

metal VBS	d(M-L1)	d(M-L2)	d(M-L3)	d(M-L4)	d(M-L5)	r(0)	beta
Mn1	2.091	1.976	1.934	1.874	1.947	1.76	0.37
	-0.331	-0.216	-0.174	-0.114	-0.187		
	-0.89459	-0.58378	-0.47027	-0.308108	-0.50541		
	0.408773	0.557784	0.624833	0.7348359	0.603261		
M(Ox.State)	2.929487						

metal VBS	d(M-L1)	d(M-L2)	d(M-L3)	d(M-L4)	d(M-L5)	d(M-L6)	r(0)	beta
Mn2	2.223	2.2277	2.099	2.187	2.152	2.225	1.79	0.37
	-0.433	-0.4377	-0.309	-0.397	-0.362	-0.435		
					-	-		
	-1.17027	-1.18297	-0.83514	-1.072973	0.97838	1.17568		
	0.310283	0.306367	0.433816	0.3419903	0.37592	0.30861		
M(Ox.State)	2.076986							

Table S1. Bond valence sum calculations to confirm the oxidation states of Mn ions in complex **3**.

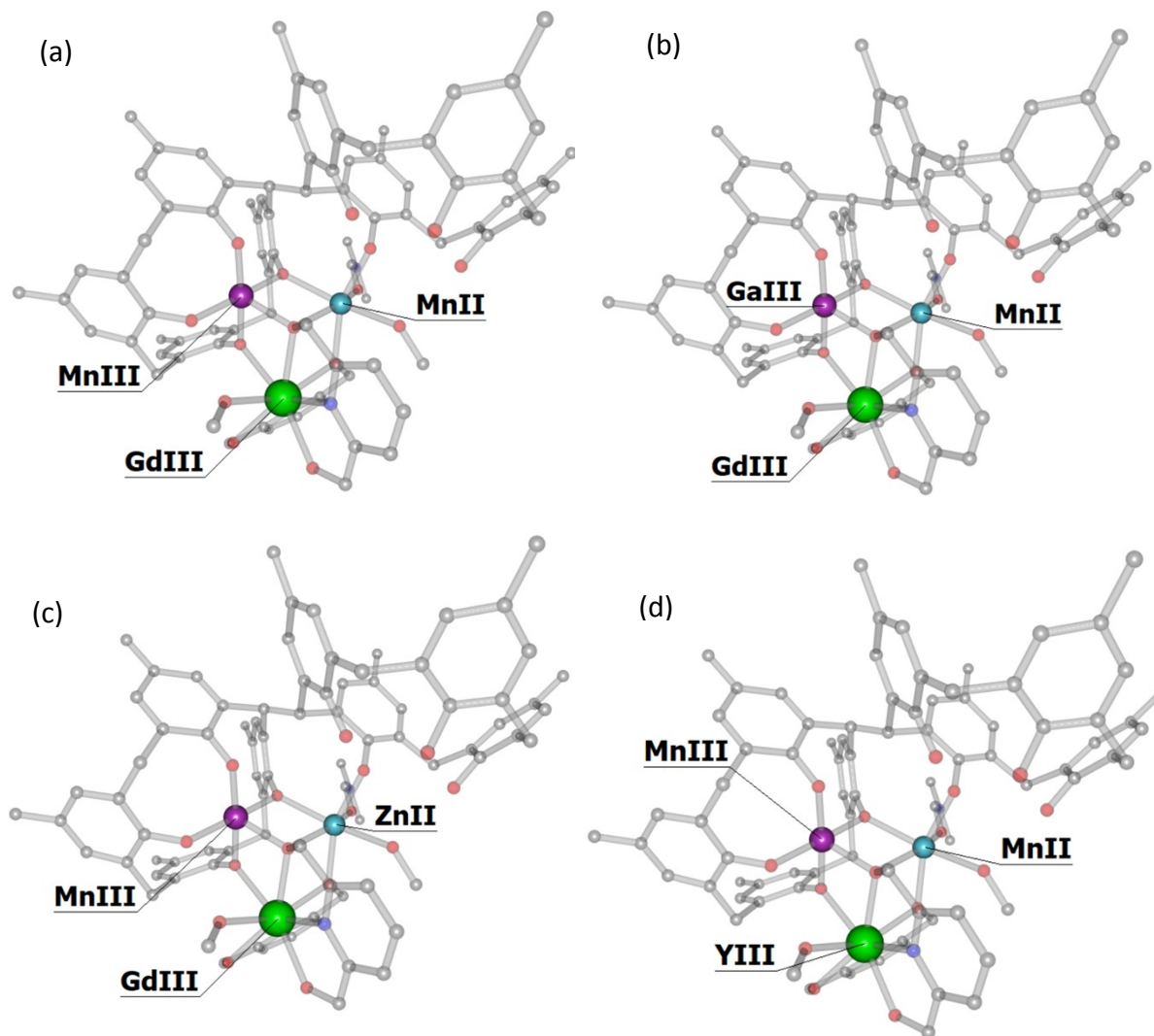


Figure S1. (a) Molecular structure of the model complex **3A**. Figures (b)-(d) show the models used to calculate the $J_{\text{Mn(II)}-\text{Gd(III)}}^{\text{exchange}}$, $J_{\text{Mn(III)}-\text{Gd(III)}}^{\text{exchange}}$ and $J_{\text{Mn(II)}-\text{Mn(III)}}^{\text{exchange}}$ pairwise interactions, respectively. In (b) the Mn(III) ion has been replaced by Ga(III). In (c) the Mn(II) ion has been replaced by Zn(II). In (d) the Gd(III) ion has been replaced with Y(III). Colour code is the same as in Figure 1.

