

Electronic Supporting Information

**Unprecedented stability enhancement of multiple charged anion through decoration
with negative electron affinity noble gases**

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Computational Details

In the present work, all the calculations are performed using Turbomole 7.2 program.^[1] The $B_{12}Ng_nF_{12}^{2-}$ ($n = 1, 2, 3, 4$ and 12) systems are optimized using dispersion corrected^[2] DFT (B3LYP–D3)^[3] and MP2^[4] methods. For all the atoms def2–TZVPP basis set is used along with 28–electron core ECP for Xe atom.^[5] Frequency calculation is performed with B3LYP–D3 functional to obtain minimum energy structure. Charge distribution analysis is performed using natural population analysis (NPA) scheme.^[6] Furthermore, to analyze the nature of chemical bond we, have performed the atoms–in–molecule (AIM) analysis^[7] and electron localization function (ELF)^[7c] analysis at B3LYP–D3/def2–TZVPP level employed with energy density function (EDF)^[8] using Multiwfn program^[9]. For $B_{12}Ng_nF_{12}^{2-}$, the dissociation energy (DE) has been calculated using B3LYP–D3 and MP2 methods. In addition to this the DE has been calculated by using DLPNO–CCSD(T) method^[10] with def2–TZVPP^[5a] basis set and def2–TZVPP/C^[11a] auxiliary basis set as implemented in ORCA4.1.2 program.^[11b] Moreover, energy decomposition analysis in conjunction with the natural orbital for chemical valence (EDA–NOCV)^[12] has been performed with ADF2017 software^[13a,13b] using B3LYP–D3 functional and TZ2P^[13c] basis set on the B3LYP–D3/def2–TZVPP optimized geometry. Scalar relativistic effect^[14] has been included in the EDA–NOCV calculations. In the EDA the total interaction energy (E^{int}) between the interacting fragments is decomposed into four energy terms: the Pauli repulsion (E^{Pauli}) between the occupied orbitals of the three fragments, the classical electrostatic attractive energy (E^{elstat}) between the interacting fragments, the attractive orbital interaction energy (E^{orb}) arising from the charge transfer and mixing of the occupied and unoccupied orbitals on the fragments and the polarization effect, and the dispersion energy (E^{disp}). Moreover, in EDA–NOCV, total deformation density ($\Delta\rho(r)$) is decomposed into its individual differential densities ($\Delta\rho_i(r)$), ($\Delta\rho(r) = \sum\Delta\rho_i(r)$) which can be represented in the pairs of NOCV. The NOCV pairs of deformation density give the direction of the charge density flow. Similarly, the total E^{orb} is decomposed into its individual ΔE_i^{orb} ($E^{\text{orb}} = \sum\Delta E_i^{\text{orb}}$) corresponding to each charge transfer channel.

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Table S1. Binding Energy of First and Second Excess Electrons ($\Delta E1$ and $\Delta E2$, in eV) in $B_{12}F_{12}^{2-}$ and $B_{12}Ng_nF_{12}^{2-}$ ($Ng = Kr-Xe$ and $n = 1, 2, 3, 4$ and 12) at B3LYP–D3/Def2–TZVPP Level of Theory.

Table S2. Optimized Ng–B and Ng–F Bond Distances (in Å) in $B_{12}Ng_nF_{12}^{2-}$ ($Ng = Ar-Xe$ and $n = 1, 2, 3, 4$ and 12) using B3LYP–D3 and MP2 Methods and Dissociation Energy (DE, kcal mol⁻¹) using B3LYP–D3 (B3), MP2 and DLPNO–CCSD(T)^a Methods with def2–TZVPP Basis Set. Covalent Ng–B and Ng–F Radii^b Reported by Cordero et al^c [Pyykkö^d] are also Provided in the Table.

Table S3. Calculated NPA Charge on Ng, B and F atoms in $B_{12}F_{12}^{2-}$ and $B_{12}Ng_nF_{12}^{2-}$ ($Ng = Ar-Xe$ and $n = 1, 2, 3, 4$ and 12) at B3LYP–D3/def2–TZVPP Level of Theory.

Table S4. Free Energy Change (ΔG , kcal mol⁻¹) of $B_{12}Ng_nF_{12}^{2-}$ ($Ng = Ar-Xe$ and $n = 1, 2, 3, 4, 12$) at 298.15 K along Path1 and Path2 Dissociation channels at B3LYP–D3/def2–TZVPP Level of Theory.

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Table S6: Calculated Values of Optimized Bond Length (in Å), B1–Ng–F Bond Angle (in Degree) and Activation Energy Barrier (AE, in kcal mol⁻¹) of Transition State Structure (along B1–Ng–F mode) of $B_{12}Ng_nF_{12}^{2-}$ ($Ng = Kr, Xe$ and $n = 1, 2, 3, 4, 12$) using B3LYP–D3/def2–TZVPP Method.

Table S7. Bond Critical Point (BCP) Properties of Ng–B (Ng–F) Bond of $B_{12}Ng_nF_{12}^{2-}$ (Ng = Kr–Xe and n = 1, 12) Compounds at B3LYP–D3/def2–TZVPP Level of Theory. BCP Properties of Ng–F Bond are Reported in the Parenthesis.

Table S8. EDA–NOCV of $B_{12}Ng_nF_{12}^{2-}$ (Ng = Kr–Xe and n = 1, 12) Along Path1 and Path2 at B3LYP–D3/TZ2P Level of Theory. The Percent Contribution of Stabilizing Energy Terms ($E^{\text{elstat}} + E^{\text{orb}} + E^{\text{disp}}$) to the Total Interaction Energy (E^{int}) is provided in the parenthesis. All Energy Terms are in kcal mol⁻¹.

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Figure S2. DOS of $B_{12}Xe_{12}F_{12}^{2-/-/0}$ and $B_{12}Kr_{12}F_{12}^{2-/-/0}$ systems using B3LYP-D3/def2-TZVPP method. Vertical arrows are pointing toward HOMO.

Figure S3. MOs energy level diagram of $B_{12}Kr_{12}F_{12}^{2-/-/0}$ using B3LYP-D3/def2-TZVPP method. The red and blue lines correspond to the alpha and beta orbitals respectively, of $B_{12}Kr_{12}F_{12}^{(-)}$ system.

Figure S4. MOs energy level diagram of $B_{12}Xe_{12}F_{12}^{2-/-/0}$ using B3LYP-D3/def2-TZVPP method. The red and blue lines correspond to the alpha and beta orbitals respectively, of $B_{12}Xe_{12}F_{12}^{(-)}$ system.

Figure S5. Scaled MOs energy level diagram of $B_{12}Kr_{12}F_{12}^{2-/-/0}$ using B3LYP-D3/def2-TZVPP method. The red and blue lines correspond to the alpha and beta orbitals respectively, of $B_{12}Kr_{12}F_{12}^{(-)}$ system. The orbital energies of the negative and neutral systems are scaled by keeping the energy of the highest occupied molecular orbitals (HOMO) of $B_{12}Kr_{12}F_{12}^{(-)}$ and $B_{12}Kr_{12}F_{12}$ to that of the HOMO of $B_{12}Kr_{12}F_{12}^{2-}$ system.

Figure S6. Scaled MOs energy level diagram of $B_{12}Xe_{12}F_{12}^{2-/0}$ using B3LYP-D3/def2-TZVPP method. The red and blue lines correspond to the alpha and beta orbitals respectively, of $B_{12}Xe_{12}F_{12}^{(-)}$ system. The orbital energies of the negative and neutral systems are scaled by keeping the energy of the highest occupied molecular orbitals (HOMO) of $B_{12}Xe_{12}F_{12}^{(-)}$ and $B_{12}Xe_{12}F_{12}$ to that of the HOMO of $B_{12}Xe_{12}F_{12}^{2-}$ system.

Figure S7. MOs pictures of lowest unoccupied molecular orbital (LUMO), highest occupied molecular orbital (HOMO), singly occupied molecular orbital (SOMO) and additional 10 outer valence occupied molecular orbitals of $B_{12}Kr_{12}F_{12}^{(2-)}$ and $B_{12}Kr_{12}F_{12}^{(-)}$ systems using B3LYP-D3/def2-TZVPP method.

Figure S8. MOs pictures of LUMO, HOMO, SOMO and additional 10 outer valence occupied molecular orbitals of $B_{12}Kr_{12}F_{12}^{(-)}$ and $B_{12}Kr_{12}F_{12}$ systems using B3LYP-D3/def2-TZVPP method.

Figure S9. MOs pictures of LUMO, HOMO, SOMO and additional 10 outer valence occupied molecular orbitals of $B_{12}Xe_{12}F_{12}^{(2-)}$ and $B_{12}Xe_{12}F_{12}^{(-)}$ systems using B3LYP-D3/def2-TZVPP method.

