

Supplemental Information:

On the impact of large-amplitude mode truncation in anharmonic frequency calculations

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1 Computational details

Harmonic frequency calculations have been performed with CFOUR version 1^[1] and MOLPRO version 2018.1^[2, 3]. Prior to each harmonic or anharmonic frequency calculation, the geometry was optimised. Symmetry was enabled in all calculations, except for the MOLPRO calculations on CH₃OH and NH₂OH. Anharmonic quartic force fields were computed from analytic Hessians, using PyPES with default settings. Masses of the following isotopes were used: ¹H, ²H≡D, ¹¹B, ¹²C, ¹⁴N, ¹⁶O, ¹⁹F, ²⁷Al, ²⁸Si, ³¹P, ³²S, ¹²¹Sb and ²⁰⁹Bi. Keyword specifications used in each calculation are listed below:

Type of calculation	Program	Keywords
CCSD(T) Hessian	CFOUR	FROZEN_CORE=ON SCF_CONV=9 CC_CONV=9 CC_PROGRAM=ECC ABCDTYPE=AOBASIS LINEQ_CONV=9 GEO_CONV=9 GEO_METHOD=NR VIB=EXACT
CCSD(T)-F12 Hessian	MOLPRO	{GThresh,OptStep=6.d-5,OptGrad=1.d-8,Energy=1.d-10,Zero=1.d-16} {Optg,Gaussian,GRMS=1.d-7,SRMS=1.d-7} {Mass,Iso} {Frequencies}
Anharmonic force field	PyPES	CFOUR_ZMAT ZMAT, DO_NUM_DIFF_NM True, DLVL_CART 4, FF_NM_TO_CNM (4)->(4), FF_CNM_TO_NM (4)->(6), SAVE_FF_NM True
VCI	PyVCI	DLVL 6, EXC_LVL 10 (or 9)

2 Fundamental wavenumbers

2.1 Computation of low-resolution band centres for NH₃, H₂O₂/D₂O₂ and CH₃OH

Due to the symmetric double-well potentials of the ammonia inversion / hydrogen peroxide torsion, the vibrational energy levels are split into two levels, labelled according to their parity as + and -. The low-resolution band centre of vibration *i* is computed as

$$\begin{aligned} 2\bar{\nu}_i &= (W_i^+ - W_{\text{g.s.}}^-) + W_i^- \\ &= (E_i^+ - E_{\text{g.s.}}^-) + (E_i^- - E_{\text{g.s.}}^+), \end{aligned} \quad (1)$$

where *W* is the term value relative to the vibrational ground state, whereas *E* includes zero-point energy. For methanol, the three-fold torsional degeneracy results in one *A* and two *E* levels. Here, the low-resolution band centre is computed as

$$\begin{aligned} 3\bar{\nu}_i &= 2\nu_i(E) + \nu_i(A) \\ &= 2W_i(E) - 2W_{\text{g.s.}}(E) + W_i(A) \\ &= 2E_i(E) - 2E_{\text{g.s.}}(E) + E_i(A) - E_{\text{g.s.}}(A). \end{aligned} \quad (2)$$

2.2 Part I – Tetratomics

Table S1: Fundamental wavenumbers for all 24 tetratomic molecules in our benchmarking set. Computational (ν_{lit}) and, when available, high-resolution gas phase (ν_{expt}) literature data (references in brackets), and in this work computed VCI(10) fundamentals ($\nu^{(10)}$) and their respective convergence errors (δ_{cvge}) are shown in cm^{-1} . Low-resolution band centres are shown for NH_3 and $\text{H}_2\text{O}_2/\text{D}_2\text{O}_2$ (see footnotes).

	Fundamental	ν_{expt}	ν_{lit}	$\nu^{(10)}$					$\delta_{\text{cvge}} = \nu^{(10)} - \nu^{(9)}$			
				ν_{ref}	$\tilde{\nu}_{\text{harm}}$	ν_{drop}	$\tilde{\nu}_{\text{drop}}$	ν_{ref}	$\tilde{\nu}_{\text{harm}}$	ν_{drop}	$\tilde{\nu}_{\text{drop}}$	
Group (A)												
NH_3^a	$\nu_1 A_1$ s str	3336.2 [4]	3342.5 [5]	3344.7	3337.3	3347.6	3353.4	-5.6	1.3	0.0	0.0	
	$\nu_2 A_1$ inversion	949.9 [6]	951.2 [5]	951.9	992.7			-0.5	-0.4			
	$\nu_3 E$ a str	3443.4 [7]	3449.0 [5]	3453.1	3450.2	3462.3	3462.0	0.0	-0.1	0.0	0.0	
	$\nu_3 E$ a str	3443.4 [7]	3449.0 [5]	3453.1	3450.2	3462.3	3462.0	0.0	-0.1	0.0	0.0	
	$\nu_4 E$ bend	1626.4 [8]	1628.7 [5]	1629.2	1624.3	1630.4	1631.6	0.0	0.0	0.0	0.0	
	$\nu_4 E$ bend	1626.4 [8]	1628.7 [5]	1629.2	1624.3	1630.4	1631.6	0.0	0.0	0.0	0.0	
PH_3	$\nu_1 A_1$ s str	2321.1 [9]	2321.0 [10]	2323.1	2324.1	2325.9	2325.7	0.0	0.0	0.0	0.0	
	$\nu_2 A_1$ inversion	992.1 [11]	991.9 [10]	991.8	998.2			0.0	0.0			
	$\nu_3 E$ a str	2326.9 [9]	2325.8 [10]	2327.8	2330.8	2332.8	2332.3	0.0	0.0	0.0	0.0	
	$\nu_3 E$ a str	2326.9 [9]	2325.8 [10]	2327.8	2330.8	2332.8	2332.3	0.0	0.0	0.0	0.0	
	$\nu_4 E$ bend	1118.3 [11]	1118.9 [10]	1119.7	1120.2	1119.9	1119.6	0.0	0.0	0.0	0.0	
	$\nu_4 E$ bend	1118.3 [11]	1118.9 [10]	1119.7	1120.2	1119.9	1119.6	0.0	0.0	0.0	0.0	
SbH_3	$\nu_1 A_1$ s str	1890.5 [12]	1893.8 [13]	1894.2	1896.0	1897.5	1897.3	0.0	0.0	0.0	0.0	
	$\nu_2 A_1$ inversion	782.2 [12]	798.9 [13]	798.4	803.0			0.0	0.0			
	$\nu_3 E$ a str	1894.5 [12]	1899.1 [13]	1899.8	1901.9	1903.5	1903.1	0.0	0.0	0.0	0.0	
	$\nu_3 E$ a str	1894.5 [12]	1899.1 [13]	1899.8	1901.9	1903.5	1903.1	0.0	0.0	0.0	0.0	
	$\nu_4 E$ bend	827.9 [12]	836.8 [13]	836.8	837.4	836.5	836.1	0.0	0.0	0.0	0.0	
	$\nu_4 E$ bend	827.9 [12]	836.8 [13]	836.8	837.4	836.5	836.1	0.0	0.0	0.0	0.0	
BiH_3	$\nu_1 A_1$ s str	1733.3 [14]	1742.4 [13]	1742.7	1745.6	1746.7	1746.6	0.0	0.0	0.0	0.0	
	$\nu_2 A_1$ inversion	726.7 [14]	733.9 [13]	733.4	738.3			0.0	0.0			
	$\nu_3 E$ a str	1734.5 [14]	1746.3 [13]	1746.7	1749.2	1750.5	1750.1	0.0	0.0	0.0	0.0	
	$\nu_3 E$ a str	1734.5 [14]	1746.3 [13]	1746.7	1749.2	1750.5	1750.1	0.0	0.0	0.0	0.0	
	$\nu_4 E$ bend	751.2 [14]	759.5 [13]	759.3	760.3	759.1	758.7	0.0	0.0	0.0	0.0	
	$\nu_4 E$ bend	751.2 [14]	759.5 [13]	759.3	760.3	759.1	758.7	0.0	0.0	0.0	0.0	
SiH_3^-	$\nu_1 A_1$ s str		1840.7 [15]	1840.4	1838.1	1839.1	1838.5	0.0	0.0	0.0	0.0	
	$\nu_2 A_1$ inversion		844.1 [15]	844.2	844.4			0.0	0.0			
	$\nu_3 E$ a str		1821.5 [15]	1824.5	1828.8	1828.9	1828.1	0.0	0.0	0.0	0.0	
	$\nu_3 E$ a str		1821.5 [15]	1824.5	1828.8	1828.9	1828.1	0.0	0.0	0.0	0.0	
	$\nu_4 E$ bend		937.8 [15]	941.0	939.6	940.1	939.8	0.0	0.0	0.0	0.0	
	$\nu_4 E$ bend		937.8 [15]	941.0	939.6	940.1	939.8	0.0	0.0	0.0	0.0	

^a Low-resolution experimental and computational literature band centres are computed according to Eq. 1. Pairs of (W_i^+, W_i^-) are listed in cm^{-1} :

Expt:

$W_{\text{g.s.}} = (0, 0.79)$,^[6] $W_1 = (3336.11, 3337.10)$, $W_2 = (932.43, 968.12)$, $W_3 = (3443.68, 3443.99)$ and $W_4 = (1626.28, 1627.37)$.

