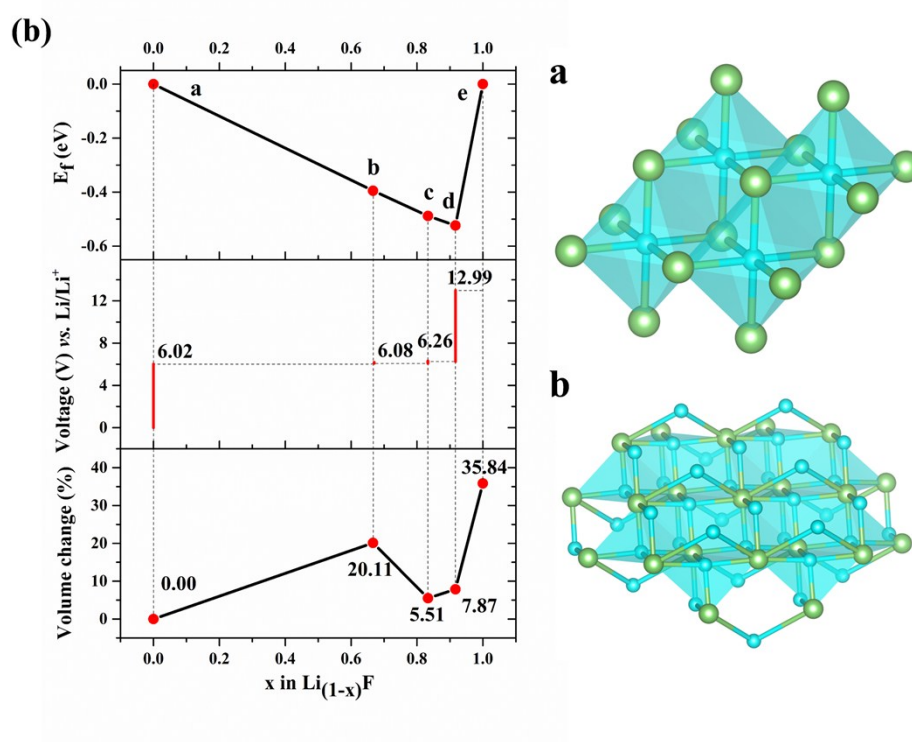
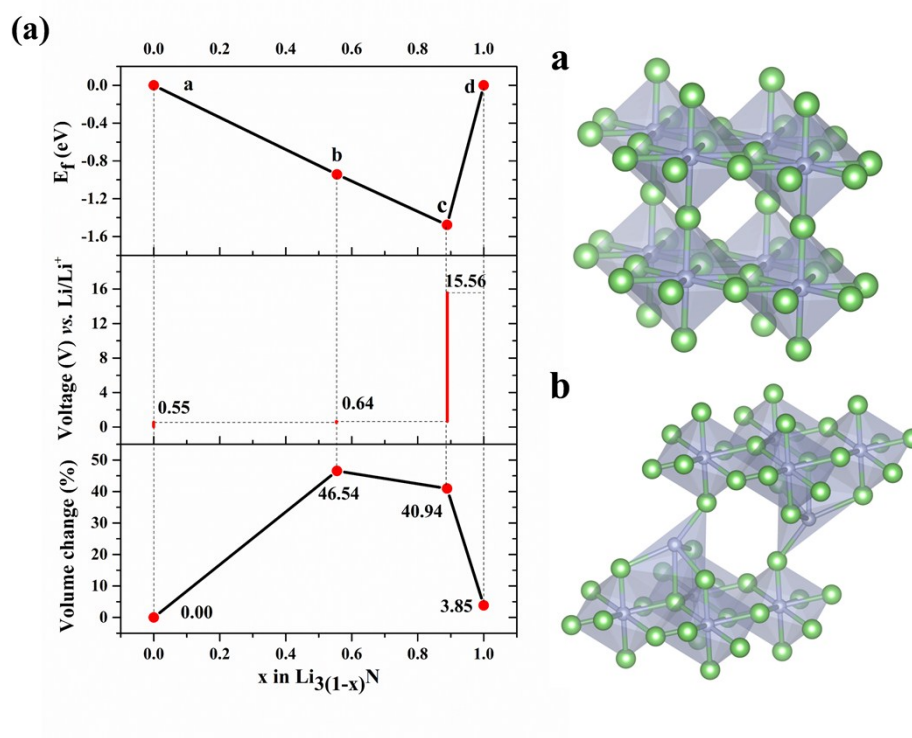