Figure S10. MOs pictures of LUMO, HOMO, SOMO and additional 10 outer valence occupied molecular orbitals of $B_{12}Xe_{12}F_{12}^{(-)}$ and $B_{12}Xe_{12}F_{12}$ systems using B3LYP-D3/def2-TZVPP method.

Figure S11. Dissociation energy (DE, kcal mol⁻¹) plot of $B_{12}Kr_nF_{12}^{2-}$ (n = 1, 2, 3, 4, 12) along Path1 and Path2 dissociation channels using B3LYP-D3, MP2 and DLPNO-CCSD(T) methods with def2-TZVPP basis set.

Figure S12. Deformation density ($\Delta\rho(r)$) pictures of the pairwise orbital interactions for $B_{12}Kr_nF_{12}^{2-}$ (n = 1 and 12) along Path1 and Path2 and their associated ΔE_i^{orb} energies (ΔE^σ and ΔE^π , in kcal mol⁻¹) obtained from the EDA-NOCV at B3LYP-D3/TZ2P level of theory. The blue and red colored surfaces indicate regions with $\Delta\rho(r) > 0$ and $\Delta\rho(r) < 0$, respectively.

Figure S13. Deformation density ($\Delta\rho(r)$) pictures of the pairwise orbital interactions for $B_{12}Xe_nF_{12}^{2-}$ ($n = 1$ and 12) along Path1 and Path2 and their associated ΔE_i^{orb} energies (ΔE^σ and ΔE^π , in kcal mol^{-1}) obtained from the EDA–NOCV at B3LYP–D3/TZ2P level of theory. The blue and red colored surfaces indicate regions with $\Delta\rho(r) > 0$ and $\Delta\rho(r) < 0$, respectively.

Table S1. Binding Energy of First and Second Excess Electrons ($\Delta E1$ and $\Delta E2$, in eV) in $B_{12}F_{12}^{2-}$ and $B_{12}Ng_nF_{12}^{2-}$ ($Ng = Kr-Xe$ and $n = 1, 2, 3, 4$ and 12) at B3LYP-D3/Def2-TZVPP Level of Theory

Dianions	$\Delta E1$		$\Delta E2$	
	Kr	Xe	Kr	Xe
$B_{12}F_{12}^{2-}$	5.51		1.31	
$B_{12}NgF_{12}^{2-}$	6.21	6.05	2.15	2.07
$1,12-B_{12}Ng_2F_{12}^{2-}$	6.94	6.40	2.53	2.70
$1,2,12-B_{12}Ng_3F_{12}^{2-}$	7.47	6.76	2.79	3.07
$1,2,7,12-B_{12}Ng_4F_{12}^{2-}$	7.69	7.05	3.16	3.37
$B_{12}Ng_{12}F_{12}^{2-}$	8.47	7.87	5.22	5.15

Table S2. Optimized Ng–B and Ng–F Bond Distances (in Å) in $B_{12}Ng_nF_{12}^{2-}$ (Ng = Ar–Xe and n = 1, 2, 3, 4 and 12) using B3LYP–D3 and MP2 Methods and Dissociation Energy (DE, kcal mol⁻¹) using B3LYP–D3 (B3), MP2 and DLPNO–CCSD(T)^a Methods with def2–TZVPP Basis Set. Covalent Ng–B and Ng–F Radii^b Reported by Cordero et al^c [Pyykkö^d] are also Provided in the Table

$B_{12}Ng_nF_{12}^{2-}$	Ng–B		Ng–F		DE Along PATH1			DE Along PATH2		
	B3	MP2	B3	MP2	B3	MP2	DLPNO–CCSD(T)	B3	MP2	DLPNO–CCSD(T)
$R_{cov(Ar-B)/(Ar-F)}$	1.900 [1.810]	1.900 [1.810]	1.630 [1.600]	1.630 [1.600]						
$B_{12}ArF_{12}^{2-}$	1.950	1.862	2.304	2.311	54.8	55.2	46.1	4.2	7.1	3.0
$1,7-B_{12}Ar_2F_{12}^{2-}$	1.946	1.853	2.253	2.246	46.1	45.5	36.2	13.9	21.0	7.6
$1,12-B_{12}Ar_2F_{12}^{2-}$	1.943	1.854	2.255	2.251	47.3	47.0	36.8	17.5	21.2	17.1
$1,2,12-B_{12}Ar_3F_{12}^{2-}$	1.948	1.850	2.207	2.182	35.4	34.1	24.6	23.7	32.0	28.2
$1,7,12-B_{12}Ar_3F_{12}^{2-}$	1.947	1.850	2.207	2.183	40.6	39.0	29.3	24.4	32.1	28.8
$1,2,7,12-B_{12}Ar_4F_{12}^{2-}$	1.958	1.853	2.173	2.126	...*	29.1	22.9	28.7	39.7	35.2
$B_{12}Ar_{12}F_{12}^{2-}$	2.005	...*	2.060	...*	3.0	...*	...*	61.2	...*	71.8
$R_{cov(Kr-B)/(Kr-F)}$	2.000 [2.020]	2.000 [2.020]	1.730 [1.810]	1.730 [1.810]						
$B_{12}KrF_{12}^{2-}$	2.098	2.011	2.339	2.322	64.6	67.3	57.9	14.0	19.2	14.7
$1,7-B_{12}Kr_2F_{12}^{2-}$	2.096	2.009	2.296	2.270	57.6	60.0	50.2	23.5	31.2	27.8
$1,12-B_{12}Kr_2F_{12}^{2-}$	2.094	2.009	2.297	2.274	58.4	60.6	50.4	26.3	31.8	27.6
$1,2,12-B_{12}Kr_3F_{12}^{2-}$	2.096	2.011	2.255	2.220	49.3	60.0	41.4	32.6	41.0	37.3
$1,7,12-B_{12}Kr_3F_{12}^{2-}$	2.096	2.011	2.255	2.220	53.0	55.2	44.7	33.2	41.0	37.7
$1,2,7,12-B_{12}Kr_4F_{12}^{2-}$	2.101	2.018	2.222	2.177	45.6	48.6	37.8	38.0	47.8	44.5
$B_{12}Kr_{12}F_{12}^{2-}$	2.130	2.084	2.113	2.062	25.7	35.6	19.6	72.0	77.2	81.7
$R_{cov(Xe-B)/(Xe-F)}$	2.240 [2.160]	2.240 [2.160]	1.970 [1.950]	1.970 [1.950]						
$B_{12}XeF_{12}^{2-}$	2.270	2.178	2.371	2.350	78.7	86.7	74.3	28.1	38.5	31.1
$1,7-B_{12}Xe_2F_{12}^{2-}$	2.268	2.179	2.340	2.315	73.6	81.7	69.7	36.3	48.3	41.7
$1,12-B_{12}Xe_2F_{12}^{2-}$	2.268	2.179	2.341	2.316	73.9	81.7	69.2	38.8	49.5	42.3
$1,2,12-B_{12}Xe_3F_{12}^{2-}$	2.271	2.184	2.308	2.280	67.8	76.6	63.5	43.6	56.6	49.7
$1,7,12-B_{12}Xe_3F_{12}^{2-}$	2.271	2.184	2.287	2.280	70.0	78.1	65.4	44.7	56.8	50.3
$1,2,7,12-B_{12}Xe_4F_{12}^{2-}$	2.277	2.190	2.282	2.250	65.1	74.2	60.9	49.0	62.8	56.3
$B_{12}Xe_{12}F_{12}^{2-}$	2.302	2.222	2.189	2.157	51.4	65.6	47.9	81.1	99.0	91.0

^aSingle point energy calculation is performed using DLPNO–CCSD(T) method on B3LYP–D3 optimized geometry

*Structure did not converge

^b $R_{cov(Ng-B)} = R_{cov(Ng)} + R_{cov(B)}$ and $R_{cov(Ng-F)} = R_{cov(Ng)} + R_{cov(F)}$

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Table S3. Calculated NPA Charge on Ng, B and F atoms in $B_{12}F_{12}^{2-}$ and $B_{12}Ng_nF_{12}^{2-}$ (Ng = Ar–Xe and n = 1, 2, 3, 4, 12) at B3LYP–D3/def2–TZVPP Level of Theory

