

Electronic Supplementary Information: Optical and Dielectric Properties of Lead Perovskite and Iodoplumbate Complexes: An *Ab initio* Study

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1 Introduction

The present electronic supporting information (ESI) contains complementary data, analyses, figures, and tables, namely, *(i)* additional computational technical details; *(ii)* definition for the geometrical and lattice parameters analyses for the pseudo-cubic; *(iii)* convergence tests as a function of the cutoff energy and number of \mathbf{k} -points; *(iv)* orthorhombic (1D, 3D), and hexagonal $APbI_3$ structures; *(iv)* finally, additional data for the optical and electronic properties.

2 Structural, Energetic, and Electronic Analyses

2.1 Goldschmidt’s Tolerance Factor

The formability of perovskites, ABX_3 , can be empirically estimated through the Goldschmidt’s tolerance factor, TF ,¹ which is given by the following equation,

$$TF = \frac{r_A + r_X}{\sqrt{2}(r_B + r_X)}, \quad (1)$$

where r_A , r_B and r_X are the ionic radii for the ions in the A , B and X sites, respectively. In general an ideal cubic perovskite structure TF ranges from 0.9 to 1.0, while for distorted quasi-cubic perovskite structures the TF range from 0.8 to 0.9, and for the hexagonal phase, $TF > 1$. From Table 1, the ammonium (AM) and dabconium (DA) cations, the TF values are not in the range of perovskite formation region, while for the Cs-, MA- and FA-cations have a favorable TF for the formation of perovskite structures.

Table 1: Lead iodide $APbI_3$ perovskites with different A-cations, radius, tolerance-factor, TF ,² at room-temperature (RT) phase. We considered the following cations, $A = Cs^+$, ammonium (AM), $[NH_4]^+$, methylammonium (MA), $[CH_3NH_3]^+$, formamidinium (FA), $[NH_2(CH)NH_2]^+$, and dabconium (DA), $[C_6H_{13}N_2]^+$.

| Property | Cs | AM | MA | FA | DA |
|------------|--------------|--------------|------------|---------------------|-----------|
| Radius (Å) | 1.67 | 1.46 | 2.17 | 2.53 | 3.39 |
| TF | 0.80 | 0.76 | 0.91 | 1.02 | 1.17 |
| RT phase | Orthorhombic | Orthorhombic | Tetragonal | Cubic and Hexagonal | Hexagonal |
| Color | yellow | yellow | black | black and yellow | yellow |

2.2 Effective Coordination Concept

In this work, we employed the effective coordination concept,^{3,4} which is useful approach to perform the analysis of the coordination number and average weighted bond lengths. The

perfect PbI_6 has have 6-coordination in MAPbI_3 at Pb-I bond length approximately 3.17 Å, and ECN decreases as with inclusion lighter element chlorine.⁵ The PbI_6 pseudo-octahedron bond angles and ECN effected by the MA cation rotation. The equations employed for the ECN is given below,

$$ECN^{\text{Pb}} = \sum_j \text{Exp} \left[1 - \left(\frac{d_{ij}}{d_{av}^i} \right)^6 \right], \quad (2)$$

where

$$d_{av}^i = \frac{\sum_j d_{ij} \text{Exp} \left[1 - \left(\frac{d_{ij}}{d_i^{\text{min}}} \right)^6 \right]}{\sum_j \text{Exp} \left[1 - \left(\frac{d_{ij}}{d_i^{\text{min}}} \right)^6 \right]}. \quad (3)$$

d_{ij} indicates the distance between the atoms i and j , while d_i^{min} indicates the minimum distance between i and the nearest neighbour atom.

2.3 Bond Angle Variance

The bond angle variance,⁶ was calculated using the following equation,

$$BAV = \frac{1}{a-1} \sum_{i=1}^a (\phi_i - \phi_0)^2, BAV = \sum_{i=1}^{12} \frac{(\phi_i - 90^\circ)^2}{11}, \quad (4)$$

where ϕ_i is the i^{th} bond angle, and ϕ_0 is the ideal bond angle for a regular octahedron.

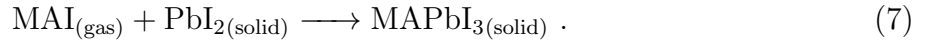
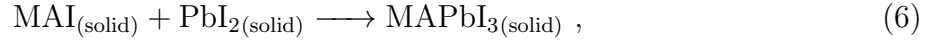
2.4 Cohesive and Formation Energies

The cohesive energy is the difference between the total energy of a solid to its constituent free atoms and this represents chemical stability of the solid. The cohesive energy of organic-inorganic perovskite defined as the energy required to separate organic molecule and inorganic species to infinite distance from each other. We employed the following equation,

$$E_{coh} = E_{tot}^{\text{MAPbI}_3} - iE_{tot}^{\text{C}} - jE_{tot}^{\text{N}} - kE_{tot}^{\text{H}} - mE_{tot}^{\text{I}} - nE_{\text{Pb}}, \quad (5)$$

where $E_{tot}^{\text{MAPbI}_3}$ is the total energy of the MAPbI₃ perovskite, while the remaining terms indicate the total energy of the respective free atoms. All the calculations are performed using the same cutoff energy.

Furthermore, we calculated also the formation energy, which is defined as follows. Formation energy of a substance is the change of energy between the final products to its initial reactants. Our DFT calculations are 0 K temperature calculations, and hence, entropy term not included in the calculation of formation enthalpy. The following chemical reactions can be represented,



Thus, the formation can be calculated using the following equation,

$$\Delta H_f(\text{APbI}_3) = E_{tot}^{\text{APbI}_3} - E_{tot}^{\text{AI}} - E_{tot}^{\text{PbI}_2} . \quad (8)$$

2.5 Optical Properties

The optical band gap and optical dielectric constant was calculated in the long-wavelength limit ($q \rightarrow 0$) by sufficiently increasing the empty states ($\text{NBANDS} = 2 \times \text{NELECT}$) within the independent particle approach by excluding the local field effects as prescribed in Gajdoš *et al*⁷ work. The convergence of dielectric function for CsPbI₃ was observed at 80 \AA^{-1} , Figure 6, dense \mathbf{k} -mesh/grid is necessary to integrate the Brillouin zone to attain accurate linear response properties.⁸ The optical properties and interband transitions of the perovskites calculated from the dielectric responses of ε_2 and ε_1 derived by summation over empty states and Kramer–Krönig^{7,9} relation using small complex shift of 0.01 eV for various polymorphs of APbI₃. The band to band transition amplitudes calculated by using our in-house code.¹⁰

$$\varepsilon_{\alpha\beta}^{(2)}(\omega) = \frac{4\pi^2 e^2}{\Omega} \lim_{q \rightarrow 0} \frac{1}{q^2} \sum_{c,\nu,\mathbf{k}} 2\omega_{\mathbf{k}} \delta(\varepsilon_{c\mathbf{k}} - \varepsilon_{\nu\mathbf{k}} - \omega) \times \langle u_{c\mathbf{k}+e_{\alpha}q} | u_{\nu\mathbf{k}} \rangle \langle u_{c\mathbf{k}+e_{\beta}q} | u_{\nu\mathbf{k}} \rangle \quad (9)$$

where, c and ν represents the conduction and valence band states, $u_{c\mathbf{k}}$ is cell periodic part of the orbitals at the \mathbf{k} -point, e is the electronic charge, Ω is the volume and ω is the light frequency.

3 Computational Convergence Tests

To obtain accurate results in the present study, we performed several computational convergence tests, which includes the following calculations: equilibrium lattice parameters (a_0 , b_0 , c_0) as a function of the number of \mathbf{k} -points in the irreducible part of the Brillouin zone (represented by the \mathbf{k} -density or \mathbf{k} -mesh) and number of plane-waves employed to the expansion of the Kohn–Sham orbitals (i.e., cutoff energy - ENCUT). The results are summarized below in Tables 2 and 3.

Table 2: The calculated lattice parameters (a_0 , b_0 , c_0), cubic deviation, and relative stabilization energy of MA [100] oriented pseudo-cubic $\text{CH}_3\text{NH}_3\text{PbI}_3$ as a function of the number of \mathbf{k} -points (\mathbf{k} -density) using the PBE functional and a cutoff energy of 842 eV.

| \mathbf{k} -density (\AA^{-1}) | \mathbf{k} -mesh $n \times n \times n$ | a_0 (\AA) | b_0 (\AA) | c_0 (\AA) | CD (\AA) | ΔE_{tot} meV |
|--|---|---------------------------|---------------------------|---------------------------|------------------------|--------------------------------|
| 20 | $3 \times 3 \times 3$ | 6.44 | 6.50 | 6.40 | 0.10 | 100.08 |
| 30 | $5 \times 5 \times 5$ | 6.43 | 6.52 | 6.49 | 0.14 | 5.75 |
| 40 | $6 \times 6 \times 6$ | 6.42 | 6.52 | 6.54 | 0.21 | -1.35 |
| 50 | $8 \times 8 \times 8$ | 6.43 | 6.52 | 6.51 | 0.17 | -0.09 |
| 60 | $9 \times 9 \times 9$ | 6.42 | 6.52 | 6.54 | 0.21 | 0.30 |
| 70 | $11 \times 11 \times 11$ | 6.42 | 6.52 | 6.54 | 0.22 | 0.16 |
| 80 | $12 \times 12 \times 12$ | 6.42 | 6.52 | 6.54 | 0.23 | 0.00 |