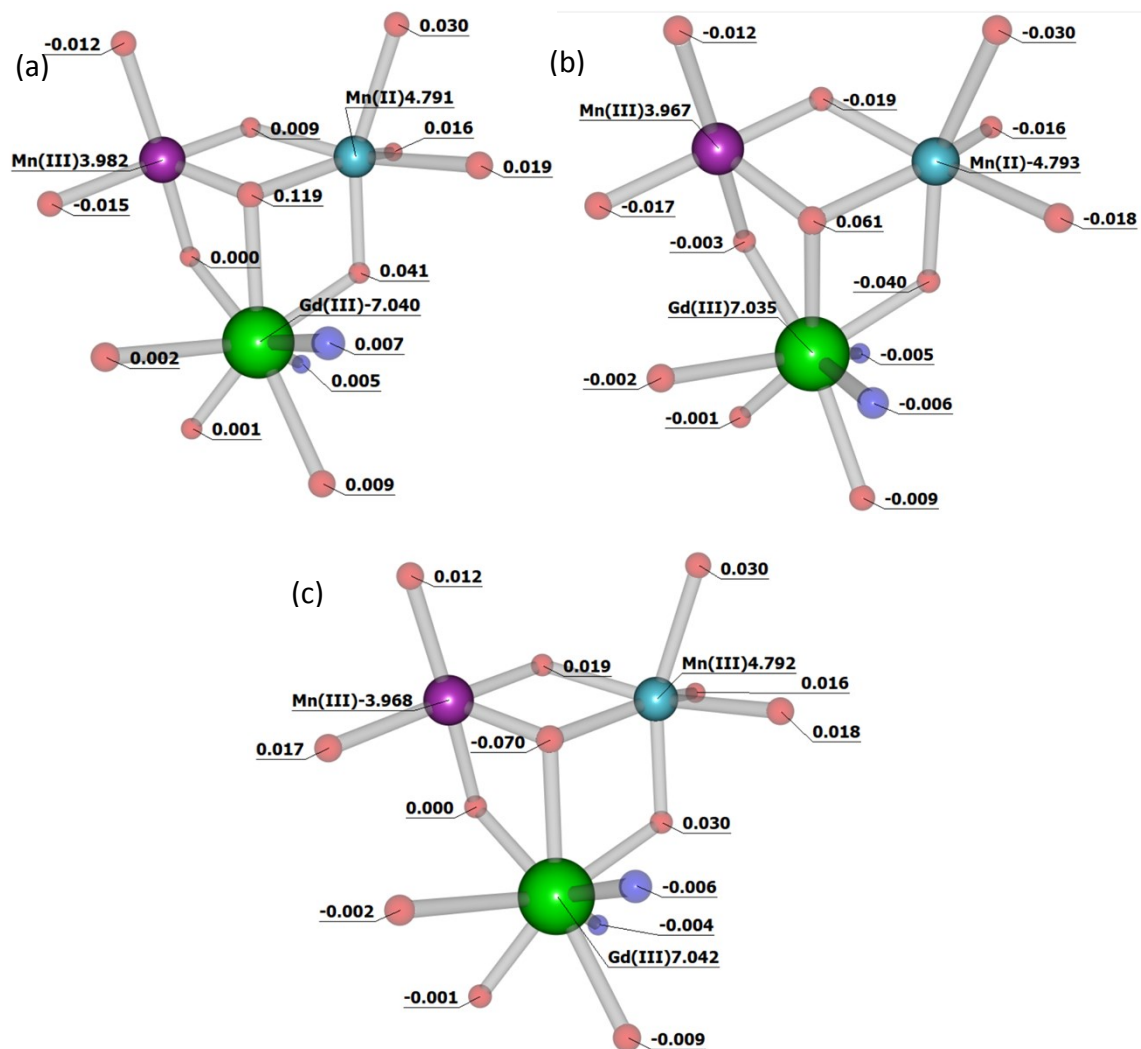


Figure S2. (a)-(c) Spin density values on selected atoms for spin states $S = 1, 3$ and 4 , respectively. Note that both experimental and computational studies suggest $S = 4$ as the ground spin state.

