

## Supporting information

### The behavior of conductivity dynamic modulus and its connection to thermodynamic bulk modulus in ionic liquids

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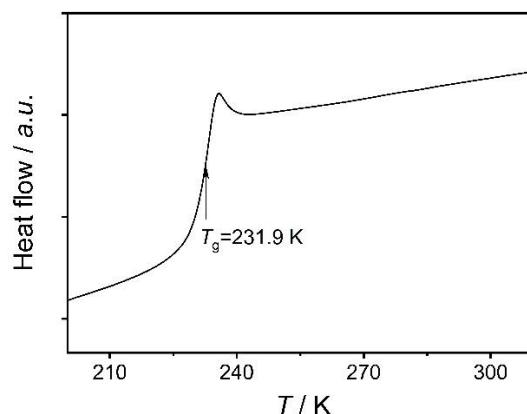


Fig. S1: DSC scan of BMPyr BOB at ambient pressure. The glass-transition temperature of BMPyr BOB is equal to 231.9 K.

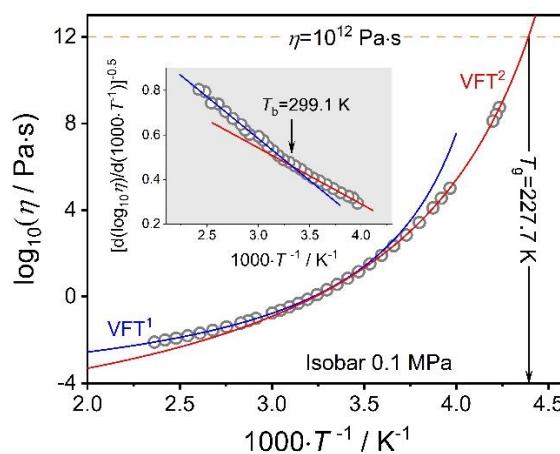


Fig. S2:  $\log_{10}\eta$  as a function of  $1000 \cdot T^{-1}$  at 0.1 MPa for BMPyr BOB; Solid lines denote the fits of VFT equation ( $\log_{10}\eta = \log_{10}\eta_0 + \log_{10}e \cdot DT_0/(T-T_0)$ ) with parameters:  $\log_{10}\eta_0 = -3.78 \pm 0.02 \text{ Pa s}$ ,  $D = 3.57 \pm 0.06$ ,  $T_0 = 219.89 \pm 0.76 \text{ K}$  (VFT<sup>1</sup>);  $\log_{10}\eta_0 = -5.35 \pm 0.05 \text{ Pa s}$ ,  $D = 7.58 \pm 0.08$ ,  $T_0 = 191.40 \pm 0.29 \text{ K}$  (VFT<sup>2</sup>). Inset: Stickel plot for tested IL.

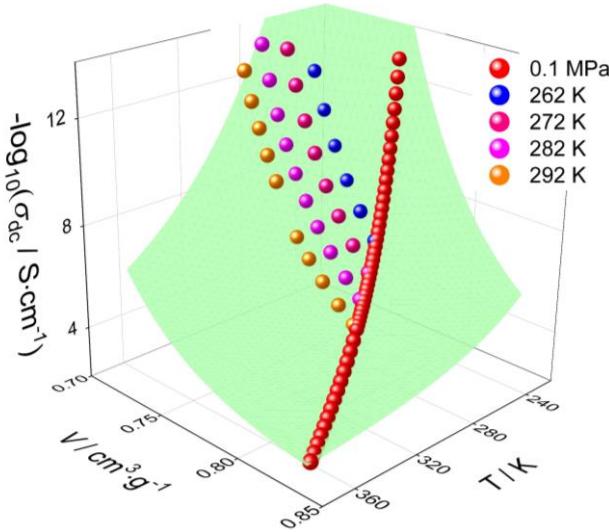


Fig S3: 3D plot of  $-\log_{10}\sigma_{dc}$  vs.  $T$ ,  $V$  for BMPyr BOB. The surface is the fit of Avramov model with the parameters:  $A=1.92\pm 0.06$  S cm<sup>-1</sup>,  $B=136.97\pm 1.34$ ,  $D_0=3.36\pm 0.05$ , and  $\gamma=4.19\pm 0.03$ .

