# Large Amplitude Angular Jump Motions Connect Temporal 

 Heterogeneity in Aqueous SolutionsDebasish Das Mahanta*, Rajib Kumar Mitra*

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## Functional form of force field for DME

We used the unified atom models for DME molecules. The interaction potential energy function (V) among the molecules is in general represented as follows,

$$
\begin{align*}
& V\left(r_{1}, r_{2}, r_{3} \ldots, r_{n}\right) \\
& \quad=\sum_{\text {bond }} \frac{1}{2} K_{b}\left(b-b_{0}\right)^{2}+\sum_{\text {angles }} \frac{1}{2} K_{\theta}\left(\theta-\theta_{0}\right)^{2}+\sum_{\text {dihedral }} K_{\varphi}[1+\cos (n \varphi-\delta)]+\sum_{i} \sum_{j>} \tag{S1}
\end{align*}
$$

The above equation (equation S1) consists of two types of interactions, bonded and non-bonded interactions. The first four terms in the equation represent the bonded interactions and the last two terms represent the non-bonded interactions. $\mathrm{K}_{\mathrm{b}}$ is the bond force constant associated with the equilibrium bond distance $\left(\mathrm{b}_{0}\right), K_{\theta}$ is the angle force constant with the equilibrium angle ( $\theta_{0}$ ). $K_{\varphi_{\text {is }}}$ the dihedral constant with periodicity n , dihedral angle $\varphi$ and phase shift $\delta . \mathrm{r}_{\mathrm{ij}}$ is the distance between the i -th and the j -th atoms with partial charges $\mathrm{q}_{\mathrm{i}}$ and $\mathrm{q}_{\mathrm{i}}$, respectively. $A=4 \epsilon \sigma_{i j}^{12}$ and $B=4 \epsilon \sigma_{i j}^{6}$ are the Lennard-Jones constant with $\epsilon$ is the depth of the potential well, and $\sigma$ is the distance where the potential vanishes to zero. Further details about the force parameters are given in the table S1.

## Radial distribution function

To compute the spatial distributions of the atoms of the molecules as a function of distance (r) in all those binary mixtures, we compute the radial distribution functions (RDF) of various possible pairs of oxygen following the equation as given below,

$$
\begin{equation*}
R D F_{i j}(r)=\left\langle\sum_{i j} \delta\left(r-r_{i j}\right)\right\rangle \tag{S2}
\end{equation*}
$$

where $\mathrm{r}_{\mathrm{ij}}$ is the distance between any i -th and j -th oxygen atoms.

## Average Number of Rotational Jumps:

According to Poissonian probability distribution function,

$$
P(N, t)=\frac{1}{N!}(t / \tau)^{N} e^{-(t / \tau)}
$$

where N can take values as $0,1,2,3, \ldots$. The average number of events in an interval t can be written as,

$$
\begin{aligned}
& \langle N(t)\rangle=\sum_{N=0}^{\infty} N(t) P(N, t) \\
& \langle N(t)\rangle=e^{-(t / \tau)}\left[\left({ }^{t} / \tau\right)+\frac{1}{2!}(t / \tau)^{2}+\frac{1}{3!}(t / \tau)^{3}+\ldots\right] \\
& \langle N(t)\rangle=e^{-(t / \tau)}\left(e^{t / \tau}-1\right) \\
& \langle N(t)\rangle=\left[1-e^{-(t / \tau)}\right]
\end{aligned}
$$

Neglecting the higher order terms of $(t / \tau)$,

$$
\begin{equation*}
\langle N(t)\rangle={ }^{t} / \tau \tag{S3}
\end{equation*}
$$

This shows that the average number of events in a certain time interval is proportional to the time (increase linearly with $t$ ).

Table S1. DME force field parameters.