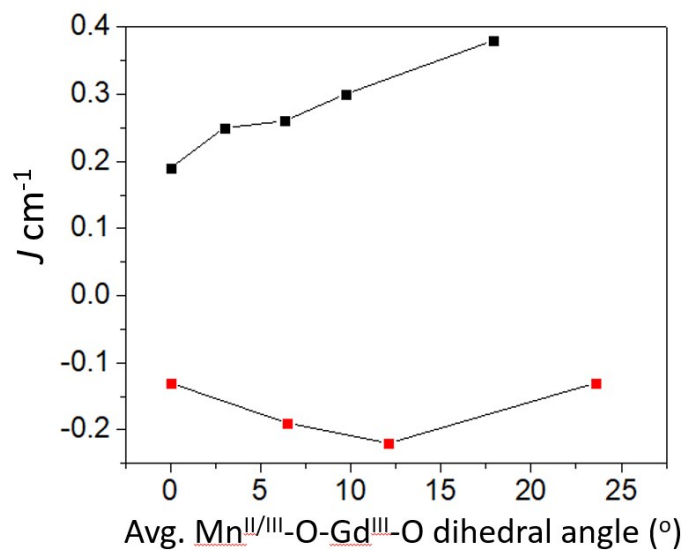


Figure S3. Magneto-structural plots performed by varying the average Mn^{II}/Mn^{III}-O-Gd^{III}-O dihedral angle with respect to the magnetic exchange coupling values ($J_{Mn(II)-Gd(III)}^{exchange}$ = black solid squares and $J_{Mn(III)-Gd(III)}^{exchange}$ = red solid squares). For both models, the change in the magnetic exchange coupling values with respect to the change in Mn^{III/II}-O-Gd^{III}-O dihedral angle are minimal.

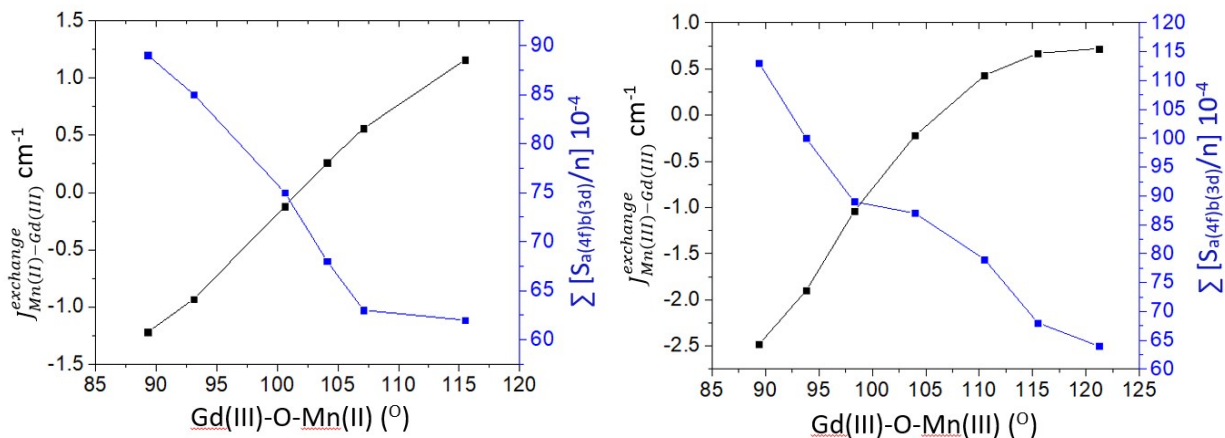


Figure S4. Magneto-structural data calculated by varying the average Mn^{II}/Mn^{III}-O-Gd^{III} angle with respect to the magnetic exchange coupling values, and average overlap integral values between SOMOs of {Mn(III/II)-3d} and {Gd(III)-4f} orbitals. Here, n = number of possible overlap integrals between the SOMOs (for 3d⁵-4f⁷ systems, n = 35 and for 3d⁴-4f⁷ systems, n = 28). The larger the average overlap integral value, the stronger the antiferromagnetic exchange interaction and vice versa.