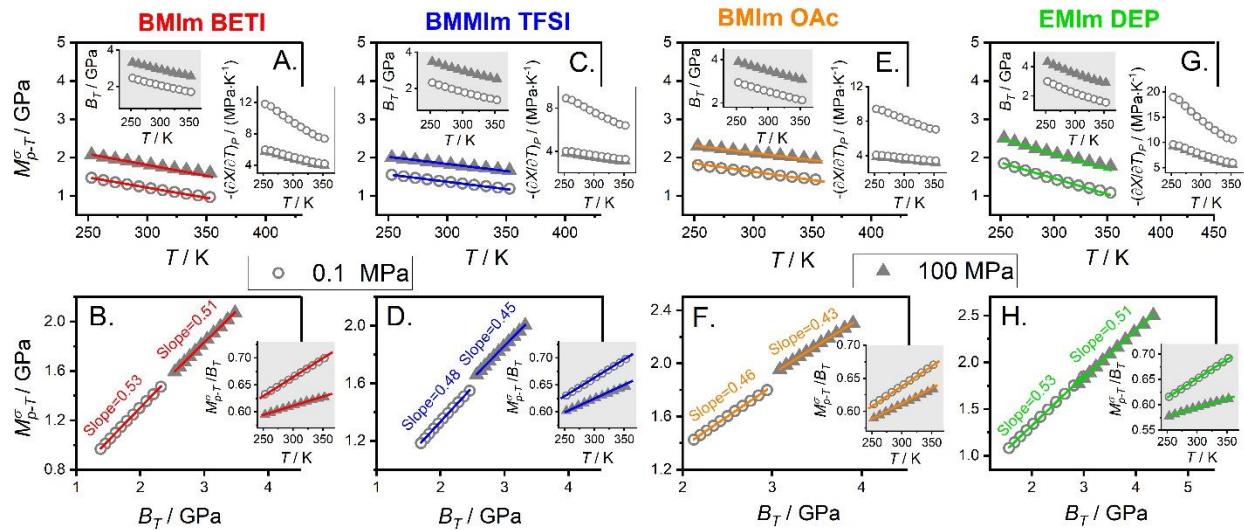


Fig. S4: The behavior of dynamic modulus and its connection to bulk modulus at isobars: 0.1 and 100 MPa for BMIm BETI (planes A and B), BMMIm TFSI (planes C and D), BMIm OAc (planes E and F), and EMIm DEP (planes G and H).

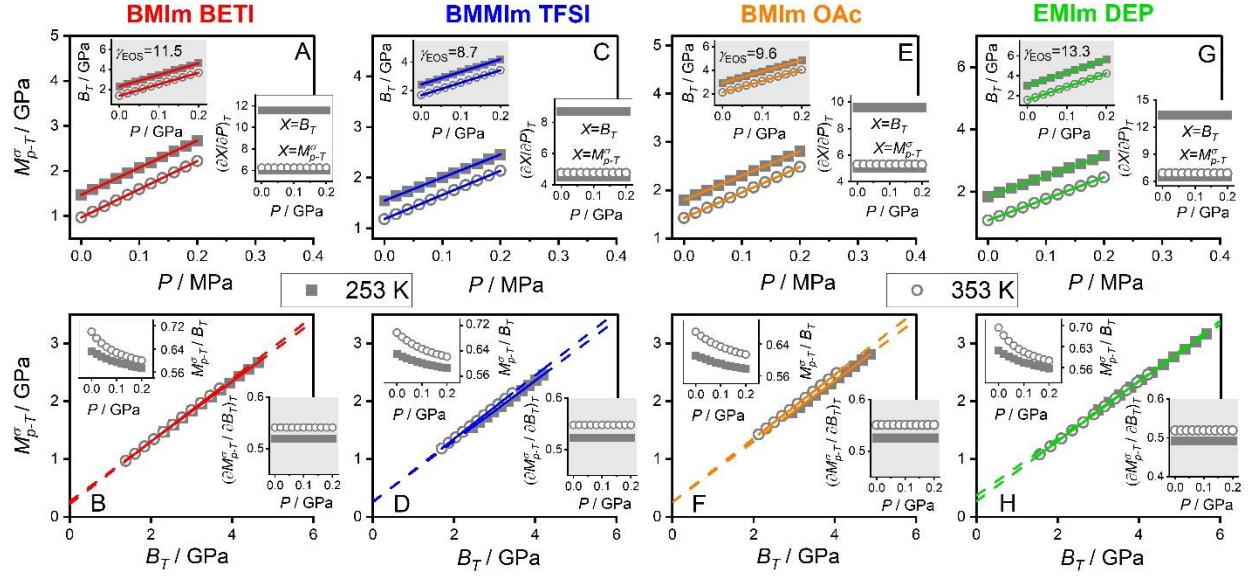


Fig. S5: The behavior of dynamic modulus and its connection to bulk modulus at isotherms: 253 K and 353 K for BMIm BETI (planes A and B), BMMIm TFSI (planes C and D), BMIm OAc (planes E and F), and EMIm DEP (planes G and H).

Table S1.

	$\gamma$	$\gamma_{EOS}$	$T_g / K$	$T_b / K$	$(dM^{\sigma}_{p-T}/dB_T)_P$ (isobar 0.1 MPa)	$(dM^{\sigma}_{p-T}/dB_T)_P$ (isobar 100 MPa)	$(dM^{\sigma}_{p-T}/dB_T)_T$ (isotherm 253 K)	$(dM^{\sigma}_{p-T}/dB_T)_T$ (isotherm 353 K)
BMPyr BOB	$4.19 \pm 0.03$	$9.7 \pm 0.1$	$227.9^\sigma$ $227.7^\eta$	$298.6^\sigma$ $299.1^\eta$	0.29	0.28	0.30	0.32
BMIM BETI	$2.85 \pm 0.05$	$11.5 \pm 0.2$	190.4	-	0.53	0.51	0.52	0.54
BMMIm TFSI	$2.75 \pm 0.05$	$8.7 \pm 0.1$	$191^\sigma$ $195^{DSC}$	$285.7^\sigma$ $276^\eta$	0.48	0.45	0.52	0.55
BMIM OAc	$2.25 \pm 0.05$	$9.6 \pm 0.1$	$200^\sigma$ $203.5^{DSC}$	257	0.46	0.43	0.53	0.55
EMIm DEP	$2.15 \pm 0.03$	$13.3 \pm 0.2$	202.7	-	0.52	0.49	0.53	0.51