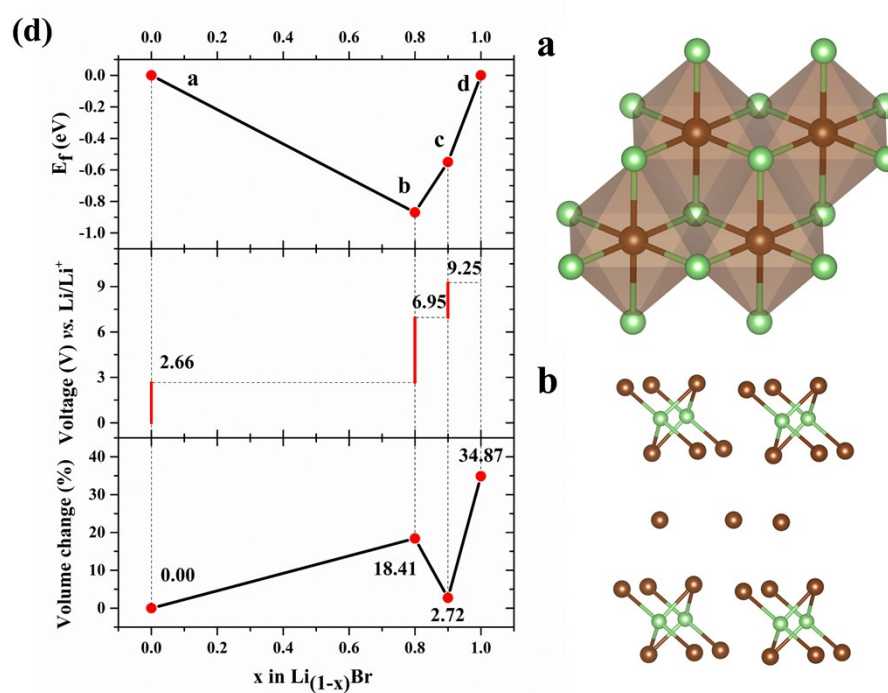
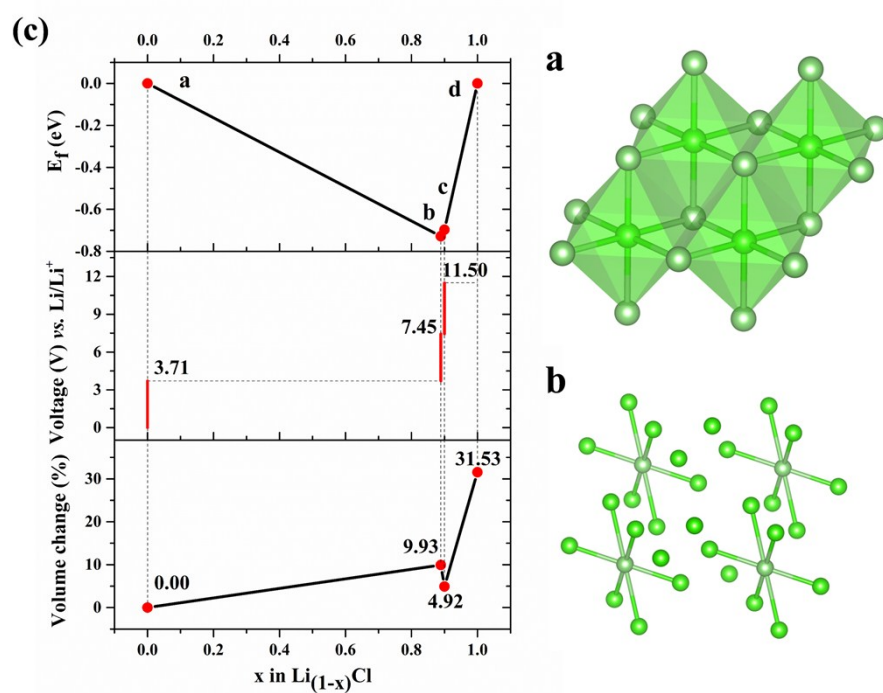