$B_{12}Ng_nF_{12}^{2-}$	$q_{tot}B$	$q_{tot}F$	$q_{tot}B+F$	$q_{tot}Ng$	$q_{avg}B$	$q_{avg}F$	$q_{avg}Ng$
$B_{12}F_{12}^{2-}$	3.64	−5.64	−2.00	...	0.30	−0.46	...
$B_{12}ArF_{12}^{2-}$	3.37	−5.89	−2.52	0.52	−0.11	−0.88	0.52
$1,7-B_{12}Ar_2F_{12}^{2-}$	3.10	−6.16	−3.06	1.06	−0.13	−0.85	0.53
$1,12-B_{12}Ar_2F_{12}^{2-}$	3.10	−6.16	−3.06	1.07	−0.12	−0.86	0.53
$1,2,12-B_{12}Ar_3F_{12}^{2-}$	2.77	−6.40	−3.63	1.63	−0.13	−0.82	0.54
$1,7,12-B_{12}Ar_3F_{12}^{2-}$	2.77	−6.40	−3.63	1.63	−0.13	−0.82	0.54
$1,2,7,12-B_{12}Ar_4F_{12}^{2-}$	2.42	−6.60	−4.18	2.18	−0.12	−0.78	0.54
$B_{12}Ar_{12}F_{12}^{2-}$	−0.72	−7.85	−8.57	6.57	−0.06	−0.65	0.55
$B_{12}KrF_{12}^{2-}$	3.27	−5.90	−2.63	0.63	−0.21	−0.86	0.63
$1,7-B_{12}Kr_2F_{12}^{2-}$	2.90	−6.18	−3.28	1.29	−0.23	−0.84	0.64
$1,12-B_{12}Kr_2F_{12}^{2-}$	2.90	−6.19	−3.29	1.29	−0.23	−0.85	0.64
$1,2,12-B_{12}Kr_3F_{12}^{2-}$	2.47	−6.45	−3.98	1.98	−0.23	−0.82	0.66
$1,7,12-B_{12}Kr_3F_{12}^{2-}$	2.47	−6.45	−3.98	1.98	−0.23	−0.82	0.66
$1,2,7,12-B_{12}Kr_4F_{12}^{2-}$	2.03	−6.70	−4.67	2.67	−0.22	−0.80	0.67
$B_{12}Kr_{12}F_{12}^{2-}$	−1.92	−8.44	−10.36	8.36	−0.16	−0.70	0.70
$B_{12}XeF_{12}^{2-}$	3.16	−5.92	−2.76	0.76	−0.33	−0.86	0.76
$1,7-B_{12}Xe_2F_{12}^{2-}$	2.67	−6.23	−3.56	1.56	−0.34	−0.84	0.78
$1,12-B_{12}Xe_2F_{12}^{2-}$	2.66	−6.23	−3.57	1.56	−0.34	−0.84	0.78
$1,2,12-B_{12}Xe_3F_{12}^{2-}$	2.14	−6.53	−4.39	2.39	−0.33	−0.83	0.80
$1,7,12-B_{12}Xe_3F_{12}^{2-}$	2.14	−6.53	−4.39	2.39	−0.33	−0.83	0.80
$1,2,7,12-B_{12}Xe_4F_{12}^{2-}$	1.59	−6.82	−5.23	3.24	−0.31	−0.81	0.81
$B_{12}Xe_{12}F_{12}^{2-}$	−3.26	−9.03	−12.29	10.29	−0.27	−0.75	0.86

Table S4. Free Energy Change (ΔG , kcal mol⁻¹) of $B_{12}Ng_nF_{12}^{2-}$ (Ng = Ar–Xe and n = 1, 2, 3, 4, 12) at 298.15 K along Path1 and Path2 Dissociation channels at B3LYP–D3/def2–TZVPP Level of Theory.

$B_{12}Ng_nF_{12}^{2-}$	ΔG	
	Path1 ^a	Path2 ^b
$B_{12}ArF_{12}^{2-}$	38.0	-15.0
$1,7-B_{12}Ar_2F_{12}^{2-}$	28.9	-4.0
$1,12-B_{12}Ar_2F_{12}^{2-}$	30.3	-1.3
$1,2,12-B_{12}Ar_3F_{12}^{2-}$	17.7	5.5
$1,7,12-B_{12}Ar_3F_{12}^{2-}$	23.4	6.4
$1,2,7,12-B_{12}Ar_4F_{12}^{2-}$	*	10.5
$B_{12}Ar_{12}F_{12}^{2-}$	-21.0	40.7
$B_{12}KrF_{12}^{2-}$	47.8	-5.2
$1,7-B_{12}Kr_2F_{12}^{2-}$	40.4	5.5
$1,12-B_{12}Kr_2F_{12}^{2-}$	41.3	7.4
$1,2,12-B_{12}Kr_3F_{12}^{2-}$	31.8	14.5
$1,7,12-B_{12}Kr_3F_{12}^{2-}$	35.8	15.3
$1,2,7,12-B_{12}Kr_4F_{12}^{2-}$	28.1	20.3
$B_{12}Kr_{12}F_{12}^{2-}$	5.2	51.4
$B_{12}XeF_{12}^{2-}$	61.7	8.7
$1,7-B_{12}Xe_2F_{12}^{2-}$	56.4	18.3
$1,12-B_{12}Xe_2F_{12}^{2-}$	56.8	19.8
$1,2,12-B_{12}Xe_3F_{12}^{2-}$	50.4	25.7
$1,7,12-B_{12}Xe_3F_{12}^{2-}$	52.8	26.8
$1,2,7,12-B_{12}Xe_4F_{12}^{2-}$	47.7	31.4
$B_{12}Xe_{12}F_{12}^{2-}$	30.7	60.4

^aPath1: $B_{12}Ng_nF_{12}^{2-}$

^bPath2: $B_{12}Ng_nF_{12}^{2-}$

Ng + F + $B_{12}Ng_{n-1}F_{11}^{2-}$

Ng + F + $B_{12}Ng_{n-1}F_{11}^{2-}$

Table S5: Calculated Values of Dissociation Energy (DE, in kcal mol⁻¹) and Free energy of Dissociation (ΔG at 298.15 K, in kcal mol⁻¹) of $B_{12}Ng_nF_{12}^{2-}$ (Ng = Ar, Kr, Xe and n = 1, 2, 3, 4, 12) along Path3 and Path4 using B3LYP-D3/def2-TZVPP Method.

$B_{12}Ng_nF_{12}^{2-}$	Path3		Path4	
	$B_{12}Ng_nF_{12}^{2-} \rightarrow B_{12}F_{12}^{2-} + nNg$		$B_{12}Ng_nF_{12}^{2-} \rightarrow B_{12}Ng_{n-1}F_{12}^{2-} + Ng$	
	DE per Ng ¹	ΔG per Ng ²	DE	ΔG
$B_{12}ArF_{12}^{2-}$	-92.67	-41.91	-92.67	-41.91
$1,12-B_{12}Ar_2F_{12}^{2-}$	-96.07	-73.67	-99.47	-105.43
$1,2,12-B_{12}Ar_3F_{12}^{2-}$	-100.41	-87.83	-109.10	-116.15
$1,7,12-B_{12}Ar_3F_{12}^{2-}$	-100.41	-87.83	-109.10	-116.14
$1,2,7,12-B_{12}Ar_4F_{12}^{2-}$	-104.25	-96.57	-115.75	-122.80
$B_{12}Ar_{12}F_{12}^{2-}$	-120.60	-122.95	-138.16	-146.39
$B_{12}KrF_{12}^{2-}$	-82.67	-32.15	-82.67	-32.15
$1,12-B_{12}Kr_2F_{12}^{2-}$	-85.47	-63.31	-88.26	-94.46
$1,2,12-B_{12}Kr_3F_{12}^{2-}$	-89.04	-76.69	-96.18	-103.47
$1,7,12-B_{12}Kr_3F_{12}^{2-}$	-89.03	-76.69	-96.17	-103.45
$1,2,7,12-B_{12}Kr_4F_{12}^{2-}$	-92.24	-84.82	-101.85	-109.23
$B_{12}Kr_{12}F_{12}^{2-}$	-105.99	-108.69	-120.51	-129.16
$B_{12}XeF_{12}^{2-}$	-68.59	-18.21	-68.59	-18.21
$1,12-B_{12}Xe_2F_{12}^{2-}$	-70.67	-48.63	-72.75	-79.04
$1,2,12-B_{12}Xe_3F_{12}^{2-}$	-73.37	-61.14	-78.79	-86.17
$1,7,12-B_{12}Xe_3F_{12}^{2-}$	-73.38	-61.15	-78.80	-86.20
$1,2,7,12-B_{12}Xe_4F_{12}^{2-}$	-75.88	-68.61	-83.40	-90.99
$B_{12}Xe_{12}F_{12}^{2-}$	-86.71	-89.68	-98.31	-107.37

¹ DE = DE^{total} /No of dissociated Ng atom, DE^{total} = E($B_{12}F_{12}^{2-}$)+n*E(Ng)-E($B_{12}Ng_nF_{12}^{2-}$)
² ΔG = ΔG ^{total} /No of dissociated Ng atom, ΔG ^{total} = G($B_{12}F_{12}^{2-}$)+n*G(Ng)-G($B_{12}Ng_nF_{12}^{2-}$)”

Table S6: Calculated Values of Optimized Bond Length (in Å), B-Ng-F Bond Angle (in Degree) and Activation Energy Barrier (AE, in kcal mol⁻¹) of Transition State Structure (along B1-Ng-F mode) of B₁₂Ng_nF₁₂²⁻ (Ng = Kr, Xe and n = 1, 2, 3, 4, 12) using B3LYP-D3/def2-TZVPP Method.