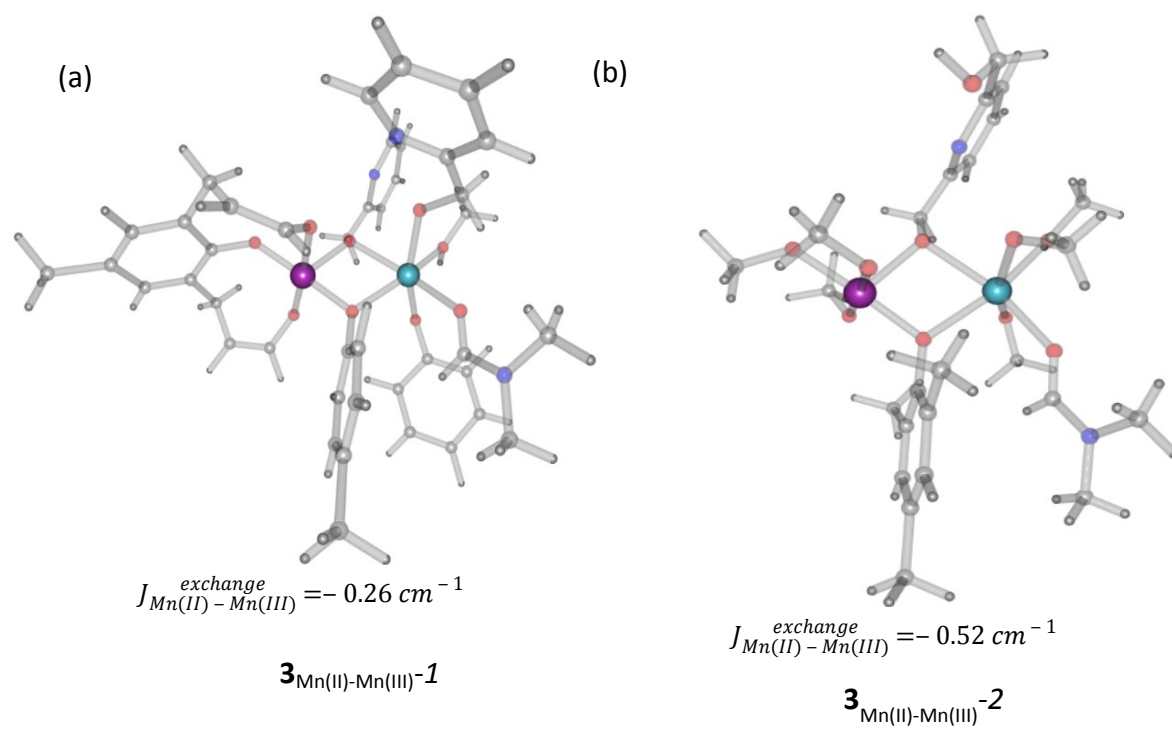


Figure S5. (a)-(b) Molecular structures for models $\mathbf{3}_{Mn(II)-Mn(III)-1}$ and $\mathbf{3}_{Mn(II)-Mn(III)-2}$, respectively. Colour code is same as in Figure 1.

