

Electronic supplementary information (ESI) for: Impact of anion shape on Li^+ solvation and on transport properties for lithium-air batteries: a molecular dynamics study

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The information contained in this material is described as:

- Section 1 comprises the time correlation functions for shear viscosity, self-diffusivity and ionic conductivity.
- Section 2 presents the system size effect analyses on transport properties.
- Section 3 has the information of structural arrangement for different molalities and temperatures.
- Section 4 consists on simulation details of initial configurations, force fields and LAMMPS running files.

1 Time correlation functions

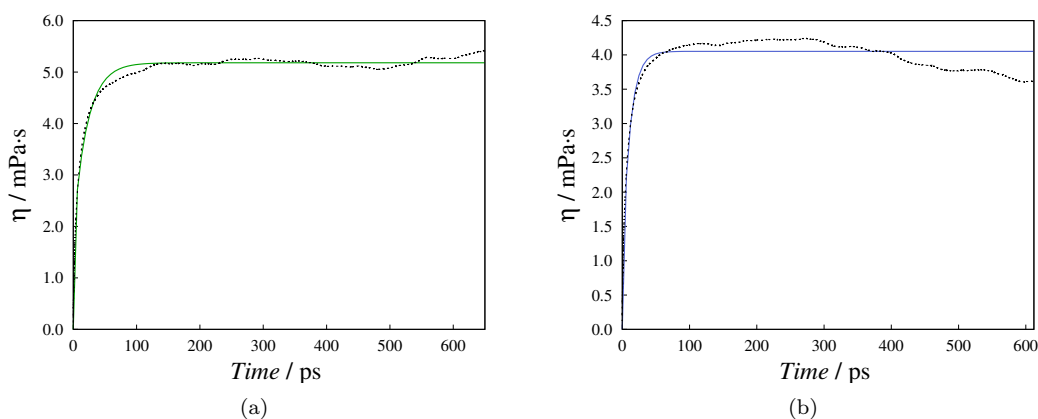


Figure S1: The shear viscosity corresponding to the running integral (Eq. 2) averaged over 30 trajectories (dashed line) and the fitting empirical function (Eq. 3) (solid line) at $1 \text{ mol}\cdot\text{kg}^{-1}$ and 298 K for: (a) LiPF_6 , and (b) LiPyr .

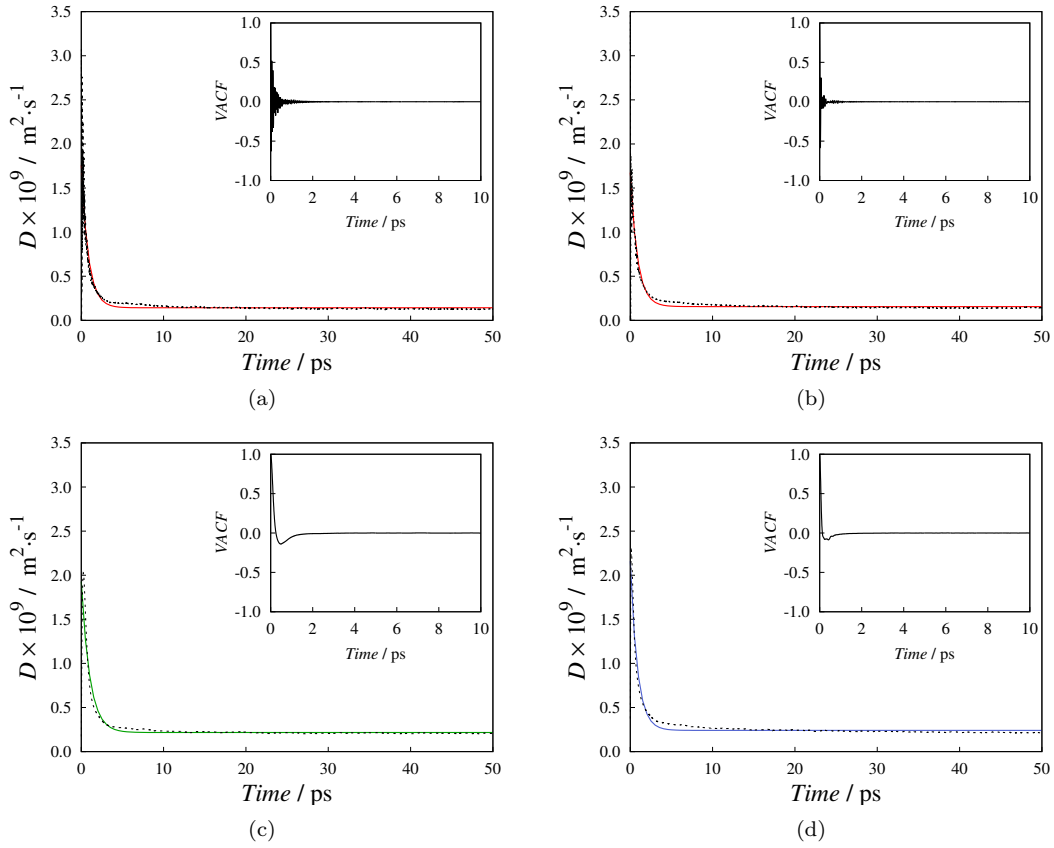


Figure S2: Self-diffusion corresponding to the running integral (Eq. 6) averaged over 10 trajectories (dashed line) and the fitting empirical function (Eq. 7) (solid line) at $1 \text{ mol} \cdot \text{kg}^{-1}$ and 298 K for: (a) Li^+ in solution with PF_6^- , (b) Li^+ in solution with Pyr^- , (c) PF_6^- , and (d) Pyr^- . The insets show the normalized velocity autocorrelation function (VACF).

