

## Supplementary Information

### **Integrated leaching-carbonation kinetic model on CO<sub>2</sub> mineralization of alkaline solid wastes in a high-gravity rotating packed bed**

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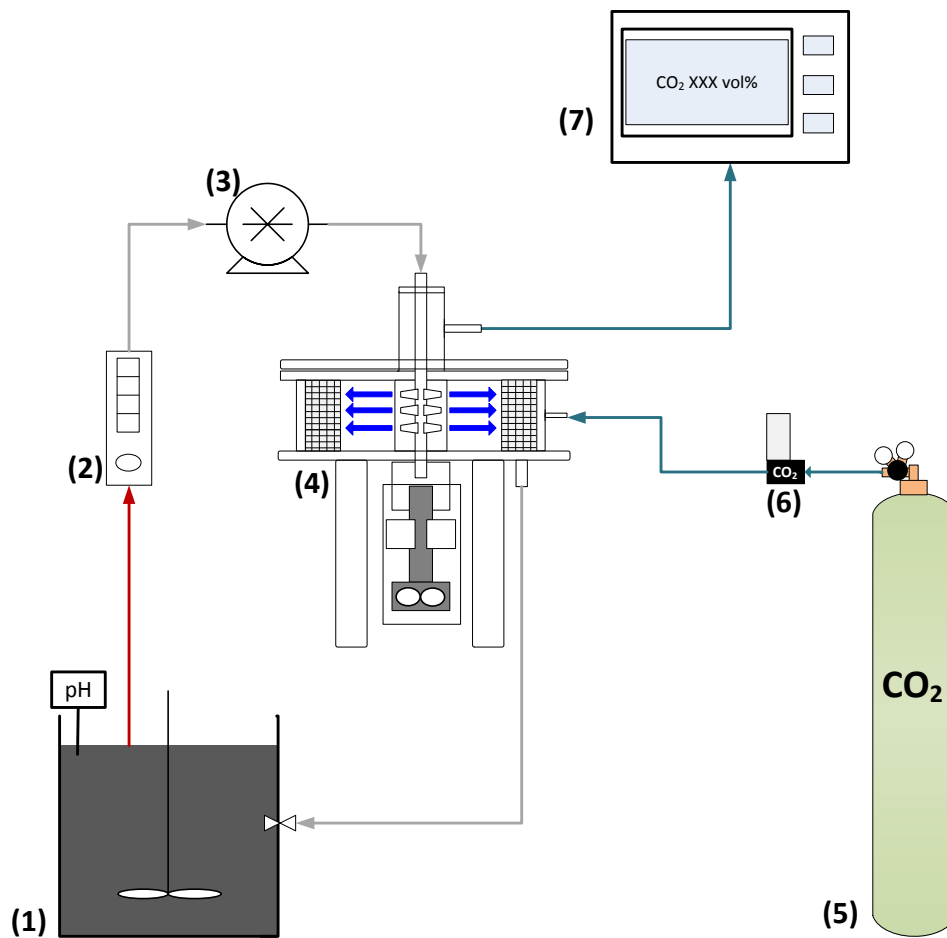