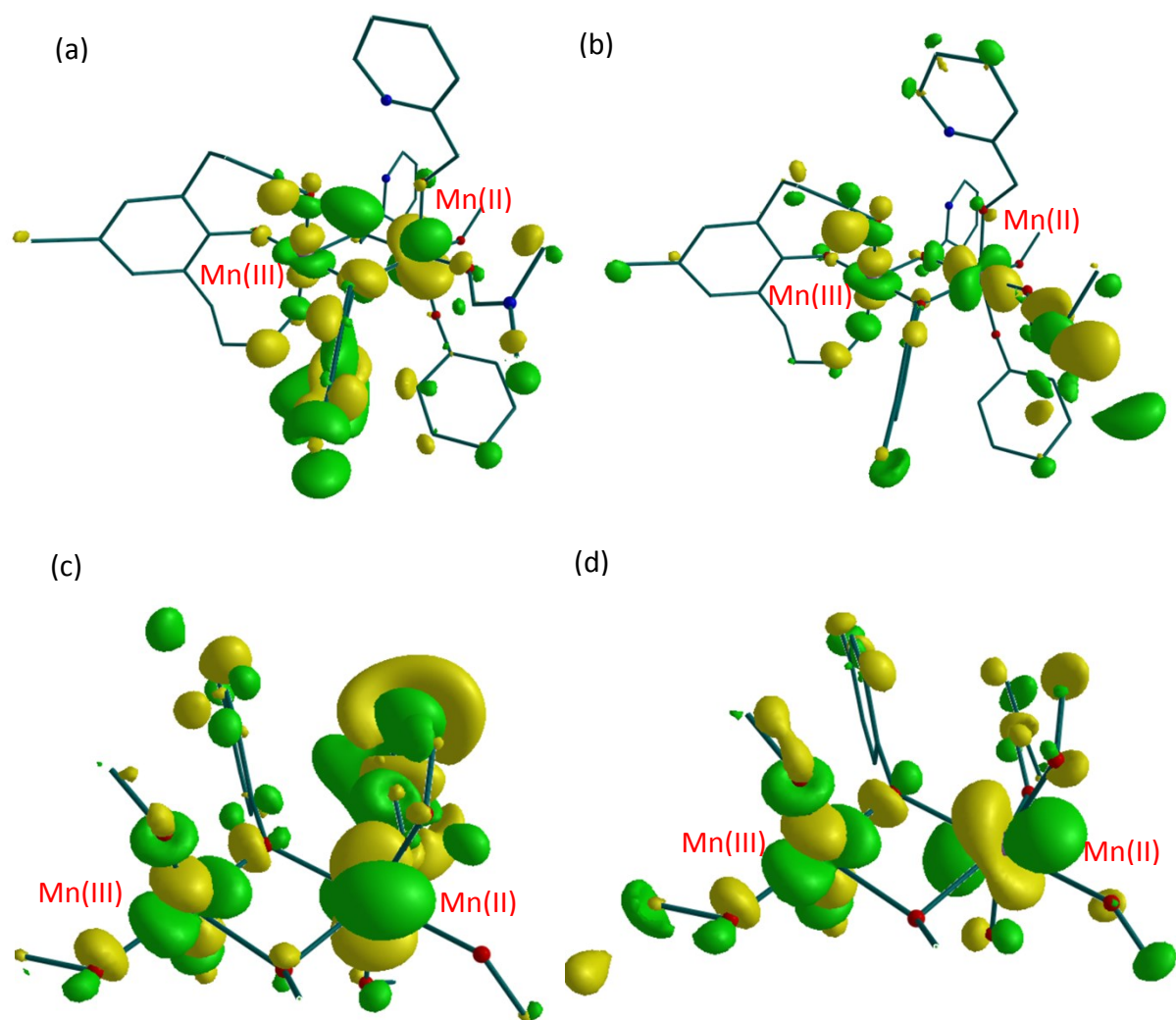


Figure S6. (a)-(b) Representative molecular orbitals showing $\text{Mn(II)}d_{yz} | p | \text{Mn(III)}d_z^2$ and $\text{Mn(II)}d_{x^2-y^2} | p | \text{Mn(III)}d_z^2$ for $\mathbf{3}_{\text{Mn(II)-Mn(III)-1}}$, and (c)-(d) $\text{Mn(II)}d_{yz} | p | \text{Mn(III)}d_z^2$ and $\text{Mn(II)}d_{xz} | p | \text{Mn(III)}d_z^2$ for $\mathbf{3}_{\text{Mn(II)-Mn(III)-2}}$, respectively.

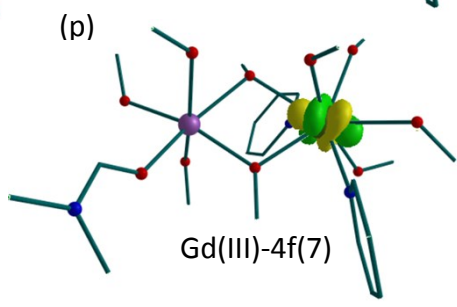
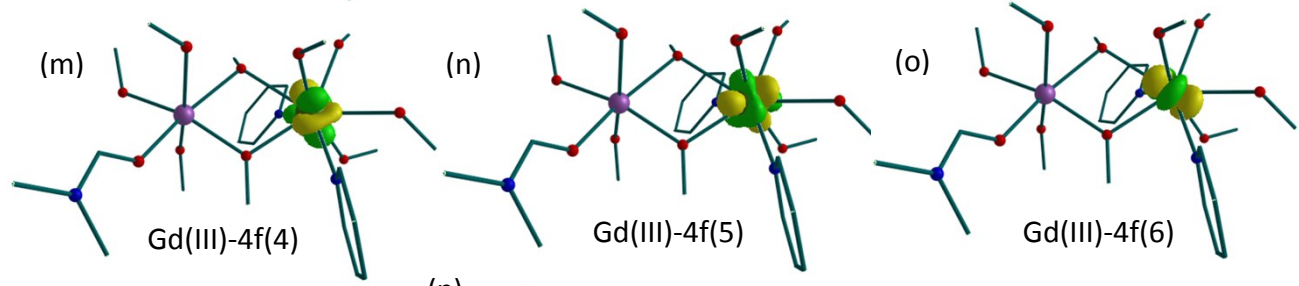
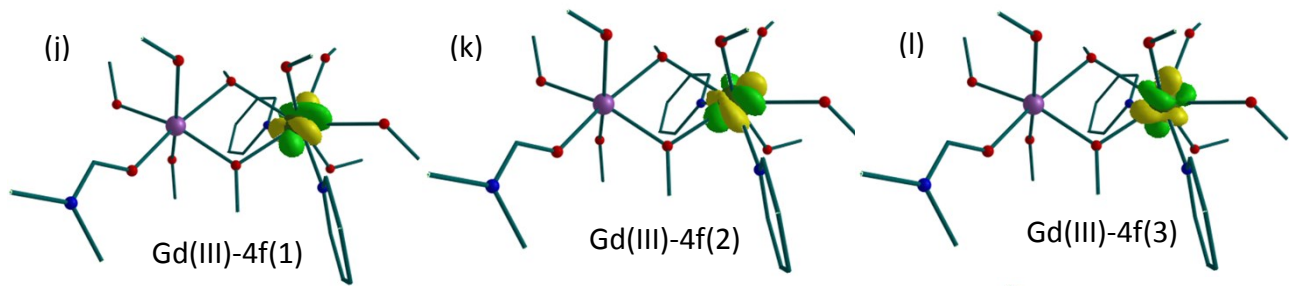
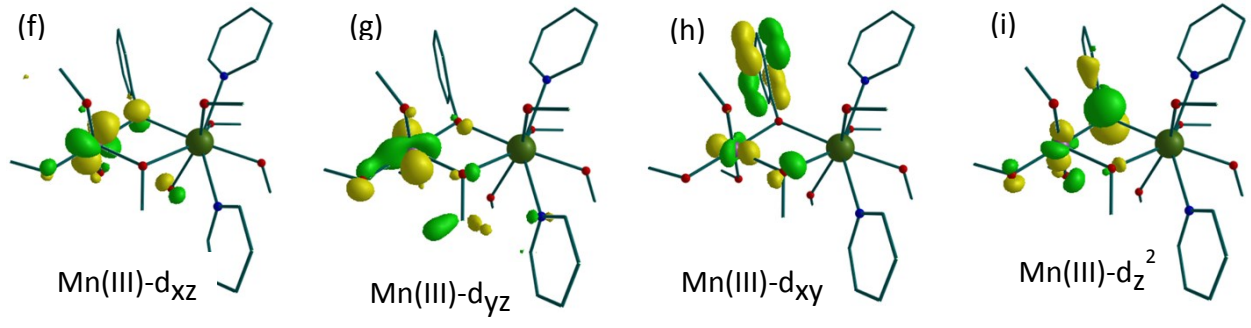
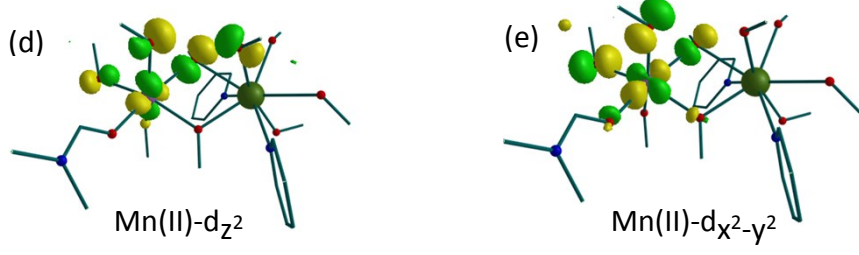
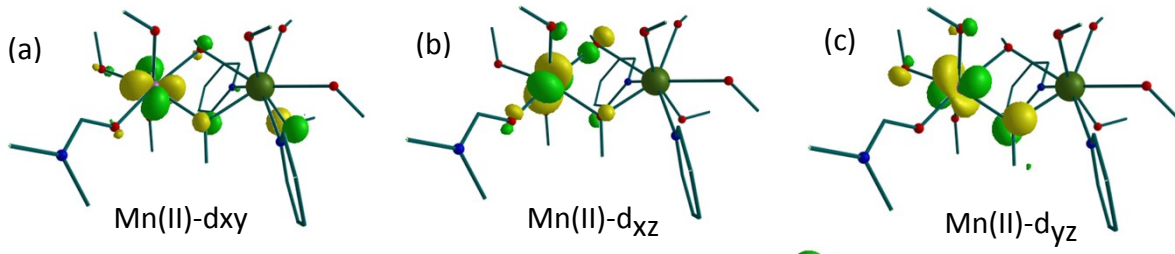


