

Supporting Information for

**First-Principles Calculation of ^{11}B Solid-State NMR
Parameters of Boron-Rich Compounds II: The
Orthorhombic Phases MgB_7 and $\text{MgB}_{12}\text{C}_2$ and the
Boron Modification $\gamma\text{-B}_{28}$**

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Table S1: Lattice parameters of primitive cells used for the calculations.^a

compound	length (Å)			angles (°)			volume (Å ³)
	<i>a</i>	<i>b</i>	<i>c</i>	α	β	γ	
MgB ₇	10.4782	5.9769	7.2719	65.735	43.908	90.000	254.4
o-MgB ₁₂ C ₂	5.6133	9.8280	6.9107	44.678	66.038	90.000	218.8

^a for γ -B₂₈ lattice parameters of primitive cell correspond to conventional orthorhombic cell.

Table S2: Structure parameters in terms of the orthorhombic axes before and after relaxation.

compound	site	Wyckoff position	start			relaxed		
			\bar{x}	\bar{y}	\bar{z}	\bar{x}	\bar{y}	\bar{z}
MgB ₇	B(1)	8 <i>i</i>	0.58356	0.75000	0.22495	0.58384	0.75000	0.22560
	B(2)	16 <i>j</i>	0.68650	0.59402	0.08645	0.68641	0.59432	0.08680
	B(3)	16 <i>j</i>	0.82803	0.50276	0.20540	0.82772	0.50337	0.20522
	B(4)	8 <i>i</i>	0.83263	0.75000	0.07391	0.83208	0.75000	0.07394
	B(5)	8 <i>i</i>	0.39129	0.25000	0.36547	0.38985	0.25000	0.36597
	Mg(1)	4 <i>a</i>	0.00000	0.50000	0.00000	0.00000	0.50000	0.00000
o-MgB ₁₂ C ₂	Mg(2)	4 <i>e</i>	0.00000	0.25000	0.38430	0.00000	0.25000	0.38423
	B(1)	8 <i>h</i>	0.00000	0.33274	0.02107	0.00000	0.33303	0.02066
	B(2)	16 <i>j</i>	0.16176	0.43614	0.16054	0.16150	0.43627	0.16042
	B(3)	16 <i>j</i>	0.76069	0.91504	0.44807	0.76053	0.91501	0.44795
	B(4)	8 <i>h</i>	0.50000	0.90606	0.31860	0.50000	0.90637	0.31848
	C	8 <i>h</i>	0.50000	0.83785	0.12929	0.50000	0.83785	0.12909
γ -B ₂₈	Mg	4 <i>e</i>	0.00000	0.25000	0.36187	0.00000	0.25000	0.36041
	B(1)	4 <i>g</i>	0.33620	0.50760	0.00000	0.33570	0.50771	0.00000
	B(2)	8 <i>h</i>	0.83910	0.71890	0.87370	0.83904	0.71918	0.87478
	B(3)	8 <i>h</i>	0.15390	0.59380	0.79240	0.15301	0.59300	0.79215
	B(4)	4 <i>g</i>	0.64690	0.72840	0.50000	0.64779	0.72925	0.50000
B(5)	4 <i>g</i>	0.66900	0.98230	0.00000	0.66966	0.98090	0.00000	

Table S3: Chemical shift parameters δ_{iso} , δ_{csa} in ppm and η_{cs} without macroscopic correction of magnetic susceptibility^a together with corresponding susceptibilities χ .^[1] All values according to PAW PPs.

compound	site	without correction ^a			$-\chi$	
		δ_{iso}	δ_{csa}	η_{cs}	$((8\pi/3) \text{ ppm})$	$(10^{-6} \text{ cm}^3/\text{mol})$
MgB ₇	B(1)	11.9	12.9	0.22	13.4	244.4
	B(2)	23.4	18.2	0.93		
	B(3)	27.3	17.4	0.97		
	B(4)	49.2	2.4	0.35		
	B(5)	-20.9	15.0	0.23		
o-MgB ₁₂ C ₂	B(1)	1.1	18.2	0.23	13.9	219.2
	B(2)	10.0	-14.9	0.97		
	B(3)	24.4	-11.2	0.49		
	B(4)	50.4	-10.7	0.54		
γ -B ₂₈	B(1)	17.7	-13.5	0.94	15.8	225.6
	B(2)	7.6	-25.9	0.90		
	B(3)	21.4	10.2	0.70		
	B(4)	23.3	-11.4	0.09		
	B(5)	23.4	20.3	0.66		