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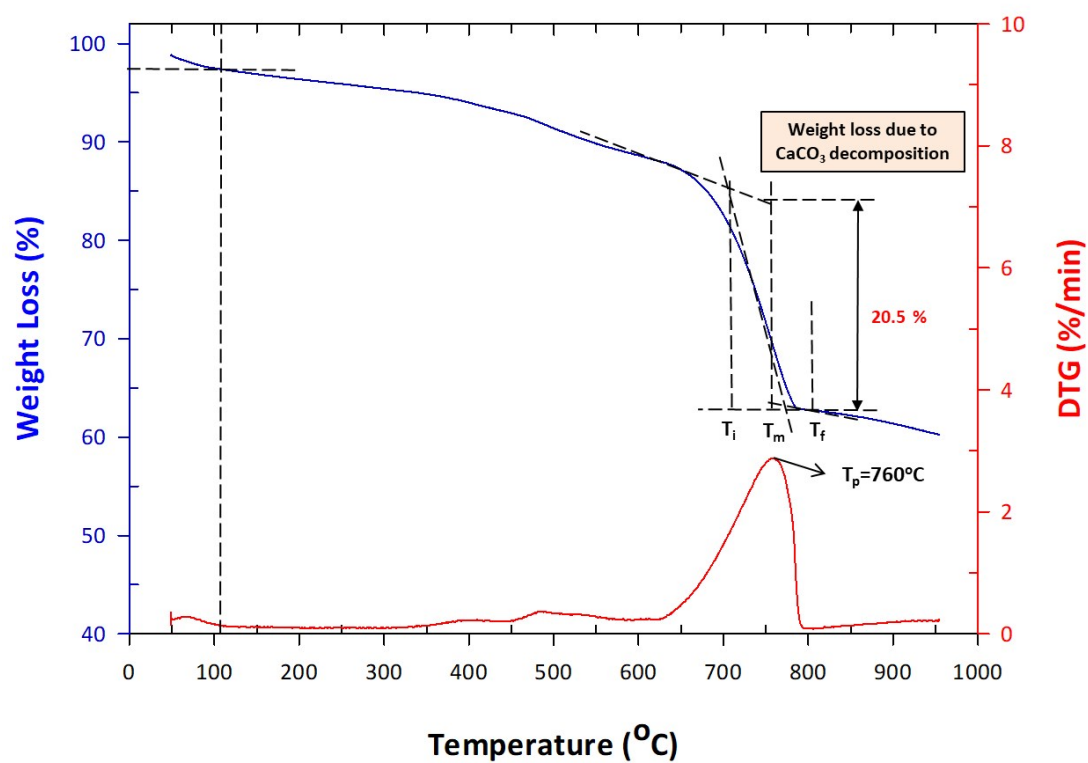
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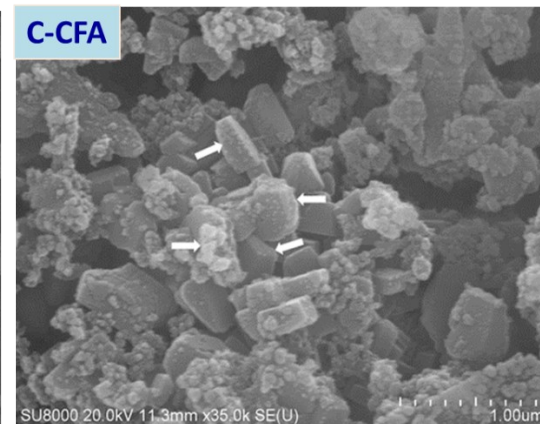
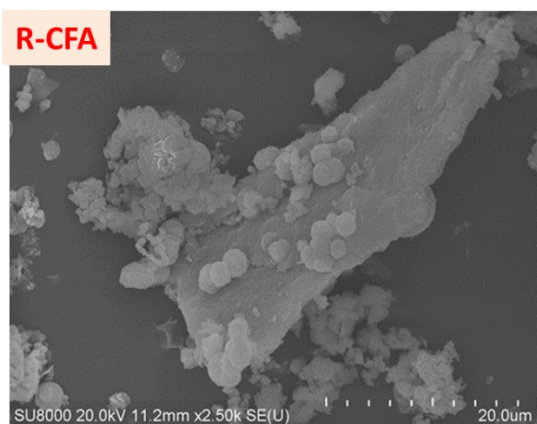
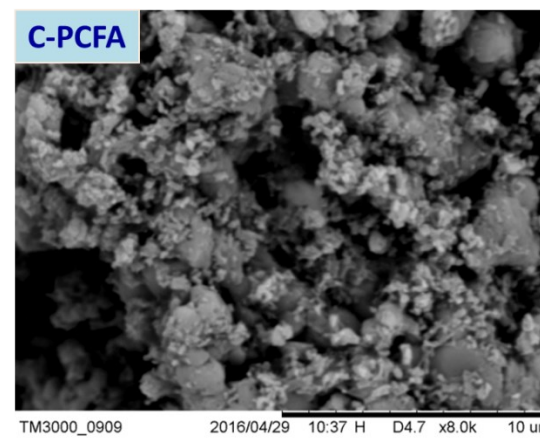
