

Supporting Information for

A Kinetic Description of How Interfaces Accelerate Reactions in Micro-compartments

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This file contains supplementary Tables S1 and S2 and Figure S1-S7

Table S1: Computed fraction of molecules at the surface of a sphere with radius, R, compared with the rectangular prism simulation geometry.

| R (μm) | Rectangular Prism | | | Sphere | | |
|--------|-------------------|--------|---|-----------------------|-----------------------|---|
| | Surface # | Bulk # | $f_{surface}$ | Surface # | Bulk # | $f_{surface}$ |
| 1 | 1.66 | 3.011 | 0.554 | 2.09×10^7 | 3.78×10^7 | 0.554 |
| 10 | 1.66 | 30.11 | 0.0554 | 2.09×10^9 | 3.78×10^{10} | 0.0554 |
| 100 | 1.66 | 301.1 | 5.54×10^{-3} | 2.09×10^{11} | 3.78×10^{13} | 5.54×10^{-3} |
| 1000 | 1.66 | 3011 | 5.54×10^{-4} | 2.09×10^{13} | 3.78×10^{16} | 5.54×10^{-4} |
| 10000 | 1.66 | 30110 | 5.54×10^{-5} | 2.09×10^{15} | 3.78×10^{19} | 5.54×10^{-5} |

Table S2: The set of elementary reaction and diffusion steps and rate coefficients used in stochastic simulations 1 and 2.

| No. | Elementary Step | Simulation 1 | Simulation 2 | units | Ref. |
|-----------------------------|---|----------------------------------|----------------------------------|---------------------------------|------|
| | Surface Compartment | Rate Coefficient | Rate Coefficient | | |
| 1 | Amine + Site \rightarrow Amine_ads | 0.066 | See Sim. 1 | M ⁻¹ s ⁻¹ | 1 |
| 2 | Amine_ads \rightarrow Amine + Site | 1.10 x 10 ⁻³ | See Sim. 1 | s ⁻¹ | 1 |
| 3 | Aldehyde + Site \rightarrow Aldehyde_ads | 0.120 | See Sim. 1 | M ⁻¹ s ⁻¹ | 1 |
| 4 | Aldehyde_ads \rightarrow Aldehyde + Site | 8.0 x 10 ⁻⁴ | See Sim. 1 | s ⁻¹ | 1 |
| 5 | Imine + Site \rightarrow Imine_ads | 0.120 | See Sim. 1 | M ⁻¹ s ⁻¹ | 1 |
| 6 | Imine_ads \rightarrow Imine + Site | 2 | See Sim. 1 | s ⁻¹ | 2, a |
| 7 | Amine_ads + Aldehyde_Ads \rightarrow Imine_ads + Site | 1.54 x 10 ⁻³ | 3.22 x 10 ⁻³ | M ⁻¹ s ⁻¹ | 3 |
| 8 | Imine_ads \rightarrow Amine_ads + Aldehyde_Ads | 1.52 x 10 ⁻³ | See Sim. 1 | s ⁻¹ | 2 |
| Diffusion Pathways | | Diffusion Coefficient | Diffusion Coefficient | | |
| 9 | Amine (Bulk) \leftrightarrow Amine (Surface) | 5.02 x 10 ⁻⁶ | See Sim. 1 | cm ² s ⁻¹ | 2 |
| 10 | Aldehyde (Bulk) \leftrightarrow Aldehyde (Surface) | 4.46 x 10 ⁻⁶ | See Sim. 1 | cm ² s ⁻¹ | 2 |
| 11 | Imine (Bulk) \leftrightarrow Imine (Surface) | 2.39 x 10 ⁻⁶ | See Sim. 1 | cm ² s ⁻¹ | 2 |
| Bulk Compartment | | Rate Coefficient | Rate Coefficient | | |
| 12 | Amine + Aldehyde \rightarrow Imine | 2.60 x 10 ⁻⁵ | See Sim. 1 | M ⁻¹ s ⁻¹ | 2 |
| 13 | Imine \rightarrow Amine + Aldehyde | 1.52 x 10 ⁻³ | See Sim. 1 | s ⁻¹ | 2 |