TS-B ₁₂ Ng _n F ₁₂ ²⁻	B-Ng	Ng-F	B-Ng-F	AE
B ₁₂ KrF ₁₂ ²⁻	2.155	2.570	81.01	25.52
1,12-B ₁₂ Kr ₂ F ₁₂ ²⁻	2.104	2.542	85.88	24.50
1,2,12-B ₁₂ Kr ₃ F ₁₂ ²⁻	2.083	2.506	87.67	22.89
1,2,7,12-B ₁₂ Kr ₄ F ₁₂ ²⁻	2.069	2.490	91.19	22.49
B ₁₂ Kr ₁₂ F ₁₂ ²⁻	2.093	2.344	117.33	16.33
B ₁₂ XeF ₁₂ ²⁻	2.347	2.581	71.70	32.52
1,12-B ₁₂ Xe ₂ F ₁₂ ²⁻	2.330	2.567	70.92	31.47
1,2,12-B ₁₂ Xe ₃ F ₁₂ ²⁻	2.301	2.520	74.12	30.21
1,2,7,12-B ₁₂ Xe ₄ F ₁₂ ²⁻	2.266	2.511	83.93	29.67
B ₁₂ Xe ₁₂ F ₁₂ ²⁻	2.267	2.432	114.42	21.23

Table S7. Bond Critical Point (BCP) Properties of Ng-B (Ng-F) Bond of B₁₂Ng_nF₁₂²⁻ (Ng = Kr-Xe and n = 1, 12) Compounds at B3LYP-D3/def2-TZVPP Level of Theory. BCP Properties of Ng-F Bond are Reported in the Parenthesis

B ₁₂ Ng _n F ₁₂ ²⁻	ρ	∇ ² ρ	V(r)	E _d (r)	ELF
B ₁₂ KrF ₁₂ ²⁻	0.09 (0.05)	-0.09 (0.18)	-0.11 (-0.05)	-0.06 (0.00)	0.58 (0.14)
B ₁₂ Kr ₁₂ F ₁₂ ²⁻	0.10 (0.08)	-0.10 (0.25)	-0.08 (-0.09)	-0.05 (-0.02)	0.83 (0.25)
B ₁₂ XeF ₁₂ ²⁻	0.09 (0.06)	-0.10 (0.17)	-0.07 (-0.06)	-0.05 (-0.01)	0.83 (0.18)
B ₁₂ Xe ₁₂ F ₁₂ ²⁻	0.09 (0.08)	-0.08 (0.21)	-0.06 (-0.10)	-0.04 (-0.02)	0.87 (0.27)

Table S8. EDA–NOCV of $B_{12}Ng_nF_{12}^{2-}$ ($Ng = Kr-Xe$ and $n = 1, 12$) Along Path1 and Path2 at B3LYP–D3/TZ2P Level of Theory. The Percent Contribution of Stabilizing Energy Terms ($E^{elstat} + E^{orb} + E^{disp}$) to the Total Interaction Energy (E^{int}) is provided in the parenthesis. All Energy Terms are in $kcal\ mol^{-1}$

$B_{12}Ng_nF_{12}^{2-}$	Path	E^{Pauli}	E^{elstat}	E^{orb}	E^{disp}	E^{def}	E^{int}
$B_{12}KrF_{12}^{2-}$	Path1	222.2	-124.0 (41.7)	-168.5 (56.7)	-4.6 (1.5)	0.9	-74.1
	Path2	107.9	-11.5 (9.0)	-111.6 (87.4)	-4.6 (3.6)	7.9	-12.0
$B_{12}Kr_{12}F_{12}^{2-}$	Path1	238.9	-113.9 (41.4)	-154.1 (56.0)	-7.3 (2.7)	0.6	-35.8
	Path2	209.9	-95.3 (33.0)	-186.4 (64.5)	-7.3 (2.5)	6.0	-73.1
$B_{12}XeF_{12}^{2-}$	Path1	241.8	-138.3 (42.1)	-185.1 (56.3)	-5.3 (1.6)	0.8	-86.1
	Path2	134.8	-28.8 (17.1)	-134.1 (79.7)	-5.3 (3.2)	9.1	-24.3
$B_{12}Xe_{12}F_{12}^{2-}$	Path1	276.0	-137.6 (41.0)	-188.0 (56.0)	-10.2 (3.0)	1.5	-58.4
	Path2	233.5	-109.6 (34.1)	-201.8 (62.7)	-10.2 (3.2)	11.1	-77.2

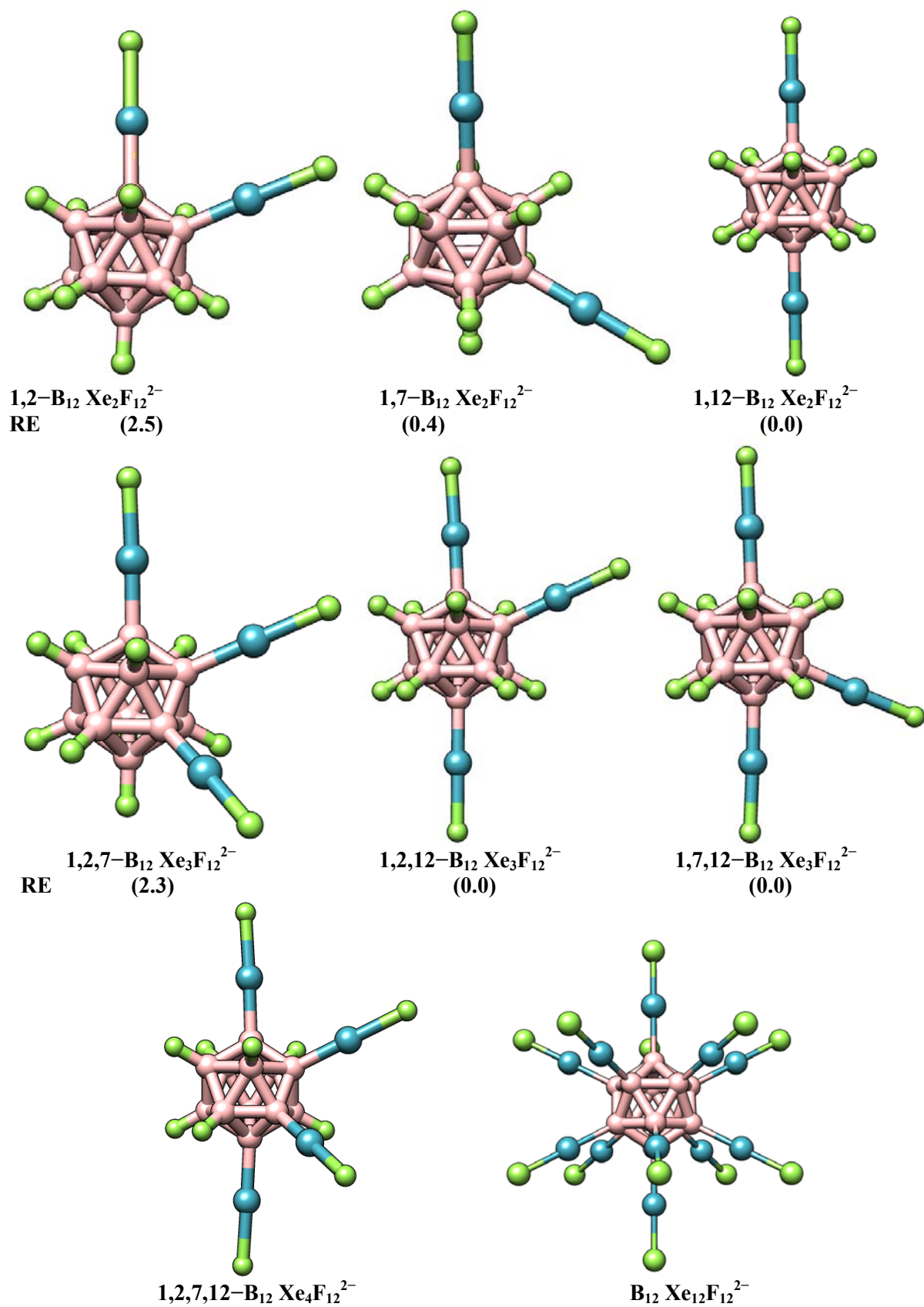


Figure S1. Optimized Structures of $\text{B}_{12}\text{Xe}_n\text{F}_{12}^{2-}$ ($n = 2-4, 12$) compound and relative energy (RE, in kcal mol^{-1}) of different isomers with respect to its corresponding most stable isomer.