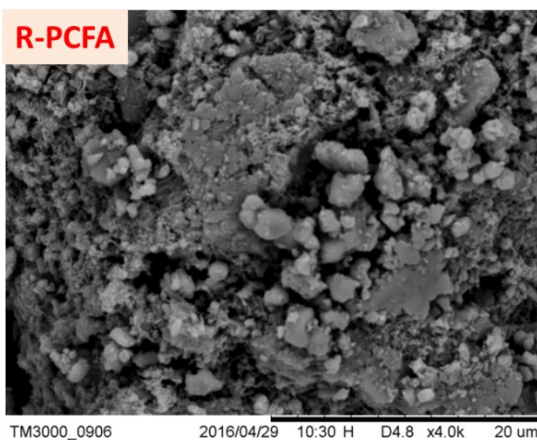
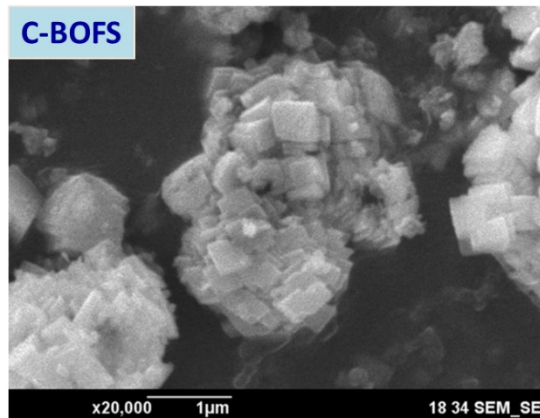
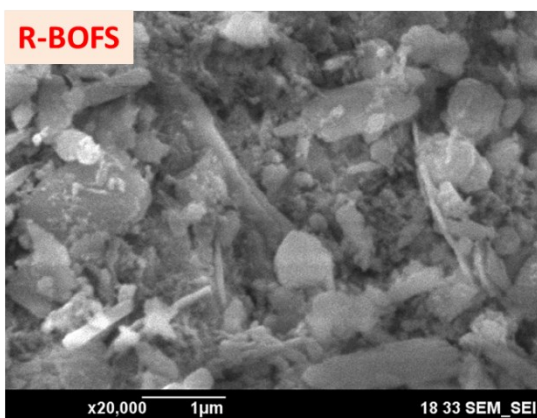
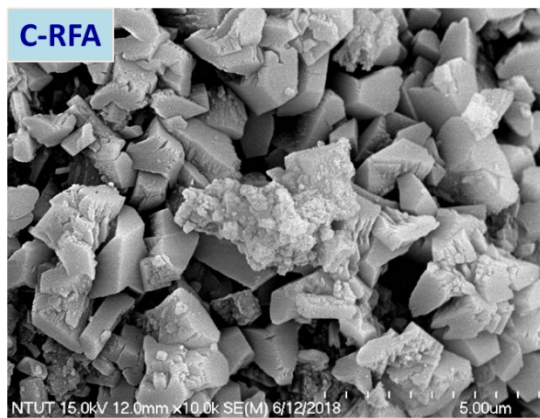
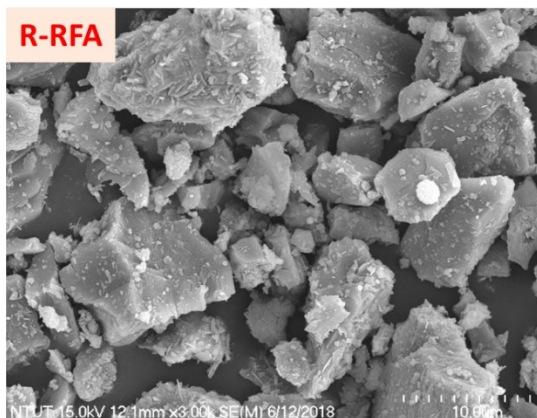
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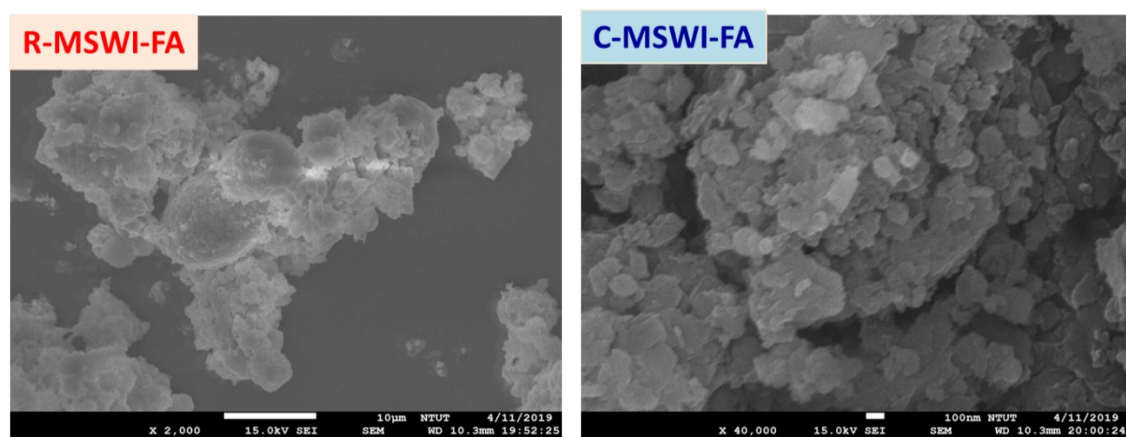