| Lennadr-Jones parameters |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Atom types | $\mathrm{C}_{6}\left(\mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ | $\mathrm{C}_{12}\left(\mathrm{~kJ} \mathrm{~mol}^{-1} \mathrm{~nm}^{12}\right)$ |  | Charge (e) | Mass (uma) |
| C (H3) | $9.3547 \times 10^{-3}$ | $3.6075 \times 10^{-3}$ |  | 0.225 | 15.035 |
| C(H2) | $5.9491 \times 10^{-3}$ | $1.7912 \times 10^{-3}$ |  | 0.225 | 14.027 |
| O | $2.0751 \times 10^{-6}$ | $1.5127 \times 10^{-3}$ |  | -0.450 | 15.999 |
| Modified atom pairs |  |  |  |  |  |
| Atom pair type |  | $\mathrm{C}_{6}\left(\mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ |  | $\mathrm{C}_{12}\left(\mathrm{~kJ} \mathrm{~mol}^{-1} \mathrm{~nm}^{12}\right)$ |  |
| $\mathrm{O}_{\text {DME }}-\mathrm{O}_{\mathrm{w}}$ |  | $0.6082 \times 10^{-2}$ |  | $0.5475 \times 10^{-5}$ |  |
| Bonds Distance (in nm) |  |  |  |  |  |
| C-C |  |  | C-O |  |  |
| 0.153 |  |  | 0.141 |  |  |
| Bond angles |  |  |  |  |  |
| Angles |  | $\Phi$ (deg) |  | $\mathrm{K}_{\Phi}\left(\mathrm{kJ} \mathrm{mol}^{-1} \mathrm{rad}^{-2}\right)$ |  |
| C-C-O |  | 109.5 |  | 418.68 |  |
| C-O-C |  | 109.5 |  | 501.22 |  |
| Proper dihedrals |  |  |  |  |  |
| Dihedrals | $\mathrm{C}_{0}\left(\mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ | $\mathrm{C}_{1}\left(\mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ | $\mathrm{C}_{2}\left(\mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ | $\mathrm{C}_{3}\left(\mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ | $\mathrm{C}_{4}\left(\mathrm{~kJ} \mathrm{~mol}^{-1}\right)$ |
| O-C-C-O | -3.10 | -0.74 | -4.69 | -6.87 | 15.4 |
| $\mathrm{C}-\mathrm{O}-\mathrm{C}-\mathrm{C}$ | 1.12 | -3.51 | -2.54 | 0.03 | 4.90 |

Table S2. Composition of the simulation box at different $X_{w}$.

| $\mathbf{X}_{\mathbf{w}}$ | Water | DME |
| :---: | :---: | :---: |
| 0.06 | 800 | 50 |
| 0.25 | 600 | 200 |
| 0.45 | 500 | 393 |
| 0.60 | 200 | 300 |
| 0.70 | 200 | 500 |
| 0.85 | 200 | 1133 |
| 0.90 | 100 | 900 |

Table S3. Waiting time of the jump events (as calculated from the linear fit of $n$. vs $t$ ) at different $\mathrm{X}_{\mathrm{w}}$.

| $\mathbf{X}_{\mathbf{w}}$ | Waiting time (ps) |
| :---: | :---: |
| 0.06 | 2.89 |
| 0.25 | 3.68 |
| 0.45 | 3.91 |
| 0.60 | 4.00 |
| 0.70 | 4.12 |
| 0.85 | 4.21 |
| 0.90 | 4.20 |



Scheme S1. Geometrical definition (both distance and angle criteria) of hydrogen bond among water molecules.


Figure S1. Radial distribution functions (RDF) in between (a) water oxygen-oxygen atoms (OW-OW), (b) DME oxygen-oxygen atoms (ODM-ODM) and (c) water oxygen-DME oxygen atoms (OW-ODM) for all the mixtures.


Figure S2. Coordination number of the rotating water molecule average over (a) water-water jumps and (b) DME-DME jumps. Arrow indicates the increasing of water concentration.


Figure S3. Average transition distance (average over only water-water jump events) from the central rotating water molecule to the initial (black lines) and the final (red lines) H-bond partner at the instant of H -bond switch (transition state; $\mathrm{t}=0$ ) at various $\mathrm{X}_{\mathrm{w}}$.


Figure S4. Progress of the average transition distance (average over only water-DME jump events) from the central rotating water molecule to the initial (black lines) and the final (red lines) H-bond partner around H -bond switching (transition state; $\mathrm{t}=0$ ) at various $\mathrm{X}_{\mathrm{w}}$.


Figure S5. Progress of the average transition distance (average over only DME-water jump events) from the central rotating water molecule to the initial (black lines) and the final (red lines) H -bond partner around H -bond switch event (transition state; $\mathrm{t}=0$ ) at various $\mathrm{X}_{\mathrm{w}}$.


Figure S6. Progress of the average transition distance (average over only DME-DME jump events) from the central rotating water molecule to the initial (black lines) and the final (red lines) H -bond partner around H -bond jump (transition state; $\mathrm{t}=0$ ) at various $\mathrm{X}_{\mathrm{w}}$.


Figure S7. Time evolution of the average transition angle for various individual types of Hbond partner exchange events for three different $\mathrm{X}_{\mathrm{w}}$.


Figure S8. The jump angle distributions of any rotating central water molecule for various type of jump events (a) water-water, (b) DME-DME, (c) water-DME and (d) DME-water at each simulated concentrations.