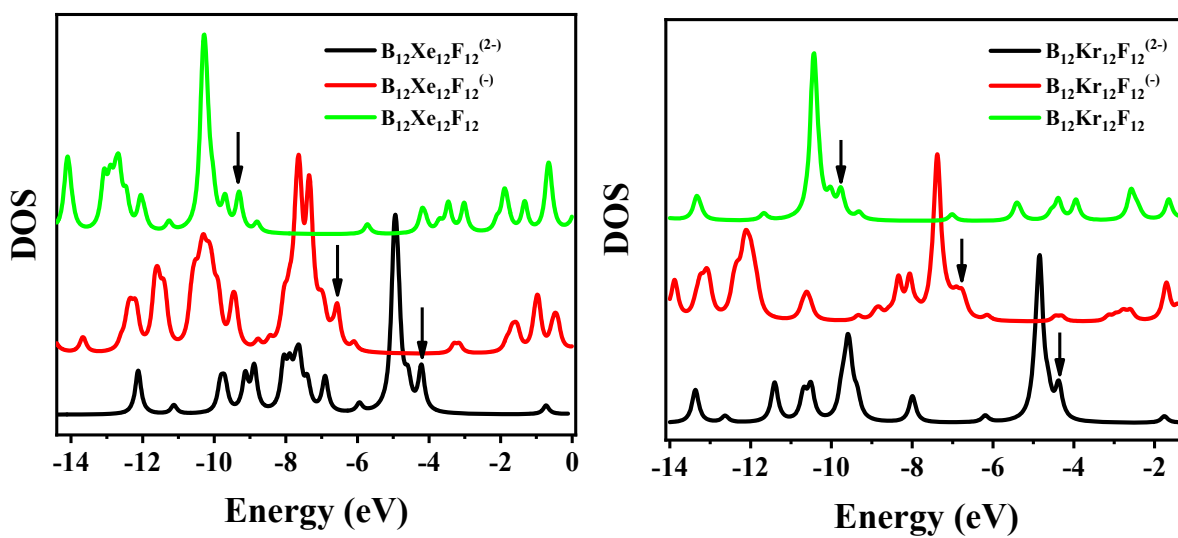


Figure S2. DOS of B₁₂Xe₁₂F₁₂^{2-/0} and B₁₂Kr₁₂F₁₂^{2-/0} systems using B3LYP-D3/def2-TZVPP method. Vertical arrows are pointing toward HOMO.

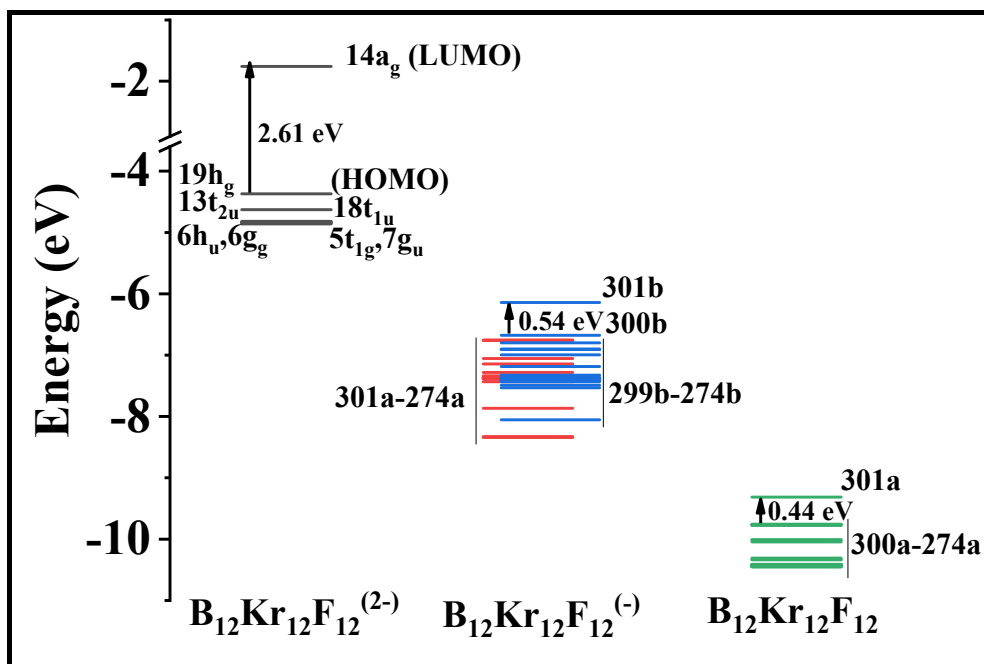


Figure S3. MOs energy level diagram of $B_{12}Kr_{12}F_{12}^{2-/0}$ using B3LYP-D3/def2-TZVPP method. The red and blue lines correspond to the alpha and beta orbitals respectively, of $B_{12}Kr_{12}F_{12}^{(-)}$ system.

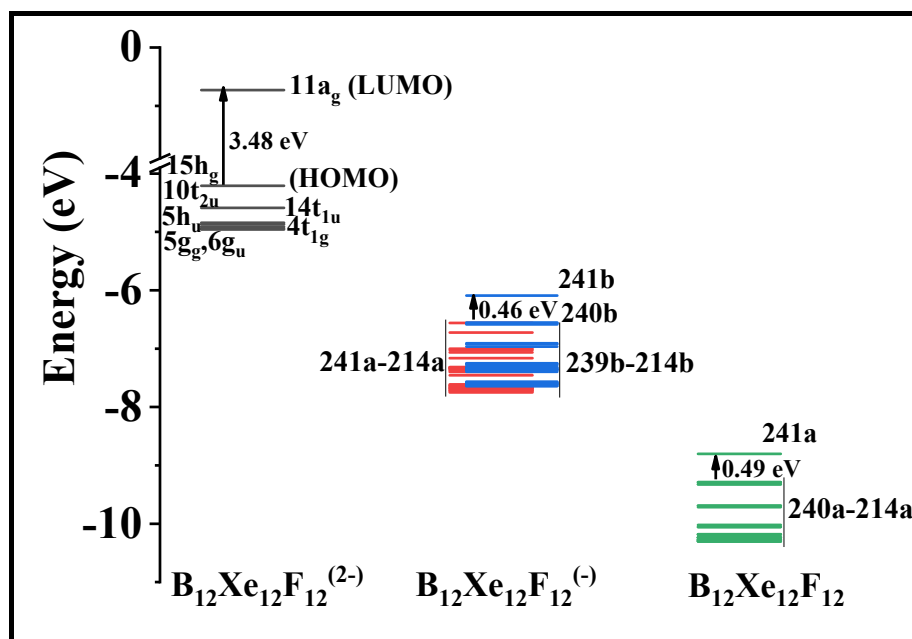


Figure S4. MOs energy level diagram of $B_{12}Xe_{12}F_{12}^{2-/0}$ using B3LYP-D3/def2-TZVPP method. The red and blue lines correspond to the alpha and beta orbitals respectively, of $B_{12}Xe_{12}F_{12}^{(-)}$ system.

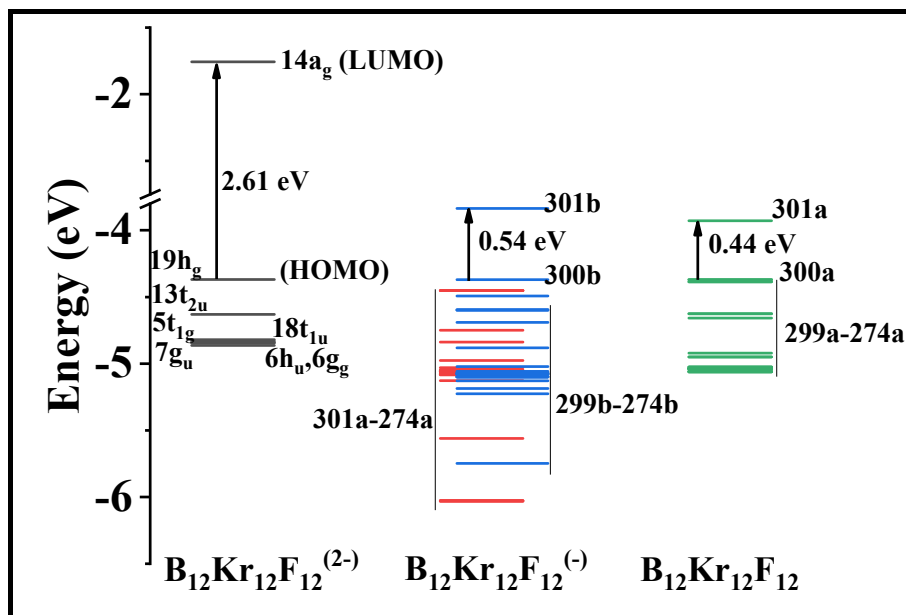


Figure S5. Scaled MOs energy level diagram of $B_{12}Kr_{12}F_{12}^{2-/0}$ using B3LYP-D3/def2-TZVPP method. The red and blue lines correspond to the alpha and beta orbitals respectively, of $B_{12}Kr_{12}F_{12}^{(-)}$ system. The orbital energies of the negative and neutral systems are scaled by keeping the energy of the highest occupied molecular orbitals (HOMO) of $B_{12}Kr_{12}F_{12}^{(-)}$ and $B_{12}Kr_{12}F_{12}$ to that of the HOMO of $B_{12}Kr_{12}F_{12}^{2-}$ system.