Table 3: The MA [100] oriented pseudo-cubic structure local geometrical parameters such as Pb–I bond length, cis I–Pb_{av}–I bond angle and SD, bond angle variance (*BAV*), ECN, PbI₆ octahedral volume, and average H-bond lengths calculated by using PBE functional at different k-density

| k-density (Å ⁻¹) | Pb–I _{av} (Å) | I–Pb _{av} –I (°) | <i>BAV</i> (°) | <i>ECN</i> ^{Pb} (NNN) | <i>Vol</i> ^{Pb} (Å ³) | <i>N</i> _{H...I} (Å) | <i>C</i> _{H...I} (Å) |
|---------------------------------|---------------------------|------------------------------|-------------------|-----------------------------------|---|----------------------------------|----------------------------------|
| 20 | 3.22 | 90.30 ± 2.51 | 6.33 | 5.97 | 44.60 | 2.70 ± 0.09 | 3.51 ± 0.05 |
| 30 | 3.25 | 89.90 ± 5.00 | 25.03 | 5.74 | 45.37 | 2.69 ± 0.07 | 3.55 ± 0.10 |
| 40 | 3.26 | 89.83 ± 6.07 | 36.90 | 5.57 | 45.61 | 2.69 ± 0.06 | 3.57 ± 0.13 |
| 50 | 3.26 | 89.86 ± 5.61 | 31.47 | 5.64 | 45.51 | 2.69 ± 0.06 | 3.56 ± 0.12 |
| 60 | 3.26 | 89.84 ± 6.04 | 36.56 | 5.58 | 45.59 | 2.69 ± 0.06 | 3.57 ± 0.13 |
| 70 | 3.26 | 89.83 ± 6.05 | 36.66 | 5.57 | 45.59 | 2.69 ± 0.06 | 3.57 ± 0.13 |
| 80 | 3.26 | 89.83 ± 6.06 | 36.71 | 5.57 | 45.54 | 2.69 ± 0.06 | 3.57 ± 0.13 |

Table 4: The MA [100] oriented CH₃NH₃PbI₃ pseudo-cubic lattice parameters, cubic deviation, and relative stabilization energy calculated using a cutoff energy of 1052 eV, using the PBE functional, and with a k-density of 40 Å⁻¹ for the Brillouin zone integration.

| Cutoff energy (eV) | <i>a</i> ₀ (Å) | <i>b</i> ₀ (Å) | <i>c</i> ₀ (Å) | CD (Å) | ΔE_{tot} (meV) |
|-----------------------|------------------------------|------------------------------|------------------------------|-----------|----------------------------------|
| 421 | 6.28 | 6.39 | 6.33 | 0.16 | 195.11 |
| 526 | 6.40 | 6.48 | 6.47 | 0.15 | 34.30 |
| 631 | 6.41 | 6.51 | 6.50 | 0.19 | 9.59 |
| 736 | 6.42 | 6.51 | 6.53 | 0.19 | 2.55 |
| 842 | 6.42 | 6.52 | 6.54 | 0.21 | 0.53 |
| 947 | 6.43 | 6.52 | 6.53 | 0.20 | -0.31 |
| 1052 | 6.43 | 6.51 | 6.55 | 0.20 | 0.00 |

Table 5: The MA [100] oriented $\text{CH}_3\text{NH}_3\text{PbI}_3$ pseudo-cubic local geometrical parameters, Pb–I bond length, cis I–Pb–I average bond angle and SD, BAV, ECN, PbI_6 octahedral volume, and average H-bond lengths calculated by using PBE functional and k-density of 40 \AA^{-1} .

| Cutoff Energy (eV) | Pb–I _{av} (\AA) | I–Pb _{av} –I ($^\circ$) | BAV ($^\circ^2$) | ECN ^{Pb} (NNN) | Vol ^{Pb} (\AA^3) | $N_{H\dots I}$ (\AA) | $C_{H\dots I}$ (\AA) |
|-----------------------|--|---------------------------------------|-----------------------|----------------------------|---|------------------------------------|------------------------------------|
| 421 | 3.18 | 89.97 ± 6.25 | 39.01 | 5.92 | 42.26 | 2.69 ± 0.02 | 3.42 ± 0.07 |
| 526 | 3.24 | 89.87 ± 5.67 | 32.20 | 5.74 | 44.71 | 2.69 ± 0.06 | 3.53 ± 0.08 |
| 631 | 3.25 | 89.86 ± 5.99 | 35.91 | 5.69 | 45.15 | 2.70 ± 0.05 | 3.57 ± 0.10 |
| 736 | 3.26 | 89.84 ± 5.90 | 34.79 | 5.60 | 45.48 | 2.69 ± 0.06 | 3.55 ± 0.12 |
| 842 | 3.26 | 89.83 ± 6.07 | 36.90 | 5.57 | 45.61 | 2.69 ± 0.06 | 3.57 ± 0.13 |
| 947 | 3.26 | 89.84 ± 6.15 | 37.91 | 5.58 | 45.63 | 2.69 ± 0.05 | 3.58 ± 0.13 |
| 1052 | 3.26 | 89.83 ± 6.00 | 35.99 | 5.55 | 45.68 | 2.69 ± 0.06 | 3.56 ± 0.13 |

4 Cubic Structures with Different Orientations for the A-cations: Cs, AM, MA, FA, DA

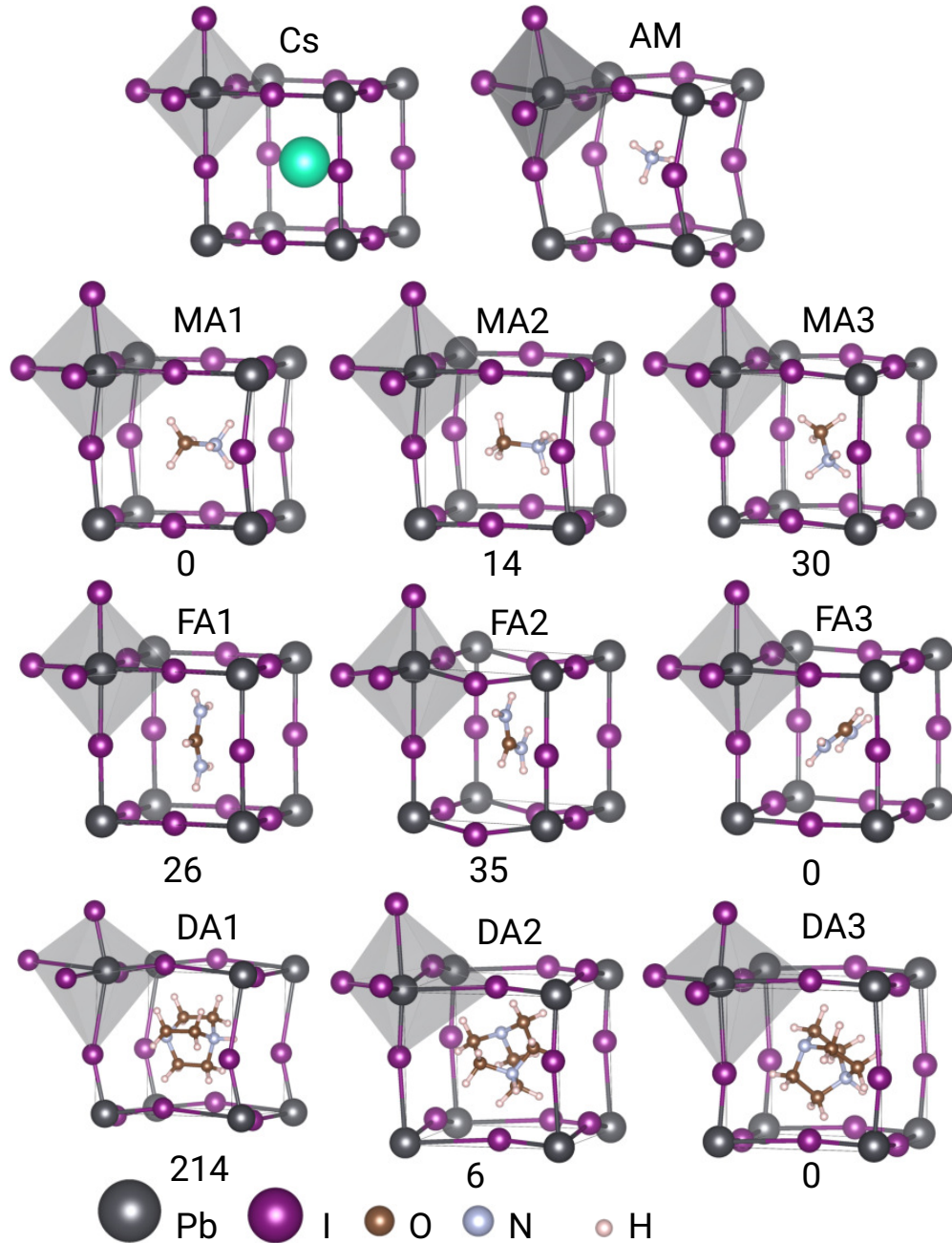


Figure 1: The cubic perovskite having the central cation of (a) Cs; the pseudo-cubic cage of PbI_3 with organic cations with distinct molecular orientations (b) ammonium (AM), (c-e) methylammonium (MA), (f-h) formamidinium (FA), and (i-k) dabconium (DA), respectively, relative stabilization energies are given in meV

5 Structural Parameters, Total Energy, and Energy Bandgap, for Different *A*-cation Orientations (*APbI₃*): MA, FA, DA

Below, we summarize the structural parameters, total energy, and energy band gap for all *A*-cations and different crystal structures.

5.1 MAPbI₃: Pseudo-cubic Structure

Table 6: MAPbI₃ perovskite pseudo-cubic crystal lattice parameters, cell volume, density, effective coordination number(ECN), quadratic elongation (QE), bond angle variance (BAV), total energy per formula unit, E_{tot} , relative stabilization energy (R.E) and energy bandgap calculated at PBE+D3 and 40 Å⁻¹.

| Property | MA1 | MA2 | MA3 |
|---|--------|--------|--------|
| a_0 (Å) | 6.30 | 6.37 | 6.40 |
| b_0 (Å) | 6.40 | 6.35 | 6.33 |
| c_0 (Å) | 6.36 | 6.39 | 6.33 |
| V (Å ³ /f.u) | 256.48 | 257.92 | 255.99 |
| Density (g cm ⁻³) | 4.01 | 3.99 | 4.02 |
| PbI ₆ vol. (Å ³) | 42.75 | 42.99 | 42.66 |
| AI ₁₂ vol. (Å ³) | 217.32 | 217.22 | 216.49 |
| Ratio (AI ₁₂ /PbI ₆) | 5.08 | 5.05 | 5.07 |
| ECN^{Pb} | 5.89 | 5.86 | 5.96 |
| ECN^A | 9.63 | 9.56 | 10.53 |
| Avg. Pb-I (Å) | 3.19 | 3.19 | 3.18 |
| Avg. Pb-I-Pb (°) | 168.73 | 170.89 | 172.40 |
| QE | 1.0104 | 1.0079 | 1.0048 |
| BAV (° ²) | 35.49 | 26.31 | 16.32 |
| E_{tot} (eV) | -51.89 | -51.87 | -51.86 |
| R.E (meV) per f.u | 0 | 14 | 30 |
| E_g (eV) at G (0,0,0) | 4.50 | 4.51 | 4.52 |

