Electronic Supplementary Information

Multifunctional Nanostructure of Au-Bi₂O₃ Fractals for CO₂ Reduction and Optical Sensing

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Fractal Analysis

In this analysis, we used FracLac (an open-source plugin run in ImageJ)¹⁻³, which uses a "box counting" method to find the fractal dimension (D_f) and lacunarity (Λ) on the pixel distribution of a SEM images of samples. Typically, D_f of an object shows the similar patterns evolving through different length-scales and follows the power law.⁴⁻⁵

$$N = k_0 \left(\frac{r_g}{r}\right)^{D_f}$$
(S1)

where N is the number of monomers, k_o is a constant prefactor of order unity, r_g is the overall aggregate radius or gyration radius, r is radius of monomer. By defining $\varepsilon = r/r_g$, equation S1 can be written as:

$$N = k_0 \left(\varepsilon\right)^{-D_f} \tag{S2}$$

Equation S2 can be reshaped after taking logarithm of both sizes as follows:

$$\ln(N) = \ln(k_0) - D_f \ln(\varepsilon)$$
(S3)

Then fractal dimension can be evaluated from the slope (D_f) of equation S3 where the x-axis is $\ln(\varepsilon)$ and the y-axis is $\ln(N)$.

After obtaining SEM images, the foreground pixels with box size ε were counted during the scan, and 12 different box sizes were set. The generated fractal after scans were used to evaluate the D_f by taking an average of $\ln(N)$ and $\ln(\varepsilon)$.

For each box size ε the mean, μ , and the standard deviation, σ , for each box size were calculated. Then the lacunarity, Λ , was evaluated for each box size as $\Lambda = (\sigma/\mu)^2$, and the average lacunarity was computed as $\Lambda = \frac{1}{n} \sum_{i} (\sigma/\mu)^2 + 1$.



Figure S1. XRD of the Au- Bi_2O_3 fractal with references of Au and Bi_2O_3 patterns: inset are optical images of Au- Bi_2O_3 fabricated on CFP at different Au concentrations and on glass at different deposition times.



Figure S2. (a,b) TEM images of the Au-Bi₂O₃ with 5% of Au at different magnifications, (c) histogram of the particle distribution of the Au and Bi₂O₃, showing that Au and Bi₂O₃ have average particle sizes of 11.8 nm and 13.6 nm respectively, and (d) the top-view SEM image obtained with an angle-sensitive backscatter detector to provide difference in contrast of different atomic number elements: herein the Au nanoparticles are brighter than Bi₂O₃.



Figure S3. XPS spectra of Au-Bi₂O₃ with 5% Au before CO₂RR test: (a) survey spectrum, (b-d) high resolution spectra of (b) Bi 4f with the Bi $4f_{7/2}$ and Bi $4f_{5/2}$ peaks at 159.35 and 164.66 eV respectively, (c) Au 4f with the Au $4f_{7/2}$ and Au $4f_{5/2}$ peaks at 84.20 and 87.87 eV respectively, and (d) O 1s with a component peaked at 530.01 eV is assigned to the oxygen in metal oxides.



Figure S4. Thermogravimetric analysis (TGA) measurement of $Au-Bi_2O_3$ with 5% Au shows that the total carbon content on the surface of the fractal platform is less than 2%.



Figure S5. Dependence of Faradaic efficiency on applied potential for control (a) Bi_2O_3 and (b) Au on CFP in CO_2 saturated 0.1 M KHCO₃.



Figure S6. Representative chronoamperometry (*i-t*) curve for Au-Bi₂O₃ (5% Au) at -1.1 V vs RHE in CO₂ saturated 0.1 M KHCO₃.



Figure S7. Stability testing results for $Au-Bi_2O_3$ at -1 V vs RHE in CO_2 saturated 0.1 M KHCO₃.



Figure S8. Morphological and compositional characterization of the Au- Bi_2O_3 (5% of Au) after CO₂RR. (a) SEM images, (b-c) TEM images of samples at different magnifications, (d) electron diffraction pattern, (e) HAADF STEM image and (f) EDS elemental mapping.



Figure S9. XPS spectra of Au-Bi₂O₃ with 5% Au after CO₂RR: (a) survey spectrum, (b-d) high resolution spectra of (b) Bi 4f with the Bi $4f_{7/2}$ and Bi $4f_{5/2}$ peaks at 159.20 and 164.50 eV respectively, (c) Au 4f with the Au $4f_{7/2}$ and Au $4f_{5/2}$ peaks at 84.20 and 87.87 eV respectively, and (d) O 1s with a component peaked at 530.73 eV is assigned to the oxygen in metal oxides.