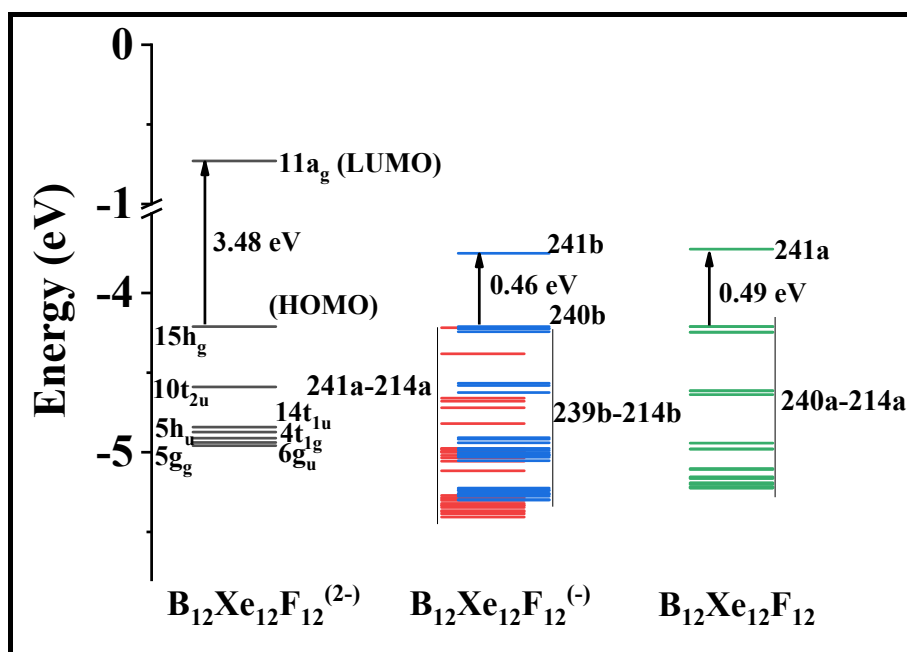


Figure S6. Scaled MOs energy level diagram of $B_{12}Xe_{12}F_{12}^{2-/0}$ using B3LYP-D3/def2-TZVPP method. The red and blue lines correspond to the alpha and beta orbitals respectively, of $B_{12}Xe_{12}F_{12}^{(-)}$ system. The orbital energies of the negative and neutral systems are scaled by keeping the energy of the highest occupied molecular orbitals (HOMO) of $B_{12}Xe_{12}F_{12}^{(-)}$ and $B_{12}Xe_{12}F_{12}$ to that of the HOMO of $B_{12}Xe_{12}F_{12}^{2-}$ system.

$B_{12}Kr_{12}F_{12}^{(2-)}$			$B_{12}Kr_{12}F_{12}^{(-)}$		
14a _g (LUMO) [B(s)+F(p)+Kr(p)]			301b (LUMO) [B(s,p)+F(p)+Kr(s)]		
19h _g -1 (HOMO) 19h _g -2 19h _g -3 [B(s,p)+F(p)+Kr(s)]			300b (HOMO) 301a (SOMO) 299a [B(s,p)+F(p)+Kr(s)]		
19h _g -4 19h _g -5 [B(s,p)+F(p)+Kr(s)]			298a 297a 296a [B(s,p)+F(p)+Kr(s)]		
13t _{2u} -1 13t _{2u} -2 13t _{2u} -3 [B(s)+F(p)+Kr(s)]			295a 294a 293a [B(s,p)+F(p)+Kr(s)] [F(p)] [F(p)+Kr(p)]		
18t _{1u} -1 18t _{1u} -2 18t _{1u} -3 [B(s,p)+F(p)]			292a 291a 290a [F(p)+Kr(p)]		

Figure S7. MOs pictures of lowest unoccupied molecular orbital (LUMO), highest occupied molecular orbital (HOMO), singly occupied molecular orbital (SOMO) and additional 10 outer valence occupied molecular orbitals of $B_{12}Kr_{12}F_{12}^{(2-)}$ and $B_{12}Kr_{12}F_{12}^{(-)}$ systems using B3LYP-D3/def2-TZVPP method.

$B_{12}Kr_{12}F_{12}^{(-)}$	$B_{12}Kr_{12}F_{12}$
301b (LUMO) [B(s,p)+F(p)+Kr(s)]	301a (LUMO) [B(s,p)+F(p)+Kr(s)]
300b (HOMO) 301a (SOMO) 299a	300a (HOMO) 299a 298a
[B(s,p)+F(p)+Kr(s)]	[B(s,p)+F(p)+Kr(s)]
298a 297a 296a	297a 296a 295a
[B(s,p)+F(p)+Kr(s)]	[B(s,p)+F(p)+Kr(s)]
295a 294a 293a	294a 293a 292a
[B(s,p)+F(p)+Kr(s)] [F(p)] [F(p)+Kr(p)]	[B(s,p)+F(p)+Kr(s)]
292a 291a 290a	291a 290a
[F(p)+Kr(p)]	[B(s,p)+F(p)+Kr(s)] [F(p)]

Figure S8. MOs pictures of LUMO, HOMO, SOMO and additional 10 outer valence occupied molecular orbitals of $B_{12}Kr_{12}F_{12}^{(-)}$ and $B_{12}Kr_{12}F_{12}$ systems using B3LYP-D3/def2-TZVPP method.

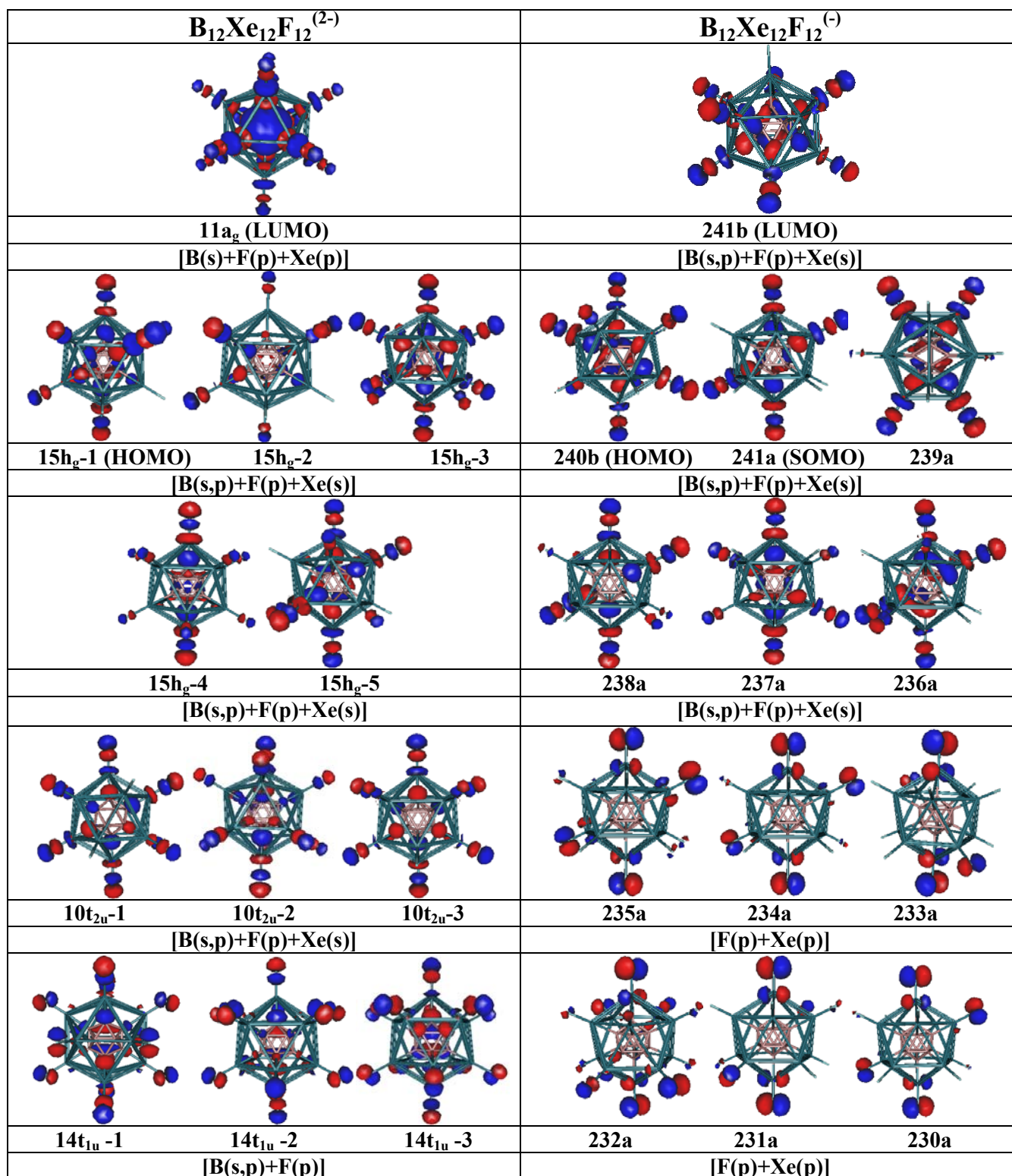


Figure S9. MOs pictures of LUMO, HOMO, SOMO and additional 10 outer valence occupied molecular orbitals of $B_{12}Xe_{12}F_{12}^{(2-)}$ and $B_{12}Xe_{12}F_{12}^{(-)}$ systems using B3LYP-D3/def2-TZVPP method.

