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Emergent quasiparticles in Euclidean tiling

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Abstract

k = 4 LATTICES

t4001

Tiling reference number t4001 with space-group P6/mmm' (191) and 25 sites in the unit cell, with vertex type indicated in Tab. S1. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S1.



FIG. S1. t4001 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4002 with space-group 'P6/mmm' (191) and 26 sites in the unit cell, with vertex type indicated in Tab. S2. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S2.

A	В	С	D	Е	F	G	Η	Ι	J	K	L	М	Ν	0
2	0	12	0	0	0	0	0	0	0	0	0	0	0	12

TABLE S2. Tiling t4002 vertex types



FIG. S2. t4002 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4003 with space-group 'Cmmm' (65) and 14 sites in the unit cell, with vertex type indicated in Tab. S3. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S3.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	4	0	0	0	0	0	0	0	2	0	0	4	4

TABLE S3. Tiling t4003 vertex types



FIG. S3. t4003 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4004 with space-group 'Cmmm' (65) and 11 sites in the unit cell, with vertex type indicated in Tab. S4. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S4.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
1	0	4	0	0	0	0	0	0	0	0	0	0	0	6

TABLE S4. Tiling t4004 vertex types



FIG. S4. t4004 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4005 with space-group 'Pmma' (51) and 14 sites in the unit cell, with vertex type indicated in Tab. S5. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S5.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
2	0	4	0	0	0	0	0	4	0	0	0	0	0	4

TABLE S5. Tiling t4005 vertex types



FIG. S5. t4005 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4006 with space-group 'Pm' (6) and 30 sites in the unit cell, with vertex type indicated in Tab. S6. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S6.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	6	0	0	0	1	0	0	6	0	0	0	11	6

TABLE S6.Tiling t4006 vertex types



FIG. S6. t4006 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4007 with space-group 'P6/mmm' (191) and 20 sites in the unit cell, with vertex type indicated in Tab. S7. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S7.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
2	0	6	0	0	0	0	0	0	0	0	0	0	0	12



FIG. S7. t4007 lattice framework, nearest neighbors band structure and radial distribution function.

TABLE S7. Tiling t4007 vertex types

Tiling reference number t4008 with space-group 'P6/mmm' (191) and 27 sites in the unit cell, with vertex type indicated in Tab. S8. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S8.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
3	0	6	0	0	0	0	0	0	0	0	0	0	0	18

TABLE S8. Tiling t4008 vertex types



FIG. S8. t4008 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4009 with space-group 'P6/m' (175) and 21 sites in the unit cell, with vertex type indicated in Tab. S9. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S9.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	6	0	0	0	0	3	6	0	0	0	0	0	6

TABLE S9.Tiling t4009 vertex types



FIG. S9. t4009 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4010 with space-group 'P6/m' (175) and 24 sites in the unit cell, with vertex type indicated in Tab. S10. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S10.

				TA	BLE S	510. Т	Tiling t	4010 ve	rtex ty	pes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	6	0	0	0	0	0	12	0	0	0	0	0	6



FIG. S10. t4010 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4011 with space-group 'Cmmm' (65) and 8 sites in the unit cell, with vertex type indicated in Tab. S11. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S11.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	2	0	0	0	0	2	0	0	0	0	0	0	4





FIG. S11. t4011 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4012 with space-group 'Cmmm' (65) and 7 sites in the unit cell, with vertex type indicated in Tab. S12. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S12.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
1	0	2	0	0	0	0	0	2	0	0	0	0	0	2

TABLE S12. Tiling t4012 vertex types



FIG. S12. t4012 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4013 with space-group 'Pmma' (51) and 8 sites in the unit cell, with vertex type indicated in Tab. S13. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S13.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
2	0	2	0	0	0	0	0	2	0	0	0	0	0	2





FIG. S13. t4013 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4014 with space-group 'P6/mmm' (191) and 19 sites in the unit cell, with vertex type indicated in Tab. S14. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S14.

				TA	BLE S	14. Ti	ling t4	014 ve	rtex ty	rpes				
А	В	С	D	Е	F	G	Η	Ι	J	Κ	L	М	Ν	0
1	0	12	0	0	0	0	0	0	0	0	0	0	0	6



FIG. S14. t4014 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4015 with space-group 'Pmmm' (47) and 7 sites in the unit cell, with vertex type indicated in Tab. S15. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S15.

				TA	BLE S	15. T	iling t4	1015 ve	ertex ty	ypes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	4	0	0	0	0	1	0	0	0	0	0	0	2



FIG. S15. t4015 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4016 with space-group 'Cmmm' (65) and 8 sites in the unit cell, with vertex type indicated in Tab. S16. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S16.

				TA	BLE S	16. T	iling t4	016 ve	rtex ty	vpes				
A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	4	0	0	0	0	0	2	0	0	0	0	0	2



FIG. S16. t4016 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4017 with space-group 'P6/m' (175) and 15 sites in the unit cell, with vertex type indicated in Tab. S17. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S17.

									v	•				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
1	0	8	0	0	0	0	0	0	0	0	0	0	0	6

TABLE S17. Tiling t4017 vertex types



FIG. S17. t4017 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4018 with space-group 'Pmmm' (47) and 12 sites in the unit cell, with vertex type indicated in Tab. S18. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S18.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	2	0	0	0	0	0	0	0	2	0	0	4	4

TABLE S18. Tiling t4018 vertex types



FIG. S18. t4018 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4019 with space-group 'Pmmm' (47) and 9 sites in the unit cell, with vertex type indicated in Tab. S19. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S19.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
1	0	2	0	0	0	0	0	0	0	0	0	0	0	6

TABLE S19. Tiling t4019 vertex types



FIG. S19. t4019 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4020 with space-group 'Cmmm' (65) and 12 sites in the unit cell, with vertex type indicated in Tab. S20. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S20.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
2	0	2	0	0	0	0	0	4	0	0	0	0	0	4





FIG. S20. t4020 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4021 with space-group 'Cmmm' (65) and 11 sites in the unit cell, with vertex type indicated in Tab. S21. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S21.