^a The value of this rate coefficient is selected to produce simulation results consistent with the experimental observations in Ref. ²

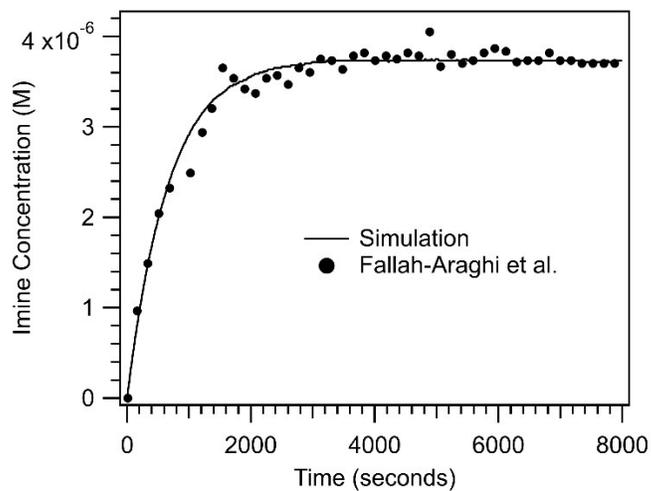


Figure S1: Imine concentration vs. reaction time measured in a bulk solution. Points are data reproduced from Ref. ² and the line is a fit from simulations in order to constrain the forward and reverse rates for the bulk reaction (Steps 12 and 13 Table 2).

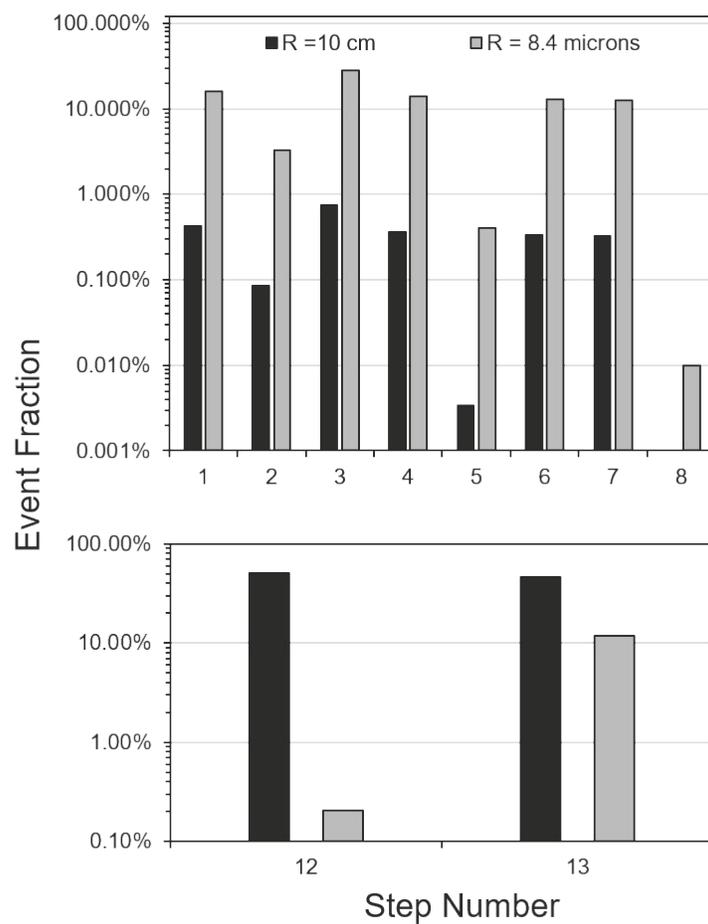


Figure S2: Event fraction in the surface (top) and bulk (bottom) compartments as a function of reaction step number (see Table 2) for $R=8.4 \mu\text{m}$ and $R = 10 \text{ cm}$.

