

**Supporting Information for
Modeling response characteristics of photo-sensitive hydrogel
electrolytes in Hofmeister salt solution for the development of smart
energy storage devices**

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Table S1. Some input parameters for the numerical simulation. 1

Table S1. Some input parameters for the numerical simulation.

Parameter	Value
Polymer chain density in the dry gel, N_R [1, 2]	$1.08 \times 10^{25} \text{ m}^{-3}$
Photo-kinetic factor, F_L [3, 4]	1.94
Logarithm of frequency factor, $\log (A_T / 1 \text{ s}^{-1})$ [5]	16.96
Activation energy, E_T [5]	114.41 kJ·mol ⁻¹
Interaction parameter at a lower temperature than LCST, χ_L	0.33
Interaction parameter at a higher temperature than LCST, χ_H	0.62
Dehydration coefficient, G_H^* [5-7]	$1.8 \times 10^{-3} \text{ mM}^{-1}$ at pH<7.0 and 0 mM ⁻¹ at pH≥7.0
Permittivity, ϵ [8]	$7.08 \times 10^{-10} \text{ C}^2 \cdot \text{N}^{-1} \cdot \text{m}^{-2}$
Logarithmic acidity constant of McH ⁺ , pKa ₁ [4]	6.8

Logarithmic acidity constant of SpH ⁺ , pKa ₂ [4]	2.6
Logarithmic acidity constant of AAH, pKa ₃ [7]	4.2
Logarithmic acidity constant of H ₂ PO ₄ ⁻ , pKa ₄ [9]	7.21
Logarithmic acidity constant of HPO ₄ ²⁻ , pKa ₅ [9]	12.32
Equilibrium constant of water, K _w [8]	10 ⁻¹⁴ M ²
Initial transition temperature, T ₀ [6]	33 °C
Temperature width of phase transition, ΔT _c [6]	4 °C
Molar volume of solvent molecule, v [10]	1.8×10 ⁻⁵ m ³ ·mol ⁻¹
Ring-opened reaction rate constant, k _o [11]	2.53×10 ⁻³ s ⁻¹
Light wavelength, λ _L [6]	436 nm
Molar absorption coefficient, ε _L [4]	2.3×10 ⁴ M ⁻¹ cm ⁻¹
Quantum yield, φ _L [12]	7%
Polymer-solvent structural constant, k ₁ and k ₂ [13]	k ₁ =0.066, k ₂ =0.263
Diffusivity of H ⁺ , D̄ _{H⁺} [14]	(8.79-11.20)×10 ⁻⁹ m ² ·s ⁻¹
Diffusivity of Na ⁺ , D̄ _{Na⁺} [15]	(1.20-1.88)×10 ⁻⁹ m ² ·s ⁻¹
Diffusivity of Cl ⁻ , D̄ _{Cl⁻} [15]	(1.84-2.82)×10 ⁻⁹ m ² ·s ⁻¹
Diffusivity of SO ₄ ²⁻ , D̄ _{SO₄²⁻} [15]	1.07×10 ⁻⁹ m ² ·s ⁻¹
Diffusivity of NO ₃ ⁻ , D̄ _{NO₃⁻} [15]	(1.75-2.61)×10 ⁻⁹ m ² ·s ⁻¹
Diffusivity of H ₂ PO ₄ ⁻ , D̄ _{H₂PO₄⁻} [16]	9.59×10 ⁻¹⁰ m ² ·s ⁻¹
Diffusivity of HPO ₄ ²⁻ , D̄ _{HPO₄²⁻} [16]	7.59×10 ⁻¹⁰ m ² ·s ⁻¹
Diffusivity of PO ₄ ³⁻ , D̄ _{PO₄³⁻} [16]	6.1×10 ⁻¹⁰ m ² ·s ⁻¹
Hydrated radii of H ⁺ , r _{H⁺} [15]	2.82 Å
Hydrated radii of Na ⁺ , r _{Na⁺} [15]	3.58 Å
Hydrated radii of Cl ⁻ , r _{Cl⁻} [15]	3.32 Å
Hydrated radii of SO ₄ ²⁻ , r _{SO₄²⁻} [15]	3.79 Å

Hydrated radii of NO_3^- , $r_{\text{NO}_3^-}$ [15]	3.35 Å
Hydrated radii of H_2PO_4^- , $r_{\text{H}_2\text{PO}_4^-}$ [17]	3.41 Å
Hydrated radii of HPO_4^{2-} , $r_{\text{HPO}_4^{2-}}$ [17]	3.79 Å
Hydrated radii of PO_4^{3-} , $r_{\text{PO}_4^{3-}}$ [17]	3.85 Å

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<http://clas.sa.ucsb.edu/staff/Resource%20folder/Chem109ABC/Acid,%20Base%20Strength/Table%20of%20Acids%20w%20Kas%20and%20pKas.pdf>.
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