A	В	С	D	Е	F	G	Η	Ι	J	K	L	М	Ν	0
0	0	2	0	0	0	0	5	0	0	0	0	0	0	4





FIG. S21. t4021 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4022 with space-group P2/m' (10) and 20 sites in the unit cell, with vertex type indicated in Tab. S22. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S22.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	2	0	0	0	0	12	0	0	0	0	0	0	6

TABLE S22. Tiling t4022 vertex types



FIG. S22. t4022 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4023 with space-group 'P - 6' (174) and 10 sites in the unit cell, with vertex type indicated in Tab. S23. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S23.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
0	0	1	0	0	0	0	3	3	0	0	0	0	0	3

TABLE S23. Tiling t4023 vertex types



FIG. S23. t4023 lattice framework, nearest neighbors band structure and radial distribution function.

24

Tiling reference number t4024 with space-group 'P - 62m' (189) and 13 sites in the unit cell, with vertex type indicated in Tab. S24. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S24.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	1	0	0	0	0	0	9	0	0	0	0	0	3

TABLE S24. Tiling t4024 vertex types



FIG. S24. t4024 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4025 with space-group 'Amm2' (38) and 48 sites in the unit cell, with vertex type indicated in Tab. S25. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S25.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
0	0	0	0	12	0	12	0	0	0	0	0	0	24	0

TABLE S25. Tiling t4025 vertex types



FIG. S25. t4025 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4026 with space-group 'Amm2' (38) and 42 sites in the unit cell, with vertex type indicated in Tab. S26. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S26.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	0	12	0	0	0	0	0	6	0	0	12	12

TABLE S26. Tiling t4026 vertex types



FIG. S26. t4026 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4027 with space-group 'Amm2' (38) and 36 sites in the unit cell, with vertex type indicated in Tab. S27. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S27.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	12	0	1	0	0	6	0	0	0	11	6

TABLE S27. Tiling t4027 vertex types



FIG. S27. t4027 lattice framework, nearest neighbors band structure and radial distribution function.

1.0

1.5

2.0

2.5

coordination shell (d_{NN})

3.0

3.5

4.0

Tiling reference number t4028 with space-group 'Amm2' (38) and 42 sites in the unit cell, with vertex type indicated in Tab. S28. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S28.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	24	0	7	0	0	0	0	0	0	11	0



TABLE S28. Tiling t4028 vertex types

FIG. S28. t4028 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4029 with space-group 'Pm' (6) and 42 sites in the unit cell, with vertex type indicated in Tab. S29. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S29.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	24	0	18	0	0	0	0	0	0	0	0

TABLE S29. Tiling t4029 vertex types



FIG. S29. t4029 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4030 with space-group 'Pm' (6) and 14 sites in the unit cell, with vertex type indicated in Tab. S30. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S30.

A	В	С	D	Е	F	G	Η	Ι	J	Κ	L	М	Ν	0
0	0	0	0	4	0	2	0	0	0	0	4	4	0	0

TABLE S30.Tiling t4030 vertex types



FIG. S30. t4030 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4031 with space-group 'Pm' (6) and 30 sites in the unit cell, with vertex type indicated in Tab. S31. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S31.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	12	0	0	6	0	0	0	0	12	0	0	0





FIG. S31. t4031 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4032 with space-group 'Amm2' (38) and 30 sites in the unit cell, with vertex type indicated in Tab. S32. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S32.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	12	0	0	6	0	0	0	0	0	12	0	0





FIG. S32. t4032 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4033 with space-group 'Amm2' (38) and 28 sites in the unit cell, with vertex type indicated in Tab. S33. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S33.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	20	0	0	0	0	0	0	0	0	8	0	0

TABLE S33. Tiling t4033 vertex types



FIG. S33. t4033 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4034 with space-group 'Amm2' (38) and 25 sites in the unit cell, with vertex type indicated in Tab. S34. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S34.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
1	0	0	6	0	0	0	0	0	6	0	12	0	0	0





FIG. S34. t4034 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4035 with space-group 'Pm' (6) and 25 sites in the unit cell, with vertex type indicated in Tab. S35. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S35.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
1	0	0	6	0	0	0	0	0	6	0	0	12	0	0

TABLE S35. Tiling t4035 vertex types



FIG. S35. t4035 lattice framework, nearest neighbors band structure and radial distribution function.
Tiling reference number t4036 with space-group 'Pmmm' (47) and 12 sites in the unit cell, with vertex type indicated in Tab. S36. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S36.

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А	В	С	D	Е	F	G	Η	Ι	J	Κ	L	М	Ν	0
0	0	0	2	0	0	0	0	0	0	2	4	4	0	0

TABLE S36. Tiling t4036 vertex types



FIG. S36. t4036 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4037 with space-group 'Pm' (6) and 14 sites in the unit cell, with vertex type indicated in Tab. S37. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S37.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	2	0	0	0	0	0	0	4	4	4	0	0

TABLE S37. Tiling t4037 vertex types



FIG. S37. t4037 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4038 with space-group 'Cmmm' (65) and 8 sites in the unit cell, with vertex type indicated in Tab. S38. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S38.

А	В	С	D	Е	F	G	Η	Ι	J	Κ	L	М	Ν	Ο
0	6	0	0	0	0	0	0	0	0	2	0	0	0	0

TABLE S38. Tiling t4038 vertex types



FIG. S38. t4038 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4039 with space-group 'Cmmm' (65) and 13 sites in the unit cell, with vertex type indicated in Tab. S39. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S39.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	8	0	0	0	0	0	1	0	0	0	0	0	4	0

TABLE S39. Tiling t4039 vertex types



FIG. S39. t4039 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4040 with space-group 'Pmmm' (47) and 13 sites in the unit cell, with vertex type indicated in Tab. S40. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S40.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
0	8	0	0	0	0	0	1	0	0	0	0	0	4	0

TABLE S40. Tiling t4040 vertex types



FIG. S40. t4040 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4041 with space-group Pmm2' (25) and 8 sites in the unit cell, with vertex type indicated in Tab. S41. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S41.

