## **Supporting Information**

## Intrinsic spin-valley-coupled Dirac state in Janus functionalized $\beta$ -BiAs monolayer

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**Figure S1-a**. Electronic band structures of FBiSbY (Y=Cl, Br and I) MLs without SOC and with SOC.



**Figure S1-b**. Electronic band structures of ClBiSbY (Y=F, Br and I) MLs without SOC and with SOC.



**Figure. S1-c**. Electronic band structures of BrBiSbY (Y=F, Cl and I) MLs without SOC and with SOC.



**Figure. S1-d**. Electronic band structures of IBiSbY (Y=F, Cl, and Br) MLs without SOC and with SOC.



**Figure. S2-a**. Electronic band structures of FBiAsY (Y= Cl, Br and I) MLs without SOC and with SOC.



**Figure. S2-b**. Electronic band structures of ClBiAsY (Y=F, Br and I) MLs without SOC and with SOC.



**Figure. S2-c**. Electronic band structures of BrBiAsY (Y=F and I) MLs without SOC and with SOC.



**Figure. S2-d**. Electronic band structures of IBiAsY (Y=F, Cl and Br) MLs without SOC and with SOC.



**Figure S3.** Cleavage energy  $E_{Cl}$  as a function of the separation distance  $d-d_0$  between two fractured parts of 3D layered BiAs. It can be seen that the cleavage energy increases quickly with the increasing separation distance and then saturates to a value corresponding to the exfoliation energy of about 0.88 J/m<sup>2</sup>, which is comparable with that of *h*-BN (~0.51 J/m<sup>2</sup>). Thus, it is feasible to obtain the BiAs ML by mechanical exfoliation from the layered bulk, like *h*-BN.



**Figure S4.** Electronic band structures of (a)  $\beta$ -BiAs and (b) BrBiAsCl MLs without SOC. The corresponding orbital-resolved electronic band structures for Bi and As atoms are displayed at the same row. It can be seen that  $\beta$ -BiAs ML is a direct semiconductor. The valence band maximum (VBM) at  $\Gamma$  point is mainly contributed by hybridization of Bi- $p_{xy}$  and As- $p_{xy}$  states, while the conduction band minimum (CBM) originates from Bi- $p_z$  and As- $p_z$  states, as well as few contributions of *s* state. Note that at the higher-lying valence band, the contribution of  $p_z$  for both Bi and As is obvious. Unlike the case of  $\beta$ -BiAs ML, BrBiAsCl ML is a direct semiconductor with greatly reduced band gap (0.772 eV) at K point. Since the electronegativity of halogen atoms is larger than that of both Bi and As atoms, the  $p_z$  electrons of the  $\beta$ -BiAs ML transfer to the halogen atoms. Therefore, the Fermi level shifts down, and the  $p_z$  states of  $\beta$ -BiAs ML strongly couple with the *s* states of halogen atoms at the deep energy level. It can be seen that the  $p_z$  state has almost no contribution to both valance and conduction bands in the vicinity of Fermi level for BrBiAsCl ML. The VBM is mainly contributed by As $p_{xy}$  and Bi-*s* orbitals, while the main contribution of CBM is As-s and Bi- $p_{xy}$  orbitals.



**Figure S5.** The electronic band structures calculated from both HSE06 (black dashed line) and GGA/PBE (red solid line) with SOC for BrBiAsCl ML. While the bands from HSE06 show some shifts with respect to the bands of PBE, the spin-splitted Dirac state is well preserved except for the change of dispersion slope. This further confirms that BrBiAsCl ML is an intrinsic svc-DSM.



**Figure S6**. The orbital-resolved band structures in the vicinity of Fermi level for Bi atoms of BrBiAsCl ML under -4% and 4% external strain. It can be seen that the energy order between *s* and  $p_{xy}$  states have been changed under strain. This means that there exists the strain induced band inversion, namely topological phase transition should occur under external strains from -4% to 4%.



**Figure S7.** In-plane spin textures ( $S_x$  and  $S_y$ ) calculated at the iso-energy surface of 0.6 eV blow the Fermi level for BrBiAsCl@*h*-BN heterostructure. From the spin projected constant energy contour plots of the spin textures in the  $k_x$ - $k_y$  plane centred at the K point, one can see the similar Rashba SOC effect like in pristine BrBiAsCl ML. Firstly, the pair of spin-splitting bands have opposite spin orientation for both  $S_x$  and  $S_y$  spin component. Secondly, the in-plane spin moments at the two rings have opposite chirality. This indicates the existence of spin-momentum locking, namely the spin orientation is perpendicular to the electron momentum.