^a correction term given by $\sigma(\mathbf{G} = \mathbf{0}) = -(8\pi/3)\chi$.^[2]

Table S4: Parameters used for spectrum simulation (beside PAW calculated values) with relative intensity I , gaussian/lorentzian width w , approximated relative area A and occupied site multiplicity. Overall distribution of gaussian to lorentzian line type was assumed to be 50 %.

compound	site	I (%)	w (ppm)	A (%)	occ. (%)
MgB ₇	B(1)	10.8	8.0 ± 1.4	13.0 ± 2.3	14.3
	B(2)	13.8	14.0 ± 0.6	28.0 ± 1.2	28.6
	B(3)	13.8	14.0 ± 0.6	28.0 ± 1.2	28.6
	B(4)	34.9	3.0 ± 0.9	15.0 ± 4.4	14.3
	B(5)	26.7	4.0 ± 0.1	16.0 ± 0.5	14.3
o-MgB ₁₂ C ₂	B(1)	5.6	33.0 ± 11.5	18.0 ± 6.4	16.7
	B(2)	24.4	13.0 ± 1.2	31.0 ± 2.8	33.3
	B(3)	33.8	10.0 ± 0.1	33.0 ± 0.4	33.3
	B(4)	36.1	5.0 ± 0.2	18.0 ± 0.9	16.7