А	В	\mathbf{C}	D	Ε	\mathbf{F}	G	Η	Ι	J	Κ	\mathbf{L}	М	Ν	0
0	4	0	0	0	0	0	0	0	0	4	0	0	0	0
							Energy (t)	4 2- -2 -4		NN b	band			
				ation	4		RDF							

TABLE S41. Tiling t4041 vertex types

FIG. S41. t4041 lattice framework, nearest neighbors band structure and radial distribution function.

2.0

2.5

coordination shell (d_{NN})

3.0

3.5

4.0

mean coordi 2

1 0 1.0

1.5

Tiling reference number t4042 with space-group 'Pmmm' (47) and 7 sites in the unit cell, with vertex type indicated in Tab. S42. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S42.

А	В	\mathbf{C}	D	Ε	\mathbf{F}	G	Η	Ι	J	Κ	\mathbf{L}	М	Ν	0
1	4	0	0	0	0	0	0	0	0	2	0	0	0	0
							Energy (t)	4 2- -2- -4-		NN b	and			
				mean coordination	4 3 2 1 0 1.0	1.5	RDF	<u> </u>	3.5	4.0				

TABLE S42. Tiling t4042 vertex types

FIG. S42. t4042 lattice framework, nearest neighbors band structure and radial distribution function.

coordination shell (d_{NN})

Tiling reference number t4043 with space-group 'Cmmm' (65) and 8 sites in the unit cell, with vertex type indicated in Tab. S43. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S43.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	N	0
2	4	0	0	0	0	0	0	0	0	2	0	0	0	0

TABLE S43. Tiling t4043 vertex types



FIG. S43. t4043 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4044 with space-group 'Amm2' (38) and 14 sites in the unit cell, with vertex type indicated in Tab. S44. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S44.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	4	0	0	0	0	0	2	0	0	0	0	0	8	0

TABLE S44. Tiling t4044 vertex types



FIG. S44. t4044 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4045 with space-group 'Pmma' (51) and 14 sites in the unit cell, with vertex type indicated in Tab. S45. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S45.

A	В	С	D	Е	F	G	Η	Ι	J	K	L	М	Ν	0
0	4	0	0	0	0	0	2	0	0	0	0	0	8	0





FIG. S45. t4045 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4046 with space-group 'Cmmm' (65) and 12 sites in the unit cell, with vertex type indicated in Tab. S46. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S46.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
0	4	0	0	0	0	0	2	0	0	0	0	0	4	2





FIG. S46. t4046 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4047 with space-group 'Pmma' (51) and 12 sites in the unit cell, with vertex type indicated in Tab. S47. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S47.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	4	0	0	0	0	0	4	0	0	0	0	0	4	0





1.5 2.0 2.5 3.0 coordination shell (d_{NN})

3.5

4.0

mean coordination

0

1.0

TABLE S47. Tiling t4047 vertex types

Tiling reference number t4048 with space-group 'Pmmm' (47) and 14 sites in the unit cell, with vertex type indicated in Tab. S48. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S48.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	4	0	0	0	0	0	2	0	0	0	0	0	8	0

TABLE S48. Tiling t4048 vertex types



FIG. S48. t4048 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4049 with space-group 'Amm2' (38) and 14 sites in the unit cell, with vertex type indicated in Tab. S49. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S49.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	4	0	0	0	0	0	2	0	0	0	0	0	8	0

TABLE S49. Tiling t4049 vertex types



FIG. S49. t4049 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4050 with space-group 'Pmmm' (47) and 12 sites in the unit cell, with vertex type indicated in Tab. S50. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S50.

A	В	С	D	Е	F	G	Η	Ι	J	Κ	L	М	Ν	0
0	4	0	0	0	0	0	2	0	0	0	0	0	4	2

TABLE S50. Tiling t4050 vertex types



S

FIG. S50. t4050 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4051 with space-group 'Amm2' (38) and 12 sites in the unit cell, with vertex type indicated in Tab. S51. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S51.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	4	0	0	0	0	0	4	0	0	0	0	0	4	0

TABLE S51. Tiling t4051 vertex types



FIG. S51. t4051 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4052 with space-group Pmm2' (25) and 7 sites in the unit cell, with vertex type indicated in Tab. S52. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S52.

А	В	С	D	Е	F	G	Η	Ι	J	Κ	L	М	Ν	0
0	3	0	0	0	0	0	0	0	0	4	0	0	0	0

TABLE S52. Tiling t4052 vertex types



FIG. S52. t4052 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4053 with space-group 'Cmmm' (65) and 8 sites in the unit cell, with vertex type indicated in Tab. S53. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S53.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	2	0	0	0	0	0	0	0	0	6	0	0	0	0

TABLE S53. Tiling t4053 vertex types



FIG. S53. t4053 lattice framework, nearest neighbors band structure and radial distribution function.

А

В

 \mathbf{C}

D

Е

 \mathbf{F}

G

Tiling reference number t4054 with space-group 'Pmmm' (47) and 8 sites in the unit cell, with vertex type indicated in Tab. S54. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S54.

2	2	0	0	0	0	0	0	0	0	4	0	0	0	
							Energy (t)	4 2- 0- -2 -4		NN b	eand		5	
					- [RDF			-				
				mean coordination	5- 3- 2- 1- 0	1.5 2 coordir	2.0 2.5 nation sł	3.0 mell (<i>d</i> _{MM}	3.5	4.0				

TABLE S54. Tiling t4054 vertex types

Η

Ι

J

Κ

 \mathbf{L}

Μ

Ν

_

0

0

FIG. S54. t4054 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4055 with space-group Pmm2' (25) and 7 sites in the unit cell, with vertex type indicated in Tab. S55. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S55.