5.2 FAPbI₃: Pseudo-cubic Structure

Table 7: FAPbI₃ perovskite pseudo-cubic crystal lattice parameters, cell volume, density, effective coordination number (ECN), quadratic elongation (QE), bond angle variance (BAV), total energy per formula unit (E_{tot}), relative stabilization energy (R.E) and bandgap (E_g) calculated at PBE+D3 and 40 Å⁻¹.

| Property | FA1 | FA2 | FA3 |
|---|--------|--------|--------|
| a_0 (Å) | 6.49 | 6.53 | 6.31 |
| b_0 (Å) | 6.32 | 6.54 | 6.61 |
| c_0 (Å) | 6.38 | 6.29 | 6.32 |
| V (Å ³ /f.u) | 261.81 | 268.68 | 263.91 |
| Density (g cm ⁻³) | 4.01 | 3.91 | 3.98 |
| PbI ₆ vol. (Å ³) | 43.63 | 44.78 | 43.63 |
| AI ₁₂ vol. (Å ³) | 220.61 | 230.17 | 223.84 |
| Ratio (AI ₁₂ /PbI ₆) | 5.06 | 5.14 | 5.09 |
| ECN^{Pb} | 5.97 | 5.36 | 5.57 |
| ECN^A | 10.89 | 9.49 | 11.49 |
| Avg. Pb-I (Å) | 3.20 | 3.25 | 3.22 |
| Avg. Pb-I-Pb (°) | 175.80 | 170.81 | 169.20 |
| QE | 1.0026 | 1.0189 | 1.0119 |
| BAV (° ²) | 8.29 | 56.73 | 33.18 |
| E_{tot} (eV) | -56.59 | -56.58 | -56.61 |
| R.E (meV) per f.u | 26 | 35 | 0 |
| E_g (eV) at G (0,0,0) | 3.72 | 3.72 | 3.80 |

5.3 DAPbI₃: Pseudo-cubic Structure

Table 8: DAPbI₃ perovskite pseudo-cubic crystal lattice parameters, cell volume, density, effective coordination number (ECN), quadratic elongation (QE), bond angle variance (BAV), total energy per formula unit (E_{tot}), relative stabilization energy (R.E) and bandgap (E_g) calculated at PBE+D3 and 40 Å⁻¹.

| Property | DA1 | DA2 | DA3 |
|---|---------|---------|---------|
| a_0 (Å) | 7.11 | 6.87 | 7.00 |
| b_0 (Å) | 6.81 | 6.77 | 7.03 |
| c_0 (Å) | 7.30 | 7.29 | 7.03 |
| V (Å ³ /f.u) | 353.03 | 338.64 | 346.10 |
| Density (g cm ⁻³) | 3.30 | 3.44 | 3.36 |
| PbI ₆ vol. (Å ³) | 58.84 | 56.44 | 57.68 |
| AI ₁₂ vol. (Å ³) | 303.93 | 292.58 | 298.55 |
| Ratio (AI ₁₂ /PbI ₆) | 5.17 | 5.18 | 5.18 |
| ECN^{Pb} | 3.06 | 3.23 | 3.09 |
| ECN^A | 10.32 | 8.88 | 10.37 |
| Avg. Pb-I (Å) | 3.59 | 3.52 | 3.52 |
| Avg. Pb-I-Pb (°) | 160.69 | 165.35 | 169.82 |
| QE | 1.0570 | 1.0407 | 1.0284 |
| BAV (° ²) | 103.60 | 3.23 | 28.39 |
| E_{tot} (eV) | -130.45 | -130.66 | -130.67 |
| R.E (meV) per f.u | 214 | 6 | 0 |
| E_g (eV) at G (0,0,0) | 3.95 | 3.76 | 4.41 |

5.4 MAPbI₃: Orthorhombic-3D Structure

Table 9: MAPbI₃ perovskite orthorhombic-3D crystal lattice parameters, cell volume, density, effective coordination number (ECN), quadratic elongation (QE), bond angle variance (BAV), total energy per formula unit (E_{tot}), relative stabilization energy (R.E) wrt stable structure, and bandgap (E_g) calculated at PBE+D3 and 40 Å⁻¹.

| Property | MA1 | MA2 | MA3 |
|---|--------|--------|--------|
| a_0 (Å) | 8.91 | 9.27 | 9.38 |
| b_0 (Å) | 8.55 | 8.70 | 8.58 |
| c_0 (Å) | 12.73 | 12.57 | 12.52 |
| α (°) | 90.00 | 90.00 | 90.00 |
| β (°) | 90.00 | 90.00 | 90.00 |
| γ (°) | 90.00 | 90.00 | 90.00 |
| V (Å ³ /f.u) | 242.25 | 253.47 | 252.08 |
| Density (g cm ⁻³) | 4.25 | 4.06 | 4.08 |
| Api. Oh rot. Pb-Pb-I (°) | 10.14 | 0.05 | 10.57 |
| Equi. Oh rot. Pb-Pb-I (°) | 16.50 | 5.15 | 8.35 |
| Equi1 Pb-I-Pb (°) | 146.97 | 174.28 | 161.18 |
| Equi2 Pb-I-Pb (°) | 146.97 | 174.28 | 161.18 |
| Api. Pb-I-Pb (°) | 159.71 | 179.90 | 158.88 |
| Oh torsion angle (°) | 12.30 | 0.00 | 9.80 |
| Pb(1) I ₆ vol. (Å ³) | 44.37 | 42.13 | 42.81 |
| Pb(2) I ₆ vol. (Å ³) | 44.37 | 42.13 | 42.81 |
| Pb(3) I ₆ vol. (Å ³) | 44.37 | 42.36 | 43.44 |
| Pb(4) I ₆ vol. (Å ³) | 44.37 | 42.36 | 43.44 |
| ECN^{Pb1} | 6.00 | 5.96 | 5.98 |
| ECN^{Pb2} | 6.00 | 5.96 | 5.98 |
| ECN^{Pb3} | 6.00 | 5.92 | 5.97 |
| ECN^{Pb4} | 6.00 | 5.92 | 5.97 |
| QE1 | 1.0043 | 1.0033 | 1.0200 |
| QE2 | 1.0043 | 1.0033 | 1.0200 |
| QE3 | 1.0043 | 1.0075 | 1.0081 |
| QE4 | 1.0043 | 1.0075 | 1.0081 |
| BAV1 (° ²) | 15.70 | 10.67 | 66.15 |
| BAV2 (° ²) | 15.70 | 10.67 | 66.15 |
| BAV3 (° ²) | 15.70 | 24.47 | 27.50 |
| BAV4 (° ²) | 15.70 | 24.47 | 27.50 |
| E_{tot} (eV) | -52.04 | -51.86 | -51.93 |
| R.E (meV) per f.u | 0 | 182 | 111 |
| E_g (eV) at G (0,0,0) | 1.76 | 1.50 | 1.76 |

5.5 FAPbI₃: Orthorhombic-3D Structure

Table 10: FAPbI₃ perovskite orthorhombic-3D crystal lattice parameters, cell volume, density, quadratic elongation (QE), effective coordination number (ECN), bond angle variance (BAV), total energy per formula unit (E_{tot}), relative stabilization energy (R.E) wrt stable structure, and bandgap (E_g) calculated at PBE+D3 and 40 Å⁻¹.

| Property | FA1 | FA2 | FA3 |
|---|--------|--------|--------|
| a_0 (Å) | 9.01 | 9.64 | 10.09 |
| b_0 (Å) | 8.90 | 8.46 | 8.02 |
| c_0 (Å) | 12.57 | 12.73 | 12.42 |
| α (°) | 90.00 | 90.00 | 90.02 |
| β (°) | 90.00 | 90.00 | 90.00 |
| γ (°) | 90.00 | 90.00 | 90.00 |
| V (Å ³ /f.u) | 251.88 | 259.68 | 251.22 |
| Density (g cm ⁻³) | 4.17 | 4.05 | 4.18 |
| Api. Oh rot. Pb-Pb-I (°) | 0.00 | 2.15 | 4.48 |
| Equi. Oh rot. Pb-Pb-I (°) | 14.93 | 4.61 | 9.79 |
| Equi1 Pb-I-Pb (°) | 150.13 | 166.71 | 149.95 |
| Equi2 Pb-I-Pb (°) | 150.13 | 170.85 | 160.22 |
| Api. Pb-I-Pb (°) | 180.00 | 175.70 | 4.48 |
| Oh torsion angle (°) | 0.00 | 0.00 | 0.00 |
| Pb(1) I ₆ vol. (Å ³) | 42.06 | 43.28 | 41.87 |
| Pb(2) I ₆ vol. (Å ³) | 42.06 | 43.28 | 41.87 |
| Pb(3) I ₆ vol. (Å ³) | 44.90 | 43.28 | 41.87 |
| Pb(4) I ₆ vol. (Å ³) | 44.90 | 43.28 | 41.87 |
| ECN^{Pb1} | 6.00 | 5.97 | 5.44 |
| ECN^{Pb2} | 6.00 | 5.97 | 5.44 |
| ECN^{Pb3} | 5.90 | 5.97 | 5.44 |
| ECN^{Pb4} | 5.90 | 5.97 | 5.44 |
| QE1 | 1.0033 | 1.0132 | 1.0753 |
| QE2 | 1.0033 | 1.0132 | 1.0753 |
| QE3 | 1.0075 | 1.0132 | 1.0753 |
| QE4 | 1.0075 | 1.0132 | 1.0753 |
| BAV1 (° ²) | 0.18 | 45.15 | 225.57 |
| BAV2 (° ²) | 0.18 | 45.15 | 225.57 |
| BAV3 (° ²) | 0.17 | 45.15 | 225.57 |
| BAV4 (° ²) | 0.17 | 45.15 | 225.57 |
| E_{tot} (eV) | -56.77 | -56.78 | -54.63 |
| R.E (meV) per f.u | 6 | 0 | 2146 |
| E_g (eV) at G (0,0,0) | 1.49 | 1.67 | 0.91 |