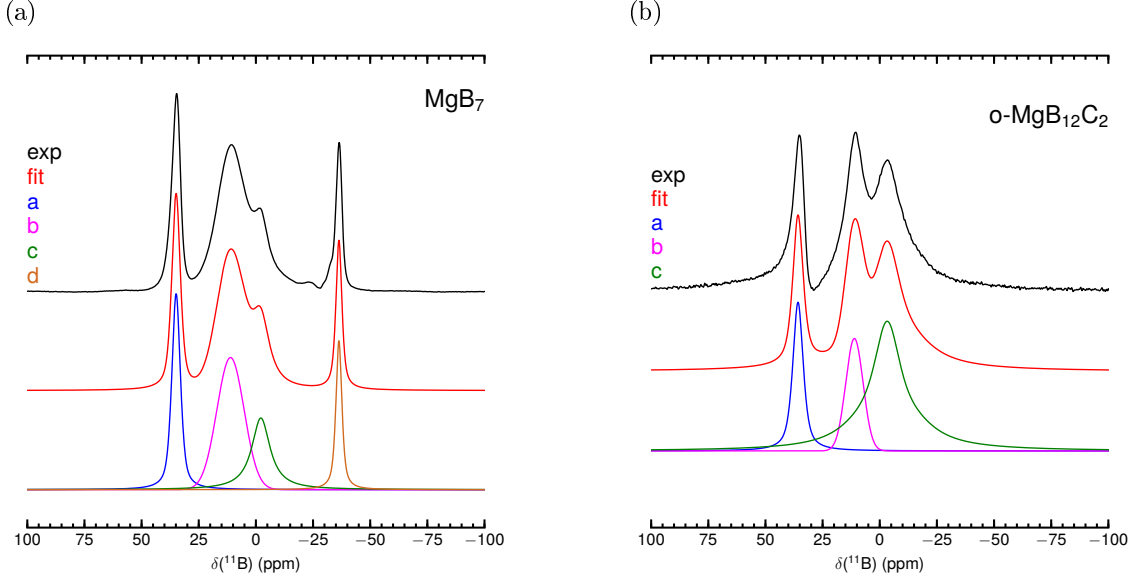


Figure S1: Central transition fits applying the “Gaus/Lor” model in the DMfit program^[3] to the recorded spectra of (a) MgB₇ and (b) o-MgB₁₂C₂: For MgB₇ we obtain $I_a : I_b : I_c : I_d = 35.7 \pm 0.2 \% : 24.1 \pm 0.1 \% : 13.1 \pm 0.2 \% : 27.1 \pm 0.2 \%$, the shifts $\delta_{\text{ctf}}^a = 34.9 \text{ ppm} \pm 0.2 \%$, $\delta_{\text{ctf}}^b = 11.1 \text{ ppm} \pm 2.8 \%$, $\delta_{\text{ctf}}^c = -2.2 \text{ ppm} \pm 25.6 \%$, $\delta_{\text{ctf}}^d = -36.3 \text{ ppm} \pm 0.3 \%$, the widths $w_a = 4.4 \text{ ppm} \pm 0.6 \%$, $w_b = 14.0 \text{ ppm} \pm 0.5 \%$, $w_c = 9.6 \text{ ppm} \pm 2.0 \%$, $w_d = 3.1 \text{ ppm} \pm 1.1 \%$ with the distribution of gaussian compared to lorentzian line type $x_a = 44 \%$, $x_b = 100 \%$ (full gaussian), $x_c = 0 \%$ (full lorentzian) and $x_d = 32 \%$; For o-MgB₁₂C₂ the fit yields $I_a : I_b : I_c = 38.0 \pm 0.5 \% : 28.8 \pm 0.5 \% : 33.2 \pm 0.4 \%$, the shifts $\delta_{\text{ctf}}^a = 35.8 \text{ ppm} \pm 0.9 \%$, $\delta_{\text{ctf}}^b = 11.1 \text{ ppm} \pm 5.7 \%$, $\delta_{\text{ctf}}^c = -3.3 \text{ ppm} \pm 34.3 \%$, the widths $w_a = 5.4 \text{ ppm} \pm 2.1 \%$, $w_b = 8.9 \text{ ppm} \pm 1.8 \%$, $w_c = 16.8 \text{ ppm} \pm 2.4 \%$ with the distribution of gaussian compared to lorentzian line type $x_a = 34 \%$, $x_b = 100 \%$ (full gaussian) and $x_c = 33 \%$.

Table S5: Euler angles α , β and γ in $^\circ$ correspond to the calculated magnetic shielding principal axis system relative to the principal axis system of the electric field gradient tensor obtained by MagresView.^[4] Values follow the ZYZ convention according to the book of M. E. Rose, Elementary Theory of Angular Momentum, Wiley, New York, 1957.

compound	site	NC			PAW		
		α	β	γ	α	β	γ
MgB ₇	B(1)	0	173	90	0	173	-90
	B(2)	-100	36	143	-101	35	144
	B(3)	-93	67	-92	-93	66	-92
	B(4)	179	162	-1	-180	72	0
	B(5)	-90	100	0	-90	100	0
o-MgB ₁₂ C ₂	B(1)	90	138	-180	90	138	-180
	B(2)	129	87	-44	130	88	-43
	B(3)	17	99	-100	19	99	-102
	B(4)	180	22	0	180	21	0
γ -B ₂₈	B(1)	90	106	90	90	106	90
	B(2)	101	60	-138	100	58	-136
	B(3)	-119	91	116	-121	90	117
	B(4)	90	101	90	90	101	90
	B(5)	90	35	180	90	34	-180

Table S6: Additional information of geometry related angles (Table 6 of the manuscript) in $^\circ$ with root-mean-square deviation (rmsd) θ_{rmsd} of θ_{av} and θ'_{rmsd} of θ'_{av} , respectively. All values correspond to optimized geometry.

compound	site	θ_{rmsd}	θ'_{rmsd}
MgB ₇	B(1)	1.35	1.22
	B(2)	0.93	0.86
	B(3)	1.27	0.98
	B(4)	0.79	0.46
o-MgB ₁₂ C ₂	B(1)	0.77	0.70
	B(2)	1.14	0.87
	B(3)	0.59	0.36
	B(4)	1.13	0.56
γ -B ₂₈	B(1)	0.22	0.24
	B(2)	0.67	0.32
	B(3)	0.33	0.30
	B(4)	0.63	0.19
(B ₁₂ H ₁₂) ²⁻		0.00	0.00

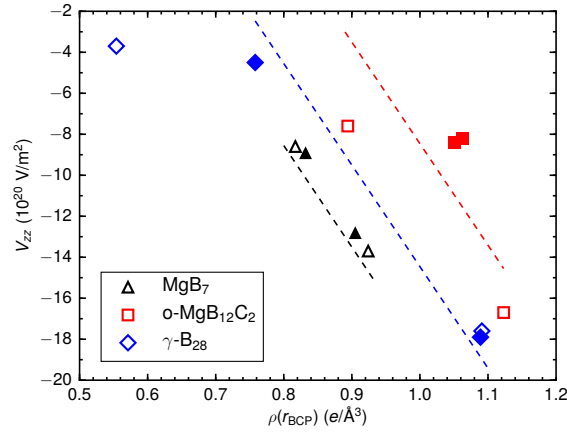


Figure S2: Values of the EFG main component V_{zz} from PAW calculations plotted against $\rho(r_{\text{BCP}})$ of B sites B(1) to B(4) in the icosahedral B₁₂ units with data from Tables 3 and 6 of the manuscript. The properties of the BCPs are associated with the exohedral bonds and in accordance to the orientation of the V_{zz} axis. Filled squares correspond to properties of sites bonded to the interstitial unit. The trend lines are meant to guide the eye.

References

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