А	В	С	D	Е	\mathbf{F}	G	Н	Ι	J	Κ	L	М	Ν	0
3	2	0	0	0	0	0	0	0	0	2	0	0	0	0

TABLE S55. Tiling t4055 vertex types



FIG. S55. t4055 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4056 with space-group 'Cmmm' (65) and 8 sites in the unit cell, with vertex type indicated in Tab. S56. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S56.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
4	2	0	0	0	0	0	0	0	0	2	0	0	0	0

TABLE S56. Tiling t4056 vertex types



FIG. S56. t4056 lattice framework, nearest neighbors band structure and radial distribution function.

57

Tiling reference number t4057 with space-group 'P4/m' (83) and 16 sites in the unit cell, with vertex type indicated in Tab. S57. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S57.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	4	0	0	0	0	0	0	0	4	8	0	0	0	0

TABLE S57. Tiling t4057 vertex types



FIG. S57. t4057 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4058 with space-group 'Cmmm' (65) and 7 sites in the unit cell, with vertex type indicated in Tab. S58. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S58.

										<u> </u>				
A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	5	0	0	0	0	0	0	0	0	2	0	0	0	0



FIG. S58. t4058 lattice framework, nearest neighbors band structure and radial distribution function.

TABLE S58. Tiling t4058 vertex types

Tiling reference number t4059 with space-group 'Amm2' (38) and 11 sites in the unit cell, with vertex type indicated in Tab. S59. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S59.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	6	0	0	0	0	0	1	0	0	0	0	0	4	0





FIG. S59. t4059 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4060 with space-group Pmm2' (25) and 11 sites in the unit cell, with vertex type indicated in Tab. S60. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S60.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	6	0	0	0	0	0	1	0	0	0	0	0	4	0

TABLE S60. Tiling t4060 vertex types



FIG. S60. t4060 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4061 with space-group 'Pmmm' (47) and 7 sites in the unit cell, with vertex type indicated in Tab. S61. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S61.

А	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	Ο
0	3	0	0	0	0	0	0	0	0	4	0	0	0	0

TABLE S61. Tiling t4061 vertex types



FIG. S61. t4061 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4062 with space-group Pmm2' (25) and 6 sites in the unit cell, with vertex type indicated in Tab. S62. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S62.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
1	3	0	0	0	0	0	0	0	0	2	0	0	0	0

TABLE S62. Tiling t4062 vertex types



FIG. S62. t4062 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4063 with space-group 'Cmmm' (65) and 7 sites in the unit cell, with vertex type indicated in Tab. S63. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S63.

А	В	С	D	Е	F	G	Η	Ι	J	Κ	L	М	Ν	0
2	3	0	0	0	0	0	0	0	0	2	0	0	0	0

TABLE S63. Tiling t4063 vertex types



FIG. S63. t4063 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4064 with space-group 'Cmmm' (65) and 12 sites in the unit cell, with vertex type indicated in Tab. S64. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S64.

A	В	С	D	Е	F	G	Η	Ι	J	K	L	М	Ν	0
0	2	0	0	0	0	0	2	0	0	0	0	0	8	0

TABLE S64. Tiling t4064 vertex types



FIG. S64. t4064 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4065 with space-group 'Pmma' (51) and 12 sites in the unit cell, with vertex type indicated in Tab. S65. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S65.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
0	2	0	0	0	0	0	2	0	0	0	0	0	8	0





FIG. S65. t4065 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4066 with space-group 'Cmmm' (65) and 10 sites in the unit cell, with vertex type indicated in Tab. S66. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S66.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	2	0	0	0	0	0	2	0	0	0	0	0	4	2





FIG. S66. t4066 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4067 with space-group 'Pmma' (51) and 10 sites in the unit cell, with vertex type indicated in Tab. S67. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S67.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	2	0	0	0	0	0	4	0	0	0	0	0	4	0





FIG. S67. t4067 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4068 with space-group Pmm2' (25) and 12 sites in the unit cell, with vertex type indicated in Tab. S68. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S68.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	2	0	0	0	0	0	2	0	0	0	0	0	8	0





FIG. S68. t4068 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4069 with space-group 'Cmmm' (65) and 12 sites in the unit cell, with vertex type indicated in Tab. S69. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S69.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	2	0	0	0	0	0	2	0	0	0	0	0	8	0





FIG. S69. t4069 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4070 with space-group 'Pmmm' (47) and 10 sites in the unit cell, with vertex type indicated in Tab. S70. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S70.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	2	0	0	0	0	0	2	0	0	0	0	0	4	2

TABLE S70. Tiling t4070 vertex types



FIG. S70. t4070 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4071 with space-group 'Cmmm' (65) and 10 sites in the unit cell, with vertex type indicated in Tab. S71. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S71.

A	В	С	D	Е	F	G	Η	Ι	J	K	L	М	Ν	0
0	2	0	0	0	0	0	4	0	0	0	0	0	4	0

TABLE S71. Tiling t4071 vertex types



FIG. S71. t4071 lattice framework, nearest neighbors band structure and radial distribution function.

1.5 2.0 2.5 3.0 coordination shell (d_{NN})

3.5

4.0

0

1.0
Tiling reference number t4072 with space-group 'Cmmm' (65) and 7 sites in the unit cell, with vertex type indicated in Tab. S72. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S72.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	1	0	0	0	0	0	0	0	0	6	0	0	0	0

TABLE S72. Tiling t4072 vertex types



FIG. S72. t4072 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4073 with space-group 'Pmmm' (47) and 7 sites in the unit cell, with vertex type indicated in Tab. S73. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S73.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
2	1	0	0	0	0	0	0	0	0	4	0	0	0	0

TABLE S73. Tiling t4073 vertex types



FIG. S73. t4073 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4074 with space-group 'Pmmm' (47) and 6 sites in the unit cell, with vertex type indicated in Tab. S74. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S74.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
3	1	0	0	0	0	0	0	0	0	2	0	0	0	0

TABLE S74. Tiling t4074 vertex types



FIG. S74. t4074 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4075 with space-group 'Cmmm' (65) and 7 sites in the unit cell, with vertex type indicated in Tab. S75. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S75.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
4	1	0	0	0	0	0	0	0	0	2	0	0	0	0

TABLE S75. Tiling t4075 vertex types



FIG. S75. t4075 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4076 with space-group 'Cmmm' (65) and 8 sites in the unit cell, with vertex type indicated in Tab. S76. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S76.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	2	0	0	0	0	0	0	0	0	6	0	0	0	0

TABLE S76. Tiling t4076 vertex types



FIG. S76. t4076 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4077 with space-group 'Amm2' (38) and 7 sites in the unit cell, with vertex type indicated in Tab. S77. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S77.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
1	2	0	0	0	0	0	0	0	0	4	0	0	0	0

TABLE S77. Tiling t4077 vertex types



FIG. S77. t4077 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4078 with space-group 'Pmma' (51) and 8 sites in the unit cell, with vertex type indicated in Tab. S78. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S78.