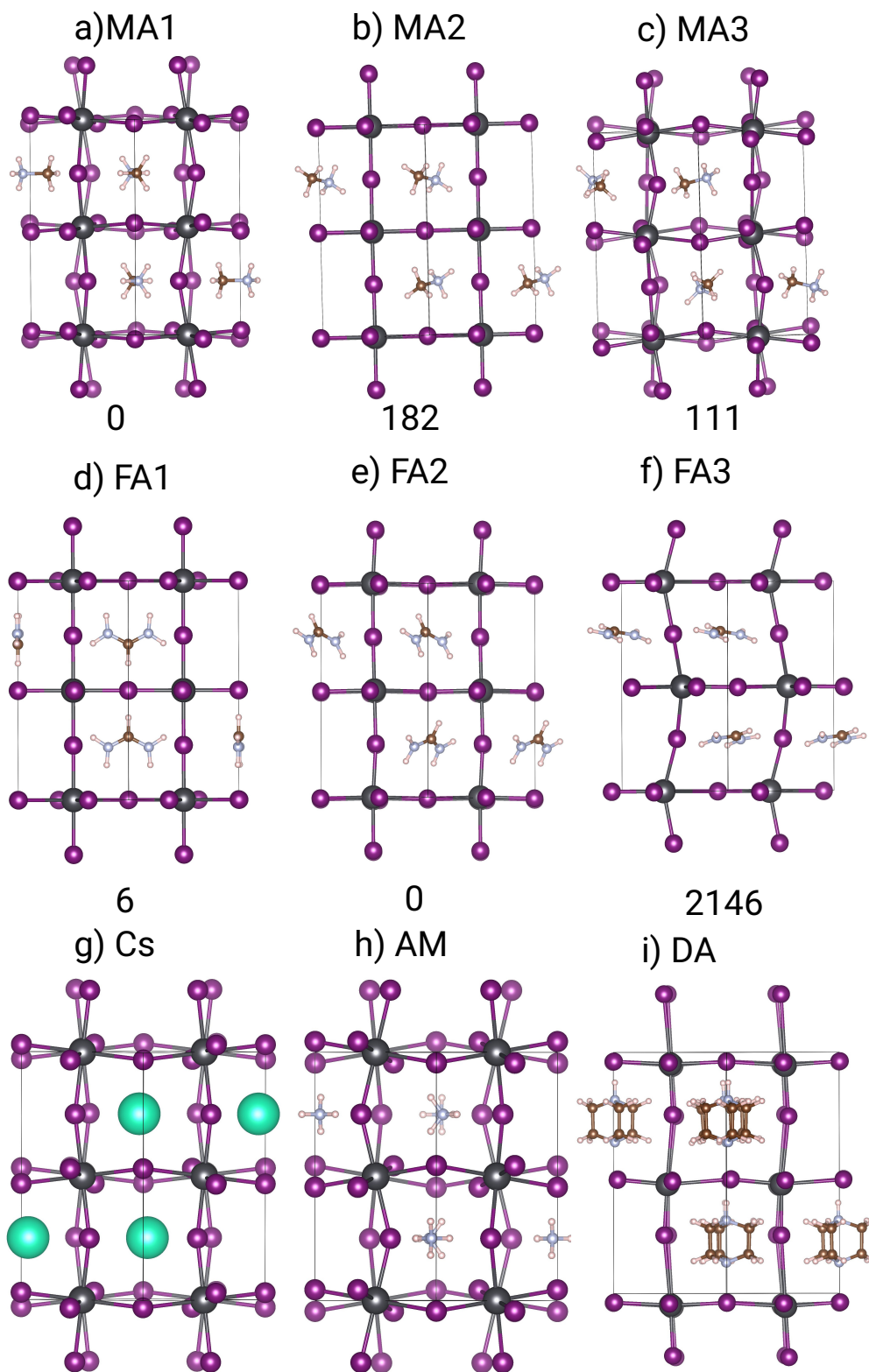


Figure 2: The orthorhombic (O3D) perovskites having the central inorganic and organic cation with distinct molecular orientations of a-c) methylammonium (MA), d-f) formamidinium (FA), g) Cs, h) ammonium (AM) and (i) dabconium (DA), respectively, relative stabilization energies are given in meV

5.6 MAPbI₃: Hexagonal Structure

Table 11: MAPbI₃ perovskite hexagonal crystal lattice parameters, cell volume, density, quadratic elongation (QE), effective coordination number (ECN), bond angle variance (BAV), total energy per formula unit (E_{tot}), relative stabilization energy (R.E) wrt stable structure, and bandgap (E_g) calculated at PBE+D3 and 40 Å⁻¹.

| Property | MA1 | MA2 | MA3 |
|---|--------|--------|--------|
| a_0 (Å) | 8.74 | 8.84 | 8.83 |
| b_0 (Å) | 8.49 | 8.47 | 8.48 |
| c_0 (Å) | 7.83 | 7.87 | 7.87 |
| α (°) | 92.71 | 96.09 | 82.58 |
| β (°) | 96.86 | 80.87 | 100.12 |
| γ (°) | 119.91 | 121.35 | 121.19 |
| V (Å ³ /f.u) | 248.07 | 248.15 | 247.84 |
| Density (g cm ⁻³) | 4.15 | 4.15 | 4.15 |
| Pb(1) I ₆ vol. (Å ³) | 45.40 | 45.05 | 45.18 |
| Pb(2) I ₆ vol. (Å ³) | 45.60 | 45.18 | 45.21 |
| ECN^{Pb1} | 5.99 | 5.94 | 5.95 |
| ECN^{Pb2} | 5.95 | 5.95 | 5.95 |
| QE1 | 1.0035 | 1.0072 | 1.0079 |
| QE2 | 1.0034 | 1.0072 | 1.0082 |
| BAV1 (° ²) | 12.25 | 23.73 | 25.95 |
| BAV2 (° ²) | 11.17 | 24.19 | 27.37 |
| E_{tot} (eV) | -52.03 | -52.01 | -51.98 |
| R.E (meV) per f.u | 0 | 15 | 49 |
| E_g (eV) at G (0,0,0) | 2.99 | 2.95 | 2.94 |

5.7 FAPbI₃: Hexagonal Structure

Table 12: FAPbI₃ perovskite hexagonal crystal lattice parameters, cell volume, density, quadratic elongation (QE), effective coordination number (ECN), bond angle variance (BAV), total energy per formula unit (E_{tot}), relative stabilization energy (R.E) wrt stable structure, and bandgap (E_g) calculated at PBE+D3 and 40 Å⁻¹.

| Property | FA1 | FA2 | FA3 |
|---|----------|--------|--------|
| a_0 (Å) | 8.56 | 8.67 | 8.58 |
| | (8.66) | | |
| b_0 (Å) | 8.68 | 8.59 | 8.81 |
| | (8.66) | | |
| c_0 (Å) | 7.99 | 7.94 | 7.88 |
| | (7.90) | | |
| α (°) | 86.27 | 87.33 | 94.14 |
| β (°) | 92.23 | 94.55 | 87.68 |
| γ (°) | 120.56 | 120.43 | 120.95 |
| V (Å ³ /f.u) | 255.04 | 254.37 | 254.98 |
| Density (g cm ⁻³) | 4.12 | 4.13 | 4.12 |
| Pb(1) I ₆ vol. (Å ³) | 45.56 | 45.04 | 45.21 |
| Pb(2) I ₆ vol. (Å ³) | 45.00 | 45.47 | 45.17 |
| ECN^{Pb1} | 5.82 | 5.94 | 5.87 |
| ECN^{Pb2} | 5.92 | 5.86 | 5.89 |
| QE1 | 1.0035 | 1.0072 | 1.0079 |
| QE2 | 1.0034 | 1.0072 | 1.0082 |
| BAV1 (° ²) | 23.24 | 22.24 | 22.38 |
| BAV2 (° ²) | 25.20 | 19.17 | 22.72 |
| E_{tot} (eV) | -56.83 | -56.83 | -56.82 |
| R.E (meV) per f.u | 0 | 1 | 10 |
| E_g (eV) at G (0,0,0) | 2.99 | 2.96 | 2.82 |

5.8 DAPbI₃: Hexagonal Structure

Table 13: DAPbI₃ perovskite hexagonal crystal lattice parameters, cell volume, density, quadratic elongation (QE), effective coordination number (ECN), bond angle variance (BAV), total energy per formula unit (E_{tot}), relative stabilization energy (R.E) wrt stable structure, and bandgap (E_g) calculated at PBE+D3 and 40 Å⁻¹.

| Property | DA1 | DA2 | DA3 |
|---|--------|--------|--------|
| a_0 (Å) | 10.01 | 10.03 | 9.96 |
| b_0 (Å) | 10.01 | 10.02 | 9.97 |
| c_0 (Å) | 7.75 | 8.04 | 8.10 |
| α (°) | 90.00 | 90.04 | 90.69 |
| β (°) | 90.00 | 89.97 | 90.00 |
| γ (°) | 120.00 | 120.02 | 119.79 |
| V (Å ³ /f.u) | 336.53 | 349.78 | 348.87 |
| Density (g cm ⁻³) | 3.46 | 3.33 | 3.34 |
| Pb(1) I ₆ vol. (Å ³) | 45.63 | 46.60 | 46.80 |
| Pb(2) I ₆ vol. (Å ³) | 46.49 | 46.18 | 45.97 |
| ECN^{Pb1} | 6.00 | 6.00 | 5.96 |
| ECN^{Pb2} | 6.00 | 5.87 | 5.93 |
| QE1 | 1.0035 | 1.0072 | 1.0079 |
| QE2 | 1.0034 | 1.0072 | 1.0082 |
| BAV1 (° ²) | 4.85 | 22.24 | 22.38 |
| BAV2 (° ²) | 2.05 | 19.17 | 22.72 |
| E_{tot} (eV) | -56.83 | -56.83 | -56.82 |
| R.E (meV) per f.u | 0 | 168 | 124 |
| E_g (eV) at G (0,0,0) | 2.99 | 2.96 | 2.82 |