**Figure S1** Schematic of batch mode CO<sub>2</sub> mineralization using alkaline solid wastes in the lab-scale high-gravity rotating packed bed. (1) Slurry tank, (2) flowmeter, (3) peristaltic pump, (4) rotating packed bed reactor, (5) gas cylinders, (6) gas flowmeters, (7) gas analyzer.



**Figure S2** TG-DTG plot for determining the conversion of carbonated ASW sample in this study.





**Figure S-3** SEM images of raw (R-) and carbonated (C-) alkaline solid wastes used in this study.

**Table S1** Fixed parameters used for estimation of liquid mass transfer coefficient.

| Parameters                                   | Symbol     | Unit                           | Values                   |
|----------------------------------------------|------------|--------------------------------|--------------------------|
| Rotating Speed                               | -          | RPM                            | 300, 600, 750, 900, 1200 |
| High-gravity factor                          | $\beta$    | -                              | 15, 59, 92, 132, 235     |
| Specific surface area of packing materials   | $a_p$      | m <sup>2</sup> /m <sup>3</sup> | 0.08                     |
| spherical equivalent diameter of the packing | $D_p$      | m                              | 0.0075                   |
| Average liquid density                       | $\rho_l$   | kg/m <sup>3</sup>              | 1023                     |
| Average gas density                          | $\rho_g$   | kg/m <sup>3</sup>              | 0.92                     |
| Liquid surface tension                       | $\sigma_L$ | N/m                            | 0.08                     |
| Schmidt number                               | $Sc$       | -                              | 437.41                   |
| Reynolds number                              | $Re$       | -                              | 17.47                    |

**Table S2** Calculated parameters used for estimation of liquid mass transfer coefficient

(All parameters were changed with the rotating speed increased).

| Parameters                                                           | Symbol          | Unit | Values                                                                                                |
|----------------------------------------------------------------------|-----------------|------|-------------------------------------------------------------------------------------------------------|
| Rotating Speed                                                       | -               | RPM  | 300, 600, 750, 900, 1200                                                                              |
| High-gravity factor                                                  | $\beta$         | -    | 15, 59, 92, 132, 235                                                                                  |
| Grashof number                                                       | $Gr$            | -    | $1.2 \times 10^5$ , $4.81 \times 10^5$ , $7.52 \times 10^5$ , $1.08 \times 10^6$ , $1.93 \times 10^6$ |
| Liquid holdup                                                        | $\varepsilon_L$ | cm   | 0.042, 0.021, 0.017, 0.014, 0.01                                                                      |
| Thickness of liquid film                                             | $\delta$        | mm   | 0.289, 0.072, 0.046, 0.032, 0.018                                                                     |
| Droplet specific surface area                                        | $a_d$           | -    | 463.51, 463.64, 463.67, 463.69, 463.71                                                                |
| Average droplet diameter                                             | $d_d$           | mm   | 0.54, 0.27, 0.21, 0.18, 0.13                                                                          |
| Ratio of Specific surface area between packing materials and droplet | $a_p/a_d$       | -    | $1.72 \times 10^{-4}$                                                                                 |

**Table S3.** Physical-chemical properties, conversion, theoretical and experimental CO<sub>2</sub> capture capacity of various ASW.