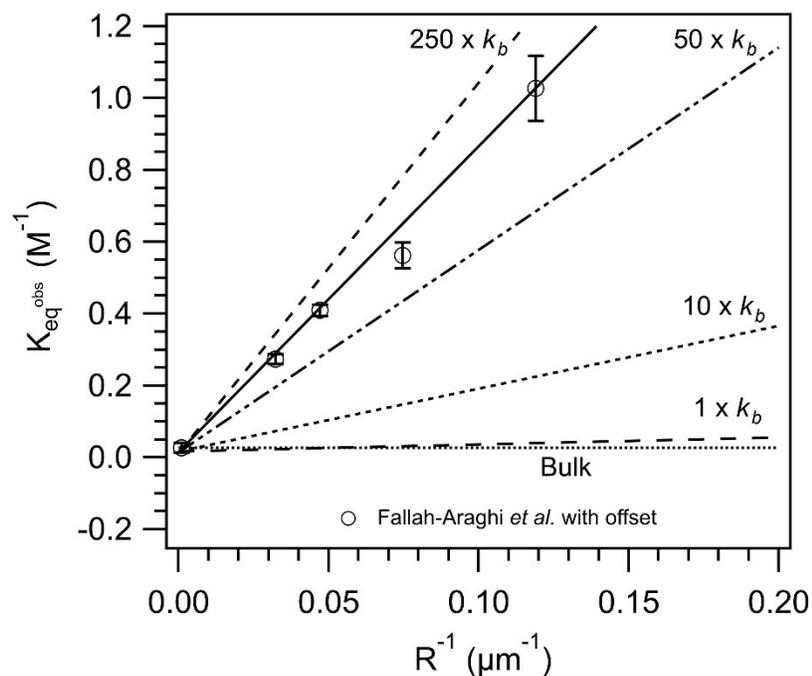


Figure S3: Sensitivity of simulated K_{eq}^{obs} vs. R^{-1} for [amine]=[aldehyde] = 15mM. Lines represent different simulated values for the surface forward rate coefficient for imine synthesis (Step 7, Table S2). These rate coefficients are expressed as multiples of the bulk value (k_b) (see Step 12, Table S2).

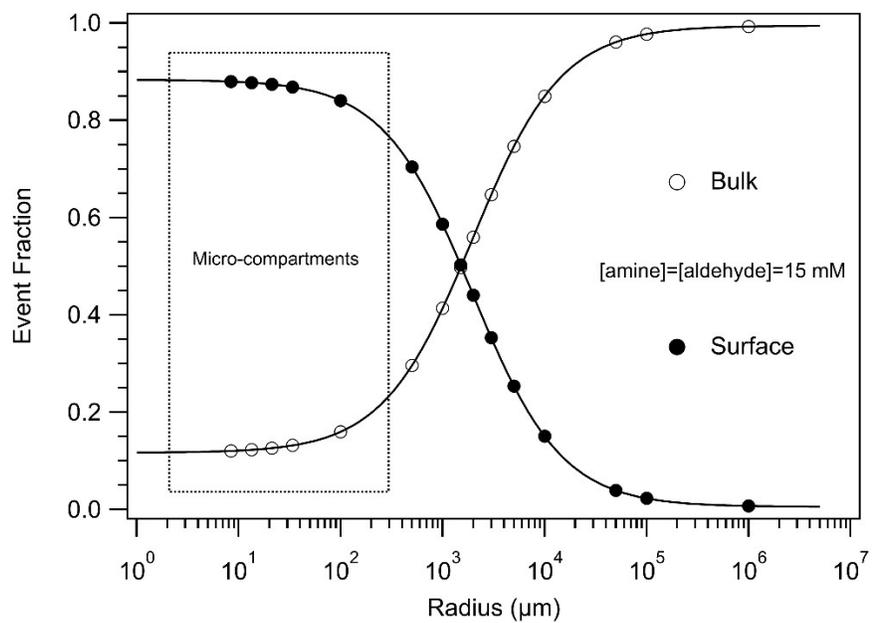


Figure S4: Bulk and surface event fractions as a function of radius for simulation 2 ($[\text{amine}] = [\text{aldehyde}] = 15 \text{ mM}$). Lines are guides for the eye.