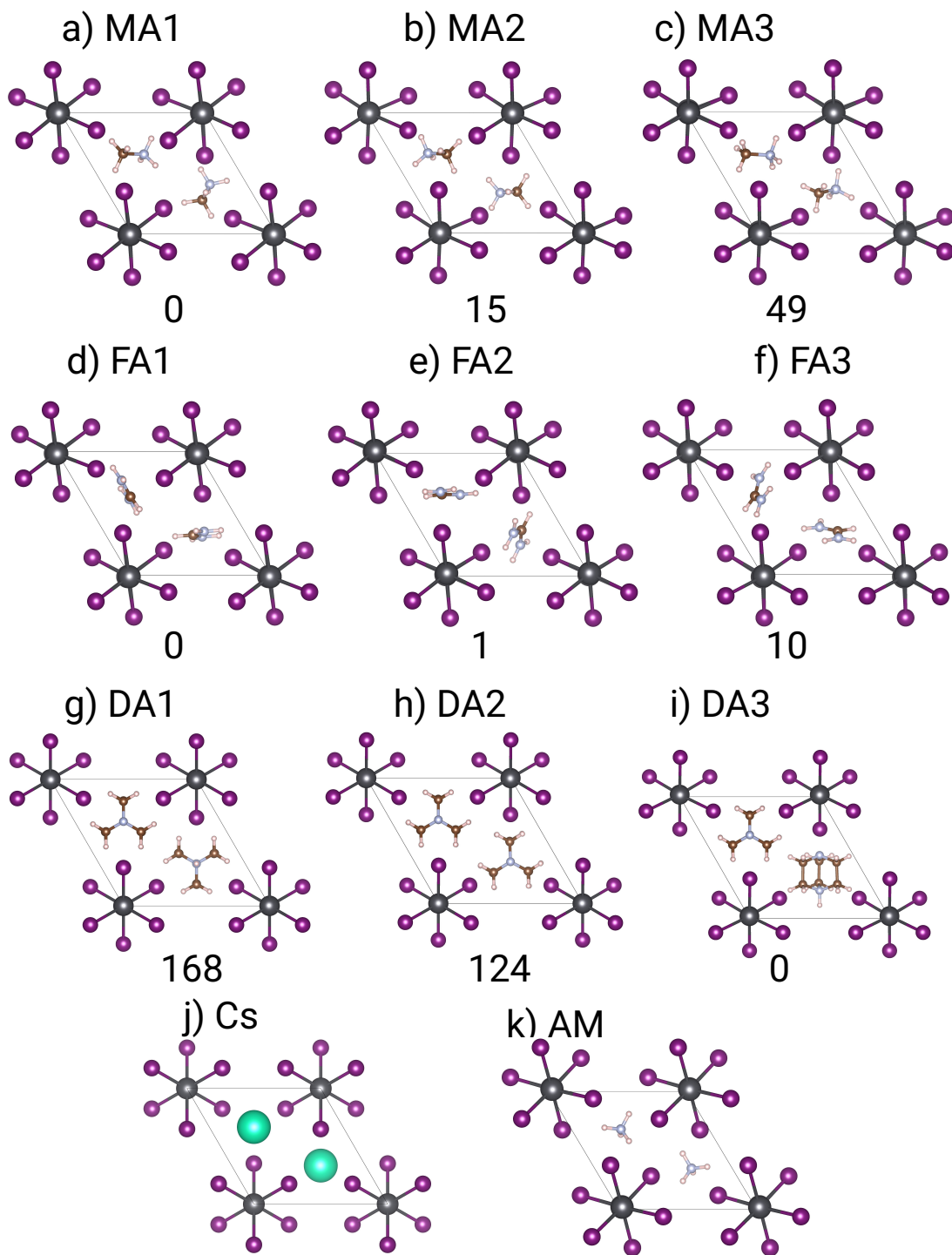


Figure 3: The hexagonal (2H) perovskites having the central cation of (a-c) methylammonium (MA), (d-f) formamidinium (FA), and (g-i) dabconium (DA), (j) Cs, (k) ammonium (AM) respectively, relative stabilization energies are given in meV.

5.9 MAPbI₃: Orthorhombic-1D Structure

Table 14: MAPbI₃ perovskite orthorhombic-1D crystal lattice parameters, cell volume, density, quadratic elongation (QE), effective coordination number (ECN), bond angle variance (BAV), total energy per formula unit (E_{tot}), relative stabilization energy (R.E) wrt stable, structure and bandgap (E_g) calculated at PBE+D3 and 40 Å⁻¹ kd

| Property | MA1 | MA2 | MA3 |
|---|--------|--------|--------|
| a_0 (Å) | 12.35 | 11.73 | 11.16 |
| b_0 (Å) | 4.72 | 4.74 | 4.70 |
| c_0 (Å) | 16.74 | 17.71 | 18.69 |
| α (°) | 90.00 | 90.00 | 90.00 |
| β (°) | 90.00 | 90.00 | 90.00 |
| γ (°) | 90.00 | 90.00 | 90.00 |
| V (Å ³ /f.u) | 243.84 | 246.56 | 244.92 |
| Density (g cm ⁻³) | 4.22 | 4.18 | 4.19 |
| Pb(1) I ₆ vol. (Å ³) | 46.13 | 46.11 | 45.77 |
| Pb(2) I ₆ vol. (Å ³) | 46.13 | 46.32 | 46.06 |
| Pb(3) I ₆ vol. (Å ³) | 46.13 | 46.31 | 45.98 |
| Pb(4) I ₆ vol. (Å ³) | 46.13 | 46.11 | 46.31 |
| ECN^{Pb1} | 5.67 | 5.77 | 5.75 |
| ECN^{Pb2} | 5.67 | 5.89 | 5.90 |
| ECN^{Pb3} | 5.67 | 5.89 | 5.82 |
| ECN^{Pb4} | 5.67 | 5.76 | 5.93 |
| QE1 | 1.0083 | 1.0092 | 1.0068 |
| QE2 | 1.0083 | 1.0082 | 1.0065 |
| QE3 | 1.0083 | 1.0081 | 1.0072 |
| QE4 | 1.0083 | 1.0092 | 1.0042 |
| BAV1 (° ²) | 25.07 | 28.99 | 21.18 |
| BAV2 (° ²) | 25.07 | 26.99 | 20.69 |
| BAV3 (° ²) | 25.07 | 26.94 | 23.22 |
| BAV4 (° ²) | 25.07 | 29.14 | 13.39 |
| E_{tot} (eV) | -51.99 | -51.99 | -52.05 |
| R.E (meV) per f.u | 74 | 67 | 0 |
| E_g (eV) at G (0,0,0) | 2.70 | 2.77 | 2.84 |

5.10 FAPbI₃: Orthorhombic-1D Structure

Table 15: FAPbI₃ perovskite orthorhombic-1D crystal lattice parameters, cell volume, density, quadratic elongation (QE), effective coordination number (ECN), bond angle variance (BAV), total energy per formula unit (E_{tot}), relative stabilization energy (R.E) and bandgap (E_g) calculated at PBE+D3 and 40 Å⁻¹.

| Property | FA1 | FA2 | FA3 |
|---|--------|--------|--------|
| a_0 (Å) | 11.76 | 12.06 | 11.09 |
| b_0 (Å) | 4.55 | 4.56 | 4.59 |
| c_0 (Å) | 19.50 | 19.14 | 20.38 |
| α (°) | 90.00 | 90.00 | 90.00 |
| β (°) | 90.00 | 90.00 | 90.00 |
| γ (°) | 90.00 | 90.00 | 90.00 |
| V (Å ³ /f.u) | 260.53 | 263.10 | 259.47 |
| Density (g cm ⁻³) | 4.03 | 4.00 | 4.05 |
| Pb(1) I ₆ vol. (Å ³) | 46.22 | 47.16 | 46.35 |
| Pb(2) I ₆ vol. (Å ³) | 46.22 | 46.10 | 46.28 |
| Pb(3) I ₆ vol. (Å ³) | 46.22 | 47.19 | 46.26 |
| Pb(4) I ₆ vol. (Å ³) | 46.22 | 46.40 | 46.32 |
| ECN^{Pb1} | 5.81 | 5.28 | 5.76 |
| ECN^{Pb2} | 5.81 | 5.74 | 5.78 |
| ECN^{Pb3} | 5.81 | 5.28 | 5.79 |
| ECN^{Pb4} | 5.81 | 5.71 | 5.77 |
| QE1 | 1.0024 | 1.0056 | 1.0060 |
| QE2 | 1.0024 | 1.0036 | 1.0060 |
| QE3 | 1.0024 | 1.0054 | 1.0057 |
| QE4 | 1.0024 | 1.0049 | 1.0060 |
| BAV1 (° ²) | 6.01 | 7.33 | 18.00 |
| BAV2 (° ²) | 6.01 | 9.73 | 18.30 |
| BAV3 (° ²) | 6.01 | 6.96 | 17.36 |
| BAV4 (° ²) | 6.01 | 14.42 | 16.83 |
| E_{tot} (eV) | -56.91 | -56.82 | -56.91 |
| R.E (meV) per f.u | 0 | 92 | 2 |
| E_g (eV) at G (0,0,0) | 3.15 | 3.07 | 3.11 |