| Items <sup>a</sup>                              |                                      | R-RFS             | C-RFS | R-BOFS | C-BOFS | R-PCFA | C-PCFA | R-CFA | C-CFA | R-MSWI-FA | C-MSWI-FA |
|-------------------------------------------------|--------------------------------------|-------------------|-------|--------|--------|--------|--------|-------|-------|-----------|-----------|
| Chemical Composition (%)                        | SiO <sub>2</sub>                     | 23.76             | 22.11 | 10.7   | 9.89   | 5.54   | 3.35   | 18.36 | 19.03 | 5.81      | 8.76      |
|                                                 | Al <sub>2</sub> O <sub>3</sub>       | 17.23             | 15.76 | 4.27   | 3.78   | 2.12   | 0.95   | 14.92 | 16.79 | 1.99      | 2.36      |
|                                                 | Fe <sub>2</sub> O <sub>3</sub>       | 11.54             | 12.47 | 37.36  | 34.07  | 0.53   | 0.65   | 2.53  | 3.19  | 1.74      | 2.55      |
|                                                 | CaO                                  | 35.18             | 33.94 | 37.05  | 37.38  | 45.39  | 46.14  | 51.46 | 50.79 | 40.02     | 53.61     |
|                                                 | MgO                                  | 6.62              | 5.72  | 5.06   | 4.18   | 1.49   | 1      | 2.45  | 2.08  | 0.94      | 1.57      |
|                                                 | SO <sub>3</sub>                      | 1.1               | 0.82  | 0.27   | 0.4    | 44.12  | 47.23  | 7.5   | 5.87  | 6.7       | 6.17      |
|                                                 | K <sub>2</sub> O                     | N.D. <sup>b</sup> | N.D.  | N.D.   | N.D.   | 0.27   | 0.16   | 0.31  | 0.1   | 4.67      | 1.98      |
|                                                 | Na <sub>2</sub> O                    | N.D.              | N.D.  | N.D.   | N.D.   | N.D.   | 0.02   | 0.38  | 0.34  | 7.47      | N.D       |
|                                                 | TiO <sub>2</sub>                     | N.D.              | N.D.  | N.D.   | N.D.   | N.D.   | N.D.   | N.D.  | N.D.  | 0.78      | 1.1       |
|                                                 | P <sub>2</sub> O <sub>5</sub>        | N.D.              | N.D.  | 2.62   | 2.76   | N.D.   | N.D.   | N.D.  | N.D.  | N.D       | N.D       |
|                                                 | MnO                                  | 1.47              | 1.53  | 2.53   | 2.37   | N.D.   | N.D.   | N.D.  | N.D.  | N.D       | N.D       |
|                                                 | Total                                | 96.9              | 92.35 | 99.86  | 94.83  | 99.46  | 99.5   | 97.91 | 98.19 | 69.34     | 78.1      |
|                                                 | F-CaO                                | 1.37              | 0.3   | 1.26   | 0.58   | 3.24   | 0.21   | 4.72  | 0.13  | 21.66     | N.D       |
| Physical Properties                             | Specific Surface (m <sup>2</sup> /g) | 1.34              | 3.58  | 10.31  | 8.35   | 1.91   | 3.58   | 4.27  | 5.35  | 14.14     | 10.78     |
|                                                 | Density (g/cm <sup>3</sup> )         | 3.06              | 2.8   | 3.39   | 2.65   | 2.8    | N.A.   | 2.01  | N.A.  | 2.27      | 2.34      |
|                                                 | Mean diameter (μm)                   | N.A. <sup>c</sup> | N.A.  | N.A.   | 10.91  | N.A.   | N.A.   | 31.49 | N.A.  | 15.03     | 14.08     |
| Theoretical $C_{cap}$ kgCO <sub>2</sub> /kg-ASW |                                      | 0.253             |       | 0.277  |        | 0.091  |        | 0.350 |       | 0.356     |           |
| Max. $\delta_{Ca}$                              | %                                    | 66.1              |       | 60.9   |        | 65.35  |        | 69.35 |       | 89.66     |           |
| Experimental kgCO <sub>2</sub> /kg-ASW          |                                      | 0.183             |       | 0.177  |        | 0.233  |        | 0.280 |       | 0.282     |           |

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$C_{cap}$

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<sup>a</sup> the acronyms R and C represent the raw and carbonated ASW. <sup>b</sup> N.D. is non-detected. <sup>c</sup> N.A. is the sample was not analyzed.