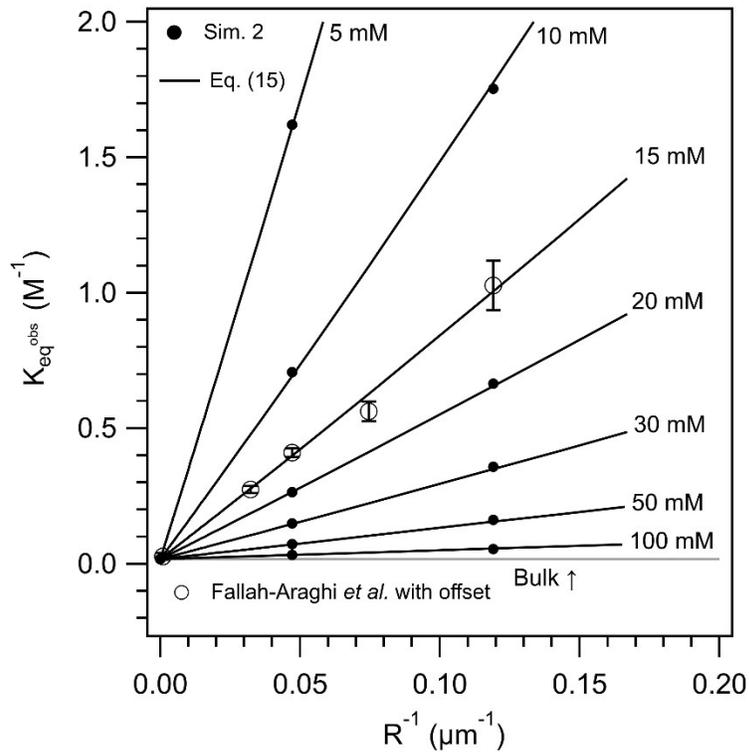


Figure S5: K_{eq}^{obs} vs. R^{-1} and concentration for [amine]=[aldehyde]. Comparison of experimental data from Ref. ², results from simulation 2 and predictions from Eq. (15). $K_{eq}^B = 0.017 M^{-1}$ and is shown in the figure as a gray line.