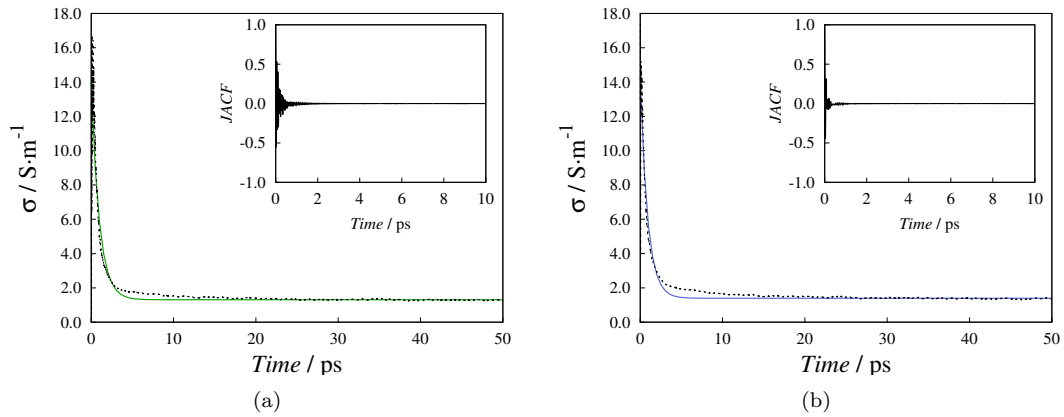


Figure S3: Ionic conductivity corresponding to the running integral (Eq. 9) averaged over 10 trajectories (dashed line) and the fitting empirical function (analogous to Eq. 7) (solid line) at $1 \text{ mol} \cdot \text{kg}^{-1}$ and 298 K for: (a) LiPF_6 , and (b) LiPyr . The insets show the normalized electrical current autocorrelation function (JACF).

2 System size analysis

System size effect at collective properties must be taken into account in molecular simulations. Several authors have discussed such an effect considering error propagation and poor statistics caused by the influence of periodic boundary conditions in small box size and limited number of molecules. [1, 2, 3, 4,

5, 6].

Although larger system sizes improve the accuracy, they also increase the computational cost. To counterbalance computation cost and good accuracy of results, three set of systems were considered. We evaluated the system size effect on the self-diffusion coefficients and the ionic conductivities; viscosity seems to be unaffected by the system size [2, 5, 7, 6, 8]. LiPF_6 and LiPyr in DMSO solutions with $1 \text{ mol}\cdot\text{kg}^{-1}$ at 298 K were simulated with the following number of lithium ions and number of DMSO molecules: 40/512, 60/768, and 80/1024 (the number of anions is equal to the number of lithium ions).

Figure S4 (a) and (c) presents results of transport coefficients as a function of the inverse of number of cations. Even though we notice decrease of uncertainties for larger systems, almost the same average trend is observed for the value of each property. However, in order to increase the accuracy of self-diffusivity coefficient, we implemented the system-size correction (Eq. 9). Figure S4 (b) illustrates the improvement on this property with correction when compared with larger systems.