А	В	\mathbf{C}	D	\mathbf{E}	\mathbf{F}	G	Η	Ι	J	Κ	\mathbf{L}	Μ	Ν	Ο
2	2	0	0	0	0	0	0	0	0	4	0	0	0	0
							Energy (t)	2 0 -2 -4		NN b	hand		· · · · · · · · · · · · · · · · · · ·	
					5F 1		RDF			7				
				mean coordination	4- 3- 2- 1- 0	1.5	2.0 2.5	5 3.0	3.5	4.0				

TABLE S78. Tiling t4078 vertex types

FIG. S78. t4078 lattice framework, nearest neighbors band structure and radial distribution function.

coordination shell (d_{NN})

Tiling reference number t4079 with space-group 'P4/mbm' (127) and 24 sites in the unit cell, with vertex type indicated in Tab. S79. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S79.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	4	0	0	0	0	0	0	0	8	12	0	0	0	0

TABLE S79. Tiling t4079 vertex types



FIG. S79. t4079 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4080 with space-group 'Pm' (6) and 26 sites in the unit cell, with vertex type indicated in Tab. S80. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S80.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
0	2	0	0	0	0	8	0	0	0	0	0	0	16	0

TABLE S80. Tiling t4080 vertex types



FIG. S80. t4080 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4081 with space-group 'Amm2' (38) and 17 sites in the unit cell, with vertex type indicated in Tab. S81. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S81.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	1	0	0	0	0	0	0	0	0	4	8	4	0	0

TABLE S81. Tiling t4081 vertex types



FIG. S81. t4081 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4082 with space-group 'Amm2' (38) and 16 sites in the unit cell, with vertex type indicated in Tab. S82. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S82.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
2	2	0	0	0	0	0	0	0	4	8	0	0	0	0





FIG. S82. t4082 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4083 with space-group 'Amm2' (38) and 36 sites in the unit cell, with vertex type indicated in Tab. S83. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S83.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	6	6	0	0	0	0	0	24	0

TABLE S83. Tiling t4083 vertex types



FIG. S83. t4083 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4084 with space-group 'P - 6m2' (187) and 25 sites in the unit cell, with vertex type indicated in Tab. S84. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S84.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
1	0	0	0	0	0	6	0	0	6	0	0	0	12	0



FIG. S84. t4084 lattice framework, nearest neighbors band structure and radial distribution function.

TABLE S84. Tiling t4084 vertex types

Tiling reference number t4085 with space-group 'Cmmm' (65) and 12 sites in the unit cell, with vertex type indicated in Tab. S85. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S85.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	0	0	0	4	0	0	2	0	0	0	4	2

TABLE S85. Tiling t4085 vertex types



FIG. S85. t4085 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4086 with space-group 'Cmmm' (65) and 11 sites in the unit cell, with vertex type indicated in Tab. S86. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S86.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	0	0	0	0	3	0	0	0	0	0	4	4

TABLE S86. Tiling t4086 vertex types





С

FIG. S86. t4086 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4087 with space-group 'Cmmm' (65) and 11 sites in the unit cell, with vertex type indicated in Tab. S87. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S87.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	0	0	0	0	7	0	0	0	0	0	4	0





FIG. S87. t4087 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4088 with space-group 'Pmma' (51) and 12 sites in the unit cell, with vertex type indicated in Tab. S88. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S88.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
2	0	0	0	0	0	0	2	4	0	0	0	0	4	0





FIG. S88. t4088 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4089 with space-group 'Pmmm' (47) and 11 sites in the unit cell, with vertex type indicated in Tab. S89. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S89.

A	В	С	D	Е	F	G	Η	Ι	J	K	L	М	Ν	0
0	0	0	0	0	0	0	3	0	0	0	0	0	4	4





FIG. S89. t4089 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4090 with space-group 'Pmmm' (47) and 11 sites in the unit cell, with vertex type indicated in Tab. S90. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S90.

				TA	BLE S	590. T	iling t4	090 ve	rtex ty	ypes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	0	7	0	0	0	0	0	4	0



FIG. S90. t4090 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4091 with space-group 'Cmmm' (65) and 12 sites in the unit cell, with vertex type indicated in Tab. S91. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S91.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
2	0	0	0	0	0	0	2	4	0	0	0	0	4	0

TABLE S91. Tiling t4091 vertex types





FIG. S91. t4091 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4092 with space-group 'Amm2' (38) and 11 sites in the unit cell, with vertex type indicated in Tab. S92. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S92.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
2	0	0	0	0	0	0	1	0	0	4	0	0	4	0

TABLE S92. Tiling t4092 vertex types





FIG. S92. t4092 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4093 with space-group 'Amm2' (38) and 11 sites in the unit cell, with vertex type indicated in Tab. S93. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S93.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	0	0	0	6	1	0	0	0	0	0	4	0





FIG. S93. t4093 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4094 with space-group 'P6/mmm' (191) and 36 sites in the unit cell, with vertex type indicated in Tab. S94. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S94.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	18	6	0	0	0	0	0	12	0



FIG. S94. t4094 lattice framework, nearest neighbors band structure and radial distribution function.