Lit:

$W_{\text{g.s.}} = (0, 0.8)$,^[5] $W_1 = (3342.4, 3343.3)$, $W_2 = (933.8, 969.5)$, $W_3 = (3449.2, 3449.6)$ and $W_4 = (1628.6, 1629.7)$.

Table S1: *Continued.*

	Fundamental	ν_{expt}	ν_{lit}	$\nu^{(10)}$				$\delta_{\text{cvge}} = \nu^{(10)} - \nu^{(9)}$			
				ν_{ref}	$\tilde{\nu}_{\text{harm}}$	ν_{drop}	$\tilde{\nu}_{\text{drop}}$	ν_{ref}	$\tilde{\nu}_{\text{harm}}$	ν_{drop}	$\tilde{\nu}_{\text{drop}}$
Group (B)											
BF_3	$\nu_1 A'_1$ s str		887.6 [16]	887.9	886.8	889.7	889.7	0.0	0.0	0.0	0.0
	$\nu_2 A''_2$ oop	691.2 [17]	696.2 [16]	696.2	693.7			0.0	0.0		
	$\nu_3 E'$ a str	1454.0 [18]	1469.6 [16]	1470.3	1472.0	1472.8	1472.8	0.0	0.0	0.0	0.0
	$\nu_3 E'$ a str	1454.0 [18]	1469.6 [16]	1470.2	1472.6	1472.8	1472.8	0.0	0.0	0.0	0.0
	$\nu_4 E'$ bend	479.4 [19]	480.6 [16]	480.9	479.4	480.4	480.4	0.0	0.0	0.0	0.0
	$\nu_4 E'$ bend	479.4 [19]	480.6 [16]	480.9	479.1	480.4	480.4	0.0	0.0	0.0	0.0
CF_3^+	$\nu_1 A'_1$ s str		1044.5 [16]	1044.8	1043.5	1046.5	1046.5	0.0	0.0	0.0	0.0
	$\nu_2 A''_2$ oop		812.6 [16]	812.7	812.4			0.0	0.0		
	$\nu_3 E'$ a str		1682.8 [16]	1683.5	1685.7	1686.9	1686.9	0.0	0.0	0.0	0.0
	$\nu_3 E'$ a str		1682.8 [16]	1683.5	1687.8	1686.9	1686.9	0.0	0.0	0.0	0.0
	$\nu_4 E'$ bend		592.6 [16]	593.0	591.5	592.7	592.7	0.0	0.0	0.0	0.0
	$\nu_4 E'$ bend		592.6 [16]	593.0	591.2	592.7	592.7	0.0	0.0	0.0	0.0
AlF_3	$\nu_1 A'_1$ s str		689.5 [20]	689.0	689.7	686.4	686.4	0.0	0.0	0.0	0.0
	$\nu_2 A''_2$ oop		301.1 [20]	301.3	300.2			0.0	0.0		
	$\nu_3 E'$ a str		951.8 [20]	951.2	951.6	951.6	951.6	0.0	0.0	0.0	0.0
	$\nu_3 E'$ a str		951.8 [20]	951.2	951.2	951.6	951.6	0.0	0.0	0.0	0.0
	$\nu_4 E'$ bend		241.4 [20]	241.4	240.8	241.1	241.1	0.0	0.0	0.0	0.0
	$\nu_4 E'$ bend		241.4 [20]	241.4	240.7	241.1	241.1	0.0	0.0	0.0	0.0
SiF_3^+	$\nu_1 A'_1$ s str		853.3 [20]	852.8	853.8	850.9	850.9	0.0	0.0	0.0	0.0
	$\nu_2 A''_2$ oop		356.7 [20]	356.8	356.1			0.0	0.0		
	$\nu_3 E'$ a str		1187.9 [20]	1187.2	1187.8	1188.0	1188.0	0.0	0.0	0.0	0.0
	$\nu_3 E'$ a str		1187.9 [20]	1187.2	1187.4	1188.0	1188.0	0.0	0.0	0.0	0.0
	$\nu_4 E'$ bend		307.2 [20]	307.2	306.5	307.0	307.0	0.0	0.0	0.0	0.0
	$\nu_4 E'$ bend		307.2 [20]	307.2	306.5	307.0	307.0	0.0	0.0	0.0	0.0
SO_3	$\nu_1 A'_1$ s str		1067.0 [21]	1066.9	1071.7	1066.5	1066.5	0.0	0.0	0.0	0.0
	$\nu_2 A''_2$ oop	497.6 [22]	498.6 [21]	496.4	500.4			0.0	0.0		
	$\nu_3 E'$ a str	1391.5 [23]	1396.3 [21]	1396.3	1397.6	1398.5	1398.5	0.0	0.0	0.0	0.0
	$\nu_3 E'$ a str	1391.5 [23]	1396.3 [21]	1396.3	1398.2	1398.5	1398.5	0.0	0.0	0.0	0.0
	$\nu_4 E'$ bend	530.1 [22]	528.1 [21]	528.3	527.2	528.0	528.0	0.0	0.0	0.0	0.0
	$\nu_4 E'$ bend	530.1 [22]	528.1 [21]	528.3	527.3	528.0	528.0	0.0	0.0	0.0	0.0
H_2CO	$\nu_1 A_1$ CH_2 s str	2782.5 [24]	2781.7 [25]	2784.1	2782.0	2788.2	2788.2	0.0	0.0	0.0	0.0
	$\nu_2 A_1$ CO str	1746.0 [26]	1744.6 [25]	1744.9	1748.5	1748.5	1748.5	0.0	0.0	0.0	0.0
	$\nu_3 A_1$ CH_2 bend	1500.2 [26]	1499.1 [25]	1499.3	1491.3	1499.9	1499.9	0.0	0.0	0.0	0.0
	$\nu_4 B_1$ oop	1167.3 [26]	1166.1 [25]	1166.1	1149.0			0.0	0.0		
	$\nu_5 B_2$ CH_2 a str	2843.3 [24]	2842.4 [25]	2845.0	2847.0	2851.8	2851.8	0.0	0.0	0.0	0.0
	$\nu_6 B_2$ CH_2 rock	1249.1 [26]	1245.6 [25]	1245.5	1237.4	1242.2	1242.2	0.0	0.0	0.0	0.0
H_2SiO	$\nu_1 A_1$ SiH_2 s str		2171.0 [27]	2171.4	2171.2	2174.7	2174.7	0.0	0.0	0.0	0.0
	$\nu_2 A_1$ SiO str		1206.9 [27]	1207.1	1209.0	1209.0	1209.0	0.0	0.0	0.0	0.0
	$\nu_3 A_1$ SiH_2 bend		994.3 [27]	994.6	991.2	995.0	995.0	0.0	0.0	0.0	0.0
	$\nu_4 B_1$ oop		690.9 [27]	690.6	684.9			0.0	0.0		
	$\nu_5 B_2$ SiH_2 a str		2191.3 [27]	2192.1	2194.2	2196.4	2196.4	0.0	0.0	0.0	0.0
	$\nu_6 B_2$ SiH_2 rock		680.1 [27]	680.1	676.8	678.3	678.3	0.0	0.0	0.0	0.0