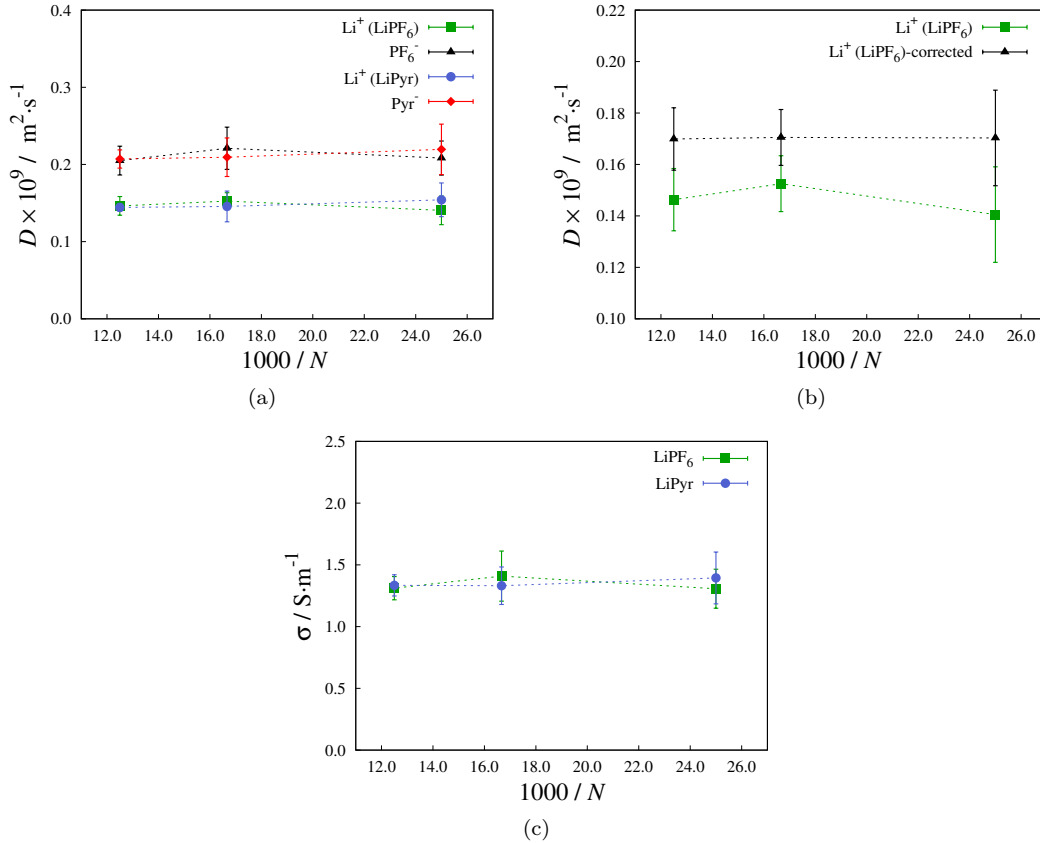


Figure S4: System size effect on the transport properties of LiPF_6 in DMSO and LiPyr in DMSO both at $1 \text{ mol}\cdot\text{kg}^{-1}$ and 298 K: (a) Self-diffusion coefficients without size effect correction, (b) Self-diffusion coefficients of Li^+ of LiPF_6 in DMSO without correction and corrected and, (c) Ionic conductivity coefficients.

3 Structural arrangement

Table S1: Coordination numbers of the first solvation shell for Li-O (DMSO), Li-F(PF₆) and Li-N(Pyr) at 1 atm for different salt molalities and at different temperatures.

Salt molality / mol·kg ⁻¹	Temperature / K			
	298			
n _{Li-O} for LiPF ₆ in DMSO	4.00	3.91	3.83	3.74
n _{Li-F} for LiPF ₆ in DMSO	0.01	0.09	0.19	0.29
n _{Li-O} for LiPyr in DMSO	4.00	3.85	3.58	3.32
n _{Li-N} for LiPyr in DMSO	0.44	0.58	0.70	0.87

Temperature / K	Salt molality / mol·kg ⁻¹		
	1.00		
n _{Li-O} for LiPF ₆ in DMSO	3.74	3.93	3.99
n _{Li-F} for LiPF ₆ in DMSO	0.29	0.08	0.01
n _{Li-O} for LiPyr in DMSO	3.32	3.08	2.80
n _{Li-N} for LiPyr in DMSO	0.87	1.00	1.14

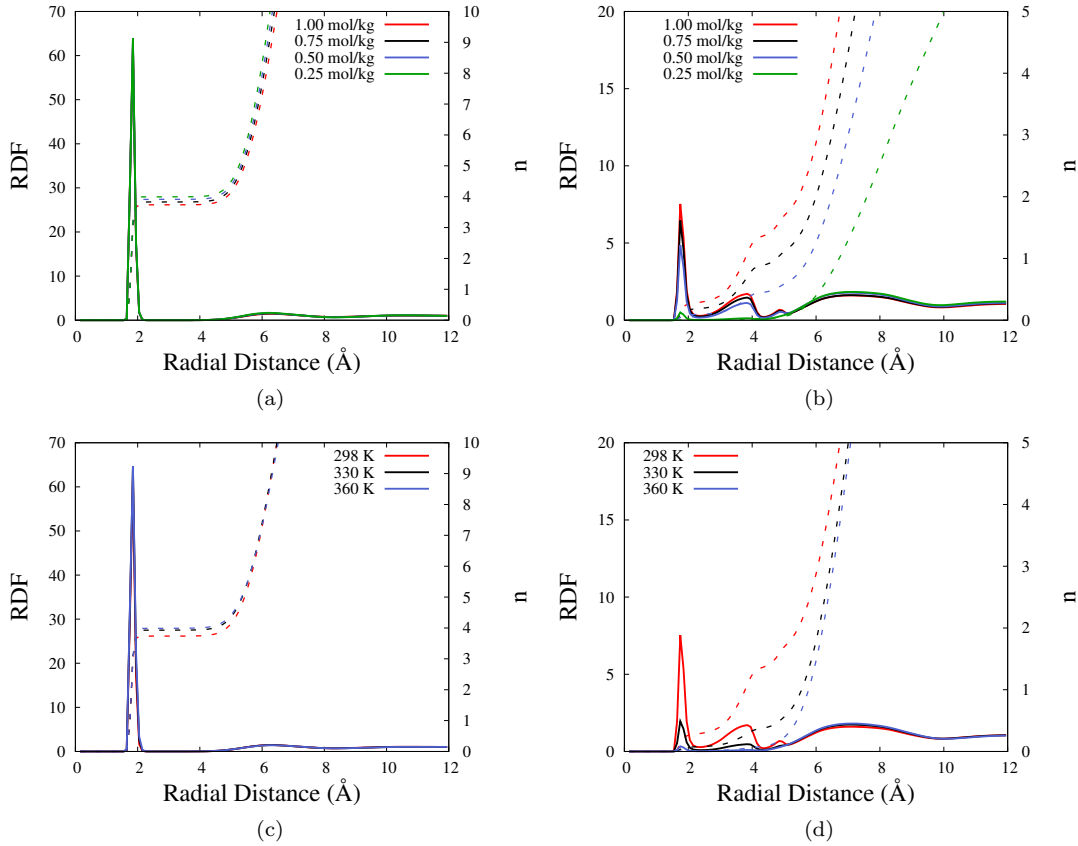


Figure S5: Radial distribution functions (RDF) (solid lines, left y axis), and coordination numbers (dashed lines, right y axis) for LiPF₆ in solution with DMSO as function of: (a) concentration at 298 K for Li-O (DMSO), (b) concentration at 298 K for Li-F (PF₆), (c) temperature at 1.0 mol·kg⁻¹ for Li-O (DMSO), and (d) temperature at 1.0 mol·kg⁻¹ for Li-F (PF₆).