TABLE S94. Tiling t4094 vertex types

Tiling reference number t4095 with space-group 'Amm2' (38) and 30 sites in the unit cell, with vertex type indicated in Tab. S95. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S95.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	0	0	0	6	12	0	0	0	0	0	12	0

TABLE S95. Tiling t4095 vertex types



FIG. S95. t4095 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4096 with space-group Pmm2' (25) and 11 sites in the unit cell, with vertex type indicated in Tab. S96. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S96.

A	В	С	D	Е	F	G	Η	Ι	J	K	L	М	Ν	0
1	0	0	0	0	0	0	0	2	0	4	0	0	4	0

TABLE S96. Tiling t4096 vertex types



FIG. S96. t4096 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4097 with space-group 'Cmmm' (65) and 12 sites in the unit cell, with vertex type indicated in Tab. S97. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S97.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	0	0	0	0	0	2	6	0	0	0	4	0

TABLE S97. Tiling t4097 vertex types



FIG. S97. t4097 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4098 with space-group 'Cmmm' (65) and 11 sites in the unit cell, with vertex type indicated in Tab. S98. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S98.

							-		-					
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
1	0	0	0	0	0	0	0	2	0	4	0	0	4	0

TABLE S98. Tiling t4098 vertex types



FIG. S98. t4098 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4099 with space-group 'P2/m' (10) and 8 sites in the unit cell, with vertex type indicated in Tab. S99. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S99.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	0	0	0	0	0	2	0	2	0	0	4	0

TABLE S99. Tiling t4099 vertex types



FIG. S99. t4099 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4100 with space-group 'Amm2' (38) and 30 sites in the unit cell, with vertex type indicated in Tab. S100. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S100.

A B C D E F G H I J K L M N 6 0 0 0 0 6 0 0 18 0 0 0					TA	BLE S	100.	Filing t	4100 v	ertex t	ypes				
6 0 0 0 6 0 0 18 0 0 0	I	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
	6	0	0	0	0	0	6	0	0	0	18	0	0	0	0



FIG. S100. t4100 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4101 with space-group 'Pm' (6) and 27 sites in the unit cell, with vertex type indicated in Tab. S101. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S101.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
3	0	0	0	0	0	6	0	0	6	12	0	0	0	0

TABLE S101. Tiling t4101 vertex types



FIG. S101. t4101 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4102 with space-group 'Amm2' (38) and 36 sites in the unit cell, with vertex type indicated in Tab. S102. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S102.

A	В	С	D	Е	F	G	Η	Ι	J	K	L	М	N	0
0	0	0	0	0	0	18	0	0	12	6	0	0	0	0

TABLE S102. Tiling t4102 vertex types



FIG. S102. t4102 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4103 with space-group 'Pm' (6) and 30 sites in the unit cell, with vertex type indicated in Tab. S103. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S103.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
6	0	0	0	0	0	6	0	0	12	6	0	0	0	0

TABLE S103. Tiling t4103 vertex types



FIG. S103. t4103 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4104 with space-group 'Amm2' (38) and 27 sites in the unit cell, with vertex type indicated in Tab. S104. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S104.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
3	0	0	0	0	0	6	0	0	18	0	0	0	0	0





FIG. S104. t4104 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4105 with space-group 'Amm2' (38) and 25 sites in the unit cell, with vertex type indicated in Tab. S105. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S105.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
1	0	0	0	0	0	18	0	0	6	0	0	0	0	0

TABLE S105. Tiling t4105 vertex types



FIG. S105. t4105 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4106 with space-group Pmm2' (25) and 10 sites in the unit cell, with vertex type indicated in Tab. S106. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S106.

										~ ~				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	6	0	0	4	0	0	0	0	0

TABLE S106. Tiling t4106 vertex types



FIG. S106. t4106 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4107 with space-group 'Amm2' (38) and 28 sites in the unit cell, with vertex type indicated in Tab. S107. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S107.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
0	0	0	0	0	0	12	0	0	16	0	0	0	0	0

TABLE S107. Tiling t4107 vertex types



FIG. S107. t4107 lattice framework, nearest neighbors band structure and radial distribution function.
Tiling reference number t4108 with space-group 'Amm2' (38) and 30 sites in the unit cell, with vertex type indicated in Tab. S108. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S108.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
0	0	0	0	0	0	12	0	0	6	0	0	12	0	0

TABLE S108. Tiling t4108 vertex types



FIG. S108. t4108 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4109 with space-group 'Cmmm' (65) and 12 sites in the unit cell, with vertex type indicated in Tab. S109. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S109.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
2	0	0	0	0	0	0	0	2	0	0	0	0	0	8





FIG. S109. t4109 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4110 with space-group 'Amm2' (38) and 30 sites in the unit cell, with vertex type indicated in Tab. S110. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S110.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
6	0	0	0	0	0	0	0	12	0	0	0	0	0	12

TABLE S110. Tiling t4110 vertex types



FIG. S110. t4110 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4111 with space-group 'P6/mmm' (191) and 19 sites in the unit cell, with vertex type indicated in Tab. S111. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S111.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	Ο
1	0	0	0	0	0	0	6	0	0	0	0	0	0	12

TABLE S111. Tiling t4111 vertex types



FIG. S111. t4111 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4112 with space-group P2/m' (10) and 7 sites in the unit cell, with vertex type indicated in Tab. S112. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S112.

				TA	BLE S	112. Т	Tiling t	4112 v	ertex t	ypes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	0	1	2	0	0	0	0	0	4



FIG. S112. t4112 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4113 with space-group '*Pbam*' (55) and 14 sites in the unit cell, with vertex type indicated in Tab. S113. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S113.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	0	2	4	0	0	0	0	0	8

TABLE S113. Tiling t4113 vertex types



FIG. S113. t4113 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4114 with space-group 'Pmmm' (47) and 9 sites in the unit cell, with vertex type indicated in Tab. S114. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S114.