Table S1: *Continued.*

	Fundamental	ν_{expt}	ν_{lit}	$\nu^{(10)}$				$\delta_{\text{cvge}} = \nu^{(10)} - \nu^{(9)}$			
				ν_{ref}	$\tilde{\nu}_{\text{harm}}$	ν_{drop}	$\tilde{\nu}_{\text{drop}}$	ν_{ref}	$\tilde{\nu}_{\text{harm}}$	ν_{drop}	$\tilde{\nu}_{\text{drop}}$
Group (C)											
HOOH ^b	ν_1 A OH s str	3608.2 [28]	3609.1 [29]	3593.0	3590.2	3607.3	3607.3	-2.8	-14.7	-0.1	-0.1
	ν_2 A s bend	1391.4 [30]	1392.4 [29]	1393.7	1388.4	1385.1	1385.1	0.3	0.0	0.0	0.0
	ν_3 A OO str	866.2 [31]	866.3 [29]	868.3	867.2	867.0	867.0	-0.4	0.4	0.0	0.0
	ν_4 A torsion	307.0 [32]	307.7 [29]	367.8	408.1			-13.4	-0.1		
	ν_5 B OH a str	3609.0 [33]	3610.3 [29]	3602.8	3602.9	3608.9	3608.9	0.4	-0.4	0.0	0.0
	ν_6 B a bend	1269.2 [30]	1269.1 [29]	1279.6	1287.6	1281.6	1281.6	-1.0	-0.1	0.0	0.0
DOOD ^c	ν_1 A OD s str		2667.2 [29]	2665.0	2663.2	2666.3	2666.3	-2.3	-0.6	0.0	0.0
	ν_2 A s bend		1026.2 [29]	1026.0	1023.5	1023.0	1023.0	-0.1	-0.4	0.0	0.0
	ν_3 A OO str		869.3 [29]	870.2	870.0	869.7	869.7	-0.2	-0.1	0.0	0.0
	ν_4 A torsion	229.1 [34]	230.1 [29]	267.7	288.1			-1.5	-0.8		
	ν_5 B a str		2666.6 [29]	2663.8	2664.3	2665.6	2665.6	-0.4	-0.4	-0.1	-0.1
	ν_6 B OD a bend		945.4 [29]	950.5	957.5	955.0	954.9	-0.3	-0.1	0.0	0.0
HSOH	ν_1 A OH str	3625.6 [35]	3625.9 [36]	3615.7	3618.4	3633.3	3633.3	-2.6	-1.9	0.0	0.0
	ν_2 A SH str	2538.0 ^d [37]	2544.4 [36]	2548.0	2545.8	2546.1	2546.1	-1.4	-0.9	0.0	0.0
	ν_3 A SOH bend		1174.0 [36]	1184.0	1188.7	1178.5	1178.5	-0.5	-0.3	0.0	0.0
	ν_4 A OSH bend		1007.7 [36]	1016.3	1007.8	1007.0	1007.0	21.5	-0.5	0.0	0.0
	ν_5 A SO str		760.0 [36]	761.0	763.6	763.4	763.4	-0.7	-0.4	0.0	0.0
	ν_6 A torsion		443.0 [36]	480.3	506.4			-1.0	-0.4		

^{b,c} Low-resolution band centres for HOOH and DOOD computed from tunnelling split energy levels (see footnote ^a):

Expt (HOOH):

$W_{\text{g.s.}} = (0, 11.44)$,^[32] $W_1 = (3609.8, 3617.95)$, $W_2 = (1395.88, 1398.32)$, $W_3 = (865.94, 877.93)$, $W_4 = (254.55, 370.89)$, $W_5 = (3610.66, 3618.84)$, $W_6 = (1264.58, 1285.12)$.

Lit (HOOH):

$W_{\text{g.s.}} = (0, 11.3)$,^[29] $W_1 = (3610.6, 3618.8)$, $W_2 = (1394.9, 1401.1)$, $W_3 = (866.0, 877.8)$, $W_4 = (255.4, 371.3)$, $W_5 = (3611.8, 3620.0)$, $W_6 = (1264.5, 1285.0)$.

Expt (DOOD):

$W_{\text{g.s.}} = (0, 1.93)$,^[34] and $W_4 = (208.87, 251.26)$.

Lit (DOOD):

$W_{\text{g.s.}} = (0, 1.9)$,^[29] and $W_4 = (210.1, 251.9)$.

^d Beckers *et al.* report a low-resolution value of 2538,^[38] which is corroborated by the high-resolution value 2537.9869(12)^[36] from the dissertation^[37] of O. Baum.