Fig. S7 Interfaced $\text{Li}_6\text{NCl}_3/\text{Li}$ (a) before, (b) after AIMD simulations at 500 K for 200 ps.





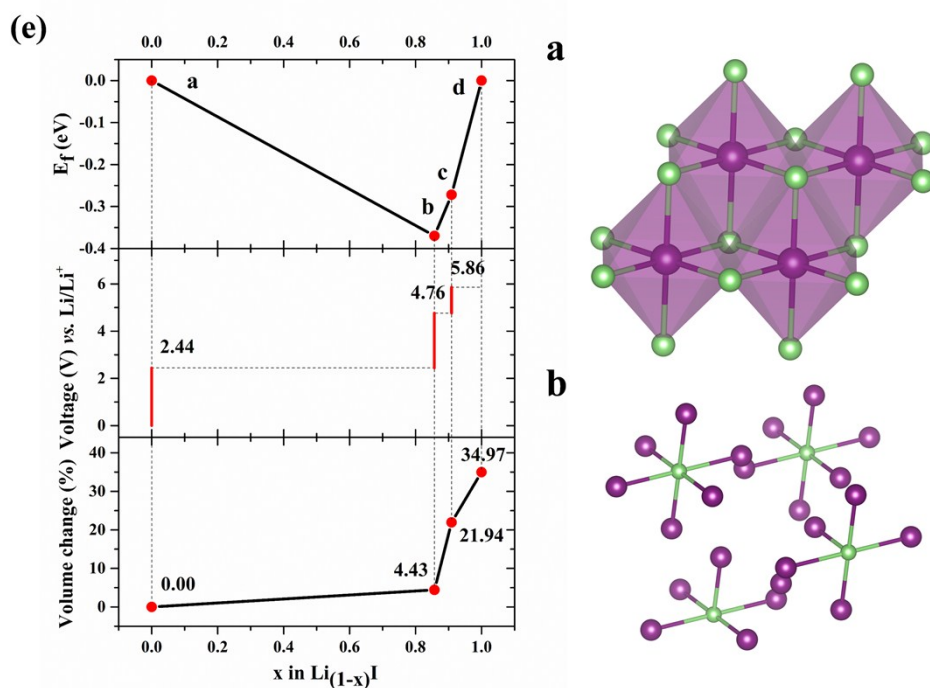
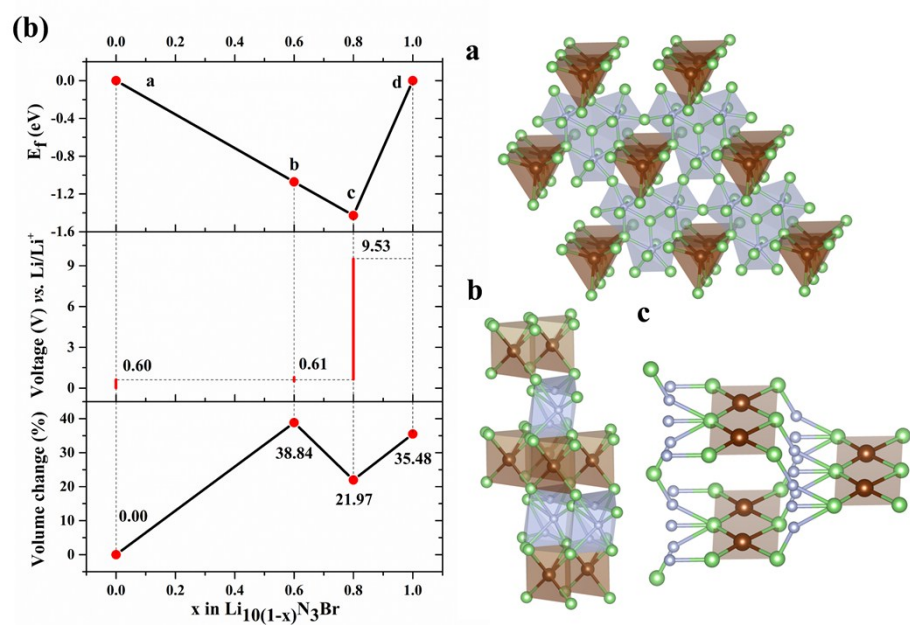
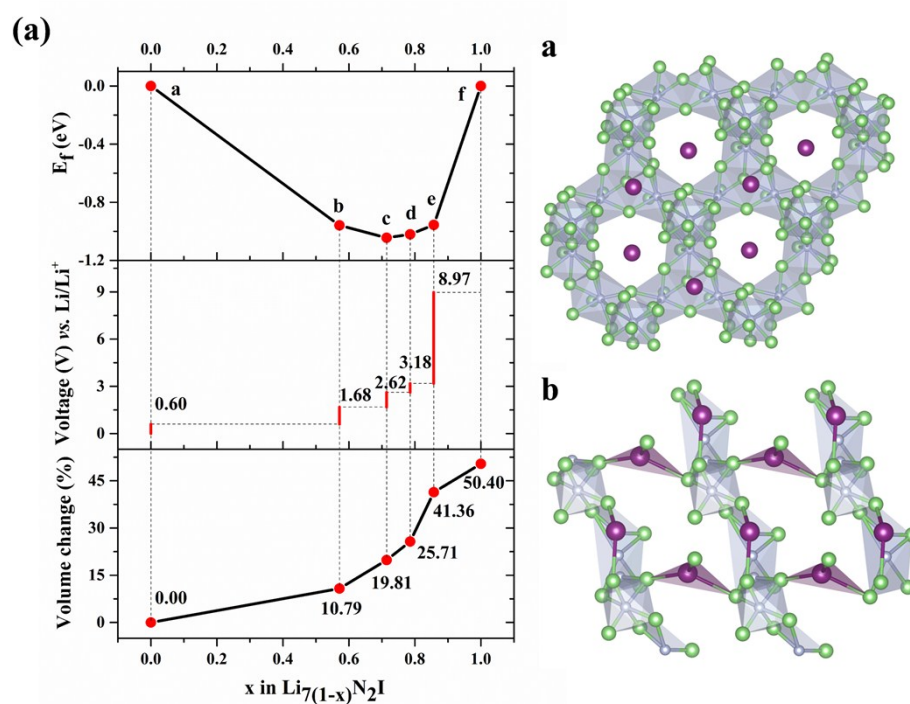


