

**Figure S0.** The free-energy state is tightly correlated with the temperature. (a) The detailed free-energy states reflected by polarization distributions against decreasing temperature and (b) the corresponding evolution of free-energy against decreasing temperature. Rapid quenching from extraordinarily high temperatures freezes the high-energy states, leading to the longer coherence length and the enhanced polarization summation.