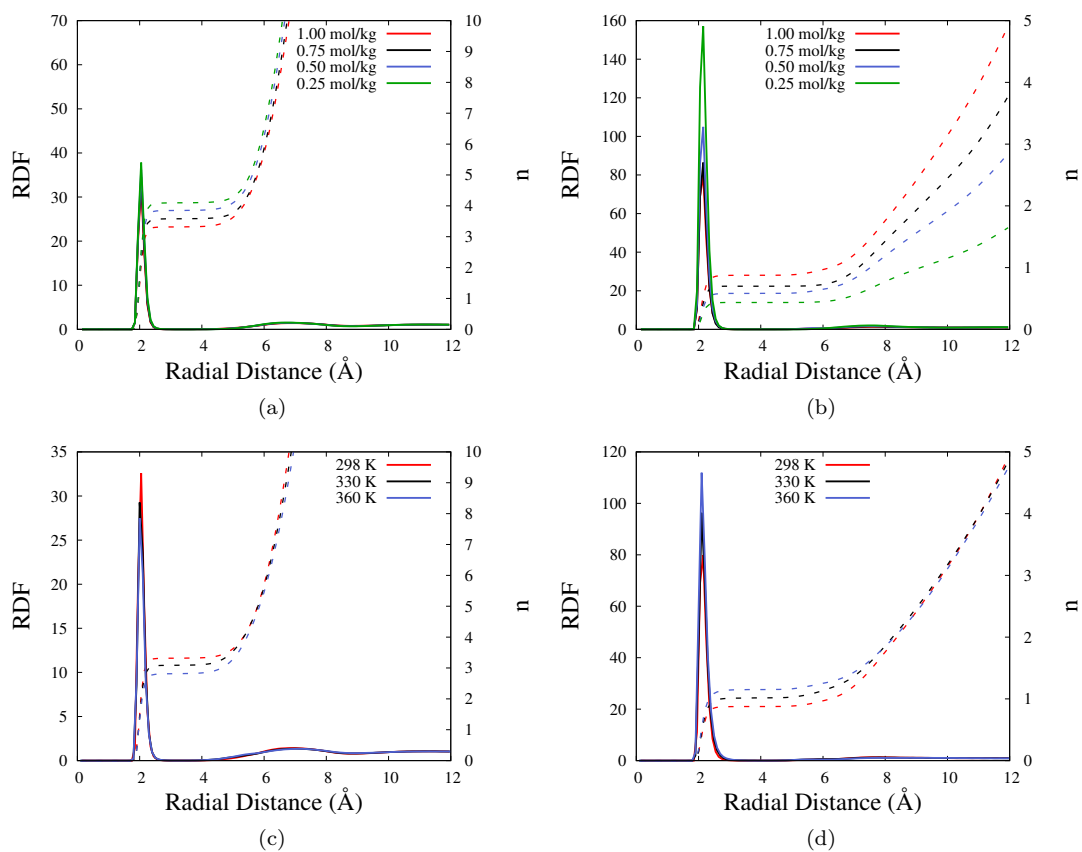


Figure S6: Radial distribution functions (RDF) (solid lines, left y axis), and coordination numbers (dashed lines, right y axis) for LiPyr in solution with DMSO as function of: (a) concentration at 298 K for Li-O (DMSO), (b) concentration at 298 K for Li-N (Pyr), (c) temperature at $1.0 \text{ mol}\cdot\text{kg}^{-1}$ for Li-O (DMSO), and (d) temperature at $1.0 \text{ mol}\cdot\text{kg}^{-1}$ for Li-N (Pyr).