Figure S7. Representative SOMOs for the Mn(II) (a)-(e), Mn(III) (f)-(i) and Gd(III) (j)-(p) ions.

Table S2. DFT computed overlap integral (OI) values corresponding to the $J_{Mn(II)-Gd(III)}^{exchange}$, $J_{Mn(III)-Gd(III)}^{exchange}$ and $J_{Mn(II)-Mn(III)}^{exchange}$ exchange pathways in complex **3**. Here α and β signify spin-up and spin-down orbitals, respectively, with the numbers relating to the corresponding SOMOs.

Gd ^{III} - α	Mn ^{II} - β	OIs	Gd ^{III} - α	Mn ^{III} - β	OIs	Mn ^{II} - α	Mn ^{III} - β	OIs	
4f(1)	d_{xz}	0.003	4f(1)	d_{xz}	0.003	d_{xz}	d_{xz}	0.024	
	d_{yz}	0.010		d_{yz}	0.001	d_{yz}	d_{yz}	0.009	
	d_{xy}	0.010		d_{xy}	0.008	d_{xy}	d_{xy}	0.090	
	$d_{x^2-y^2}$	0.012		d_z^2	0.003	d_z^2	d_z^2	0.065	
	d_z^2	0.009		4f(2)	d_{xz}	0.011	d_{yz}	d_{xz}	0.035
4f(2)	d_{xz}	0.001	d_{yz}		0.011	d_{yz}	d_{yz}	0.001	
	d_{yz}	0.013	d_{xy}	0.005	d_{xy}	d_{xy}	0.027		
	d_{xy}	0.003	d_z^2	0.005	d_z^2	d_z^2	0.102		
	$d_{x^2-y^2}$	0.002	4f(3)	d_{xz}	0.004	d_{xy}	d_{xz}	0.009	
d_z^2	0.014	d_{yz}		0.010	d_{yz}	d_{yz}	0.028		
4f(3)	d_{xz}	0.001		d_{xy}	0.009	d_{xy}	d_{xy}	0.024	
	d_{yz}	0.006	4f(4)	d_z^2	0.010	d_z^2	d_z^2	0.004	
	d_{xy}	0.001		d_{xz}	0.010	$d_{x^2-y^2}$	d_{xz}	0.053	
	$d_{x^2-y^2}$	0.008		d_{yz}	0.006	d_{yz}	d_{yz}	0.043	
d_z^2	0.003	d_{xy}		0.005	d_{xy}	d_{xy}	0.096		
4f(4)	d_{xz}	0.004	4f(5)	d_z^2	0.011	d_z^2	d_z^2	0.075	
	d_{yz}	0.001		d_{xz}	0.011	d_{xz}	d_{xz}	0.017	
	d_{xy}	0.003		d_{yz}	0.003	d_{yz}	d_{yz}	0.032	
	$d_{x^2-y^2}$	0.007		d_{xy}	0.016	d_{xy}	d_{xy}	0.008	
4f(5)	d_z^2	0.004	4f(6)	d_z^2	0.017	d_z^2	d_z^2	0.026	
	d_{xz}	0.004		4f(7)	d_{xz}	0.004			
	d_{yz}	0.001			d_{yz}	0.009			
	d_{xy}	0.003			d_{xy}	0.019			
	$d_{x^2-y^2}$	0.018			d_z^2	0.001			
4f(6)	d_z^2	0.001	4f(8)	d_{xz}	0.000				
	d_{xz}	0.002		d_{yz}	0.003				
	d_{yz}	0.016		d_{xy}	0.200				
	d_{xy}	0.005		d_z^2	0.013				
	$d_{x^2-y^2}$	0.002							
4f(7)	d_z^2	0.011							
	d_{xz}	0.001							
	d_{yz}	0.009							
	d_{xy}	0.006							
4f(8)	$d_{x^2-y^2}$	0.001							
	d_z^2	0.006							

