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Supplementary Information

# A single-ion conducting covalent organic frameworks for aqueous rechargeable Zn-ion batteries

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## **Experimental details**

#### Materials

1,4-phenylenediamine-2-sulfonic acid (Pa-SO<sub>3</sub>H), 1,4-dioxane, mesitylene, acetic acid, zinc acetate and polytetrafluoroethylene (PTFE, 60 wt% dispersion in H<sub>2</sub>O) were purchased from Merck. The Zn metal foil (99.98%) was purchased from Alfa Aesar. 1,3,5-triformylphloroglucinol (Tp),<sup>S1</sup> the sulfonic acid COF (TpPa-SO<sub>3</sub>H),<sup>S2,S3</sup> the non-sulfonated COF (TpPa)<sup>S4</sup> and  $\alpha$ -MnO<sub>2</sub><sup>S5</sup> were synthesised as previously reported. All other chemicals were obtained from commercial sources and used as received unless otherwise noted.

## Synthesis of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub>

TpPa-SO<sub>3</sub>H (605 mg) was suspended in a 1 M aqueous zinc acetate solution (40 mL) and stirred for 72 h at room temperature, during which the solution was exchanged at an interval of 24 h. The resultant powders were collected by filtration and washed with H<sub>2</sub>O to ensure the removal of excess zinc acetate. After dried under vacuum at 120 °C for overnight, the reddish powders of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> were obtained (yield: 612 mg, 91%).

#### Structural and physicochemical characterisations

The elemental analysis was performed using a Leco TruSpec Micro CHN analyser. The Zn content was determined by inductively coupled plasma optical emission spectrometry (ICP-OES) using a Varian 700-ES. The Fourier transform infrared (FT-IR) spectrum was recorded using a Bruker ALPHA Laser class 1. The cross polarisation magic angle spinning <sup>13</sup>C nuclear magnetic resonance (CP-MAS <sup>13</sup>C NMR) experiment was performed using an Agilent VNMRS 600 MHz NMR spectrometer at a 20 kHz spinning rate. Chemical shifts were referenced to hexamethylbenzene at 17.3 ppm as an external standard. Morphological analyses were performed using a Hitachi S-4800 field-emission scanning electron microscope (FE-SEM) equipped with a JEOL JSM-6400 energy dispersive X-ray spectroscopy (EDS) detector and a Tecnai G2 F20 X-Twin transmission electron microscope (TEM) equipped with an Oxford INCA X-sight 7688 EDS detector. X-ray diffraction (XRD) patterns were recorded through a transmittance mode at the 6D UNIST-PAL beamline of the Pohang Accelerator Laboratory or using a Rigaku D/MAX2500. N<sub>2</sub> gas sorption isotherms were measured at 77 K with a Micromerites ASAP 2020 physisorption analyser. Brunauer–Emmett–Teller (BET) and non-

local density functional theory (NLDFT) methods were utilised to calculate the specific surface area and the pore size, respectively. The thermogravimetric analysis (TGA) was performed on a TA Instruments Q500 thermogravimetric analyser under a N<sub>2</sub> atmosphere at a heating rate of 10 °C min<sup>-1</sup>. Time-of-flight secondary ion mass spectroscopy (TOF-SIMS) mapping images were obtained using IONTOF TOF-SIMS 5. The X-ray photoelectron spectroscopy (XPS) analysis was conducted using a Thermo Fisher Scientific ESCALAB 250Xi.

## **Electrochemical characterisations**

The self-standing TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> pellets were prepared by a cold-pressing method under *ca*. 40 MPa at room temperature. The flexible TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> membranes were prepared by mixing PTFE (5 wt%) with the TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> powders. The obtained pellets and membranes were hydrated before the electrochemical tests.

#### [Ionic conductivity]

Ionic conductivity was measured with  $Zn^{2+}$  blocking Ti|TpPa-SO<sub>3</sub>Zn<sub>0.5</sub>|Ti cells based on an electrochemical impedance spectroscopy (EIS) analysis in a frequency range from  $10^{-2}$  to  $10^{6}$  Hz at an applied amplitude of 10 mV using a Bio-logic VSP classic potentiostat. The ionic conductivity ( $\sigma$ ) was determined according to the following equation:

$$\sigma = \frac{l}{RA}$$

where *l* is the pellet (or membrane) thickness, *R* is the resistance and *A* is the area in contact with the electrodes. The control experiment without  $Zn^{2+}$  was conducted using a Ti|TpPa|Ti cell.