Table S1: *Continued.*

	Fundamental	ν_{expt}	ν_{lit}	$\nu^{(10)}$				$\delta_{\text{cvge}} = \nu^{(10)} - \nu^{(9)}$				
				ν_{ref}	$\tilde{\nu}_{\text{harm}}$	ν_{drop}	$\tilde{\nu}_{\text{drop}}$	ν_{ref}	$\tilde{\nu}_{\text{harm}}$	ν_{drop}	$\tilde{\nu}_{\text{drop}}$	
Group (D)												
<i>t</i> -HNNH	$\nu_1 A_g$ NH s str		3033.3 [39]	3036.5	3042.6	3044.3	3044.3	-0.1	-0.1	-0.1	-0.1	
	$\nu_2 A_g$ NH s bend		1579.4 [39]	1579.7	1584.8	1582.0	1582.0	0.0	0.0	0.0	0.0	
	$\nu_3 A_g$ NN str		1519.3 [39]	1519.3	1524.3	1524.1	1524.1	0.0	0.0	0.0	0.0	
	$\nu_4 A_u$ torsion		1288.6 [40]	1294.2 [39]	1294.2	1318.5		0.0	0.0			
	$\nu_5 B_u$ NH a str		3120.3 [40]	3125.0 [39]	3114.8	3117.8	3123.8	3123.8	-0.1	-0.1	-0.1	
	$\nu_6 B_u$ NH a bend		1316.4 [40]	1317.5 [39]	1317.9	1323.1	1316.0	1316.0	0.0	0.0	0.0	
<i>c</i> -HSiOH ^e	$\nu_1 A'$ OH str		3676.2 [41]	3662.0	3666.4	3681.9	3681.9	-2.7	-3.0	-0.1	-0.1	
	$\nu_2 A'$ SiH str		1891.0 [41]	1872.6	1878.5	1870.5	1870.5	0.9	2.0	-0.3	-0.3	
	$\nu_3 A'$ a bend		939.0 [41]	948.1	954.4	946.1	946.1	-0.7	-2.6	-0.2	-0.2	
	$\nu_4 A'$ SiO str		841.1 [41]	841.6	842.4	842.7	842.7	-0.3	-0.2	-0.1	-0.1	
	$\nu_5 A'$ s bend		727.0 [41]	745.5	754.7	738.3	738.3	-2.2	0.1	-0.1	-0.1	
	$\nu_6 A''$ torsion		599.6 [41]	626.7	652.2			-0.5	-1.5			
<i>t</i> -HSiOH	$\nu_1 A'$ OH str		3673.1 [41]	3665.9	3663.6	3678.0	3678.0	14.8	-0.3	0.0	0.0	
	$\nu_2 A'$ SiH str		1950.0 [41]	1951.3	1954.3	1955.0	1955.0	-0.3	-0.2	-0.1	-0.1	
	$\nu_3 A'$ s bend		929.9 [41]	940.4	952.9	941.3	941.3	0.1	-0.5	-0.3	-0.3	
	$\nu_4 A'$ SiO str		836.9 [41]	837.6	839.3	839.1	839.1	-0.3	-0.2	-0.1	-0.1	
	$\nu_5 A'$ a bend		788.4 [41]	797.7	801.8	792.5	792.5	-0.6	-0.4	-0.3	-0.3	
	$\nu_6 A''$ torsion		632.7 [41]	652.4	687.1			-1.0	-0.6			
<i>c</i> -DSiOD	$\nu_1 A'$ OD str		2713.1 [41]	2711.0	2711.3	2717.0	2717.0	0.6	-0.2	0.0	0.0	
	$\nu_2 A'$ SiD str		1372.8 [41]	1375.0	1362.3	1374.8	1374.8	-0.3	-0.2	-0.1	-0.1	
	$\nu_3 A'$ SiO str		838.4 [41]	838.6	839.0	839.6	839.6	-0.1	-0.1	0.0	0.0	
	$\nu_4 A'$ a bend		718.2 [41]	721.2	725.3	720.8	720.8	-0.2	-0.2	-0.1	-0.1	
	$\nu_5 A'$ s bend		523.4 [41]	528.5	534.2	526.5	526.5	-0.3	-0.2	-0.1	-0.1	
	$\nu_6 A''$ torsion		450.2 [41]	458.6	474.5			-0.4	-0.3			
<i>t</i> -DSiOD	$\nu_1 A'$ OD str		2709.7 [41]	2707.9	2706.8	2712.6	2712.6	-0.1	-0.1	0.0	0.0	
	$\nu_2 A'$ SiD str		1423.6 [41]	1425.8	1429.5	1427.4	1427.4	-0.2	-0.2	-0.1	-0.1	
	$\nu_3 A'$ SiO str		834.7 [41]	835.0	836.3	836.2	836.2	-0.1	-0.1	0.0	0.0	
	$\nu_4 A'$ s bend		705.3 [41]	707.3	714.6	709.5	709.5	-0.2	-0.1	-0.1	-0.1	
	$\nu_5 A'$ a bend		573.4 [41]	576.2	578.9	574.1	574.1	-0.2	-0.1	-0.1	-0.1	
	$\nu_6 A''$ torsion		469.2 [41]	475.9	496.0			-0.4	-0.3			
<i>c</i> -HOCO	$\nu_1 A'$ OH str		3452.3 [42]	3442.7	3441.6	3449.4	3449.4	-1.0	3.2	-0.1	-0.1	
	$\nu_2 A'$ C=O str		1824.1 [42]	1830.1	1823.4	1823.9	1823.9	8.5	0.0	0.0	0.0	
	$\nu_3 A'$ COH bend		1280.2 [42]	1296.6	1289.3	1275.8	1275.8	-0.7	-0.3	0.0	0.0	
	$\nu_4 A'$ C–O str		1042.4 [42]	1048.2	1050.3	1049.9	1049.9	-0.2	-0.4	0.0	0.0	
	$\nu_5 A'$ OCO bend		601.2 [42]	602.9	603.2	600.0	600.0	-0.9	-0.1	0.0	0.0	
	$\nu_6 A''$ torsion		540.2 [42]	588.9	596.8			-1.0	-0.8			
<i>t</i> -HOCOf ^f	$\nu_1 A'$ OH str		3635.7 [43]	3641.0 [44]	3627.8	3632.3	3650.5	3650.5	3.5	1.8	-0.1	-0.1
	$\nu_2 A'$ C=O str		1852.6 [45]	1862.0 [44]	1861.0	1861.4	1861.6	1861.6	-0.7	-0.3	0.0	0.0
	$\nu_3 A'$ COH bend		1212.7 [44]	1224.8	1228.6	1219.5	1219.5	-0.1	-0.3	-0.1	-0.1	
	$\nu_4 A'$ C–O str		1052.0 [44]	1049.7	1054.2	1053.2	1053.2	-0.8	-0.4	0.0	0.0	
	$\nu_5 A'$ OCO bend		616.0 [44]	619.1	618.6	615.5	615.5	-0.6	-0.4	0.0	0.0	
	$\nu_6 A''$ torsion		475.4 [44]	541.6	572.2			-5.1	-2.0			
<i>c</i> -DOCO	$\nu_1 A'$ OD str		2551.6 [42]	2551.2	2547.8	2550.2	2550.2	0.0	0.0	0.0	0.0	
	$\nu_2 A'$ C=O str		1827.5 [42]	1826.7	1826.4	1827.2	1827.2	0.0	0.0	0.0	0.0	
	$\nu_3 A'$ C–O str		1123.1 [42]	1123.5	1124.9	1125.5	1125.5	0.0	0.0	0.0	0.0	
	$\nu_4 A'$ COD bend		960.9 [42]	969.9	944.1	960.1	960.1	-0.2	-0.2	0.0	0.0	
	$\nu_5 A'$ OCO bend		539.8 [42]	541.7	542.4	540.2	540.2	0.0	0.0	0.0	0.0	
	$\nu_6 A''$ torsion		446.9 [42]	471.2	478.6			-0.1	-0.1			
<i>t</i> -DOCO ^g	$\nu_1 A'$ OD str		2684.1 [46]	2685.1 [44]	2687.4	2689.8	2693.8	2693.8	-0.7	1.2	0.0	0.0
	$\nu_2 A'$ C=O str		1851.6 [45]	1859.8 [44]	1859.1	1859.5	1859.8	1859.8	-0.1	-0.2	0.0	0.0
	$\nu_3 A'$ C–O str		1086.4 [44]	1087.4	1090.3	1090.0	1090.0	-0.1	-0.1	0.0	0.0	
	$\nu_4 A'$ COD bend		902.6 [44]	905.9	910.5	906.3	906.3	-0.1	-0.1	0.0	0.0	
	$\nu_5 A'$ OCO bend		590.1 [44]	593.2	593.2	589.6	589.6	-0.1	-0.1	0.0	0.0	
	$\nu_6 A''$ torsion		368.0 [44]	401.1	422.5			-0.5	-0.4			

^e Consistent with results by Martin^[41], we observe a strong Fermi resonance between ν_2 and $2\nu_3$, where the resonant is located at 1857.9 (ν_{lit}), 1904.7 (ν_{ref}) and 1901.8 ($\nu_{\text{drop}}/\tilde{\nu}_{\text{drop}}$), indicating an inverse assignment to Ref. [41].

^f In Ref. [47] reported VCI data on the CcCRE QFF for *t*-HOCO are incorrect,^[44] instead CcCR-based values are taken from Ref. [44].

^g No CcCRE-based VCI data for *t*-DOCO are reported in the literature.

Table S2: From V_{ref} computed transition wavenumbers (cm^{-1}) and percentage wavefunction contributions P (squared VCI coefficients) from respective VCI basis functions, as a function of VCI excitation level for states that become near-degenerate with: the OSH bending fundamental of HSOH (ν_4), the OH stretching fundamental of *t*-HSiOH (ν_1), the symmetric NH stretching fundamental of NH₃ (ν_1), the terminal C=O stretching fundamental of *c*-HOCO (ν_2) and the OH torsional fundamental of HOOH (ν_4). States are automatically grouped according to their leading wavefunction coefficients. Bolded values indicate logical regroupings of states and associated transition frequencies that could plausibly be assigned as fundamentals.

	V_{ref}	VCI(8)	VCI(9)	VCI(10)		V_{ref}	VCI(8)	VCI(9)	VCI(10)	
HSOH	Fundamental	1002.3	994.8	1016.3		<i>t</i> -HSiOH	Fundamental	3666.3	3651.0	3665.9
	$P(\nu_4)$	87%	48%	52%	$P(\nu_1)$	89%	42%	57%		
	$P(2\nu_6)$	8%	39%	37%	$P(3\nu_3 + \nu_4)$	< 1%	< 1%	2%		
	Resonant	1040.4	1016.1	992.9	$P(8\nu_6)$	< 1%	21%	< 1%		
	$P(\nu_4)$	9%	40%	44%	Resonant	3675.7	3661.2			
	$P(2\nu_6)$	72%	24%	44%	$P(\nu_1)$	25%	28%			
NH ₃	Fundamental	3345.1	3344.7	3339.2		<i>c</i> -HOCO	$P(3\nu_3 + \nu_4)$	20%	13%	
	$P(\nu_1)$	69%	69%	38%	$P(8\nu_6)$	11%	< 1%			
	$P(3\nu_2)$	< 1%	< 1%	24%	Fundamental	1821.9	1821.7	1830.1		
	Resonant	3539.5	3432.3	3352.6	$P(\nu_2)$	68%	66%	59%		
	$P(\nu_1)$	< 1%	< 1%	31%	$P(\nu_5 + 2\nu_6)$	8%	9%	23%		
	$P(3\nu_2)$	52%	55%	32%	Resonant	1840.0	1837.9	1815.9		
HOOH	$P(5\nu_2)$	19%	14%	6%	$P(\nu_2)$	21%	22%	29%		
	Fundamental	382.4	381.2	367.8	$P(\nu_5 + 2\nu_6)$	41%	39%	30%		
	$P(\nu_4)$	86%	85%	67%						
	$P(\nu_1 + 8\nu_4)$			< 1% 7%						
	Resonant			428.1						
	$P(\nu_4)$			18%						
	$P(\nu_1 + 8\nu_4)$			30%						

Table S3: From \tilde{V}_{harm} computed transition wavenumbers (cm^{-1}) and percentage wavefunction contributions P (squared VCI coefficients) from respective VCI basis functions for the symmetric OH stretch of HOOH (ν_1) which becomes near-degenerate with $2\nu_2 + \nu_3$, as a function of VCI excitation level. VCI eigenstates are automatically grouped according to their leading basis state wavefunction coefficients.