Table S3. DFT computed overlap integral (OI) values corresponding to the magneto-structural correlation developed from model $\mathbf{3}_{\text{Mn(II)-Gd(III)}}$ (Figure S1 (b)) with respect to the average Mn^{II}-O-Gd^{III} angle. Here α and β signify spin-up and spin-down orbitals, respectively. with the numbers relating to the corresponding SOMOs. Here, $\sum Sa(4f)b(3d)$ represents the total OIs between {Gd(III)4f⁷} and {Mn(II)3d⁵} SOMOs. n = number of possible overlap integrals between the SOMOs (for 3d⁵-4f⁷ systems, n = 35).

α	β	89.3 °	93.1 °	100.6 °	104.1 °	107.1 °	115.5 °
		OIs	OIs	OIs	OIs	OIs	OIs
4f(1)	d_{xz}	0.002	0.009	0.018	0.018	0.017	0.002
	d_{yz}	0.019	0.021	0.018	0.016	0.015	0.009
	d_{xy}	0.028	0.026	0.022	0.019	0.016	0.007
	$d_{x^2-y^2}$	0.012	0.010	0.007	0.006	0.006	0.000
	d_z^2	0.001	0.000	0.002	0.002	0.003	0.003
4f(2)	d_{xz}	0.006	0.003	0.003	0.004	0.006	0.014
	d_{yz}	0.007	0.007	0.005	0.003	0.002	0.001
	d_{xy}	0.002	0.000	0.003	0.003	0.004	0.003
	$d_{x^2-y^2}$	0.010	0.007	0.003	0.002	0.002	0.000
	d_z^2	0.003	0.003	0.004	0.005	0.005	0.007
4f(3)	d_{xz}	0.001	0.003	0.008	0.008	0.009	0.016
	d_{yz}	0.002	0.005	0.003	0.002	0.001	0.001
	d_{xy}	0.011	0.012	0.008	0.004	0.001	0.010
	$d_{x^2-y^2}$	0.002	0.003	0.005	0.006	0.006	0.000
	d_z^2	0.001	0.002	0.004	0.004	0.005	0.008
4f(4)	d_{xz}	0.010	0.011	0.011	0.019	0.013	0.011
	d_{yz}	0.016	0.011	0.003	0.004	0.008	0.014
	d_{xy}	0.021	0.014	0.001	0.001	0.002	0.006
	$d_{x^2-y^2}$	0.011	0.010	0.009	0.004	0.002	0.000
	d_z^2	0.003	0.002	0.001	0.014	0.014	0.013
4f(5)	d_{xz}	0.015	0.025	0.022	0.004	0.004	0.015
	d_{yz}	0.035	0.025	0.002	0.000	0.001	0.002
	d_{xy}	0.016	0.011	0.001	0.006	0.011	0.021
	$d_{x^2-y^2}$	0.006	0.007	0.003	0.007	0.006	0.000
	d_z^2	0.008	0.012	0.014	0.003	0.003	0.006
4f(6)	d_{xz}	0.008	0.002	0.006	0.004	0.002	0.008
	d_{yz}	0.002	0.011	0.005	0.004	0.003	0.001
	d_{xy}	0.000	0.007	0.013	0.012	0.010	0.003
	$d_{x^2-y^2}$	0.010	0.003	0.011	0.011	0.010	0.000
	d_z^2	0.015	0.012	0.003	0.003	0.003	0.003
4f(7)	d_{xz}	0.002	0.000	0.013	0.013	0.010	0.013
	d_{yz}	0.008	0.007	0.012	0.010	0.008	0.004
	d_{xy}	0.001	0.003	0.007	0.008	0.009	0.012
	$d_{x^2-y^2}$	0.010	0.013	0.006	0.005	0.003	0.000
	d_z^2	0.007	0.000	0.005	0.003	0.001	0.005
$\sum Sa(4f)b(3d)$		0.311	0.297	0.261	0.237	0.221	0.218
$\sum Sa(4f)b(3d)/n$		0.0089	0.0085	0.0075	0.0068	0.0063	0.0062

Table S4. DFT computed overlap integral (OI) values corresponding to the magneto-structural correlation developed from model $\mathbf{3}_{\text{Mn(III)-Gd(III)}}$ (Figure S1 (c)) with respect to average Mn^{III}-O-Gd^{III} angle. Here α and β signify spin-up and spin-down orbitals, respectively, with the numbers relating to the corresponding SOMOs. Here, $\sum Sa(4f)b(3d)$ represents the total OIs between {Gd(III)4f⁷} and {Mn(III)3d⁴} SOMOs. n = number of possible overlap integrals between the SOMOs (for 3d⁴-4f⁷ systems, n = 28).