## $[Zn^{2+} transference number]^{S6}$

The time-dependent current flowing through a Zn|TpPa-SO<sub>3</sub>Zn<sub>0.5</sub>|Zn cell and the impedance of the cell before and after direct current (DC) polarisation (20 mV) were measured. The Zn<sup>2+</sup> transference number ( $t_{Zn^{2+}}$ ) was determined according to the following equation:

$$t_{\mathrm{Zn}^{2+}} = \frac{I_{\mathrm{ss}}(\Delta V - I_0 R_0)}{I_0 (\Delta V - I_{\mathrm{ss}} R_{\mathrm{ss}})}$$

where  $I_{ss}$  is the steady-state current,  $I_0$  is the initial current,  $\Delta V$  is the applied potential,  $R_0$  and  $R_{ss}$  are the interfacial resistances before and after polarisation, respectively.

## [Linear sweep voltammetry]

Linear sweep voltammetry (LSV) was conducted with a  $Zn|TpPa-SO_3Zn_{0.5}|Ti$  cell operated under a sweep rate of 0.2 mV s<sup>-1</sup> in a voltage range from -0.2 to 3 V (vs.  $Zn/Zn^{2+}$ ) at room temperature.

## [*Zn stripping/plating experiments*]

The galvanostatic cyclability of a Zn|TpPa-SO<sub>3</sub>Zn<sub>0.5</sub>|Zn cell and a Zn|liquid electrolyte (LE)|Zn cell (LE = 2 M ZnSO<sub>4</sub> in H<sub>2</sub>O) was examined at room temperature (current density = 0.1 mA cm<sup>-2</sup>, capacity = 0.1 mAh cm<sup>-2</sup>). The reversibility of Zn stripping/plating was investigated with the Zn||Ti configurations, in which Zn metal was electrochemically plated on the Ti working electrode and subsequently stripped out during a cycle (current density = 0.1 mA cm<sup>-2</sup>, capacity = 0.1 mAh cm<sup>-2</sup>). The Zn||Cu configurations were used for monitoring Zn electroplating behaviour (current density = 0.3 mA cm<sup>-2</sup>, capacity = 3 mAh cm<sup>-2</sup>).

## [Zn//MnO<sub>2</sub> battery tests]

The electrode slurry composed of MnO<sub>2</sub>, carbon black and polyvinylidene fluoride in a weight ratio of 7/2/1 was dispersed in N-methyl-2-pyrrolidone and casted onto a Ti foil current collector. The solvent was removed under vacuum at 60 °C for overnight. The prepared MnO<sub>2</sub> cathode was immersed with an LE (2 M ZnSO<sub>4</sub> + 0.2 M MnSO<sub>4</sub> in H<sub>2</sub>O) and assembled with TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> (or a glass fibre containing the LE) and a Zn metal anode. The resultant Zn||MnO<sub>2</sub> cells were tested under a current density of 0.6 A g<sup>-1</sup> at room temperature.

#### Simulation details

## Density functional theory (DFT) calculations

The structural model of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> was constructed based on those reported for TpPa-SO<sub>3</sub>X (X = H, Li),<sup>S2,S3</sup> in which Zn atoms were introduced upon consideration of the charge balance between the sulfonated framework and Zn<sup>2+</sup>. The stable positions of Zn atoms were investigated by geometry optimisation. All DFT calculations were performed using DMol<sup>3</sup> program.<sup>S7,S8</sup> The generalised gradient approximation with Perdew–Burke–Ernzerhof functional (GGA-PBE)<sup>S9</sup> was used for the exchange-correlation energy. The double numerical polarisation basis set with spin-polarised calculations were used, while core-electron treatment was conducted with the DFT semi-core pseudopotential. The dispersion correction pertaining to van der Waals interactions was applied with semi-empirical Tkatchenko-Scheffler (TS)

scheme.<sup>S10</sup> The Brillouin zone was sampled by Monkhorst-Pack<sup>S11</sup>  $1 \times 1 \times 2$  *k*-point mesh for all systems. The self-consistent field (SCF) convergence for each electronic energy was set as  $1.0 \times 10^{-6}$  Ha. The convergence precision of geometry optimisation for energy, force and displacement were set to  $1.0 \times 10^{-5}$  Ha, 0.002 Ha Å<sup>-1</sup> and 0.005 Å, respectively.