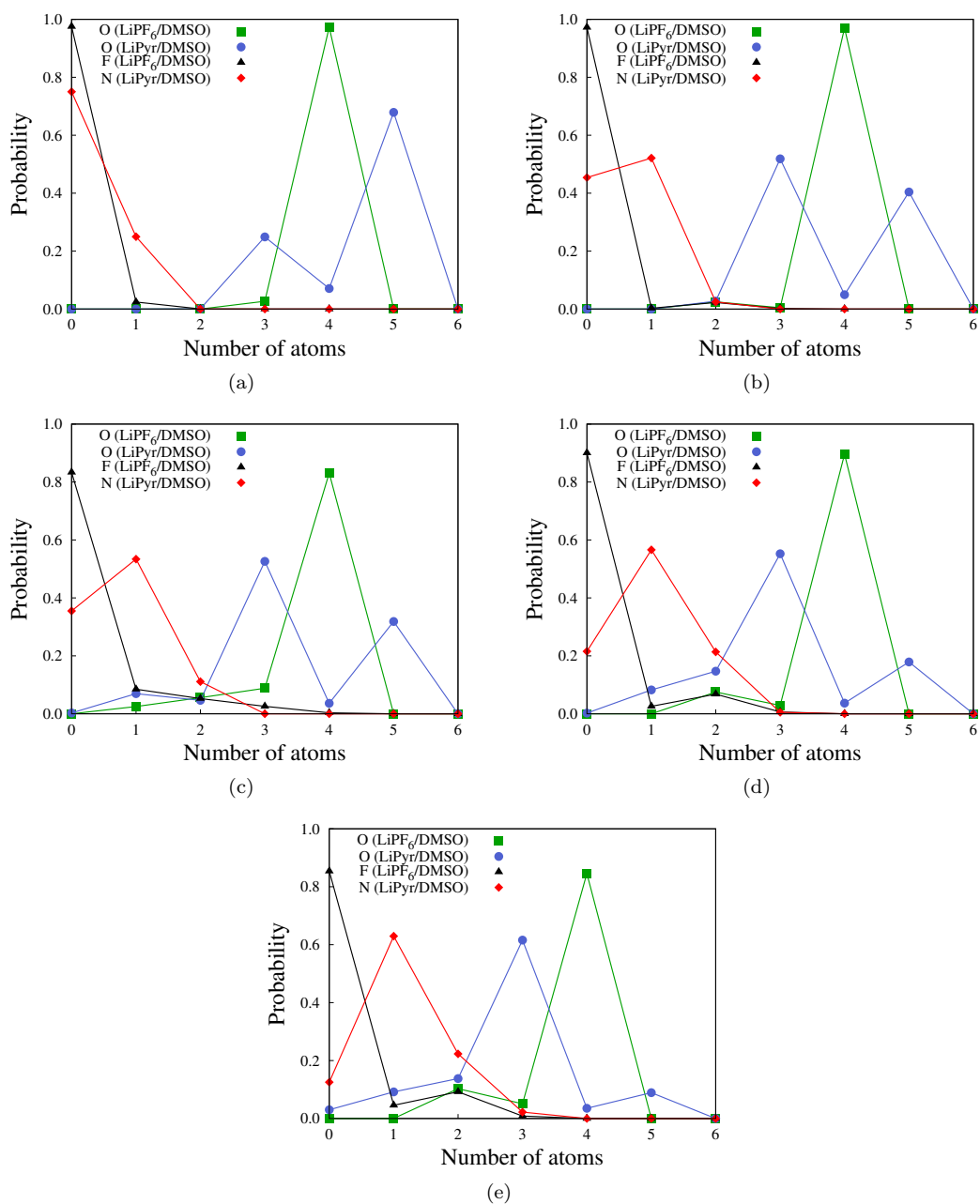


Figure S7: Solvation probability distribution of the first shell layer at: (a) 0.25 mol·kg⁻¹ and 298 K, (b) 0.50 mol·kg⁻¹ and 298 K, (c) 0.75 mol·kg⁻¹ and 298 K, (d) 1.00 mol·kg⁻¹ and 330 K, (e) 1.00 mol·kg⁻¹ and 360 K,

4 Simulation details

4.1 Molecular sketches

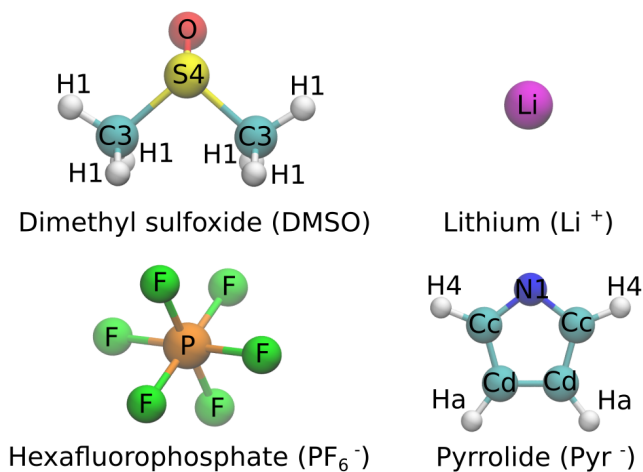


Figure S8: Schematic illustrations of molecular structures for DMSO, PF₆⁻, Li⁺, and Pyr⁻ with assignment of atom types.

4.2 Dimethyl sulfoxide Molecule

```
! ATOM:
!! index (int): atom index
!! name (str): atom name (required)
!! type (str): atomtype name
!! charge (float, e): partial atomic charge
!! x (float, angstrom): atom coordinate
!! y (float, angstrom): atom coordinate
!! z (float, angstrom): atom coordinate
ATOM name type charge x y z ! 10
S1 s4 0.359151 0.03900 0.26600 0.62000 ! 1
O1 o -0.485225 0.55900 1.49000 -0.10400 ! 2
C1 c3 -0.498374 -1.71300 0.05400 0.11500 ! 3
H1 h1 0.187137 -1.77400 0.06600 -0.97400 ! 4
H2 h1 0.187137 -2.10400 -0.87800 0.52700 ! 5
H3 h1 0.187137 -2.26000 0.90200 0.52700 ! 6
C2 c3 -0.498374 0.69300 -1.19800 -0.27200 ! 7
H4 h1 0.187137 0.25900 -2.10800 0.14700 ! 8
H5 h1 0.187137 0.46500 -1.09900 -1.33400 ! 9
H6 h1 0.187137 1.77200 -1.19600 -0.12100 ! 10

! BOND:
BOND ! 9
O1 S1 ! 1 1.514
C1 S1 ! 2 1.836
C2 S1 ! 3 1.835
C1 H1 ! 4 1.091
C1 H2 ! 5 1.091
C1 H3 ! 6 1.090
C2 H4 ! 7 1.092
C2 H5 ! 8 1.091
C2 H6 ! 9 1.090
```

```

! ANGLE:
ANGLE ! 15
H1 C1 S1 ! 1 109.073
H2 C1 S1 ! 2 109.676
H3 C1 S1 ! 3 106.567
H4 C2 S1 ! 4 109.681
H5 C2 S1 ! 5 109.052
H6 C2 S1 ! 6 106.508
C1 S1 O1 ! 7 106.834
C2 S1 O1 ! 8 106.865
C1 S1 C2 ! 9 96.563
H1 C1 H2 ! 10 111.483
H1 C1 H3 ! 11 109.923
H2 C1 H3 ! 12 109.991
H4 C2 H5 ! 13 111.483
H4 C2 H6 ! 14 110.000
H5 C2 H6 ! 15 109.987