**Table S4.** Effect of operating conditions on the carbonation kinetics parameters for various.

| ASW types | $S_g$ (m <sup>2</sup> /g) <sup>a</sup> | M (g/mole) <sup>b</sup> | Operating conditions |           |                        | Model parameters       |                            |                                                |       |
|-----------|----------------------------------------|-------------------------|----------------------|-----------|------------------------|------------------------|----------------------------|------------------------------------------------|-------|
|           |                                        |                         | $\beta$              | L/S ratio | Max. $\delta_{Ca}$ (%) | $k_p$                  | $(\times 10^3)k_s$         | $(\times 10^{-4})k_s k_p$ (min <sup>-1</sup> ) | $r^2$ |
|           |                                        |                         |                      |           |                        | (m <sup>2</sup> /mole) | (mole/min/m <sup>2</sup> ) |                                                |       |
| RFS       | 1.335                                  | 159.18                  | 15                   | 20        | 43.86                  | 0.483                  | 2.04                       | 0.098                                          | 0.709 |
|           |                                        |                         | 59                   | 20        | 53.91                  | 0.393                  | 2.32                       | 0.091                                          | 0.994 |
|           |                                        |                         | 92                   | 20        | 63.01                  | 0.337                  | 5.79                       | 0.195                                          | 0.973 |
|           |                                        |                         | 132                  | 20        | 65.83                  | 0.323                  | 3.29                       | 0.106                                          | 0.670 |
|           |                                        |                         | 235                  | 20        | 66.11                  | 0.321                  | 9.12                       | 0.293                                          | 0.978 |
|           |                                        |                         | 235                  | 10        | 63.49                  | 0.333                  | 2.61                       | 0.087                                          | 0.936 |
|           |                                        |                         | 235                  | 20        | 63.01                  | 0.337                  | 5.79                       | 0.195                                          | 0.973 |
|           |                                        |                         | 235                  | 30        | 57.13                  | 0.36                   | 1.60                       | 0.058                                          | 0.974 |
|           |                                        |                         | 235                  | 40        | 60.23                  | 0.346                  | 1.90                       | 0.066                                          | 0.982 |
|           |                                        |                         | 235                  | 50        | 54.29                  | 0.385                  | 1.79                       | 0.069                                          | 0.956 |
|           |                                        |                         | 15                   | 20        | 58.65                  | 2.657                  | 0.66                       | 0.176                                          | 0.947 |
|           |                                        |                         | 59                   | 20        | 58.58                  | 2.660                  | 0.76                       | 0.201                                          | 0.898 |
|           |                                        |                         | 92                   | 20        | 58.21                  | 2.677                  | 0.86                       | 0.229                                          | 0.911 |
|           |                                        |                         | 132                  | 20        | 51.35                  | 3.035                  | 0.40                       | 0.123                                          | 0.962 |
| BOF       | 10.31                                  | 151.15                  | 235                  | 20        | 47.35                  | 3.291                  | 0.69                       | 0.228                                          | 0.836 |
|           |                                        |                         | 235                  | 10        | 51.35                  | 3.035                  | 0.43                       | 0.131                                          | 0.948 |
|           |                                        |                         | 235                  | 20        | 58.54                  | 2.662                  | 0.66                       | 0.176                                          | 0.943 |
|           |                                        |                         | 235                  | 30        | 55.32                  | 2.817                  | 0.39                       | 0.109                                          | 0.862 |
|           |                                        |                         | 235                  | 40        | 50.35                  | 3.095                  | 0.74                       | 0.230                                          | 0.910 |
|           |                                        |                         | 235                  | 50        | 52.23                  | 2.984                  | 0.44                       | 0.131                                          | 0.932 |