## Molecular dynamics (MD) simulations

All MD simulations were carried out in Large-scale Atomic/Molecular Massively Parallel Simulator (LAMMPS).<sup>S12</sup> The visualisation was conducted with 3D visualisation Open Visualisation Tool (OVITO).<sup>S13</sup> Based upon the thermodynamically stable structure of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> obtained from DFT calculation, a  $4 \times 4 \times 54$  supercell was constructed. The carbon atoms of the framework were assumed to be dynamically rigid. H<sub>2</sub>O was saturated in the pores of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> for similarity with the experimental conditions. An LE system with the same magnitude was constructed by a fixed density of 1.31 g cc<sup>-1</sup> for 2 M ZnSO<sub>4</sub> in H<sub>2</sub>O. Both systems were equilibrated with *NVT* ensemble at 298 K for 2 ns. After then, an external electric field of 1.0 V Å<sup>-1</sup> in the *-z*-axis direction was applied to the systems for 3 ns. The Zn<sup>2+</sup> number density profiles, velocity distributions and fraction of Zn–O coordination numbers were obtained by analysis of average trajectories during the last 1 ns of this stage.

The Nose–Hoover thermostat was used to control temperature.<sup>S14</sup> The Assisted Model Building with Energy Refinement (AMBER) force field<sup>S15</sup> was used for both TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> and LE systems. The optimised AMBER force field for  $SO_4^{2-}$ ,<sup>S16</sup> the optimised non-bonded interaction for Zn<sup>2+</sup>,<sup>S17</sup> the general AMBER force field (GAFF)<sup>S18</sup> for the other atoms were used for this analysis. The Mulliken charge<sup>S19</sup> obtained from the DFT calculation was assigned as a partial atomic charge for all systems.



Scheme S1 Synthesis of TpPa-SO<sub>3</sub> $Zn_{0.5}$ .

## Tables

	C	Н	N	Zn
Calcd. (wt%) for C <sub>72</sub> H <sub>42</sub> N <sub>12</sub> O <sub>30</sub> S <sub>6</sub> Zn <sub>3</sub>	44.49	2.18	8.65	10.09
Found (wt%)	44.32	2.62	8.79	9.82

Table S1 CHN analysis and ICP-OES (for Zn) results for TpPa-SO $_3$ Zn $_{0.5}$ 

	TpPa-SO <sub>3</sub> Zn <sub>0.5</sub>
Formula	$C_{72}H_{42}N_{12}O_{30}S_6Zn_3$
Symmetry	Triclinic
Space group	<i>P</i> 1
a (Å)	22.8345
<i>b</i> (Å)	22.9434
<i>c</i> (Å)	6.8744
α (°)	89.8514
β (°)	89.7964
γ (°)	120.5433

Table S2 Unit cell parameters of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub>

Anionic host	Guest	$t_{Zn^{2+}}$	Ref.
Zinc sulfonated COF (TpPa-SO <sub>3</sub> Zn <sub>0.5</sub> )	H <sub>2</sub> O	0.91	This study
Zn <sup>2+</sup> -paired anionic MOF (ZnMOF-808)	H <sub>2</sub> O	0.93	S20
Zinc sulfonated poly(ether ether ketone) (Zn-SPEEK)	H <sub>2</sub> O	0.89	S21
Sulfonated perfluoro polyolefin (3M-Nafion)	3 M ZnSO <sub>4</sub> in H <sub>2</sub> O	0.52	S22
Zinc sulfonated perfluoro polyolefin (ZPSAM)	$H_2O$	0.2	S23

**Table S3**  $t_{Zn^{2+}}$  values of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> and previously reported Zn<sup>2+</sup> conducting polyanions

		TpPa-SO <sub>3</sub> Zn <sub>0.5</sub>	LE (2 M ZnSO <sub>4</sub> in H <sub>2</sub> O)
Number of species	$Zn^{2+}$	2592	3216
	TpPa-SO <sub>3</sub> <sup>-</sup>	1 (139968 atoms)	_
	SO4 <sup>2-</sup>	_	3216
	H <sub>2</sub> O	46656	89208
Total number of atoms		282528	286920
Cell parameters	<i>a</i> (Å)		91.34
	<i>b</i> (Å)		91.77
	<i>c</i> (Å)		371.22
	α (°)		90
	β (°)		90
	γ (°)		120