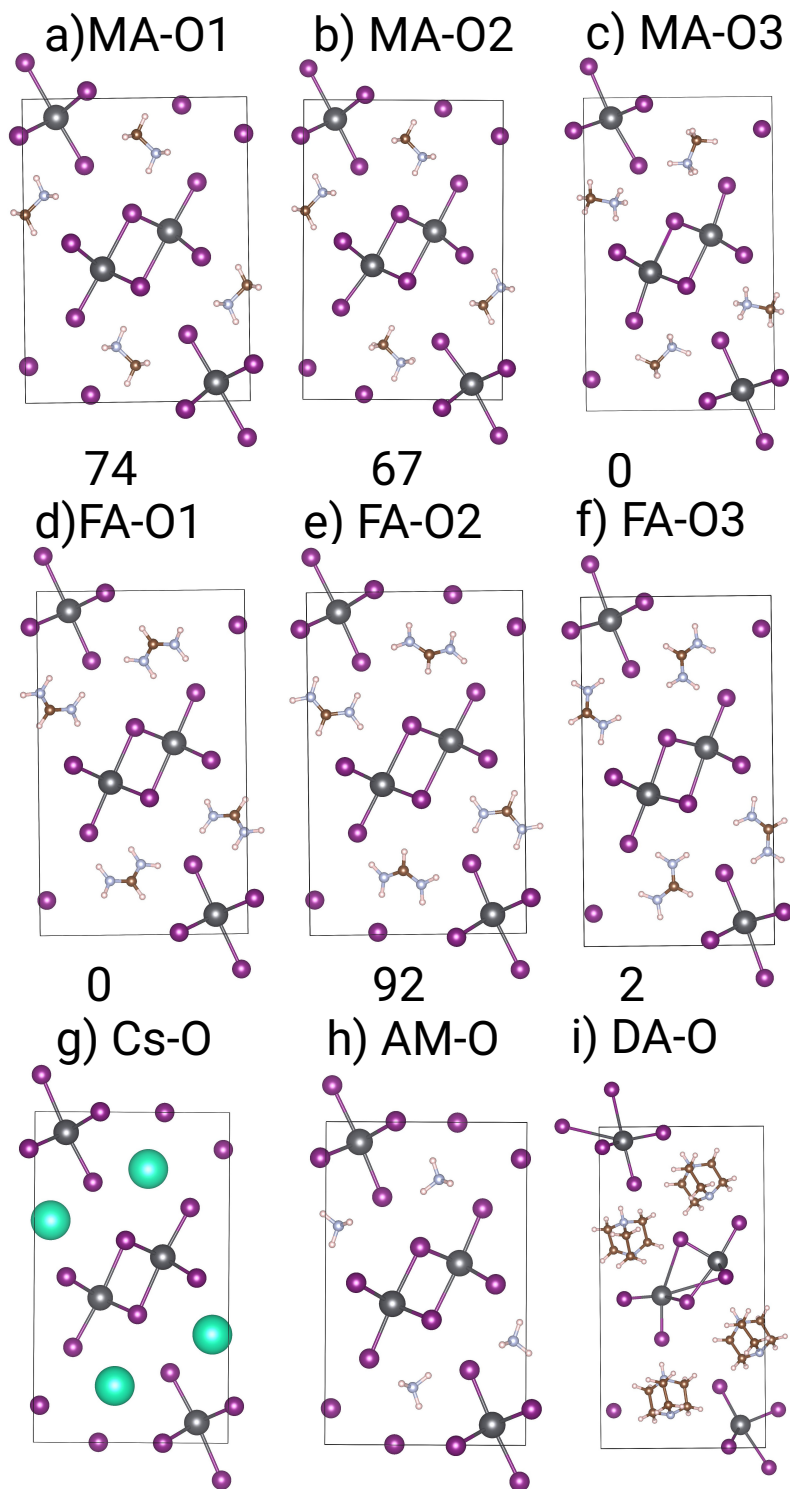


Figure 4: The orthorhombic (O1D) non-perovskite having the central inorganic and organic cation with distinct molecular orientations of a-c) methylammonium (MA), d-f) formamidinium (FA), g) Cs, h) ammonium (AM) and (i) dabconium (DA), respectively, relative stabilization energies are given in meV.

6 Structural Parameters, Energetic, and Electronic Properties for the Lowest Energy Configurations for the APbI₃ Structures for A = Cs, AM, MA, FA, DA

6.1 APbI₃: Cubic and Pseudo-cubic Structures

Table 16: APbI₃ perovskite cubic and pseudo-cubic crystal lattice parameters, cell volume, density, polyhedral ratio, discrepancy factor (d), quadratic elongation (QE), effective coordination number (ECN), bond angle variance (BAV), Δx -ionic displacement, cohesive energy, lattice energy, enthalpy of formation and bandgap, E_g , calculated at PBE+D3 and 40 Å⁻¹ (experimental measurements in parentheses).

| Property | Cs | AM | MA1 | FA3 | DA3 |
|---|---------------------|--------|---------------------|-----------------|--------|
| a_0 (Å) | 6.31 (6.29) | 6.28 | 6.30 (6.31) | 6.31 (6.36) | 7.00 |
| b_0 (Å) | 6.31 (6.29) | 6.28 | 6.40 (6.31) | 6.61 (6.36) | 7.03 |
| c_0 (Å) | 6.31 (6.29) | 6.28 | 6.36 (6.31) | 6.32 (6.36) | 7.03 |
| Vol. (Å ³ /f.u) | 251.06 (249.64) | 247.64 | 256.48 (251.60) | 263.91 | 346.10 |
| Density (g cm ⁻³) | 4.77 (4.81) | 4.06 | 4.01 (4.05) | 3.98 | 3.36 |
| PbI ₆ vol. (Å ³) | 41.84 (41.61) | 41.27 | 42.75 | 43.63 | 57.68 |
| Al ₁₂ vol. (Å ³) | 209.22 (208.03) | 221.52 | 217.32 | 223.84 | 298.55 |
| Ratio (Al ₁₂ /PbI ₆) | 5.00 | 5.37 | 5.08 | 5.09 | 5.18 |
| d^{Pb} | 0.498 | 0.256 | 0.288 | 0.219 | -0.087 |
| ECN^{Pb} | 6.00 | 6.00 | 5.89 | 5.57 | 3.09 |
| Avg. Pb-I (Å) | 3.15 | 3.19 | 3.19 | 3.22 | 3.52 |
| Avg. Pb-I-Pb (°) | 180.00 | 159.25 | 168.73 | 169.20 | 160.69 |
| QE | 1.0000 | 1.0335 | 1.0104 | 1.0119 | 1.0284 |
| BAV (° ²) | 0.00 | 115.03 | 35.49 | 33.18 | 28.39 |
| ΔA (in Å) | 0.00 | 0.55 | 0.52 | 0.25 | 0.36 |
| ΔPb (in Å) | 0.00 | 0.30 | 0.15 | 0.25 | 0.44 |
| ΔI (in Å) | 0.00 | 0.64 | 0.43 | 0.17 | 0.47 |
| E_{coh} per atom (eV) | -2.81 | -2.94 | -3.30 | -4.06 | -4.02 |
| ΔH (kJ/mol) | -237.34 | 42.13 | 11.59 | 24.17 | 6.07 |
| E_g (eV) at R (0.5,0.5,0.5) | 1.36 | 2.02 | 1.63 | 1.64 | 2.13 |
| E_g (eV) at G (0,0,0) | 4.28 | 3.68 | 4.50 | 3.80 | 4.41 |

6.2 APbI₃: Hexagonal and Pseudo-hexagonal Structures

Table 17: APbI₃ perovskite hexagonal/pseudo-hexagonal crystal lattice parameters, cell volume per f.u, density, and enthalpy of formation calculated, total energy per formula unit, E_{tot} , relative stabilization energy (R.E) wrt cubic structure and bandgap, E_g , calculated at PBE+D3 and 40 Å⁻¹. The experimental measurements are in parentheses.

| Property | Cs | AM | MA1 | FA1 | DA1 |
|-------------------------------------|---------|--------|--------|---------|--------|
| a_0 (Å) | 8.60 | 8.37 | 8.74 | 8.56 | 10.01 |
| b_0 (Å) | 8.60 | 8.36 | 8.49 | 8.68 | 10.01 |
| c_0 (Å) | 7.57 | 7.88 | 7.83 | 7.99 | 7.75 |
| α (°) | 90.00 | 95.00 | 92.71 | 86.27 | 90.00 |
| β (°) | 90.00 | 92.49 | 96.86 | 92.23 | 90.00 |
| γ (°) | 120.00 | 120.33 | 119.31 | 120.56 | 120.00 |
| Vol. (Å ³ /f.u) | 242.35 | 235.74 | 248.07 | 255.04 | 336.53 |
| Density (g cm ⁻³) | 4.91 | 4.27 | 4.15 | 4.12 | 3.46 |
| | | | | (4.19) | |
| Pb(1) I ₆ | 44.78 | 45.52 | 45.40 | 45.56 | 45.63 |
| Pb(2) I ₆ | 44.78 | 45.66 | 45.60 | 45.00 | 46.49 |
| ECN^{Pb1} | 6.00 | 5.98 | 5.99 | 5.82 | 6.00 |
| ECN^{Pb2} | 6.00 | 5.98 | 5.95 | 5.92 | 6.00 |
| QE1 | 1.0003 | 1.0032 | 1.0035 | 1.0071 | 1.0013 |
| QE2 | 1.0003 | 1.0031 | 1.0034 | 1.0072 | 1.0006 |
| BAV1 (° ²) | 0.94 | 11.20 | 12.25 | 23.24 | 4.85 |
| BAV2 (° ²) | 0.94 | 10.97 | 11.17 | 25.20 | 2.05 |
| E_{coh} per atom (eV) | -2.82 | -2.99 | -3.31 | -4.08 | -4.03 |
| ΔH (kJ/mol) | -244.50 | 3.77 | -2.21 | 3.11 | -12.96 |
| R.E (kJ mol ⁻¹) per f.u | -7.16 | -38.36 | -13.79 | -21.06 | -19.03 |
| E_g (eV) at G (0,0,0) | 2.53 | 3.42 | 2.99 | 2.99 | 2.56 |

HEXAGONAL/PSEUDO-HEXAGONAL

6.3 APbI₃: Non-perovskite orthorhombic-1D Structure

Table 18: APbI₃ non-perovskite orthorhombic-1D crystal lattice parameters, cell volume per f.u, density, and enthalpy of formation, total energy per formula unit, E_{tot} , and relative stabilization energy (R.E) wrt cubic structure calculated at PBE+D3 and 40 Å⁻¹. The experimental measurements are in parentheses.