	\tilde{V}_{harm}	VCI(8)	VCI(9)	VCI(10)
HOOH	Fundamental	3596.9	3604.9	3590.2
	$P(\nu_1)$	43%	53%	39%
	$P(2\nu_2 + \nu_3)$	36%	23%	38%
	Resonant	3608.9	3592.7	3600.9
	$P(\nu_1)$	42%	32%	39%
	$P(2\nu_2 + \nu_3)$	29%	45%	28%

2.3 Part II – Pentatomics and hexatomics

Table S4: Fundamental wavenumbers for methyleneimine (CH_2NH), hydroxylamine (NH_2OH) and formaldoxime (CH_2NOH). Computational anharmonic (ν_{lit}) and high-resolution gas phase (ν_{expt}) literature data (references in brackets), harmonic (ω), and computed VCI(9) fundamentals ($\nu^{(9)}$) are shown in cm^{-1} . All reported VCI(9) fundamentals are converged to within 0.1 cm^{-1} , if not stated otherwise. s and a refer to symmetric and antisymmetric combinations, respectively.

	Fundamental	ω^a		$\nu^{(9)}$			ν_{lit}^b	ν_{expt}^c
		CC	CC-F12	ν_{ref}	ν_{drop}	$\tilde{\nu}_{\text{drop}}$		
CH_2NH	$\nu_1 A'$ NH str	3435.1	3449.6	3280.7 ^d	3288.5 ^d	3288.5 ^d	3275.3 [48]	3262.6 [49]
	$\nu_2 A'$ CH_2 a str	3150.9	3156.3	3026.6	3028.0	3027.7	3029.7 [48]	3024.5 [50]
	$\nu_3 A'$ CH_2 s str	3050.5	3052.6	2912.4	2915.0	2915.2	2909.5 [48]	2914.2 [50]
	$\nu_4 A'$ CN str	1666.5	1675.7	1636.3	1638.9	1639.4	1636.6 [48]	1638.3 [51]
	$\nu_5 A'$ CH_2 scissor	1475.5	1480.6	1450.2	1451.2	1451.4	1447.8 [48]	1452.0 [52]
	$\nu_6 A'$ CNH bend	1375.1	1380.6	1347.2	1347.7	1347.0	1340.1 [48]	1344.3 [52]
	$\nu_7 A'$ CH_2 rock	1067.1	1072.7	1059.2	1058.3	1057.6	1053.6 [48]	1058.2 [53]
	$\nu_8 A''$ NH torsion	1148.7	1155.7	1128.4			1124.8 [48]	1127.0 [53]
	$\nu_9 A''$ CH_2 wag	1071.2	1078.9	1064.0	1062.0	1060.4	1059.9 [48]	1060.8 [53]
NH_2OH	$\nu_1 A'$ OH str	3826.5	3845.3		3663.0	3663.0		3649.9 [54]
	$\nu_2 A'$ NH_2 s str	3444.7	3458.5		3291.2 ^{e,f}	3303.9 ^{e,g}		3294.2 [54]
	$\nu_3 A'$ NH_2 scissor	1663.2	1669.7		1608.4	1608.2		1604.5 [54]
	$\nu_4 A'$ NOH bend	1402.7	1409.1		1360.8	1360.7		1353.3 [54]
	$\nu_5 A'$ NH_2 wag	1154.9	1157.0		1116.0	1114.8		1115.5 [54]
	$\nu_6 A'$ NO str	920.2	937.1		900.2	900.1		895.2 [54]
	$\nu_7 A''$ NH_2 a str	3529.6	3544.4		3361.2	3361.2		3358.8 [54]
	$\nu_8 A''$ NH_2 twist	1327.2	1336.1		1298.2	1298.3		1294.5 [54]
	$\nu_9 A''$ OH torsion	406.7	410.2					386.0 [54]
CH_2NOH	$\nu_1 A'$ OH str	3823.3	3842.0		3663.9	3663.9		3650.3 [55]
	$\nu_2 A'$ CH_2 a str	3245.9	3252.9		3111.1	3111.1		3109.7 [55]
	$\nu_3 A'$ CH_2 s str	3115.4	3118.1		2974.4	2974.4		2974.2 [55]
	$\nu_4 A'$ CN str	1677.3	1687.7		1642.8	1642.8		1639.5 [56]
	$\nu_5 A'$ CH_2 scissor	1446.2	1451.6		1410.2	1410.2		1410.5 [56]
	$\nu_6 A'$ NOH bend	1343.1	1350.6		1315.0	1315.0		1319.0 [56]
	$\nu_7 A'$ CH_2 rock	1172.5	1182.3		1162.0	1161.9		1157.3 [57]
	$\nu_8 A'$ NO str	906.2	924.7		897.5	897.5		892.6 [56]
	$\nu_9 A'$ CNO bend	528.8	533.8		529.5	529.5		530.0 [57]
	$\nu_{10} A''$ CH_2 wag	961.5	968.5		957.0	957.0		952.6 [58]
	$\nu_{11} A''$ NOH wag	785.0	791.2		776.5	776.5		772.8 [57]
	$\nu_{12} A''$ OH torsion	404.7	413.4					397.7 [57]

^a This work: CC = fc-CCSD(T)/aVTZ; CC-F12 = fc-CCSD(T)-F12a/VTZ-F12

^b VCI at CCSD(T)-F12a/aVTZ

^c Experimental data for CH_2NH and CH_2NOH are compactly summarised in Ref. [56].

^d Fermi resonance between ν_1 and $2\nu_4$:

ν_{ref} : 3280.7 cm^{-1} (81% ν_1 , 4% $2\nu_4$) and 3260.0 cm^{-1} (4% ν_1 , 81% $2\nu_4$)

ν_{drop} : 3288.5 cm^{-1} (81% ν_1 , 4% $2\nu_4$) and 3265.1 cm^{-1} (4% ν_1 , 82% $2\nu_4$)

$\tilde{\nu}_{\text{drop}}$: 3288.6 cm^{-1} (81% ν_1 , 4% $2\nu_4$) and 3266.3 cm^{-1} (4% ν_1 , 82% $2\nu_4$)

^e Strong resonance mixing between ν_2 , $3\nu_5$ and $2\nu_3$:

ν_{drop} : 3309.5 cm^{-1} (27% ν_2 , 37% $3\nu_5$, 6% $2\nu_3$), 3291.2 cm^{-1} (45% ν_2 , 21% $3\nu_5$, 3% $2\nu_3$) and 3193.7 cm^{-1} (12% ν_2 , 78% $2\nu_3$)

$\tilde{\nu}_{\text{drop}}$: 3303.9 cm^{-1} (50% ν_2 , 19% $3\nu_5$, 9% $2\nu_3$), 3282.9 cm^{-1} (21% ν_2 , 41% $3\nu_5$) and 3193.3 cm^{-1} (12% ν_2 , 78% $2\nu_3$)

^f $\nu^{(9)} - \nu^{(8)}$ convergence uncertainty: 1.2 cm^{-1}

^g $\nu^{(9)} - \nu^{(8)}$ convergence uncertainty: 1.8 cm^{-1}

Table S5: Fundamental transition wavenumbers (ν) and tunnel splittings ($\Delta = \nu(E) - \nu(A) + \Delta_{\text{g.s.}}$) for methanol (CH_3OH) in the molecular symmetry group representation G_6 . Experimental references are shown in brackets, see footnotes on how transition wavenumbers were obtained. All reported values are in units of cm^{-1} .