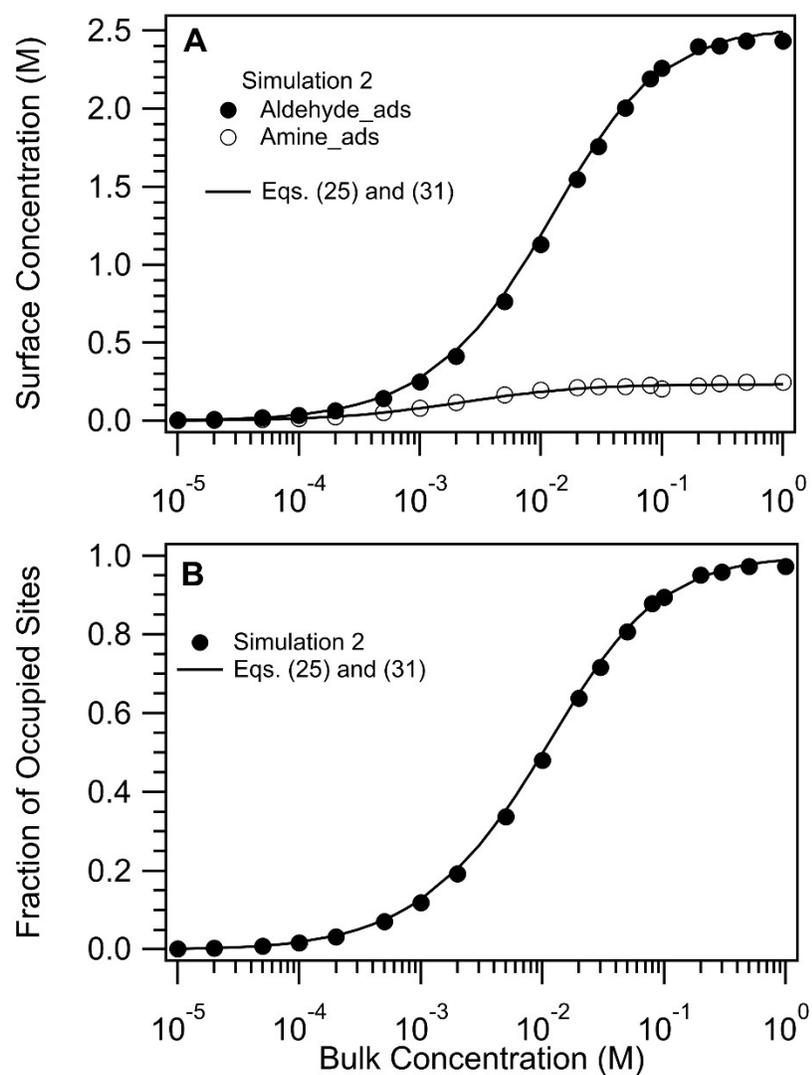


Figure S6: Surface concentrations of (A) adsorbed amine and aldehyde and (B) fraction of occupied surface sites vs. bulk concentration for $R = 8.4 \mu\text{m}$. Simulation 2 results (points) are compared with predictions from Eqs. (31) and (25).

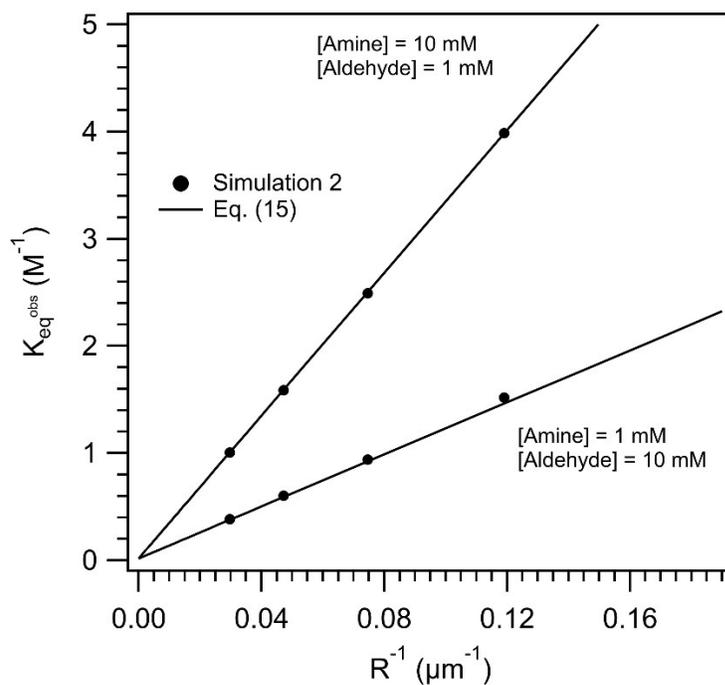


Figure S7: K_{eq}^{obs} vs. R^{-1} for non-stoichiometric reactant concentrations (i.e. [amine] \neq [aldehyde]): simulation 2 (points) and prediction (lines) from Eq. (15).

Supporting References

1. Tomoaia, G.; Tomoaia-Cotisel, A.; Tomoaia-Cotisel, M.; Mocanu, A., Kinetic study of adsorption of some biocompounds at the oil/water interface. *Cent. Eur. J. Chem.* **2005**, *3*, (2), 347-360.
2. Fallah-Araghi, A.; Meguellati, K.; Baret, J.-C.; Harrak, A. E.; Mangeat, T.; Karplus, M.; Ladame, S.; Marques, C. M.; Griffiths, A. D., Enhanced Chemical Synthesis at Soft Interfaces: A Universal Reaction-Adsorption Mechanism in Microcompartments. *Phys. Rev. Lett.* **2014**, *112*, (2), 028301.

3. Meguellati, K.; Fallah-Araghi, A.; Baret, J.-C.; El Harrak, A.; Mangeat, T.; Marques, C. M.; Griffiths, A. D.; Ladame, S., Enhanced imine synthesis in water: from surfactant-mediated catalysis to host–guest mechanisms. *Chem. Commun.* **2013**, *49*, (96), 11332-11334.