| Property | Cs | AM | MA3 | FA1 | DA |
|-------------------------------------|------------------|------------------|--------|-----------|--------|
| a_0 (Å) | 10.64 (10.43) | 10.57 (10.30) | 11.16 | 11.76 | 11.31 |
| b_0 (Å) | 4.84 (4.79) | 4.76 (4.74) | 4.70 | 4.55 6.13 | |
| c_0 (Å) | 18.08 (17.76) | 17.02 (17.29) | 18.69 | 19.50 | 22.09 |
| α (°) | 90.00 | 90.00 | 90.00 | 90.00 | 90.00 |
| β (°) | 90.00 | 90.00 | 90.00 | 90.00 | 90.00 |
| γ (°) | 90.00 | 90.00 | 90.00 | 90.00 | 90.00 |
| V (Å ³ /f.u) | 232.76 | 214.16 | 244.92 | 260.53 | 383.09 |
| Density (g cm ⁻³) | 5.14 (5.39) | 4.70 (4.22) | 4.20 | 4.03 | 3.04 |
| Pb(1) I ₆ | 46.18 | 45.24 | 45.80 | 46.22 | 46.93 |
| ECN^{Pb1} | 5.75 | 5.93 | 5.75 | 5.81 | 3.35 |
| ECN^{Pb2} | 5.75 | 5.93 | 5.90 | 5.81 | 3.41 |
| ECN^{Pb3} | 5.75 | 5.93 | 5.82 | 5.81 | 4.09 |
| ECN^{Pb4} | 5.75 | 5.93 | 5.93 | 5.81 | 3.00 |
| QE1 | 1.0062 | 1.0045 | 1.0068 | 1.0024 | 1.3761 |
| BAV1 (° ²) | 12.64 | 13.90 | 21.18 | 6.01 | |
| E_{coh} per atom (eV) | -2.83 | -3.00 | -3.31 | -4.08 | -4.00 |
| ΔH (kJ/mol) | -249.19 | -9.48 | -4.26 | -4.10 | -12.54 |
| R.E (kJ mol ⁻¹) per f.u | -11.86 | -51.61 | -16.81 | -28.27 | 41.75 |
| E_g (eV) at G (0,0,0) | 2.76 | 2.81 | 2.77 | 3.15 | 2.98 |

ORTHORHOMBIC-1D

6.4 APbI₃: Orthorhombic-3D Structure

Table 19: APbI₃ perovskite orthorhombic-3D crystal lattice parameters, cell volume per f.u, density, and enthalpy of formation calculated, total energy per formula unit, E_{tot} , relative stabilization energy (R.E) wrt cubic structure at PBE+D3 and 40 Å⁻¹ (experimental measurements in parentheses).

| Property | Cs | AM | MA1 | FA2 | DA |
|-------------------------------------|------------------|--------|------------------|--------|--------|
| a_0 (Å) | 8.82 (8.62) | 8.58 | 8.91 (8.84) | 8.46 | 9.63 |
| b_0 (Å) | 8.76 (8.85) | 8.61 | 8.55 (8.56) | 9.64 | 9.74 |
| c_0 (Å) | 12.66 (12.50) | 12.47 | 12.73 (12.59) | 12.73 | 15.13 |
| α (°) | 90.00 | 90.00 | 90.00 | 90.00 | 90.00 |
| β (°) | 90.00 | 90.00 | 90.00 | 90.00 | 90.00 |
| γ (°) | 90.00 | 90.00 | 90.00 | 90.00 | 90.00 |
| V (Å ³ /f.u) | 244.66 | 230.16 | 242.25 | 259.68 | 354.71 |
| Density (g cm ⁻³) | 4.89 (5.02) | 4.37 | 4.25 (4.32) | 4.05 | 3.28 |
| Api. Oh rot. Pb-Pb-I (°) | 8.97 | 14.31 | 10.14 | 2.15 | 5.63 |
| Equi. Oh rot. Pb-Pb-I (°) | 13.05 | 18.97 | 16.53 | 4.61 | 10.29 |
| Equi1 Pb-I-Pb (°) | 153.85 | 142.05 | 146.97 | 170.84 | 161.89 |
| Equi2 Pb-I-Pb (°) | 153.85 | 142.05 | 146.97 | 166.70 | 164.75 |
| Api. Pb-I-Pb (°) | 162.06 | 151.37 | 159.71 | 175.70 | 165.79 |
| Oh torsion angle (°) | 11.42 | 15.91 | 12.30 | 0.00 | 121.28 |
| Pb(1) I ₆ | 43.47 | 44.23 | 44.37 | 43.28 | 57.59 |
| ECN^{Pb1} | 6.00 | 6.00 | 6.00 | 5.97 | 3.19 |
| QE1 | 1.0006 | 1.0006 | 1.0043 | 1.0132 | 1.0525 |
| BAV1 (° ²) | 1.99 | 2.17 | 15.70 | 45.15 | 82.95 |
| E_{coh} per atom (eV) | -2.82 | -2.99 | -3.31 | -4.07 | -4.01 |
| ΔH (kJ/mol) | -241.50 | -0.02 | -3.63 | 8.42 | 28.02 |
| R.E (kJ mol ⁻¹) per f.u | -4.16 | -44.02 | -15.22 | -15.75 | 26.23 |
| E_g (eV) at G | 1.63 | 1.87 | 1.76 | 1.67 | 2.07 |

ORTHORHOMBIC-3D

7 $APbI_3$: Octahedral Volume Changes

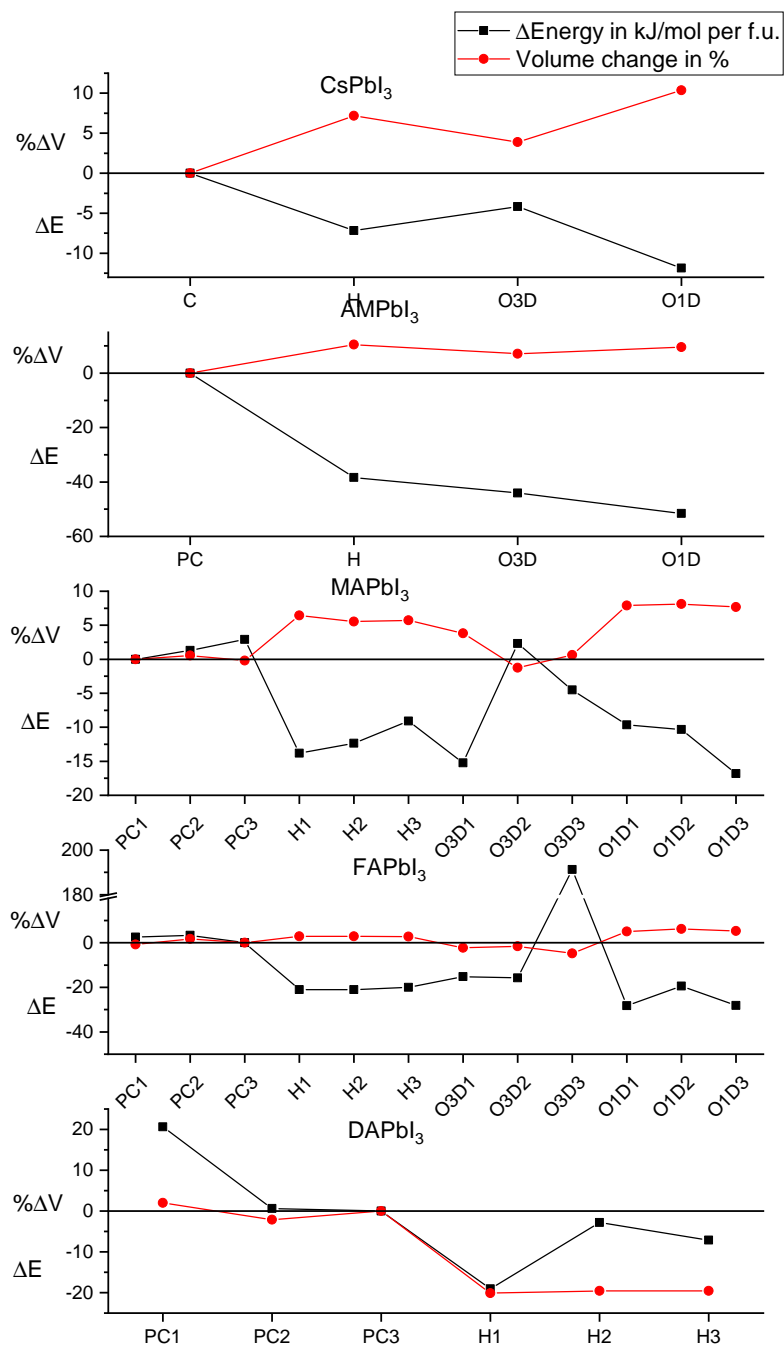


Figure 5: Percentage of change in octahedral volumes among different polytypes of $APbI_3$, PbI_6 volume of cubic/pseudo-cubic structure taken as reference

8 Perovskites Optical Properties

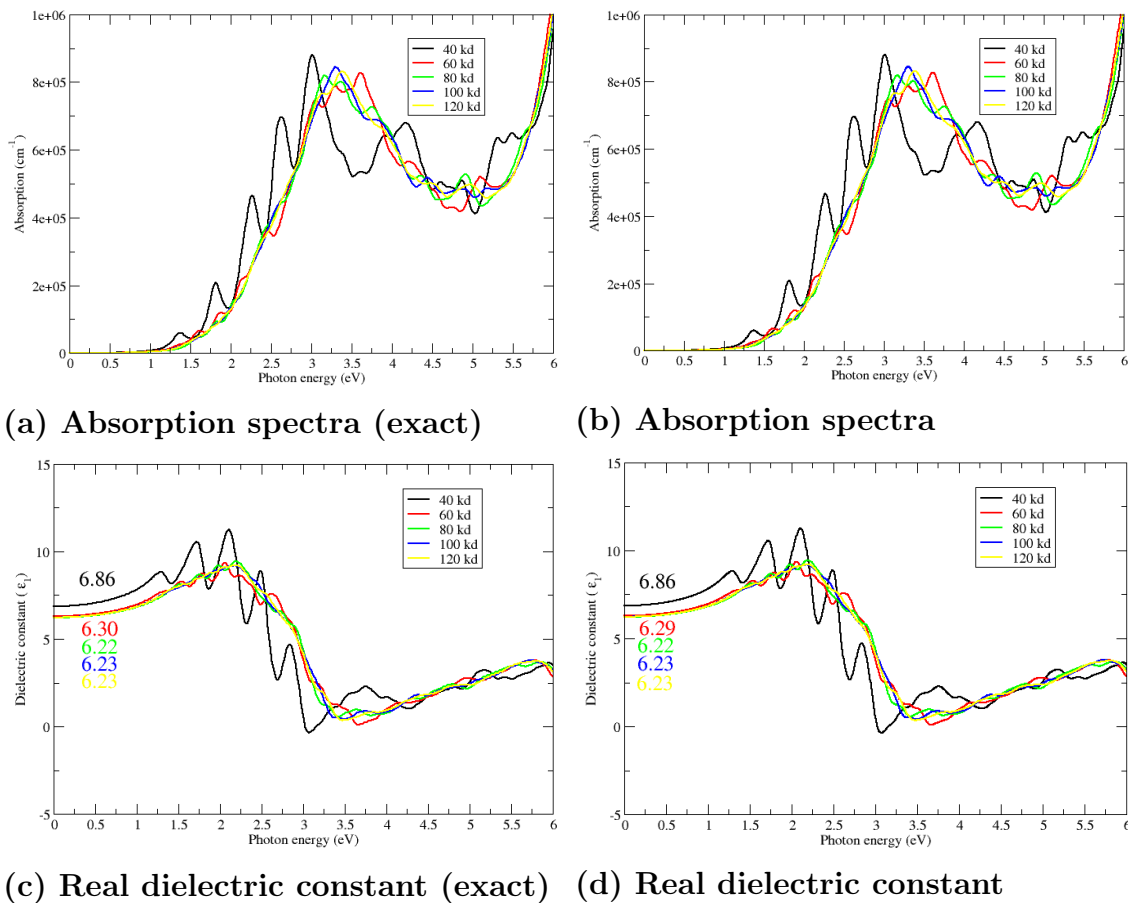


Figure 6: Computational study of the convergence of the dielectric functions as a function of the number of k-points for the cubic CsPbI_3 structure: (a) absorption spectra using a CSHIFT of 0.1 eV (ALGO = Exact, NELM = 1), (b) Absorption spectra using a CSHIFT of 0.1 eV (ALGO = Normal), c) real dielectric constant (ALGO = Exact, NELM = 1), d) real dielectric constant (ALGO = Normal).