Methanol (G_6)	Ref. [59]			Ref. [60]			Expt.			
	$\nu(A)$	$\nu(E)$	Δ	$\nu(A)$	$\nu(E)$	Δ	$\nu(A)$	$\nu(E)$	Δ	Ref.
g.s. A_1/E			8.8			8.7			9.12	[61]
$\nu_1 A_1/E$ OH str	3680.2	3677.9	6.5	3675.0	3673.2	6.9	3685.32	3682.49	6.29	[62]
$\nu_2 A_1/E$ CH ₃ a str	3005.2	2993.6	-2.8	2986.3	2976.9	-0.7	3006.99	2994.61	-3.26	[63]
$\nu_3 A_1/E$ CH ₃ s str	2844.4	2841.2	5.6	2839.5	2839.9	9.1	2844.72	2844.67	9.07	[64]
$\nu_4 A_1/E$ CH ₃ a bend	1484.0	1469.9	-5.3	1483.8	1472.4	-2.7	1486.08	1474.14	-2.82	[65]
$\nu_5 A_1/E$ CH ₃ s bend	1450.2	1449.0	7.6	1446.8	1446.8	8.7	1453.32	1452.96	8.76	[65]
$\nu_6 A_1/E$ COH bend	1321.0	1337.1	24.9	1321.9	1333.2	20.0	1320.63	1335.20	23.69	[66]
$\nu_7 A_1/E$ CH ₃ rock	1074.0	1069.8	4.6	1079.9	1078.8	7.6	1074.66	1070.15	4.61	[67]
$\nu_8 A_1/E$ CO str	1031.0	1030.6	8.4	1026.3	1028.1	10.5	1034.37	1033.53	8.27	[67]
$\nu_9 A_2/E$ CH ₃ a str	2956.5	2943.7	-4.0	2961.5	2949.4	-3.4	2966.64	2952.04	-5.48	[68]
$\nu_{10} A_2/E$ CH ₃ a bend	1465.0	1451.5	-4.7	1475.1	1462.2	-4.2	1481.45	1464.80	-7.53	[65]
$\nu_{11} A_2/E$ CH ₃ rock	1159.9	1143.6	-7.5	1156.5	1142.4	-5.4	1163.97	1147.35	-7.50	[67]

Low-resolution band centres are computed for each fundamental according to Eq. 2:

- g.s. Moruzzi *et al.*^[61] report Taylor expansion coefficients for absolute term energies in Tabs. 8.1 (A) and 8.3 (E). From these, we compute the ground state term values $E_{\text{g.s.}}(A) = 128.7822 \text{ cm}^{-1}$ and $E_{\text{g.s.}}(E) = 137.9036 \text{ cm}^{-1}$, yielding a zero-point splitting of $\Delta_{\text{g.s.}} = 9.12 \text{ cm}^{-1}$. For consistency, this value is used to compute E transitions for all other vibrational fundamentals.
- ν_1 Hunt *et al.*^[62] list relative term values in Tabs. 1 (A) and 2 (E): $W_1(A) = 3685.3222 \text{ cm}^{-1}$ and $W_1(E) = 3691.6122 \text{ cm}^{-1}$.
- ν_2 Xu *et al.*^[63] report both, absolute term values for the ground state ($E_{\text{g.s.}}(A) = 127.817 \text{ cm}^{-1}$ and $E_{\text{g.s.}}(E) = 136.939 \text{ cm}^{-1}$) and ν_2 ($E_2(A) = 3134.804 \text{ cm}^{-1}$ and $E_2(E) = 3131.549 \text{ cm}^{-1}$) in Tab. 4. We obtain relative term values as $W_2(A/E) = E_2(A/E) - 127.817 \text{ cm}^{-1}$.
- ν_3 Hunt *et al.*^[64] report transition wavenumbers $\nu_3(A) = (2844.72 \pm 0.01) \text{ cm}^{-1}$ and $\nu_3(E) = (2844.67 \pm 0.05) \text{ cm}^{-1}$ in Tab. 2.
- ν_4 Temsamani *et al.*^[65] report absolute term values for ν_4 , ν_5 and ν_{10} in Tab. 7. For ν_4 they report values of $E_4(A) = 1614.19 \text{ cm}^{-1}$ and $E_4(E) = 1611.37 \text{ cm}^{-1}$. In Tab. 4 they report a zero-point energy of $E_{\text{g.s.}}(A) = 128.1069 \text{ cm}^{-1}$ which they calculated with constants reported by Xu and Hougen^[69]. We obtain relative term values as $W_i(A/E) = E_i(A/E) - 128.1069 \text{ cm}^{-1}$.
- ν_5 See ν_4 . $E_5(A) = 1581.43 \text{ cm}^{-1}$ and $E_5(E) = 1590.19 \text{ cm}^{-1}$.
- ν_6 Lees *et al.*^[66] report transition wavenumbers for ν_6 in Tab. 1: $\nu_6(A) = 1320.633 \text{ cm}^{-1}$ and $\nu_6(E) = 1335.199 \text{ cm}^{-1}$.
- ν_7 Lees *et al.*^[67] re-fitted Fourier coefficients for ν_7 , ν_8 , ν_{11} and other vibrational states. Using their coefficients in Tab. 2, we obtain relative term values of $W_7(A) = 1074.661 \text{ cm}^{-1}$ and $W_7(E) = 1079.269 \text{ cm}^{-1}$.
- ν_8 See ν_7 . $W_8(A) = 1034.373 \text{ cm}^{-1}$ and $W_8(E) = 1042.646 \text{ cm}^{-1}$.
- ν_9 Wang and Perry^[68] report absolute term values for ν_2 , ν_3 and ν_9 ($E_9(A) = 3094.75 \text{ cm}^{-1}$ and $E_9(E) = 3089.27 \text{ cm}^{-1}$). The zero-point energy is computed by constants reported by Xu and Hougen^[69]. We obtain relative term values as $W_i(A/E) = E_i(A/E) - 128.1069 \text{ cm}^{-1}$.
- ν_{10} See ν_4 . $E_{10}(A) = 1609.65 \text{ cm}^{-1}$ and $E_{10}(E) = 1602.03 \text{ cm}^{-1}$.
- ν_{11} See ν_7 . $W_{11}(A) = 1163.970 \text{ cm}^{-1}$ and $W_{11}(E) = 1156.465 \text{ cm}^{-1}$.

Table S6: Fundamental transition wavenumbers (cm^{-1}) for methanol (CH_3OH) in the single-reference point group symmetry representation C_s . Low-resolution computational and experimental literature values ($\bar{\nu}$), harmonic (ω) and single-reference VCI(9) fundamental transition wavenumbers ($\nu^{(9)}$) are shown. All reported VCI(9) fundamentals are converged to within 0.1 cm^{-1} , if not stated otherwise.

Methanol (C_s)	ω^a		$\nu^{(9)}$		$\bar{\nu}$		
	CC	CC-F12	ν_{drop}	$\tilde{\nu}_{\text{drop}}$	Ref. [59]	Ref. [60]	Expt.
$\nu_1 A'$ OH str	3843.6	3864.0	3685.6	3685.6	3678.7	3673.8	3683.4
$\nu_2 A'$ CH ₃ a str	3128.3	3137.1	3002.9	3002.7	2997.5	2980.0	2998.7
$\nu_3 A'$ CH ₃ s str	3010.9	3016.1	2840.9	2840.7	2842.3	2839.8	2844.7
$\nu_4 A'$ CH ₃ a bend	1522.8	1521.0	1475.5	1475.1	1474.6	1476.2	1478.1
$\nu_5 A'$ CH ₃ s bend	1484.1	1484.6	1448.3	1448.4	1449.4	1446.8	1453.1
$\nu_6 A'$ COH bend	1379.2	1382.5	1347.9	1347.8	1331.7	1329.4	1330.3
$\nu_7 A'$ CH ₃ rock	1082.3	1089.2	1067.2	1067.1	1071.2	1079.2	1071.7
$\nu_8 A'$ CO str	1053.6	1061.3	1033.3	1033.4	1030.7	1027.5	1033.8
$\nu_9 A''$ CH ₃ a str	3069.2	3076.3	2953.0 ^{b,c}	2952.1 ^{b,c}	2948.0	2953.4	2956.9
$\nu_{10} A''$ CH ₃ a bend	1512.3	1510.8	1464.5	1464.0	1456.0	1466.5	1470.4
$\nu_{11} A''$ CH ₃ rock	1175.9	1180.9	1155.7	1155.5	1149.0	1147.1	1152.9