```

```

! DIHEDRAL:
DIHEDRAL ! 12
H1 C1 S1 O1 ! 1 51.617
H1 C1 S1 C2 ! 2 -58.255
H2 C1 S1 O1 ! 3 173.971
H2 C1 S1 C2 ! 4 64.099
H3 C1 S1 O1 ! 5 -67.004
H3 C1 S1 C2 ! 6 -176.877
H4 C2 S1 O1 ! 7 -173.946
H4 C2 S1 C1 ! 8 -64.101
H5 C2 S1 O1 ! 9 -51.602
H5 C2 S1 C1 ! 10 58.244
H6 C2 S1 O1 ! 11 67.051
H6 C2 S1 C1 ! 12 176.897

```

4.3 Hexafluorophosphate Molecule

```

! ATOM:
!! index (int): atom index
!! name (str): atom name (required)
!! type (str): atomtype name
!! charge (float, e): partial atomic charge
!! x (float, angstrom): atom coordinate
!! y (float, angstrom): atom coordinate
!! z (float, angstrom): atom coordinate
ATOM name type charge x y z ! 7
P1 p 1.07 0.18051 0.87394 0.02384 ! 1
F1 f -0.345 0.16559 0.88898 1.66961 ! 2
F2 f -0.345 0.19542 0.85891 -1.62194 ! 3
F3 f -0.345 1.35402 2.02802 0.02393 ! 4
F4 f -0.345 -0.99301 -0.28013 0.02374 ! 5
F5 f -0.345 -0.97348 2.04736 0.00265 ! 6
F6 f -0.345 1.33449 -0.29947 0.04502 ! 7

```

```

! BOND:
BOND ! 6
P1 F1 ! 1
P1 F2 ! 2
P1 F3 ! 3
P1 F4 ! 4
P1 F5 ! 5

```



```
P1   F6   ! 6
```

```
! ANGLE:
```

```
ANGLE ! 12
```

```
F1   P1   F3   ! 1
F1   P1   F4   ! 1
F1   P1   F5   ! 1
F1   P1   F6   ! 1
F2   P1   F3   ! 1
F2   P1   F4   ! 1
F2   P1   F5   ! 1
F2   P1   F6   ! 1
F3   P1   F5   ! 1
F3   P1   F6   ! 1
F4   P1   F5   ! 1
```

4.4 Lithium Molecule

```
! ATOM:
```

```
!! index (int): atom index
!! name (str): atom name (required)
!! type (str): atomtype name
!! charge (float, e): partial atomic charge
!! x (float, angstrom): atom coordinate
!! y (float, angstrom): atom coordinate
!! z (float, angstrom): atom coordinate
```

```
ATOM name type charge x y z ! 1
```

```
Li1   li   1.000000   0.00000   0.00000   0.00000   ! 1
```

4.5 Pyrrolide Molecule

```
! ATOM:
```

```
!! index (int): atom index
!! name (str): atom name (required)
!! type (str): atomtype name
!! charge (float, e): partial atomic charge
!! x (float, angstrom): atom coordinate
!! y (float, angstrom): atom coordinate
!! z (float, angstrom): atom coordinate
```

```
ATOM name type charge x y z ! 9
```

```
C1   cc   0.102030  -14.18600   7.64900   -0.31800   ! 1
C2   cc  -0.328829  -12.77900   7.60400   -0.31800   ! 2
C3   cd  -0.328829  -12.35800   8.96400   -0.31800   ! 3
C4   cd   0.102030  -13.54500   9.72200   -0.31800   ! 4
N1   n1  -0.672421  -14.65900   8.93000   -0.31800   ! 5
H1   h4  -0.004135  -14.87600   6.80100   -0.31800   ! 6
H2   ha   0.067145  -12.14700   6.71400   -0.31800   ! 7
H3   ha   0.067145  -11.33400   9.34200   -0.31800   ! 8
H4   h4  -0.004135  -13.63600  10.81100   -0.31800   ! 9
```

```
! BOND:
```

```
BOND ! 9
```

```
C1   C2   ! 1   1.408
C1   N1   ! 2   1.366
C1   H1   ! 3   1.093
C2   C3   ! 4   1.424
C2   H2   ! 5   1.092
C3   C4   ! 6   1.408
C3   H3   ! 7   1.092
```

```
C4  N1  ! 8    1.367
C4  H4  ! 9    1.093
```

! ANGLE:

ANGLE ! 13

```
C1  C2  C3  ! 1  105.369
C1  C2  H2  ! 2  127.211
C1  N1  C4  ! 3  105.145
C2  C1  N1  ! 4  112.098
C2  C1  H1  ! 5  127.303
C2  C3  C4  ! 6  105.361
C2  C3  H3  ! 7  127.462
C3  C2  H2  ! 8  127.421
C3  C4  N1  ! 9  112.027
C3  C4  H4  ! 10 127.338
C4  C3  H3  ! 11 127.177
H1  C1  N1  ! 12 120.599
H4  C4  N1  ! 13 120.634
```

! DIHEDRAL:

DIHEDRAL ! 16

```
N1  C1  C2  C3  ! 1
H1  C1  C2  C3  ! 2  180.000
N1  C1  C2  H2  ! 3  180.000
H1  C1  C2  H2  ! 4
C2  C1  N1  C4  ! 5
H1  C1  N1  C4  ! 6  180.000
C1  C2  C3  C4  ! 7
H2  C2  C3  C4  ! 8 -180.000
C1  C2  C3  H3  ! 9  180.000
H2  C2  C3  H3  ! 10
C2  C3  C4  N1  ! 11
H3  C3  C4  N1  ! 12  180.000
C2  C3  C4  H4  ! 13  180.000
H3  C3  C4  H4  ! 14
C3  C4  N1  C1  ! 15
H4  C4  N1  C1  ! 16  180.000
```

! IMPROPER:

IMPROPER ! 4

```
C2  H1  C1  N1  ! 1 -180.000
C1  C3  C2  H2  ! 2  180.000
C2  C4  C3  H3  ! 3  180.000
C3  H4  C4  N1  ! 4  180.000
```

4.6 Force Field for DMSO/LiPF₆

Masses

```
1  32.060 # s4 DMS
2  16.000 # o DMS
3  12.010 # c3 DMS
4  1.008  # h1 DMS
5  6.941  # li LI
6  31.000 # p PF6
7  19.000 # f PF6
```

Pair Coeffs # lj/charmm/coul/long

1 0.35 3.564 0.35 3.564
2 0.12 3.029 0.12 3.029
3 0.078 3.635 0.078 3.635
4 0.024 2.388 0.024 2.388
5 0.10314 1.4424 0.10314 1.4424
6 0.13169 3.695 0.13169 3.695
7 0.028716 2.9347 0.028716 2.9347

Bond Coeffs # harmonic

1 540 1.53
2 240 1.8
3 322 1.11
4 370.8 1.606

Angle Coeffs # harmonic

1 46.1 111.3
2 79 106.75
3 34 95
4 35.5 108.4
5 139.4 90

Dihedral Coeffs # charmm

1 0.2 3 0 0
2 0.2 3 0 0

4.7 Force Field for DMSO/LiPyr

Masses

1 32.060 # s4 DMS
2 16.000 # o DMS
3 12.010 # c3 DMS
4 1.008 # h1 DMS
5 6.941 # li LI
6 12.010 # cc PYR
7 12.010 # cd PYR
8 14.010 # n1 PYR
9 1.008 # h4 PYR
10 1.008 # ha PYR

Pair Coeffs

1 0.350 3.564 # s4 DMS
2 0.120 3.029 # o DMS
3 0.078 3.635 # c3 DMS
4 0.024 2.388 # h1 DMS
5 0.0182660800896 2.126 # li LI
6 0.0859427210304 3.400 # cc PYR
7 0.0859427210304 3.400 # cd PYR
8 0.169885665734 3.250 # n1 PYR
9 0.0149893860096 2.511 # h4 PYR
10 0.0149893860096 2.600 # ha PYR

Bond Coeffs

1 540 1.53 # harmonic DMS o s4

2 240 1.80 # harmonic DMS c3 s4
 3 322 1.11 # harmonic DMS c3 h1
 4 418.018786099 1.429 # harmonic PYR cc cc
 5 539.937622253 1.309 # harmonic PYR cc n1
 6 349.86553511 1.083 # harmonic PYR cc h4
 7 503.661639974 1.371 # harmonic PYR cc cd
 8 346.968143194 1.085 # harmonic PYR cc ha
 9 418.018786099 1.429 # harmonic PYR cd cd
 10 346.968143194 1.085 # harmonic PYR cd ha
 11 539.937622253 1.309 # harmonic PYR cd n1
 12 349.86553511 1.083 # harmonic PYR cd h4

Angle Coeffs

1 46.1 111.3 # harmonic DMS h1 c3 s4
 2 79.0 106.75 # harmonic DMS c3 s4 o
 3 34.0 95.0 # harmonic DMS c3 s4 c3
 4 35.5 108.4 # harmonic DMS h1 c3 h1
 5 68.1135334848 114.19 # harmonic PYR cc cc cd
 6 47.4286574016 119.26 # harmonic PYR cc cc ha
 7 0.0 0.0 # harmonic PYR cc n1 cd
 8 71.6424337152 122.98 # harmonic PYR cc cc n1
 9 45.5301607104 129.47 # harmonic PYR cc cc h4
 10 68.1135334848 114.19 # harmonic PYR cc cd cd
 11 48.3183294912 122.89 # harmonic PYR cc cd ha
 12 48.3183294912 122.89 # harmonic PYR cd cc ha
 13 71.6424337152 122.98 # harmonic PYR cd cd n1
 14 45.5301607104 129.47 # harmonic PYR cd cd h4
 15 46.9877931072 121.51 # harmonic PYR cd cd ha
 16 52.6137775488 116.36 # harmonic PYR h4 cc n1
 17 52.6137775488 116.36 # harmonic PYR h4 cd n1