Table 20: Energy gap (in eV), transition type and transition amplitude (a.u.) at high symmetrical k-points of cubic/PC APbI₃ compounds

| C/PC | Band | Energy | Type | Amplitude | k-point |
|------|-------|--------|-------|-----------|------------------|
| Cs | 23-24 | 1.36 | (1,1) | 20.78 | (0.50,0.50,0.50) |
| | 23-24 | 1.36 | (2,2) | 20.81 | (0.50,0.50,0.50) |
| | 23-24 | 1.36 | (3,3) | 3.94 | (0.50,0.50,0.50) |
| | 23-24 | 1.36 | (1,3) | -9.05 | (0.50,0.50,0.50) |
| | 23-24 | 1.40 | (2,2) | 43.92 | (0.47,0.50,0.47) |
| AM | 23-24 | 2.02 | (1,1) | 5.64 | (0.50,0.50,0.50) |
| | 23-24 | 2.02 | (2,2) | 5.97 | (0.50,0.50,0.50) |
| | 23-24 | 2.02 | (3,3) | 5.94 | (0.50,0.50,0.50) |
| MA1 | 26-27 | 1.63 | (1,1) | 0.00 | (0.50,0.50,0.50) |
| | 26-27 | 1.63 | (2,2) | 14.21 | (0.50,0.50,0.50) |
| | 26-27 | 1.63 | (3,3) | 7.67 | (0.50,0.50,0.50) |
| FA1 | 28-29 | 1.42 | (1,1) | 0.00 | (0.50,0.50,0.50) |
| | 28-29 | 1.42 | (2,2) | 0.00 | (0.50,0.50,0.50) |
| | 28-29 | 1.42 | (3,3) | 20.91 | (0.50,0.50,0.50) |
| FA3 | 28-29 | 1.64 | (1,1) | 7.74 | (0.47,0.47,0.47) |
| | 28-29 | 1.64 | (1,1) | 7.59 | (0.50,0.50,0.50) |
| DA3 | 42-43 | 2.18 | (1,1) | 0.02 | (0.50,0.50,0.50) |
| | 42-43 | 2.18 | (2,2) | 0.02 | (0.50,0.50,0.50) |
| | 42-43 | 2.18 | (2,2) | 0.01 | (0.50,0.50,0.50) |
| | 42-43 | 2.31 | (3,3) | 0.19 | (0.50,0.50,0.00) |

Table 21: Energy gap (in eV), transition type and transition amplitude (a.u.) at high symmetrical k-points of orthorhombic-3D APbI₃ compounds

| O3D | Band | Energy | Type | Amplitude | k-point |
|-----|---------|--------|-------|-----------|------------------|
| Cs | 92-93 | 1.63 | (1,1) | 0.00 | (0.00,0.00,0.00) |
| | 92-93 | 1.63 | (2,2) | 0.00 | (0.00,0.00,0.00) |
| | 92-93 | 1.63 | (3,3) | 6.88 | (0.00,0.00,0.00) |
| AM | 92-93 | 1.87 | (1,1) | 0.00 | (0.00,0.00,0.00) |
| | 92-93 | 1.87 | (2,2) | 4.08 | (0.00,0.00,0.00) |
| | 92-93 | 1.87 | (3,3) | 0.00 | (0.00,0.00,0.00) |
| MA1 | 104-105 | 1.76 | (1,1) | 0.00 | (0.00,0.00,0.00) |
| | 104-105 | 1.76 | (2,2) | 5.12 | (0.00,0.00,0.00) |
| | 104-105 | 1.76 | (3,3) | 0.00 | (0.00,0.00,0.00) |
| FA2 | 112-113 | 1.67 | (1,1) | 0.00 | (0.00,0.00,0.00) |
| | 112-113 | 1.67 | (2,2) | 7.96 | (0.00,0.00,0.00) |
| | 112-112 | 1.67 | (3,3) | 0.01 | (0.00,0.00,0.00) |
| DA | 168-169 | 2.18 | (1,1) | 0.00 | (0.00,0.00,0.00) |
| | 168-169 | 2.18 | (2,2) | 0.00 | (0.00,0.00,0.00) |
| | 168-169 | 2.18 | (3,3) | 0.00 | (0.00,0.00,0.00) |
| | 168-169 | 2.38 | (2,2) | 0.01 | (0.50,0.50,0.00) |

Table 22: Energy gap (in eV), transition type and transition amplitude (a.u.) at high symmetrical k-points of orthorhombic-1D APbI₃ compounds

| O1D | Band | Energy | Type | Amplitude | k-point |
|-----|---------|--------|-------|-----------|------------------|
| Cs | 92-93 | 2.56 | (1,1) | 0.00 | (0.39,0.00,0.00) |
| | 92-93 | 2.56 | (2,2) | 0.00 | (0.39,0.00,0.00) |
| | 92-93 | 2.56 | (3,3) | 0.21 | (0.39,0.00,0.00) |
| AM | 92-93 | 2.43 | (1,1) | 0.00 | (0.42,0.00 0.00) |
| | 92-93 | 2.43 | (2,2) | 0.00 | (0.0,0.00,0.00) |
| | 92-93 | 2.43 | (3,3) | 0.29 | (0.00,0.00,0.00) |
| MA1 | 104-105 | 2.45 | (1,1) | 0.00 | (0.50,0.00,0.00) |
| | 104-105 | 2.45 | (2,2) | 0.00 | (0.50,0.00,0.00) |
| | 104-105 | 2.45 | (3,3) | 0.00 | (0.50,0.00,0.00) |
| | 104-105 | 2.46 | (1,1) | 0.03 | (0.50,0.00,0.50) |
| FA2 | 112-113 | 2.89 | (1,1) | 0.00 | (0.42,0.00,0.00) |
| | 112-113 | 2.89 | (2,2) | 0.01 | (0.42,0.00,0.00) |
| | 112-112 | 2.89 | (3,3) | 0.22 | (0.42,0.00,0.00) |
| DA | 168-169 | 2.67 | (1,1) | 0.01 | (0.00,0.34,0.00) |
| | 168-169 | 2.67 | (2,2) | 0.01 | (0.00,0.34,0.00) |
| | 168-169 | 2.67 | (3,3) | 0.00 | (0.00,0.34,0.00) |

Table 23: Energy gap (in eV), transition type and transition amplitude (a.u.) at high symmetrical k-points of hexagonal APbI₃ compounds

| H | Band | Energy | Type | Amplitude | k-point |
|-----|-------|--------|-------|-----------|------------------|
| Cs | 46-47 | 2.53 | (1,1) | 0.00 | (0.00,0.00,0.00) |
| | 46-47 | 2.53 | (2,2) | 0.00 | (0.00,0.00,0.00) |
| | 46-47 | 2.53 | (3,3) | 0.00 | (0.00,0.00,0.00) |
| | 46-47 | 2.60 | (1,1) | 0.92 | (0.50,0.00,0.00) |
| AM | 46-47 | 3.07 | (1,1) | 0.25 | (0.50,0.00,0.00) |
| | 46-47 | 3.07 | (2,2) | 0.04 | (0.50,0.00,0.00) |
| | 46-47 | 3.07 | (3,3) | 0.01 | (0.50,0.00,0.00) |
| MA1 | 52-53 | 2.99 | (1,1) | 0.21 | (0.00,0.00,0.00) |
| | 52-53 | 2.99 | (2,2) | 1.14 | (0.00,0.00,0.00) |
| | 52-53 | 2.99 | (3,3) | 0.02 | (0.00,0.00,0.00) |
| FA1 | 56-57 | 2.99 | (1,1) | 0.11 | (0.00,0.00,0.00) |
| | 56-57 | 2.99 | (2,2) | 0.00 | (0.00,0.00,0.00) |
| | 56-57 | 2.99 | (3,3) | 0.00 | (0.00,0.00,0.00) |
| DA1 | 84-85 | 2.55 | (1,1) | 0.00 | (0.00,0.00,0.05) |
| | 84-85 | 2.55 | (2,2) | 0.00 | (0.00,0.00,0.05) |
| | 84-85 | 2.55 | (3,3) | 0.00 | (0.00,0.00,0.05) |
| | 84-85 | 2.56 | (3,3) | 0.01 | (0.00,0.00,0.13) |

Table 24: Formation enthalpies (in eV) of CsPbI₃ polymorphs and pseudo-cubic MAPbI₃ unit-cell. (Note: Enthalpies of PBE+SOC functional calculated by doing single point energies on PBE optimized geometries of CsI, PbI₂ and CsPbI₃)

| CsPbI ₃ | PBE | PBE+SOC | PBE+D3 |
|--------------------|-------|---------|--------|
| Cubic | 0.01 | -0.02 | -0.10 |
| O3D | -0.11 | -0.13 | -0.15 |
| O1D | -0.16 | -0.17 | -0.23 |
| H | -0.07 | -0.08 | -0.18 |
| MAPbI ₃ | PBE | PBE+SOC | PBE+D3 |
| PC | 0.04 | 0.01 | 0.12 |

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