|         |       |        |     |    |       |       |      |       |       |
|---------|-------|--------|-----|----|-------|-------|------|-------|-------|
| PCFA    | 1.91  | 123.38 | 15  | 20 | 58.32 | 0.404 | 4.43 | 0.179 | 0.975 |
|         |       |        | 59  | 20 | 60.32 | 0.391 | 3.41 | 0.133 | 0.986 |
|         |       |        | 92  | 20 | 65.35 | 0.361 | 6.32 | 0.228 | 0.979 |
|         |       |        | 132 | 20 | 54.32 | 0.434 | 1.68 | 0.073 | 0.773 |
|         |       |        | 235 | 20 | 56.55 | 0.417 | 2.26 | 0.094 | 0.847 |
|         |       |        | 235 | 10 | 61.24 | 0.385 | 2.42 | 0.093 | 0.810 |
|         |       |        | 235 | 15 | 58.23 | 0.405 | 3.65 | 0.148 | 0.857 |
|         |       |        | 235 | 20 | 57.57 | 0.409 | 1.61 | 0.066 | 0.762 |
|         |       |        | 235 | 25 | 57.58 | 0.409 | 2.99 | 0.122 | 0.890 |
|         |       |        | 15  | 20 | 54.5  | 0.853 | 2.66 | 0.227 | 0.988 |
| CFA     | 4.27  | 108.52 | 59  | 20 | 55.8  | 0.833 | 1.81 | 0.151 | 0.841 |
|         |       |        | 92  | 20 | 62.33 | 0.746 | 2.70 | 0.201 | 0.939 |
|         |       |        | 132 | 20 | 63.25 | 0.735 | 2.61 | 0.192 | 0.938 |
|         |       |        | 235 | 20 | 63.85 | 0.728 | 2.05 | 0.149 | 0.880 |
|         |       |        | 235 | 20 | 63.5  | 0.732 | 1.77 | 0.130 | 0.818 |
|         |       |        | 235 | 30 | 67.38 | 0.690 | 2.34 | 0.162 | 0.888 |
|         |       |        | 235 | 40 | 69.35 | 0.670 | 2.19 | 0.147 | 0.838 |
|         |       |        | 235 | 50 | 63.65 | 0.730 | 2.28 | 0.167 | 0.861 |
|         |       |        | 15  | 20 | 58.35 | 3.391 | 0.47 | 0.161 | 0.900 |
|         |       |        | 59  | 20 | 73.58 | 2.689 | 0.61 | 0.164 | 0.906 |
| MSWI-FA | 14.14 | 139.93 | 92  | 20 | 82.32 | 2.404 | 0.61 | 0.146 | 0.907 |
|         |       |        | 132 | 20 | 88.32 | 2.240 | 0.84 | 0.188 | 0.953 |
|         |       |        | 235 | 20 | 89.66 | 2.207 | 1.03 | 0.227 | 0.980 |
|         |       |        | 235 | 10 | 79.8  | 2.479 | 0.73 | 0.181 | 0.931 |
|         |       |        | 235 | 20 | 85.5  | 2.314 | 0.62 | 0.143 | 0.801 |
|         |       |        | 235 | 30 | 89.66 | 2.207 | 1.03 | 0.227 | 0.980 |

|     |    |       |       |      |       |       |
|-----|----|-------|-------|------|-------|-------|
| 235 | 40 | 75.33 | 2.627 | 0.55 | 0.146 | 0.901 |
| 235 | 50 | 72.25 | 2.739 | 0.64 | 0.175 | 0.956 |

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<sup>a</sup>S<sub>g</sub> was referred to the specific surface area of the ASW particle. <sup>b</sup>M was calculated the molecular weight of CaO divided by weigh percentage of CaO in the ASW.

**Table S5.** Influence of operating parameters on kinetics parameters of  $\text{Ca}^{2+}$  leaching behavior for various ASW.