Dihedral Coeffs

1 0.2 3 0 0.0 # charmm DMS h1 c3 s4 o
 2 0.2 3 0 0.0 # charmm DMS h1 c3 s4 c3
 3 3.99732847258 2 180 0.0 # charmm PYR cd cc cc n1
 4 3.99732847258 2 180 0.0 # charmm PYR cd cc cc h4
 5 3.99732847258 2 180 0.0 # charmm PYR ha cc cc n1
 6 3.99732847258 2 180 0.0 # charmm PYR h4 cc cc ha
 7 0.0 2 180 0.0 # charmm PYR cc cc n1 cd
 8 0.0 2 180 0.0 # charmm PYR h4 cc n1 cd
 9 3.99732847258 2 180 0.0 # charmm PYR cc cc cd cd
 10 3.99732847258 2 180 0.0 # charmm PYR ha cc cd cd
 11 3.99732847258 2 180 0.0 # charmm PYR cc cc cd ha
 12 3.99732847258 2 180 0.0 # charmm PYR ha cc cd ha
 13 3.99732847258 2 180 0.0 # charmm PYR cc cd cd n1
 14 3.99732847258 2 180 0.0 # charmm PYR ha cd cd n1
 15 3.99732847258 2 180 0.0 # charmm PYR cc cd cd h4
 16 3.99732847258 2 180 0.0 # charmm PYR h4 cd cd ha
 17 0.0 2 180 0.0 # charmm PYR cd cd n1 cc
 18 0.0 2 180 0.0 # charmm PYR h4 cd n1 cc

Improper Coeffs

1 1.09926135821 -1 2 # cvff PYR cc h4 cc n1
 2 1.09926135821 -1 2 # cvff PYR cc cd cc ha
 3 1.09926135821 -1 2 # cvff PYR cc cd cd ha

```
4 1.09926135821 -1 2 # cvff PYR cd h4 cd n1
```

4.8 LAMMPS Initialization File for DMSO/LiPF₆

```
#OPLS DMSO/LiPF6

# Initialization
units          real
dimension      3
boundary       p p p
atom_style     full

variable       NRUNP equal 2E6
variable       NRUNE equal 1E6
variable       NRUNV equal 10E6
variable       NRUND equal 1E6
variable       VIEMP equal 298
variable       VPRES equal 1.0
pair_style     lj/charmm/coul/long 10.0 12.0
pair_modify    tail yes
pair_modify    mix arithmetic
bond_style     harmonic
angle_style    harmonic
dihedral_style charmm
kspace_style   ppm 1.0E-4

read_data      electrolyte.data

group          dmso type 1 2 3 4
group          li type 5
group          pf6 type 6 7

# Setup atoms
velocity       all create ${VIEMP} 118647 mom yes rot yes dist gaussian

# Settings
timestep       1.0
neighbor       2.0 bin
neighbor_modify delay 0 every 1 check yes

# Operations
fix            1 all npt temp ${VIEMP} ${VIEMP} 100 iso ${VPRES} ${VPRES} 1000

# Output
thermo         5
thermo_style   custom time temp press pe ke etotal density vol
log            npt.lammps

# Actions
run            ${NRUNP}

# Operations
unfix         1
fix           2 all nvt temp ${VIEMP} ${VIEMP} 100

run            ${NRUNE}

# Output
thermo        5
```

```

thermo_style    custom time pxx pxy pxz pyy pyz pzz density vol
log            nvt.lammps

# Actions
run            ${NRUNV}

reset_timestep 0

# Output
thermo         5
thermo_style   custom time temp etotal density vol
log            nvt.lammps
dump           myDump1 li custom 5 li.data id type mass vx vy vz
dump           myDump2 pf6 custom 5 pf6.data id type mass vx vy vz
compute        myRDF all rdf 120 5 2 5 4 5 6 5 7
fix            RDF all ave/time 1 1E6 1E6 c.myRDF[*] file rdf.data mode vector

```

```

# Actions
run            ${NRUND}

```

4.9 LAMMPS Initialization File for DMSO/LiPyr

```
#OPLS DMSO/LiPYR
```

```

# Initialization
units          real
dimension      3
boundary       p p p
atom_style     full

variable       NRUNP equal 2E6
variable       NRUNE equal 1E6
variable       NRUNV equal 10E6
variable       NRUND equal 1E6
variable       VIEMP equal 298
variable       VPRES equal 1.0
pair_style     lj/charmm/coul/long 10.0 12.0
pair_modify    tail yes
pair_modify    mix arithmetic
bond_style     harmonic
angle_style    harmonic
dihedral_style charmm
improper_style cvff
kspace_style   ppm 1.0E-4

read_data      electrolyte.data

group          dmso type 1 2 3 4
group          li type 5
group          pyr type 6 7 8 9 10

# Setup atoms
velocity       all create ${VIEMP} 432393 mom yes rot yes dist gaussian

# Settings
timestep       1.0
neighbor       2.0 bin
neighbor_modify delay 0 every 1 check yes

# Operations

```

```

fix                1 all npt temp ${VIEMP} ${VIEMP} 100 iso ${VPRES} ${VPRES} 1000

# Output
thermo            5
thermo_style      custom time press pe ke etotal density vol
log               npt.lammps

# Actions
run               ${NRUNP}

# Operations
unfix            1
fix              2 all nvt temp ${VIEMP} ${VIEMP} 100

run               ${NRUNE}

# Output
thermo            5
thermo_style      custom time pxx pxy pxz pyy pyz pzz density vol
log               nvt.lammps

# Actions
run               ${NRUNV}

reset_timestep    0
# Output
thermo            5
thermo_style      custom time temp etotal density vol
log               nvtd.lammps
dump              myDump1 li custom 5 li.data id type mass vx vy vz
dump              myDump2 pyr custom 5 pyr.data id type mass vx vy vz
compute           myRDF all rdf 120 5 2 5 4 5 8 5 9 5 10
fix               RDF all ave/time 1 1E6 1E6 c.myRDF[*] file rdf.data mode vector

# Actions
run               ${NRUND}

```

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