^a This work: CC = fc-CCSD(T)/aVTZ; CC-F12 = fc-CCSD(T)-F12a/VTZ-F12

^b Very strong resonance mixing between ν_9 and $\nu_4 + \nu_5$:

ν_{drop} : 2953.0 cm^{-1} (33% ν_9 , 44% $\nu_4 + \nu_5$) and 2921.7 cm^{-1} (28% ν_9 , 35% $\nu_4 + \nu_5$)

$\tilde{\nu}_{\text{drop}}$: 2952.1 cm^{-1} (35% ν_9 , 52% $\nu_4 + \nu_5$) and 2921.3 cm^{-1} (27% ν_9 , 37% $\nu_4 + \nu_5$)

^c $\nu^{(9)} - \nu^{(8)}$ convergence uncertainty: 0.2 cm^{-1}

3 R matrices

In the following, **R** matrices (see main text, Eq. 4) are reported for all investigated molecular topologies (group D similar to group B), where **R** contains elements $R_{ij} = \partial Q_i / \partial S_j$. The internal coordinate labels SPF, BA, DA and SOOP stand for Simons-Parr-Finlan, bond angle, dihedral angle and sine of out-of-plane angle, respectively. ν_i denotes the i^{th} normal mode.

3.1 Tetratomic examples: NH₃, SO₃ and H₂O₂

Cartesian coordinates (Angst)

1	N	0.00	0.00	0.07
2	H	-0.46	0.82	-0.31
3	H	-0.48	-0.80	-0.31
4	H	0.94	-0.01	-0.31

Redundant internal coordinates

Connectivity

S ₁	SPF	(1-2)
S ₂	SPF	(1-3)
S ₃	SPF	(1-4)
S ₄	BA	(2-1-3)
S ₅	BA	(2-1-4)
S ₆	BA	(3-1-4)

R matrix for $V_{\text{ref}} / \sim V_{\text{harm}} / V_{\text{drop}}$

ν_i		Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆
1	A ₁	s stretch	-47	-47	-47	-3	-3	-3
2	A ₁	inversion	-1	-1	-1	40	40	40
3	E	a stretch	47	14	-61	1	0	-1
3	E	a stretch	-43	63	-19	0	-1	1
4	E	a bend	1	2	-3	40	-30	-10
4	E	a bend	3	-2	-1	12	29	-41

R matrix for $\sim V_{\text{drop}}$

ν_i		Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆
1	A ₁	s stretch	-49	-49	-49	139	139	139
3	E	a stretch	47	14	-61	1	0	-1
3	E	a stretch	-43	63	-19	0	-1	1
4	E	a bend	1	2	-3	40	-30	-10
4	E	a bend	3	-2	-1	12	29	-41

Cartesian coordinates (Angst)

1	S	0.00	0.00	0.00
2	O	1.43	0.00	0.00
3	O	-0.71	-1.23	0.00
4	O	-0.71	1.23	0.00

Redundant internal coordinates

Connectivity

S ₁	SPF	(1-2)
S ₂	SPF	(1-3)
S ₃	SPF	(1-4)
S ₄	BA	(2-1-3)
S ₅	BA	(2-1-4)
S ₆	BA	(3-1-4)
S ₇	SOOP	(1-2-4-3)

R matrix for $V_{\text{ref}} / \sim V_{\text{harm}} / V_{\text{drop}}$

ν_i		Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆	S ₇
1	A ₁ '	s stretch	266	266	266	0	0	0	0
2	A _z ''	oop	0	0	0	0	0	0	-504
4	E'	a bend	121	9	-129	162	-11	-151	0
4	E'	a bend	-80	144	-65	81	-181	100	0
3	E'	a stretch	1	241	-242	-6	6	0	0
3	E'	a stretch	279	-140	-139	-3	-3	6	0

R matrix for $\sim V_{\text{drop}}$

ν_i		Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆	-
1	A ₁ '	s stretch	266	266	266	0	0	0	-
3	E'	a stretch	1	241	-242	-6	6	0	-
3	E'	a stretch	279	-140	-139	-3	-3	6	-
4	E'	a bend	121	9	-129	162	-11	-151	-
4	E'	a bend	-80	144	-65	81	-181	100	-

Cartesian coordinates (Angst)

1	H	-0.90	-0.79	-0.49
2	O	-0.73	0.00	0.03
3	O	0.73	0.00	0.03
4	H	0.90	0.79	-0.49

Redundant internal coordinates

Connectivity

S ₁	SPF	(1-2)
S ₂	SPF	(2-3)
S ₃	SPF	(3-4)
S ₄	BA	(1-2-3)
S ₅	BA	(2-3-4)
S ₆	DA	(1-2-3-4)

R matrix for $V_{\text{ref}} / \sim V_{\text{harm}} / V_{\text{drop}}$

ν_i		Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆
1	A	OH ₂ s stretch	-53	4	-53	1	1	0
2	A	s bend	-4	-88	-4	-53	-53	-4
3	A	OO stretch	3	329	3	-1	-1	-3
4	A	torsion	0	-17	0	1	1	-52
5	B	OH ₂ a stretch	53	0	-53	0	0	0
6	B	a bend	-1	0	1	-52	52	0

R matrix for $\sim V_{\text{drop}}$

ν_i		Label	S ₁	S ₂	S ₃	S ₄	S ₅	-
1	A	OH ₂ s stretch	-53	4	-53	1	1	-
2	A	s bend	-4	-87	-4	-53	-53	-
3	A	OO stretch	3	330	3	-1	-1	-
5	B	OH ₂ a stretch	53	0	-53	0	0	-
6	B	a bend	-1	0	1	-52	52	-

3.2 Pentatomics: CH₂NH and NH₂OH

Cartesian coordinates (Angst)					R matrix for V _{ref} /~V _{harm} /N _{drop}												
v _i		Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆	S ₇	S ₈	S ₉	S ₁₀					
1	C	0.00	0.03	-0.63		6	3	-4	-80	-1	1	0	-2	0	0		
2	N	0.00	0.03	0.64		2	-75	37	-4	0	0	0	0	0	0		
3	H	0.00	-0.93	0.99		-6	39	76	-3	0	-1	1	-1	0	0		
4	H	0.00	0.99	-1.15		208	9	9	6	-8	-11	19	6	0	0		
5	H	0.00	-0.87	-1.25		182	5	4	5	22	14	-36	10	0	0		
Redundant internal coordinates					R matrix for ~V _{drop}												
Connectivity					v _i		Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆	S ₇	S ₈	S ₁₁	-
S ₁	SPF	(1-2)			1	A'	NH stretch	6	3	-4	-80	-1	1	0	-2	0	-
S ₂	SPF	(1-4)			2	A'	CH ₂ a stretch	2	-75	37	-4	0	0	0	0	0	-
S ₃	SPF	(1-5)			3	A'	CH ₂ s stretch	-6	39	76	-3	0	-1	1	-1	0	-
S ₄	SPF	(2-3)			4	A'	CN stretch	208	9	9	6	-8	-11	19	6	0	-
S ₅	BA	(2-1-4)			5	A'	CH ₂ scissor	182	5	4	5	22	14	-36	10	0	-
S ₆	BA	(2-1-5)			6	A'	CNH bend	10	-9	8	-3	-28	31	-3	-56	0	-
S ₇	BA	(4-1-5)			7	A'	CH ₂ rock	20	-4	6	-2	-45	46	-1	53	0	0
S ₈	BA	(1-2-3)			8	A''	NH torsion	0	0	0	0	0	0	0	0	40	21
S ₉	DA	(4-1-2-3)			9	A''	CH ₂ wag	0	0	0	0	0	0	0	0	41	-48
S ₁₀	DA	(5-1-2-3)			R matrix for ~V _{drop}												
S ₁₁	SOOP	(1-2-5-4)															
Cartesian coordinates (Angst)					R matrix for V _{ref} /~V _{harm} /N _{drop}												
1	N	0.00	-0.01	-0.74	v _i		Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆	S ₇	S ₈	S ₉	S ₁₀
2	O	0.00	-0.01	0.71	1	A'	OH stretch	-3	-1	-1	76	0	0	0	0	0	0
3	H	0.00	-0.95	0.91	2	A'	NH ₂ s stretch	2	-57	-57	-1	0	0	-3	0	-1	1
4	H	0.81	0.56	-0.97	3	A'	NH ₂ scissor	38	1	1	2	27	27	-34	12	-9	9
5	H	-0.81	0.56	-0.97	4	A'	NOH bend	-91	-3	-3	-4	-13	-13	-9	-66	-9	9
Redundant internal coordinates					5	A'	NH ₂ wag	101	1	1	2	41	41	10	-32	19	-19
Connectivity					6	A'	NO stretch	304	3	3	3	-8	-8	-6	2	-6	6
S ₁	SPF	(1-2)			7	A''	NH ₂ a stretch	0	56	-56	0	-1	1	0	0	0	0
S ₂	SPF	(1-4)			8	A''	NH ₂ twist	0	-5	5	0	-55	55	0	0	2	2
S ₃	SPF	(1-5)			9	A''	OH torsion	0	1	-1	0	-3	3	0	0	-31	-31
S ₄	SPF	(2-3)			R matrix for ~V _{drop}												
S ₅	BA	(2-1-4)			v _i		Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆	S ₇	S ₈	-	-
S ₆	BA	(2-1-5)			1	A'	OH stretch	-3	-1	-1	76	0	0	0	0	-	-
S ₇	BA	(4-1-5)			2	A'	NH ₂ s stretch	2	-57	-57	-1	-1	-1	-4	0	-	-
S ₈	BA	(1-2-3)			3	A'	NH ₂ scissor	38	1	1	2	24	24	-44	12	-	-
S ₉	DA	(4-1-2-3)			4	A'	NOH bend	-91	-3	-3	-4	-17	-17	-19	-66	-	-
S ₁₀	DA	(5-1-2-3)			5	A'	NH ₂ wag	101	1	1	2	48	48	31	-32	-	-