| ASW types | Operating conditions |           | Max. $C_{\text{Ca}^{2+}}$ (mg/L) | Model parameters        |                             |                             |
|-----------|----------------------|-----------|----------------------------------|-------------------------|-----------------------------|-----------------------------|
|           | $\beta$              | L/S ratio |                                  | $S_{\text{max}}$ (mg/L) | $k_a$ ( $\text{min}^{-1}$ ) | $k_d$ ( $\text{min}^{-1}$ ) |
| RFS       | 15                   | 20        | 1453                             | 252                     | 0.0814                      | 0.3335                      |
|           | 59                   | 20        | 1518                             | 565                     | 0.0249                      | 0.2228                      |
|           | 92                   | 20        | 1703                             | 995                     | 0.0149                      | 0.1865                      |
|           | 132                  | 20        | 1812                             | 1329                    | 0.0133                      | 0.2849                      |
|           | 235                  | 20        | 1805                             | 1400                    | 0.0119                      | 0.4516                      |
|           | 235                  | 10        | 1805                             | 1400                    | 0.0109                      | 0.3167                      |
|           | 235                  | 20        | 1635                             | 1217                    | 0.0112                      | 0.1035                      |
|           | 235                  | 30        | 1224                             | 809                     | 0.0155                      | 0.2809                      |
|           | 235                  | 40        | 832                              | 519                     | 0.0258                      | 0.2467                      |
|           | 235                  | 50        | 708                              | 410                     | 0.0363                      | 0.2055                      |
| BOFS      | 15                   | 20        | 1385                             | 550                     | 0.0536                      | 0.7801                      |
|           | 59                   | 20        | 1213                             | 410                     | 0.0734                      | 0.9791                      |
|           | 92                   | 20        | 1157                             | 501                     | 0.0463                      | 1.3251                      |
|           | 132                  | 20        | 1124                             | 519                     | 0.0522                      | 0.5327                      |
|           | 235                  | 20        | 1193                             | 591                     | 0.0355                      | 0.2093                      |
|           | 235                  | 10        | 1433                             | 798                     | 0.0187                      | 0.5621                      |
|           | 235                  | 20        | 1285                             | 640                     | 0.0303                      | 0.9705                      |
|           | 235                  | 30        | 1232                             | 629                     | 0.0225                      | 0.1465                      |
|           | 235                  | 40        | 1192                             | 567                     | 0.0206                      | 0.1909                      |
|           | 235                  | 50        | 1101                             | 566                     | 0.0262                      | 0.9410                      |
| PCFA      | 15                   | 20        | 1297                             | 481                     | 0.0429                      | 0.3417                      |

|         |     |    |       |      |        |        |
|---------|-----|----|-------|------|--------|--------|
| CFA     | 59  | 20 | 1048  | 272  | 0.0596 | 0.2247 |
|         | 92  | 20 | 1136  | 390  | 0.0256 | 0.5354 |
|         | 132 | 20 | 1114  | 381  | 0.0246 | 0.8603 |
|         | 235 | 20 | 1198  | 391  | 0.0236 | 0.1490 |
|         | 367 | 20 | 1124  | 318  | 0.0333 | 0.2564 |
|         | 235 | 10 | 1153  | 371  | 0.0613 | 0.4618 |
|         | 235 | 15 | 1121  | 317  | 0.0603 | 0.1467 |
|         | 235 | 20 | 1088  | 354  | 0.0520 | 0.1264 |
|         | 235 | 25 | 953   | 355  | 0.0647 | 0.1021 |
|         | 235 | 30 | 829   | 136  | 0.0802 | 0.0767 |
|         | 15  | 20 | 2564  | 2285 | 0.0102 | 0.5732 |
|         | 59  | 20 | 2543  | 2272 | 0.0095 | 0.6994 |
|         | 92  | 20 | 2571  | 2399 | 0.0091 | 0.1505 |
|         | 132 | 20 | 2523  | 2364 | 0.0108 | 0.7163 |
|         | 235 | 20 | 2533  | 2398 | 0.0111 | 0.6769 |
|         | 235 | 20 | 2533  | 2398 | 0.0111 | 0.7752 |
|         | 235 | 30 | 2322  | 2124 | 0.0135 | 0.6753 |
|         | 235 | 40 | 2059  | 1694 | 0.0155 | 0.6365 |
|         | 235 | 50 | 2006  | 1619 | 0.0193 | 0.6081 |
|         | 15  | 20 | 6821  | 2395 | 0.0205 | 0.1705 |
| MSWI-FA | 59  | 20 | 6928  | 2680 | 0.0190 | 0.8590 |
|         | 92  | 20 | 7058  | 3033 | 0.0182 | 0.9166 |
|         | 132 | 20 | 7358  | 3406 | 0.0155 | 0.7437 |
|         | 235 | 20 | 6895  | 3183 | 0.0152 | 0.6612 |
|         | 235 | 10 | 13058 | 4057 | 0.0311 | 0.4348 |
|         | 235 | 20 | 7125  | 2511 | 0.0284 | 0.6844 |

|     |    |      |      |        |        |
|-----|----|------|------|--------|--------|
| 235 | 30 | 6895 | 3183 | 0.0152 | 0.6612 |
| 235 | 40 | 4458 | 2235 | 0.0151 | 0.5753 |
| 235 | 50 | 4005 | 2219 | 0.0116 | 0.6868 |

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