$B_{12}Xe_{12}F_{12}^{(-)}$	$B_{12}Xe_{12}F_{12}$
241b (LUMO)	241a (LUMO)
[B(s,p)+F(p)+Xe(s)]	[B(s,p)+F(p)+Xe(s)]
240b (HOMO) 241a (SOMO) 239a	240a (HOMO) 239a 238a
[B(s,p)+F(p)+Xe(s)]	[B(s,p)+F(p)+Xe(s)]
238a 237a 236a	237a 236a 235a
[B(s,p)+F(p)+Xe(s)]	[B(s,p)+F(p)+Xe(s)]
235a 234a 233a	234a 233a 232a
[F(p)+Xe(p)]	[B(s,p)+F(p)+Xe(s)]
232a 231a 230a	231a 230a
[F(p)+Xe(p)]	[B(s,p)+F(p)+Xe(s)] [F(p)+Xe(p)]

Figure S10. MOs pictures of LUMO, HOMO, SOMO and additional 10 outer valence occupied molecular orbitals of $B_{12}Xe_{12}F_{12}^{(-)}$ and $B_{12}Xe_{12}F_{12}$ systems using B3LYP-D3/def2-TZVPP method.

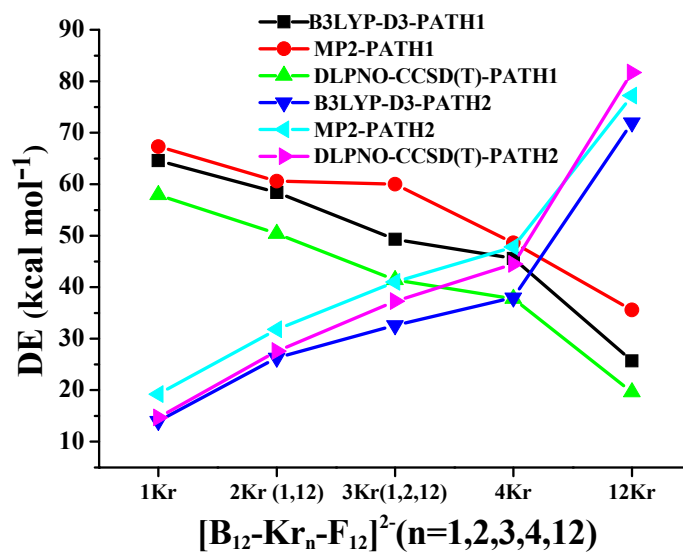


Figure S11. Dissociation energy (DE, kcal mol⁻¹) plot of B₁₂Kr_nF₁₂²⁻ (n = 1, 2, 3, 4, 12) along Path1 and Path2 dissociation channels using B3LYP-D3, MP2 and DLPNO-CCSD(T) methods with def2-TZVPP basis set.

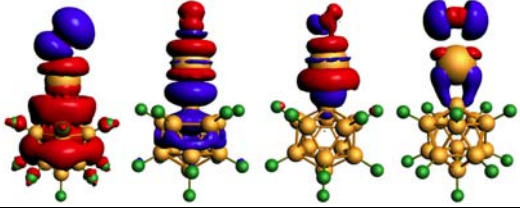
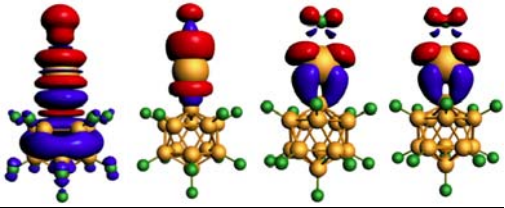
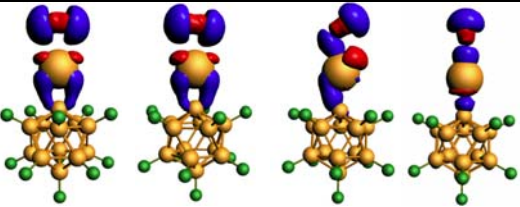
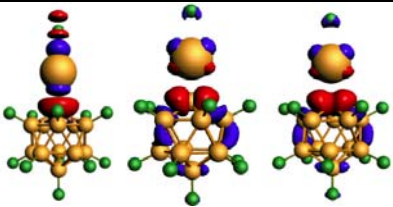
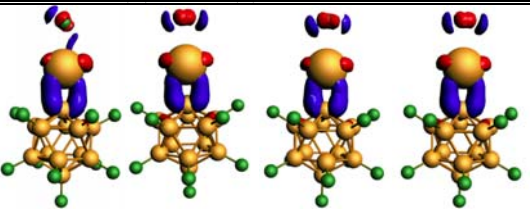
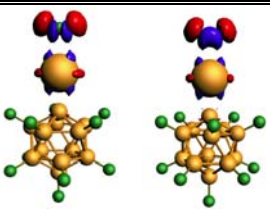
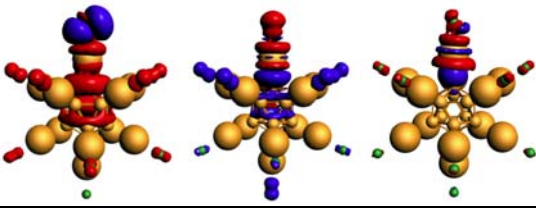
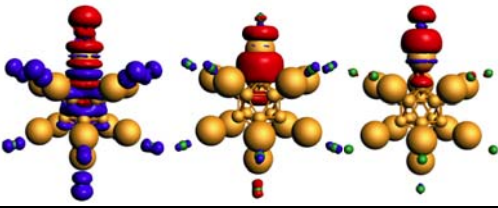
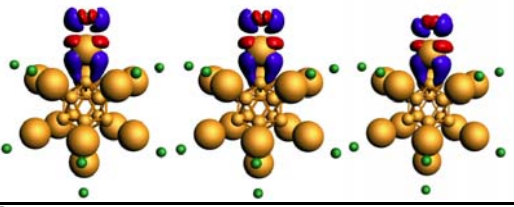
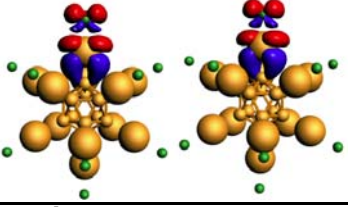
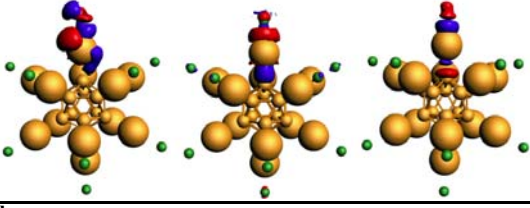
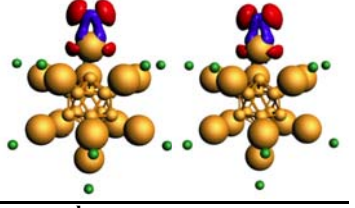
Path1 (Dianion+F+Ng) [$E^{\text{orb}} = \sum \Delta E_i^{\text{orb}}$] $\text{KrB}_{12}\text{F}_{12}^{2-}$ ($E^{\text{orb}} = -168.5$)	Path2 (Anion+F ⁻ +Ng) [$E^{\text{orb}} = \sum \Delta E_i^{\text{orb}}$] $\text{KrB}_{12}\text{F}_{12}^{2-}$ ($E^{\text{orb}} = -111.6$)
 $\Delta E_i^{\text{orb}} = -132.9(\text{b}) \quad -15.3(\text{a}) \quad -9.5(\text{b}) \quad 0.22(\text{a})$	 $\Delta E_i^{\text{orb}} = -89.3 \quad -4.4 \quad -5.3 \quad -5.3$
 $\Delta E_i^{\text{orb}} = -1.0(\text{b}) \quad 0.3(\text{a}) \quad -1.6(\text{b}) \quad -0.8(\text{a})$	 $\Delta E_i^{\text{orb}} = -3.1 \quad -0.45 \quad -0.45$
 $\Delta E_i^{\text{orb}} = -1.1(\text{b}) \quad -0.7(\text{a}) \quad -1.0(\text{b}) \quad -0.5(\text{a})$	 $\Delta E_i^{\text{orb}} = -0.19 \quad -0.19$
Path1 (Dianion+F+Ng) [$E^{\text{orb}} = \sum \Delta E_i^{\text{orb}}$] $\text{Kr}_{12}\text{B}_{12}\text{F}_{12}^{2-}$ ($E^{\text{orb}} = -154.1$)	Path2 (Anion+F ⁻ +Ng) [$E^{\text{orb}} = \sum \Delta E_i^{\text{orb}}$] $\text{Kr}_{12}\text{B}_{12}\text{F}_{12}^{2-}$ ($E^{\text{orb}} = -186.4$)
 $\Delta E_i^{\text{orb}} = -88.3(\text{b}) \quad -31.0(\text{a}) \quad -13.5(\text{b})$	 $\Delta E_i^{\text{orb}} = -146.9 \quad -10.8 \quad -6.4$
 $\Delta E_i^{\text{orb}} = -1.9(\text{a}) \quad -2.6(\text{b}) \quad -0.93(\text{a})$	 $\Delta E_i^{\text{orb}} = -8.5 \quad -8.5$
 $\Delta E_i^{\text{orb}} = -2.8(\text{b}) \quad -2.7(\text{a}) \quad -2.2(\text{a})$	 $\Delta E_i^{\text{orb}} = -0.2 \quad -0.2$