# Table S4 Details on model systems constructed for MD simulations

conductors				
Single $Zn^{2+}$ conductor	Cycling time of the Zn  Zn cell, h (current density, mA cm <sup>-2</sup> ; capacity, mAh cm <sup>-2</sup> )	Battery application (operating voltage, V)	Cycle number (current density, A g <sup>-1</sup> )	Ref.
Zinc sulfonated COF (TpPa-SO <sub>3</sub> Zn <sub>0.5</sub> )	500 (0.1; 0.1)	Zn  MnO <sub>2</sub> ( <i>ca</i> . 1.4)	800 (0.6)	This study
Zn <sup>2+</sup> -paired anionic MOF (ZnMOF-808)	360 (0.1; 0.05)	Zn  VS <sub>2</sub> (ca. 0.7)	250 (0.2)	S20
Zinc sulfonated poly(ether ether ketone) (Zn-SPEEK)	50 (1; 0.5)	Ι	I	S21
Sulfonated polyacrylonitrile (PAN-S)	350 (0.5; 0.25)	1	1	S24

Table S5 Characteristics of electrochemical cells containing TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> compared with those containing previously reported single Zn<sup>2+</sup>

Figs.



Fig. S1 (a) CP-MAS <sup>13</sup>C NMR and (b) FT-IR spectra of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub>.



Fig. S2 TEM image of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub>.



**Fig. S3** Theoretical unit cell structure of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> displayed along (a) *c*- and (b) *a*-axes. (c) Optimal geometry of Zn<sup>2+</sup>.



Fig. S4 Electrostatic potential (ESP) for TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> mapped on the electron density surface.



Fig. S5 Pore size distribution of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub>.



**Fig. S6** Cross-sectional SEM images of (a) a TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> pellet and (b) a TpPa-SO<sub>3</sub>Zn<sub>0.5</sub>– PTFE composite membrane (arrows: PTFE fibres).



Fig. S7 EIS profiles of the hydrated TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> measured at varied temperatures.



Fig. S8 (a) Chemical structure, (b) XRD patterns and (c)  $N_2$  gas isotherms of TpPa.



Fig. S9 EIS profile of the hydrated TpPa measured at room temperature.



**Fig. S10** (a) Velocity distribution of  $Zn^{2+}$  in TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> and LE (2 M ZnSO<sub>4</sub> in H<sub>2</sub>O) in the *z*-axis. (b) Fraction of Zn–O coordination numbers in TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> and LE. O<sub>w</sub> belongs to H<sub>2</sub>O, O<sub>f</sub> belongs to TpPa-SO<sub>3</sub><sup>-</sup> and O<sub>s</sub> belongs to SO<sub>4</sub><sup>2-</sup>.



Fig. S11 TGA curve of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub>.



Fig. S12 LSV profile of TpPa-SO<sub>3</sub>Zn<sub>0.5</sub>.



Fig. S13 XRD patterns of TpPa-SO $_3$ Zn $_{0.5}$  (as a PTFE composite membrane) before and after the Zn plating/stripping test. \*PTFE.



Fig. S14 (a) XPS spectra (Zn  $2p_{3/2}$  and S 2p) of Zn metal electrodes after Zn plating/stripping tests in contact with TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> (top) or LE (2 M ZnSO<sub>4</sub> in H<sub>2</sub>O; bottom). (b) XRD patterns of Zn metal electrodes before (black) and after Zn plating/stripping tests in contact with TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> (purple) or LE (green). \*Zn<sub>4</sub>SO<sub>4</sub>(OH)<sub>6</sub>·5H<sub>2</sub>O (PDF 39-0688).





Fig. S15 (a) SEM and TEM (the inset) images, (b) XRD pattern (PDF 44-0141) and (c) cyclic voltammograms of  $\alpha$ -MnO<sub>2</sub>.



**Fig. S16** (a) Cycling performance of a  $Zn|LE|MnO_2$  cell (LE = 2 M ZnSO<sub>4</sub> + 0.2 M MnSO<sub>4</sub> in H<sub>2</sub>O). (b) SEM image of the Zn metal anode after the 400<sup>th</sup> cycle. (c) TEM (left) and EDS mapping (for Mn; right) images of the MnO<sub>2</sub> cathode after the 400<sup>th</sup> cycle.



Fig. S17 XPS spectra (Mn  $2p_{3/2}$ ) of MnO<sub>2</sub> cathodes cycled in contact with TpPa-SO<sub>3</sub>Zn<sub>0.5</sub> (top) or LE (2 M ZnSO<sub>4</sub> + 0.2 M MnSO<sub>4</sub> in H<sub>2</sub>O; bottom).

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