α	β	89.4 °	93.8 °	98.3 °	104.0 °	110.5 °	115.5 °	121.2 °
		OIs	OIs	OIs	OIs	OIs	OIs	OIs
4f(1)	d_{xz}	0.008	0.008	0.010	0.010	0.006	0.003	0.007
	d_{yz}	0.015	0.013	0.007	0.007	0.002	0.002	0.001
	d_{xy}	0.018	0.017	0.015	0.013	0.008	0.002	0.000
	d_z^2	0.013	0.018	0.020	0.021	0.027	0.027	0.025
4f(2)	d_{xz}	0.001	0.012	0.000	0.009	0.007	0.007	0.009
	d_{yz}	0.005	0.001	0.002	0.000	0.003	0.002	0.001
	d_{xy}	0.005	0.006	0.005	0.002	0.002	0.003	0.003
	d_z^2	0.009	0.006	0.001	0.002	0.007	0.007	0.007
4f(3)	d_{xz}	0.015	0.008	0.018	0.008	0.006	0.004	0.004
	d_{yz}	0.026	0.012	0.002	0.008	0.015	0.015	0.012
	d_{xy}	0.012	0.004	0.000	0.002	0.005	0.005	0.004
	d_z^2	0.001	0.006	0.007	0.007	0.011	0.011	0.007
4f(4)	d_{xz}	0.011	0.005	0.006	0.008	0.005	0.004	0.008
	d_{yz}	0.017	0.005	0.004	0.001	0.003	0.002	0.000
	d_{xy}	0.010	0.015	0.015	0.015	0.005	0.000	0.001
	d_z^2	0.014	0.016	0.018	0.019	0.020	0.020	0.017
4f(5)	d_{xz}	0.007	0.004	0.002	0.002	0.004	0.003	0.002
	d_{yz}	0.014	0.013	0.007	0.008	0.004	0.005	0.003
	d_{xy}	0.012	0.006	0.013	0.012	0.004	0.004	0.005
	d_z^2	0.005	0.012	0.009	0.014	0.014	0.013	0.012
4f(6)	d_{xz}	0.010	0.003	0.003	0.002	0.001	0.003	0.011
	d_{yz}	0.004	0.003	0.004	0.005	0.013	0.013	0.014
	d_{xy}	0.009	0.011	0.005	0.002	0.011	0.009	0.009
	d_z^2	0.031	0.022	0.010	0.005	0.008	0.004	0.003
4f(7)	d_{xz}	0.004	0.001	0.009	0.009	0.010	0.009	0.004
	d_{yz}	0.016	0.015	0.010	0.009	0.002	0.003	0.000
	d_{xy}	0.009	0.016	0.022	0.023	0.007	0.003	0.005
	d_z^2	0.016	0.022	0.025	0.021	0.011	0.007	0.004
$\sum Sa(4f)b(3d)$		0.317	0.280	0.249	0.244	0.221	0.190	0.178
$\sum Sa(4f)b(3d)/n$		0.0113	0.0100	0.0089	0.0087	0.0079	0.0068	0.0064

Table S5. DFT computed overlap integral (OI) values corresponding to models $\mathbf{3}_{\text{Mn(II)-Mn(III)-1}}$ and $\mathbf{3}_{\text{Mn(II)-Mn(III)-2}}$, respectively (Figure S5). Here α and β signify spin-up and spin-down orbitals, respectively, with the numbers relating to the corresponding SOMOs. Here, $\sum Sa(3d)b(3d)$ represents the total OIs between $\{\text{Mn(II)}3d^5\}$ and $\{\text{Mn(III)}3d^4\}$ SOMOs. n = number of possible overlap integrals between the SOMOs (for $3d^5$ - $3d^4$ systems, $n = 20$).

Mn(III)- β	Mn(II)- α	$\mathbf{3}_{\text{Mn(II)-Mn(III)-1}}$	$\mathbf{3}_{\text{Mn(II)-Mn(III)-2}}$
		OIs	OIs
d_{xz}	d_{xz}	0.005	0.057
	d_{yz}	0.012	0.004
	d_{xy}	0.047	0.018
	$d_{x^2-y^2}$	0.016	0.013
	d_z^2	0.085	0.064
d_{yz}	d_{xz}	0.003	0.028
	d_{yz}	0.049	0.007
	d_{xy}	0.009	0.016
	$d_{x^2-y^2}$	0.004	0.039
	d_z^2	0.029	0.026
d_{xy}	d_{xz}	0.001	0.093
	d_{yz}	0.019	0.005
	d_{xy}	0.019	0.019
	$d_{x^2-y^2}$	0.003	0.026
	d_z^2	0.010	0.020
d_z^2	d_{xz}	0.038	0.017
	d_{yz}	0.139	0.246
	d_{xy}	0.043	0.188
	$d_{x^2-y^2}$	0.178	0.016
	d_z^2	0.030	0.022
$\sum Sa(3d)b(3d)$		0.739	0.924
$\sum Sa(3d)b(3d)/n$		0.037	0.046