Figure S12. Deformation density ($\Delta\rho(r)$) pictures of the pairwise orbital interactions for $\text{B}_{12}\text{Kr}_n\text{F}_{12}^{2-}$ ($n = 1$ and 12) along Path1 and Path2 and their associated ΔE_i^{orb} energies (ΔE^{σ} and ΔE^{π} , in kcal mol^{-1}) obtained from the EDA–NOCV at B3LYP–D3/TZ2P level of theory. The blue and red colored surfaces indicate regions with $\Delta\rho(r) > 0$ and $\Delta\rho(r) < 0$, respectively.

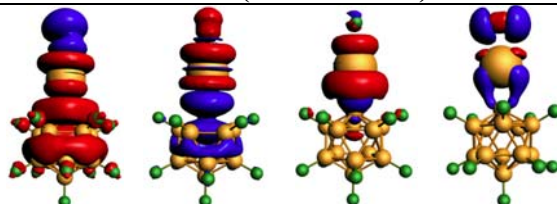
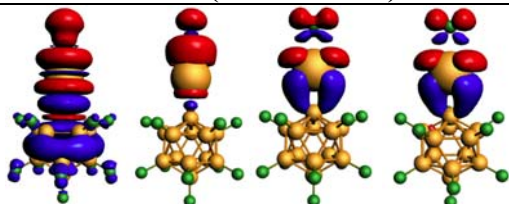
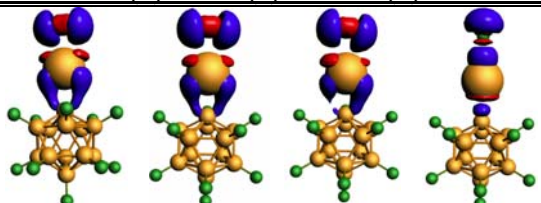
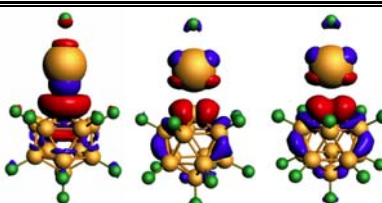
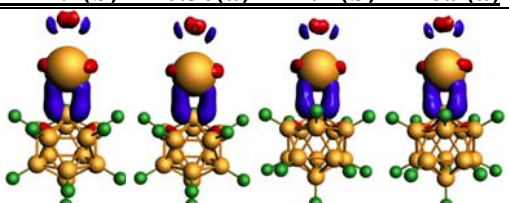
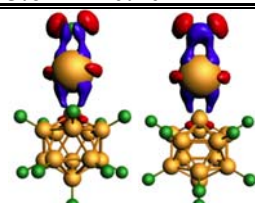
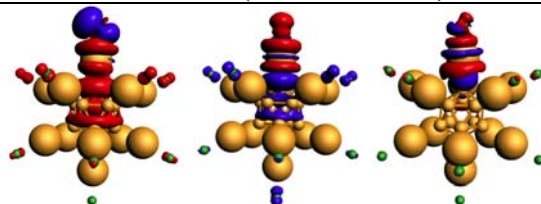
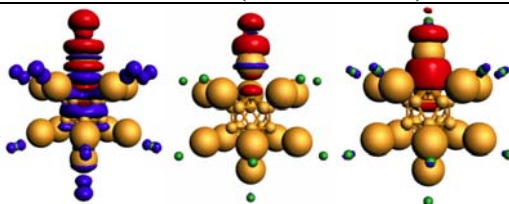
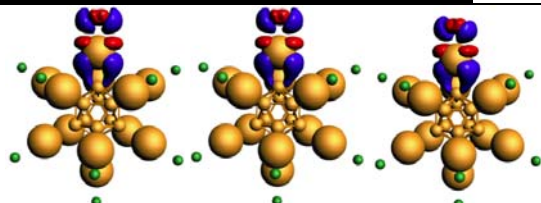
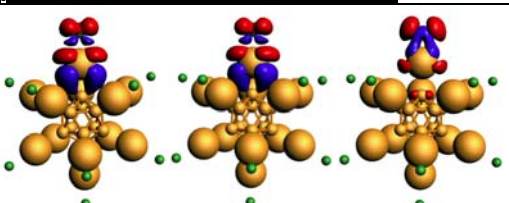
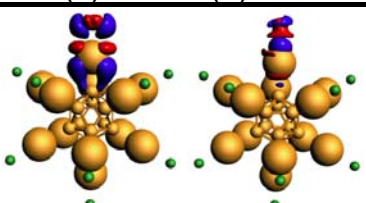
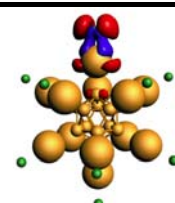
Path1 (Dianion+F+Ng) [$E^{\text{orb}} = \sum \Delta E_i^{\text{orb}}$] $\text{XeB}_{12}\text{F}_{12}^{2-}$ ($E^{\text{orb}} = -185.1$)	Path2 (Anion+F ⁻ +Ng) [$E^{\text{orb}} = \sum \Delta E_i^{\text{orb}}$] $\text{XeB}_{12}\text{F}_{12}^{2-}$ ($E^{\text{orb}} = -134.1$)
 $\Delta E_i^{\text{orb}} = -144.0(\text{b}) \quad -19.1(\text{a}) \quad -11.0(\text{b}) \quad -0.31 \text{ a}$	 $\Delta E_i^{\text{orb}} = -111.3 \quad -4.8 \quad -5.3 \quad -5.3$
 $\Delta E_i^{\text{orb}} = -1.1(\text{b}) \quad -0.30(\text{a}) \quad -1.1(\text{b}) \quad -0.9(\text{a})$	 $\Delta E_i^{\text{orb}} = -3.6 \quad -0.40 \quad -0.40$
 $\Delta E_i^{\text{orb}} = -1.0(\text{b}) \quad -0.7(\text{a}) \quad -0.7(\text{a}) \quad -1.0(\text{a})$	 $\Delta E_i^{\text{orb}} = -0.48 \quad -0.48$
 $\Delta E_i^{\text{orb}} = -116.2(\text{b}) \quad -36.8(\text{a}) \quad -13.3(\text{b})$	 $\Delta E_i^{\text{orb}} = -161.5 \quad -8.1 \quad -8.0$
 $\Delta E_i^{\text{orb}} = -2.0(\text{a}) \quad -2.7(\text{b}) \quad -1.1(\text{a})$	 $\Delta E_i^{\text{orb}} = -9.3 \quad -9.3 \quad -0.5$
 $\Delta E_i^{\text{orb}} = -3.3(\text{b}) \quad -2.9(\text{a})$	 $\Delta E_i^{\text{orb}} = -0.5$

Figure S13. Deformation density ($\Delta\rho(r)$) pictures of the pairwise orbital interactions for $\text{B}_{12}\text{Xe}_n\text{F}_{12}^{2-}$ ($n = 1$ and 12) along Path1 and Path2 and their associated ΔE_i^{orb} energies (ΔE^{σ} and ΔE^{π} , in kcal mol^{-1}) obtained from the EDA–NOCV at B3LYP–D3/TZ2P level of theory. The blue and red colored surfaces indicate regions with $\Delta\rho(r) > 0$ and $\Delta\rho(r) < 0$, respectively.