А	В	\mathbf{C}	D	Е	\mathbf{F}	G	Н	Ι	J	Κ	\mathbf{L}	М	Ν	0
0	0	0	0	0	0	0	7	0	0	0	0	0	0	2

TABLE S114. Tiling t4114 vertex types



FIG. S114. t4114 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4115 with space-group 'Cmmm' (65) and 10 sites in the unit cell, with vertex type indicated in Tab. S115. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S115.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
2	0	0	0	0	0	0	2	4	0	0	0	0	0	2

TABLE S115. Tiling t4115 vertex types



FIG. S115. t4115 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4116 with space-group 'P2/m' (10) and 8 sites in the unit cell, with vertex type indicated in Tab. S116. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S116.

А	В	С	D	Ε	\mathbf{F}	G	Η	Ι	J	Κ	\mathbf{L}	М	Ν	0
0	0	0	0	0	0	0	2	4	0	0	0	0	0	2

TABLE S116. Tiling t4116 vertex types



FIG. S116. t4116 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4117 with space-group 'Cmmm' (65) and 9 sites in the unit cell, with vertex type indicated in Tab. S117. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S117.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	0	5	0	0	0	0	0	0	4

TABLE S117. Tiling t4117 vertex types



FIG. S117. t4117 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4118 with space-group 'P - 62m' (189) and 21 sites in the unit cell, with vertex type indicated in Tab. S118. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S118.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	0	9	6	0	0	0	0	0	6





FIG. S118. t4118 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4119 with space-group 'P6/m' (175) and 24 sites in the unit cell, with vertex type indicated in Tab. S119. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S119.

А	В	С	D	Е	\mathbf{F}	G	Н	Ι	J	Κ	L	М	Ν	Ο
0	0	0	0	0	0	0	12	6	0	0	0	0	0	6

TABLE S119. Tiling t4119 vertex types



FIG. S119. t4119 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4120 with space-group '*Pbam*' (55) and 16 sites in the unit cell, with vertex type indicated in Tab. S120. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S120.

				TA	BLE S	120. Т	Tiling t	4120 v	ertex t	ypes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	0	4	8	0	0	0	0	0	4



FIG. S120. t4120 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4121 with space-group 'Cmmm' (65) and 7 sites in the unit cell, with vertex type indicated in Tab. S121. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S121.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	0	0	0	0	1	2	0	0	0	0	0	4





FIG. S121. t4121 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4122 with space-group Pmm2' (25) and 7 sites in the unit cell, with vertex type indicated in Tab. S122. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S122.

				TA	BLE S	122. Т	Tiling t	4122 v	ertex t	ypes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
3	0	0	0	0	0	0	0	2	0	0	0	0	0	2



FIG. S122. t4122 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4123 with space-group 'Cmmm' (65) and 8 sites in the unit cell, with vertex type indicated in Tab. S123. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S123.

				TA	BLE S	123. Т	Tiling t	4123 v	ertex t	ypes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
4	0	0	0	0	0	0	0	2	0	0	0	0	0	2



FIG. S123. t4123 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4124 with space-group Pmma' (51) and 10 sites in the unit cell, with vertex type indicated in Tab. S124. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S124.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
2	0	0	0	0	0	0	4	4	0	0	0	0	0	0

TABLE S124. Tiling t4124 vertex types



FIG. S124. t4124 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4125 with space-group P2/m' (10) and 16 sites in the unit cell, with vertex type indicated in Tab. S125. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S125.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
0	0	0	0	0	0	0	8	8	0	0	0	0	0	0

TABLE S125. Tiling t4125 vertex types



FIG. S125. t4125 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4126 with space-group 'Pmmm' (47) and 9 sites in the unit cell, with vertex type indicated in Tab. S126. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S126.

				TA	BLE S	126. Л	Tiling t	4126 v	ertex t	ypes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	0	1	4	0	4	0	0	0	0



FIG. S126. t4126 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4127 with space-group 'P2/m' (10) and 9 sites in the unit cell, with vertex type indicated in Tab. S127. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S127.

										• -				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	0	1	4	0	4	0	0	0	0

TABLE S127. Tiling t4127 vertex types



FIG. S127. t4127 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4128 with space-group 'Pmmm' (47) and 7 sites in the unit cell, with vertex type indicated in Tab. S128. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S128.

				TA	BLE S	128. Л	Tiling t	4128 v	ertex t	ypes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
2	0	0	0	0	0	0	1	4	0	0	0	0	0	0



FIG. S128. t4128 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4129 with space-group 'Pmma' (51) and 10 sites in the unit cell, with vertex type indicated in Tab. S129. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S129.

				TA	BLE S	129. Л	Tiling t	4129 v	ertex t	ypes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	0	2	8	0	0	0	0	0	0



FIG. S129. t4129 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4130 with space-group 'Amm2' (38) and 36 sites in the unit cell, with vertex type indicated in Tab. S130. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S130.

А	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
12	0	0	0	0	0	0	0	0	0	12	12	0	0	0

TABLE S130. Tiling t4130 vertex types



FIG. S130. t4130 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4131 with space-group 'P - 6m2' (187) and 32 sites in the unit cell, with vertex type indicated in Tab. S131. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S131.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
2	0	0	0	0	0	0	0	0	12	6	12	0	0	0

TABLE S131. Tiling t4131 vertex types



FIG. S131. t4131 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4132 with space-group P2/m' (10) and 16 sites in the unit cell, with vertex type indicated in Tab. S132. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S132.

				TA	BLE S	132. Л	Tiling t	4132 v	ertex t	ypes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	0	0	0	4	0	8	4	0	0



FIG. S132. t4132 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4133 with space-group Pmm2' (25) and 7 sites in the unit cell, with vertex type indicated in Tab. S133. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S133.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
1	0	0	0	0	0	0	0	0	0	6	0	0	0	0

TABLE S133. Tiling t4133 vertex types



FIG. S133. t4133 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4134 with space-group 'Cmmm' (65) and 8 sites in the unit cell, with vertex type indicated in Tab. S134. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S134.