3.3 Hexatomics: CH₂NOH and CH₃OH

Cartesian coordinates (Angst)														
v _i	Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆	S ₇	S ₈	S ₉	S ₁₀	S ₁₁	S ₁₂	S ₁₃
1	N	-0.37	0.21	-0.33										
2	O	-0.37	-0.55	0.86										
3	C	0.83	0.45	-0.70										
4	H	-1.32	-0.67	1.03										
5	H	1.69	0.09	-0.14										
6	H	0.94	1.04	-1.60										
Redundant internal coordinates														
Connectivity														
S ₁	SPF	(1-2)												
S ₂	SPF	(1-3)												
S ₃	SPF	(2-4)												
S ₄	SPF	(3-5)												
S ₅	SPF	(3-6)												
S ₆	BA	(2-1-3)												
S ₇	BA	(1-2-4)												
S ₈	BA	(1-3-5)												
S ₉	BA	(1-3-6)												
S ₁₀	BA	(5-3-6)												
S ₁₁	DA	(3-1-2-4)												
S ₁₂	DA	(2-1-3-5)												
S ₁₃	DA	(2-1-3-6)												

R matrix for V _{ref} /~V _{harm} /V _{drop}														
v _i	Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆	S ₇	S ₈	S ₉	S ₁₀	-	S ₁₂	S ₁₃
1	A'	OH str	2	1	-76	1	0	0	0	0	0	0	0	0
2	A'	CH ₂ a str	3	2	0	40	-73	1	0	0	0	0	0	0
3	A'	CH ₂ s str	-1	-8	0	75	42	-1	0	0	0	0	0	0
4	A'	CN str	-27	209	-1	11	8	-9	-19	-4	-8	12	0	0
5	A'	CH ₂ scissor	41	-56	2	-1	3	18	36	-20	-14	33	0	0
6	A'	NOH bend	23	164	3	2	7	22	57	0	19	-19	0	0
7	A'	CH ₂ rock	-51	-16	0	-9	9	35	-21	-45	43	2	0	0
8	A'	NO str	331	82	5	-2	7	28	1	-15	19	-4	0	0
9	A'	CNO bend	-90	-109	-9	3	-10	-230	15	-35	30	5	0	0
10	A''	CH ₂ wag	0	0	0	0	0	0	0	0	0	0	51	-40
11	A''	NOH wag	0	0	0	0	0	0	0	0	0	-10	35	61
12	A''	OH torsion	0	0	0	0	0	0	0	0	0	71	13	5

Cartesian coordinates (Angst)														
v _i	Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆	S ₇	S ₈	S ₉	S ₁₀	S ₁₁	S ₁₂	S ₁₃
1	O	0.69	-0.06	0.00										
2	C	-0.73	0.01	0.00										
3	H	-1.10	-1.01	0.00										
4	H	1.04	0.83	0.00										
5	H	-1.11	0.52	-0.89										
6	H	-1.11	0.52	0.89										
Redundant internal coordinates														
Connectivity														
S ₁	SPF	(1-2)												
S ₂	SPF	(1-4)												
S ₃	SPF	(2-3)												
S ₄	SPF	(2-5)												
S ₅	SPF	(2-6)												
S ₆	BA	(2-1-4)												
S ₇	BA	(1-2-3)												
S ₈	BA	(1-2-5)												
S ₉	BA	(1-2-6)												
S ₁₀	BA	(3-2-5)												
S ₁₁	BA	(3-2-6)												
S ₁₂	BA	(5-2-6)												
S ₁₃	DA	(4-1-2-3)												
S ₁₄	DA	(4-1-2-5)												
S ₁₅	DA	(4-1-2-6)												

R matrix for V _{ref} /~V _{harm} /V _{drop}														
v _i	Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆	S ₇	S ₈	S ₉	S ₁₀	S ₁₁	S ₁₂	S ₁₃
1	A'	OH str	-3	76	-1	0	0	1	0	0	0	0	0	0
2	A'	CH ₃ a str	-1	1	80	-19	-19	-1	0	0	0	1	1	-1
3	A'	CH ₃ s str	-4	0	-29	-58	-58	0	0	1	1	0	0	-1
4	A'	CH ₃ a bend	1	1	-1	1	1	7	16	-13	-13	-12	-12	33
5	A'	CH ₃ s bend	-31	-1	2	1	1	-1	-25	-22	-22	25	25	20
6	A'	COH bend	37	4	10	-4	-4	56	32	-13	-13	0	0	-4
7	A'	CH ₃ rock	-211	-2	1	-6	-6	-40	36	-23	-23	4	4	4
8	A'	CO str	-242	-5	-7	-3	-3	28	-33	10	10	4	4	4
9	A''	CH ₃ a str	0	0	0	60	-60	0	0	-1	1	1	-1	0
10	A''	CH ₃ a bend	0	0	0	2	-2	0	0	-14	14	27	-27	0
11	A''	CH ₃ rock	0	0	0	9	-9	0	0	52	-52	0	0	20
12	A''	torsion	0	0	0	0	0	0	-4	4	-1	1	0	-23

R matrix for ~V _{drop}															
v _i	Label	S ₁	S ₂	S ₃	S ₄	S ₅	S ₆	S ₇	S ₈	S ₉	S ₁₀	S ₁₁	S ₁₂	-	
1	A'	OH str	-3	76	-1	0	0	1	0	0	0	0	0	-	-
2	A'	CH ₃ a str	-1	1	80	-19	-19	-1	0	0	0	1	1	-1	
3	A'	CH ₃ s str	-4	0	-29	-58	-58	0	0	1	1	0	0	-1	
4	A'	CH ₃ a bend	1	1	-1	1	1	7	11	-10	-10	-18	-18	43	
5	A'	CH ₃ s bend	-31	-1	2	1	1	-1	-24	-23	-23	27	27	17	
6	A'	COH bend	37	4	10	-4	-4	56	38	-17	-17	6	6	-14	
7	A'	CH ₃ rock	-211	-2	1	-6	-6	-40	43	-26	-26	10	10	-7	
8	A'	CO str	-242	-5	-7	-3	-3	28	-38	12	12	-1	-1	12	
9	A''	CH ₃ a str	0	0	0	60	-60	0	0	-1	1	1	-1	0	
10	A''	CH ₃ a bend	0	0	0	2	-2	0	0	-9	9	37	-37	0	
11	A''	CH ₃ rock	0	0	0	9	-9	0	0	57	-57	12	-12	0	

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