

## Supporting information:

### 1. Static and Dynamic Light Scattering (SLS and DLS)

Static light scattering (SLS) and dynamic light scattering (DLS) were conducted as a function of the detection angle  $\theta$ . In SLS measurements, the scattering intensities for sample ( $I_s$ ), toluene ( $I_{tol}$ ), and PBS as solvent ( $I_0$ ) were measured as a function of the scattering angle  $\theta$  (range from 30 to 130°). Furthermore, the dark current  $I_{dark}$  (detector intensity with laser switched off) was measured. The obtained intensities were converted into Rayleigh scattering ( $R$ ) to obtain absolute scattering of the sample according to equation 1:

$$(1) \quad R(\theta) = \left( \frac{I_s(\theta) - I_0(\theta)}{I_{tol}(\theta) - I_{dark}} \right) \frac{n_s^2}{n_{tol}^2} R_{tol}$$

In which  $n_{tol} = 1.494$  and  $n_s = 1.332$  are the refractive index of the reference and solvent, respectively, and  $R_{tol}$  is the known absolute Rayleigh scattering for toluene at 632.8 nm wavelength. For  $R_{tol}$ , we used  $1.02 \cdot 10^{-3} \text{ m}^{-1}$ .<sup>1</sup> Then, the scattering angle  $\theta$  was converted into the wave vector  $q$  based on equation 2:

$$(2) \quad q = \frac{4\pi n_s \sin \frac{\theta}{2}}{\lambda}$$

where  $\lambda$  is the wavelength in vacuum.

- Therefore,  $R_g$  was obtained according to Guinier<sup>2</sup> by plotting  $\ln(R)$  as a function of  $q^2$  in which the slope is equal to:  $\frac{R_g^2}{3}$  (results are shown in table 1)
- Hydrodynamic radius ( $R_h$ ) was obtained by DLS. The decay rate,  $\Gamma$ , extracted from the second order cumulant was plotted as a function of  $q^2$ . For monodisperse particles this should result in a straight line with a slope equals to the diffusion coefficient  $D$  and from that  $R_h$  was obtained using the Stokes Einstein equation 3: (results are shown in table 1)

$$(3) \quad D = \frac{kT}{6\pi\eta R_h}$$

- To obtain  $M_w$ , the absolute scattering intensity  $R$  was plotted as a function of  $q$  and extrapolated to  $q = 0$ . The absolute scattering  $R$  should equal to: (results are shown in table 1)

$$(4) \quad R = K_r C M_w S(q) P(qR)$$

At low concentration, the structure factor  $S(q) \approx 1$  and at  $q \rightarrow 0$  the form factor was considered  $P(qR) = 1$ , therefore,  $R(q \rightarrow 0) = K_r C M_w$  where  $K_r$  an optical constant (equation 5) and  $C$  the particle concentration in  $\text{kg} \cdot \text{m}^{-3}$ .

$$(5) \quad K_r = \frac{4n_s^2 \pi^2}{\lambda^4 N_{Av}} \left( \frac{dn}{dc} \right)^2$$

**Table 1:** Characteristics of core crosslinked flower-like micelles measured at 10 and 40 °C; For comparison, micelle characteristics at other temperatures have been reported before for a slightly different polymer batch.<sup>3</sup>

T (°C)	R <sub>g</sub> (nm) <sup>a</sup>	R <sub>h</sub> (nm) <sup>b</sup>	R <sub>g</sub> /R <sub>h</sub>	M <sub>w</sub> (mic.) (10 <sup>6</sup> Da)	N <sub>agg</sub> <sup>d</sup>
10	46.0±0.8	48.2±0.9	0.95±0.00	16.3±0.4	430±10
40	30±0.8	35.4±0.4	0.85±0.01	14.8±0.2	381±10

## 2. Calculation of Effective Volume Fraction ( $\varphi$ )

$$V_t = \text{Micelles (mg)} \times 0.83 \text{ cm} \cdot \text{g}^{-1} (\text{partial specific volume of PNIPAM})^1 + \text{PBS (mL)}$$

$$\text{Number of micelles} = \frac{\text{Micelles (gr)}}{N_A \times M_w \text{ micelle}}, \text{ where } N_A \text{ is Avogadro constant and } M_w \text{ micelle molecular weight (15.55} \times 10^6 \text{ kDa as the average molecular weight of micelles at 10 and 40 } ^\circ\text{C was considered)}$$

$$V_m = \text{number of micelles} \times \text{volume of micelles at the corresponding temperature}$$

**Table 2:** The summary of results for calculation of  $\varphi$ .  $T_c$  is 28 °C.

Sample conc. (wt%)	Micelles (mg)	PBS (mL)	Sample volume ( $V_t$ ) (mL)	Number of micelles ( $\times 10^{15}$ )	Volume of micelles ( $V_m$ )(mL)		$\varphi$ or ( $\frac{V_t}{V_m}$ )	
					Below $T_c$	Above $T_c$	Below $T_c$	Above $T_c$
7.5	75	0.925	0.987	2.89	1.34	0.52	1.36	0.53
10	100	0.900	0.983	3.86	1.79	0.69	1.82	0.7
12.5	125	0.875	0.979	4.82	2.23	0.87	2.28	0.88
15	150	0.850	0.975	5.79	2.68	1.04	2.75	1.07
20	200	0.800	0.966	7.72	3.57	1.39	3.7	1.43
30	300	0.700	0.949	11.6	5.36	2.08	5.65	2.19

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2. Guinier, A.; Fournet, G., *Small-Angle Scattering of X-Rays*. John Wiley and Sons, Inc., New York, 1955.
3. Najafi, M.; Kordalivand, N.; Moradi, M. A.; van den Dikkenberg, J.; Fokkink, R.; Friedrich, H.; Sommerdijk, N.; Hembury, M.; Vermonden, T., Native Chemical Ligation for Cross-Linking of Flower-Like Micelles. *Biomacromolecules* **2018**, *19* (9), 3766-3775.
4. Sommer, C.; Pedersen, J. S.; Stein, P. C., Apparent Specific Volume Measurements of Poly(ethylene oxide), Poly(butylene oxide), Poly(propylene oxide), and Octadecyl Chains in the Micellar State as a Function of Temperature. *The Journal of Physical Chemistry B* **2004**, *108* (20), 6242-6249.