А	В	С	D	Е	F	G	Η	Ι	J	Κ	L	М	Ν	0
2	0	0	0	0	0	0	0	0	0	6	0	0	0	0

TABLE S134. Tiling t4134 vertex types



FIG. S134. t4134 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4135 with space-group 'Cmmm' (65) and 8 sites in the unit cell, with vertex type indicated in Tab. S135. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S135.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
2	0	0	0	0	0	0	0	0	0	6	0	0	0	0

TABLE S135. Tiling t4135 vertex types



FIG. S135. t4135 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4136 with space-group 'Pmmm' (47) and 7 sites in the unit cell, with vertex type indicated in Tab. S136. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S136.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
5	0	0	0	0	0	0	0	0	0	2	0	0	0	0

TABLE S136. Tiling t4136 vertex types



FIG. S136. t4136 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4137 with space-group 'Cmmm' (65) and 8 sites in the unit cell, with vertex type indicated in Tab. S137. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S137.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
6	0	0	0	0	0	0	0	0	0	2	0	0	0	0

TABLE S137. Tiling t4137 vertex types



FIG. S137. t4137 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4138 with space-group 'Amm2' (38) and 21 sites in the unit cell, with vertex type indicated in Tab. S138. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S138.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	N	0
3	0	0	0	0	0	0	0	0	6	12	0	0	0	0





FIG. S138. t4138 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4139 with space-group 'Cmmm' (65) and 7 sites in the unit cell, with vertex type indicated in Tab. S139. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S139.

A	В	С	D	Е	F	G	Η	Ι	J	K	L	М	Ν	0
3	0	0	0	0	0	0	0	0	0	4	0	0	0	0

TABLE S139. Tiling t4139 vertex types



FIG. S139. t4139 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4140 with space-group 'Pmma' (51) and 8 sites in the unit cell, with vertex type indicated in Tab. S140. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S140.

А	В	С	D	Е	F	G	Η	Ι	J	Κ	L	М	Ν	0
4	0	0	0	0	0	0	0	0	0	4	0	0	0	0

TABLE S140. Tiling t4140 vertex types



FIG. S140. t4140 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4141 with space-group 'Amm2' (38) and 7 sites in the unit cell, with vertex type indicated in Tab. S141. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S141.

A	В	С	D	Е	F	G	Η	Ι	J	K	L	М	Ν	0
3	0	0	0	0	0	0	0	0	0	4	0	0	0	0

TABLE S141. Tiling t4141 vertex types





FIG. S141. t4141 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4142 with space-group $Pmc2'_1$ (26) and 16 sites in the unit cell, with vertex type indicated in Tab. S142. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S142.

А	В	С	D	Ε	\mathbf{F}	G	Η	Ι	J	Κ	\mathbf{L}	Μ	Ν	0
0	0	0	0	0	0	0	0	0	4	12	0	0	0	0

TABLE S142. Tiling t4142 vertex types



FIG. S142. t4142 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4143 with space-group 'P2/m' (10) and 8 sites in the unit cell, with vertex type indicated in Tab. S143. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S143.

				TA	BLE S	143. Т	Tiling t	4143 v	ertex t	ypes				
А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
0	0	0	0	0	0	0	0	0	4	4	0	0	0	0



FIG. S143. t4143 lattice framework, nearest neighbors band structure and radial distribution function.
Tiling reference number t4144 with space-group $Pmc2'_1$ (26) and 16 sites in the unit cell, with vertex type indicated in Tab. S144. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S144.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	Ν	0
0	0	0	0	0	0	0	0	0	12	4	0	0	0	0

TABLE S144. Tiling t4144 vertex types



FIG. S144. t4144 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4145 with space-group 'Cmmm' (65) and 9 sites in the unit cell, with vertex type indicated in Tab. S145. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S145.

А	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
1	0	0	0	0	0	0	0	0	4	4	0	0	0	0

TABLE S145. Tiling t4145 vertex types



FIG. S145. t4145 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4146 with space-group 'Pm' (6) and 19 sites in the unit cell, with vertex type indicated in Tab. S146. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S146.

A	В	С	D	Е	F	G	Н	Ι	J	Κ	L	М	Ν	0
7	0	0	0	0	0	0	0	0	6	6	0	0	0	0

TABLE S146. Tiling t4146 vertex types



FIG. S146. t4146 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4147 with space-group 'Pm' (6) and 10 sites in the unit cell, with vertex type indicated in Tab. S147. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S147.

А	В	\mathbf{C}	D	Е	\mathbf{F}	G	Н	Ι	J	Κ	\mathbf{L}	М	Ν	0
2	0	0	0	0	0	0	0	0	6	2	0	0	0	0

TABLE S147. Tiling t4147 vertex types



FIG. S147. t4147 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4148 with space-group 'P6/m' (175) and 20 sites in the unit cell, with vertex type indicated in Tab. S148. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S148.

	TABLE S148. Tiling t4148 vertex types													
А	В	С	D	Е	F	G	Η	Ι	J	Κ	L	М	Ν	0
14	0	0	0	0	0	0	0	6	0	0	0	0	0	0



FIG. S148. t4148 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4149 with space-group 'P6/mmm' (191) and 24 sites in the unit cell, with vertex type indicated in Tab. S149. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S149.

	TABLE S149. Tiling t4149 vertex types													
А	В	С	D	Е	F	G	Η	Ι	J	Κ	L	М	Ν	0
18	0	0	0	0	0	0	0	6	0	0	0	0	0	0



FIG. S149. t4149 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4150 with space-group 'P6/m' (175) and 19 sites in the unit cell, with vertex type indicated in Tab. S150. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S150.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
7	0	0	0	0	0	0	0	12	0	0	0	0	0	0

TABLE S150. Tiling t4150 vertex types



FIG. S150. t4150 lattice framework, nearest neighbors band structure and radial distribution function.

Tiling reference number t4151 with space-group 'P2/m' (10) and 8 sites in the unit cell, with vertex type indicated in Tab. S151. The respective lattice structure, nearest neighbors band structure, and radial distribution function is shown in Fig S151.

A	В	С	D	Е	F	G	Н	Ι	J	K	L	М	N	0
2	0	0	0	0	0	0	0	6	0	0	0	0	0	0





FIG. S151. t4151 lattice framework, nearest neighbors band structure and radial distribution function.

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