Fig. S8 The energy convex hulls, voltage plateau, and volume change rate during the process of Li^+ depletion through ATAT simulation for (a) $\text{Li}_{3(1-x)}\text{N}$ ($0 \leq x \leq 1$) (b) $\text{Li}_{(1-x)}\text{F}$ ($0 \leq x \leq 1$) (c) $\text{Li}_{(1-x)}\text{Cl}$ ($0 \leq x \leq 1$) (d) $\text{Li}_{(1-x)}\text{Br}$ ($0 \leq x \leq 1$) (e) $\text{Li}_{(1-x)}\text{I}$ ($0 \leq x \leq 1$). The structures for some stable interphases are displayed on the right side.



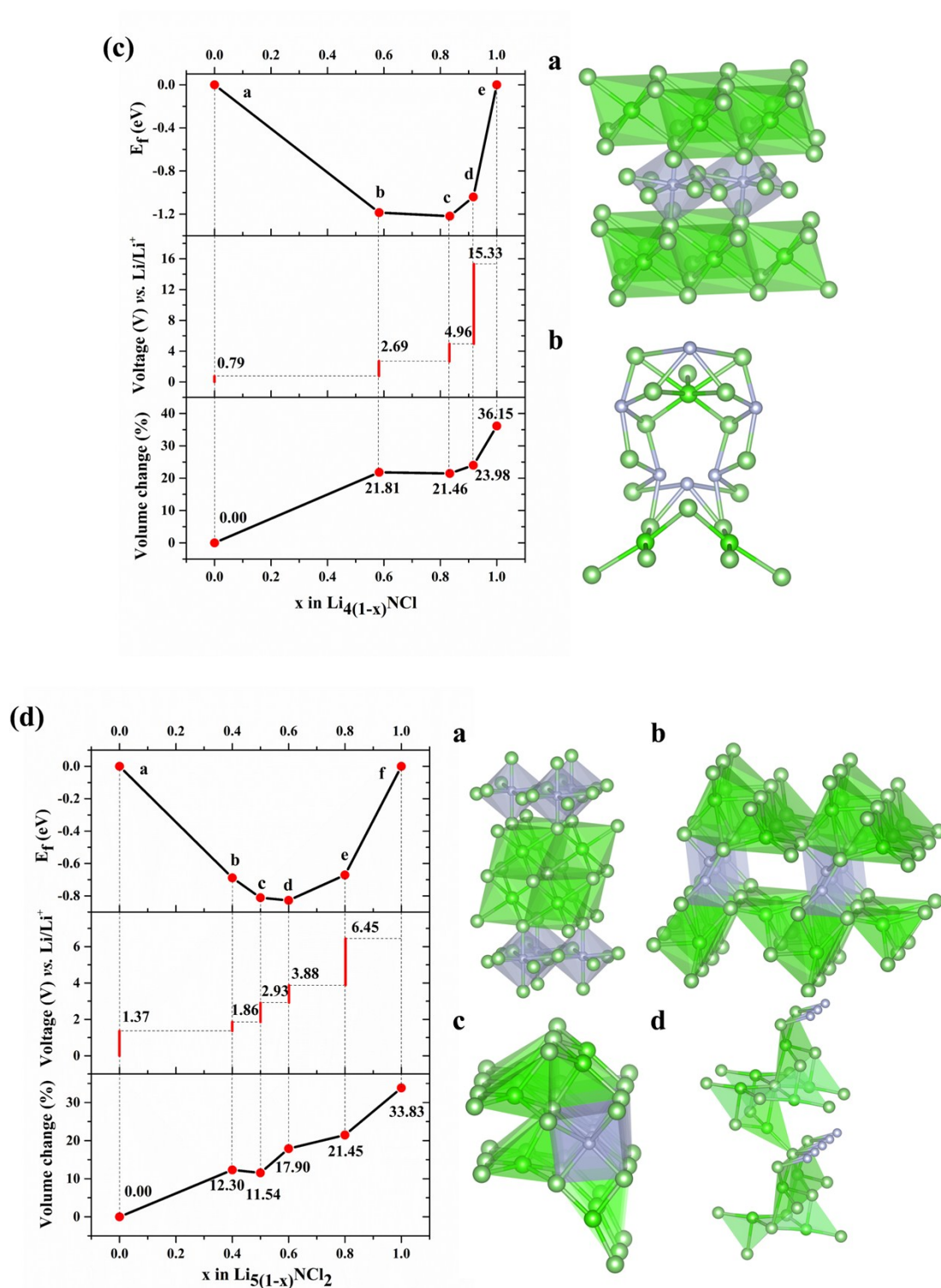


Fig. S9 The convex hulls, voltage plateau, and volume change rate during the process of Li^+ depletion through ATAT simulation for (a) $\text{Li}_{7(1-x)}\text{N}_2\text{I}$ ($0 \leq x \leq 1$) (b) $\text{Li}_{10(1-x)}\text{N}_3\text{Br}$ ($0 \leq x \leq 1$) (c) $\text{Li}_{4(1-x)}\text{NCl}$ ($0 \leq x \leq 1$), and (d) $\text{Li}_{5(1-x)}\text{NCl}_2$ ($0 \leq x \leq 1$). The structures for some stable interphases are displayed on the right side.

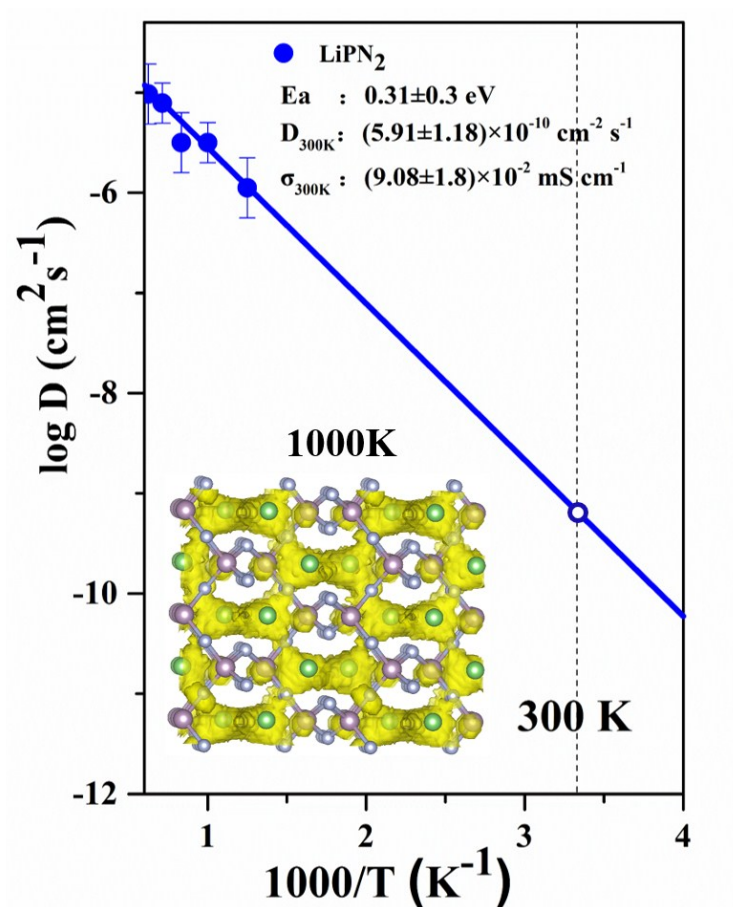


Fig. S10 Diffusion coefficients (D) for lithium ions in LiPN_2 from AIMD simulation. Some useful information, including of E_a activation barrier, Diffusion coefficients $D_{300\text{K}}$ at 300 K, Li^+ ionic conductivity $\sigma_{300\text{K}}$ at 300 K, and diffusion trajectories of Li^+ ions at 1000 K, are in insets.

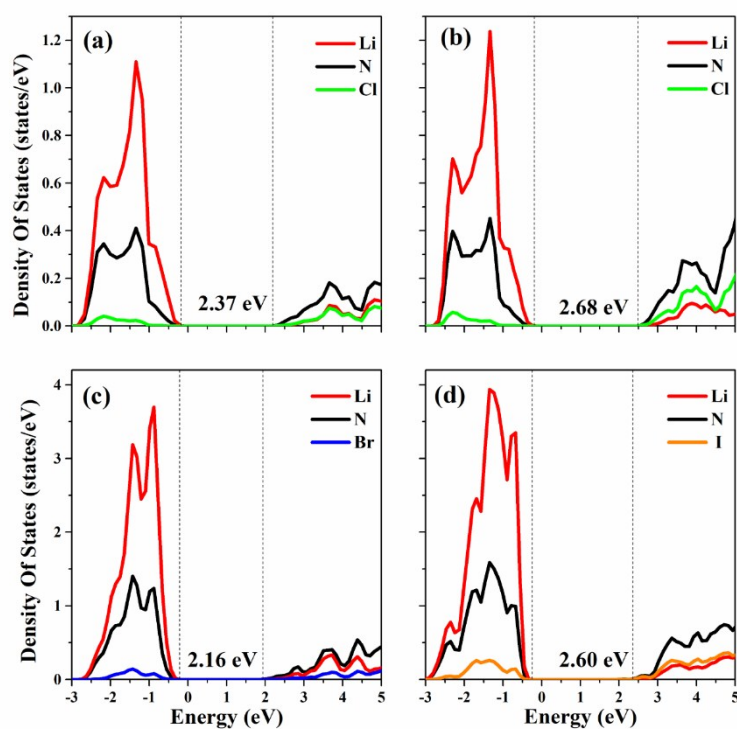


Fig. S11 The projected density of states calculated using the HSE06 functional for (a) Li_4NCl , (b) Li_6NCl_3 , (c) $\text{Li}_{10}\text{N}_3\text{Br}$, (d) $\text{Li}_7\text{N}_2\text{I}$.

Table S1 Summary of data for the Li^+ ionic conductivities of referential compounds.

System	E_a (eV)	$D_{300\text{K}}$ ($\text{cm}^2 \text{s}^{-1}$)	$\sigma_{300\text{K}}$ (mS cm^{-1})
Li_3N	0.48 ± 0.07	$(4.83 \pm 1.35) \times 10^{-11}$	$(2.04 \pm 0.57) \times 10^{-2}$
$\text{Li}_3\text{N-vacancy}$	0.28 ± 0.03	$(1.23 \pm 0.14) \times 10^{-8}$	5.07 ± 0.56
LiF	0.45 ± 0.08	$(2.73 \pm 0.82) \times 10^{-12}$	$(9.84 \pm 2.95) \times 10^{-4}$
LiCl	0.42 ± 0.06	$(3.14 \pm 0.81) \times 10^{-11}$	$(5.56 \pm 0.15) \times 10^{-3}$
LiBr	0.52 ± 0.08	$(2.2 \pm 0.64) \times 10^{-12}$	$(6.45 \pm 1.87) \times 10^{-4}$
LiI	0.58 ± 0.11	$(1.32 \pm 0.44) \times 10^{-12}$	$(2.96 \pm 0.98) \times 10^{-4}$
$\text{Li}_{3.92}\text{NCl}$	0.30 ± 0.03	$(8.17 \pm 0.71) \times 10^{-9}$	2.12 ± 0.40
$\text{Li}_{4.92}\text{NCl}_2$	0.32 ± 0.02	$(3.31 \pm 0.51) \times 10^{-9}$	1.01 ± 0.19
$\text{Li}_{5.93}\text{NCl}_3$	0.44 ± 0.04	$(5.72 \pm 0.62) \times 10^{-11}$	$(1.53 \pm 0.29) \times 10^{-2}$