Figure S10. (a) Electron impedance spectroscopy (EIS), (b) Mott-Schottky (MS) analysis (the slope of the Mott-Schottky plot for each sample was linearly fitted in the potential window between -1.2 and -0.5 V), and (c) relative electron density of different Au concentration.



Figure S11. EPR spectra of Bi_2O_3 and $Au-Bi_2O_3$ (baseline subtracted). The spectra were obtained using 10.8 mg Bi_2O_3 and 9.0 mg Au/Bi_2O_3 under 120 K.



Figure S12. FEM simulation results demonstrating the distribution of the electric field in Bi_2O_3 containing (a) 1% and (b) 10% Au. More "hot edges" can be seen when the Au concentration was increased from 1% to 10%.



Figure S13. TEM images and histograms of the Au-Bi₂O₃ with different Au concentration. (a-c) 1% Au and (d-f) 10% Au. The mean of particle size has increased from 6.52 to 35.13 nm when the Au concentration increased from 1 to 10%. This increase leads to more Au surface exposed to the electrolyte to get involved into CO₂RR into CO product, resulting in an increase in the ratio of CO to formate product.



Figure S14. Dependence of current density on applied potentials for $Au-Bi_2O_3$ with different Au loading in CO_2 saturated 0.1 M KHCO₃.

Figure S15. Dependence of FE_{H2} and FE_{CO} at -1.1 V vs RHE for Au-Bi₂O₃ with different Au loading in CO₂ saturated 0.1 M KHCO₃.

Figure S16. Cyclic voltammetry from different samples at different scant rates (a) Bi_2O_3 , (bd) Au- Bi_2O_3 with 1%, 5%, and 10% Au respectively, and (e) capacitive current vs scan rates plot at applied potential of 0.7 vs RHE for all samples.

Figure S17. Growth rate. (a-c) Cross-sectional scanning electron microscope images of the 3D fractal Au (5%)- Bi_2O_3 metamaterials for aerosol deposition times of 1, 2 and 3 minutes, respectively. (d) Film thickness as a function of the deposition time indicates a linear growth rate, proving an excellent way for tuning the metamaterial properties.

Figure S18. (a) Static extinction measurements of the 6.1 µm thick (3 min of deposition time) Au-Bi₂O₃ upon 4 vol% acetone injection at room temperature (RT). Note the drastic change that this VOC causes on the optical properties. (b) Plasmonic shift as a function of surrounding refractive index difference ($\Delta n = n_{gas} - n_{air}$) for the different tested VOCs. (c) Plasmonic wavelength shift upon different on/off injection cycles of acetone with different concentrations at room temperature for 8.5µm sample.

Figure S19. (a-d) The generated fractal structure of the 500 nm particles from different viewpoints with a plane cutting cross the structure to obtain the projection area, (e) the projection area obtained from the 3D structure of Bi_2O_3 (yellow) after adding three gold nanoparticles (red), and (f) electric field norm with flux distribution (arrow) obtained from the Electrostatics model from COMSOL Multiphysics.

Supporting Tables:

Table S1. CO₂RR catalytic performances of various Bi-based catalysts in similar operating conditions for HCOO⁻ production.

Catalyst	Electrolyte	Onset Potential (V vs RHE)	Operating Potential (V vs RHE)	Current Density (mA/cm ²)	Mass specific formate partial current density (mA/mg)	Faradaic Efficiency for HCOO ⁻ (%)	Reference
Au-Bi ₂ O ₃ fractal	0.1 M KHCO ₃	-0.6	-1.1	-22.6	-54	97	This Work
Bi ₂ O ₃ nanotubes derived Bi	0.5 M KHCO ₃	-0.6	-1.0	-64	-60	~94	6
Bi-Sn	0.5 M KHCO ₃ with 600 rpm stirring	-0.64	-1.14	-61	(Mass loading not provided)	94	7
Bi ₂ S ₃ derived Bi	0.5 M NaHCO ₃	-0.55	-0.75	-5	-14.7	84	8
Bi nanosheets	0.5 M NaHCO ₃	-0.65	-0.9	-15	-15	99	9
Fractal-Bi ₂ O ₃	0.1 M KHCO ₃	-0.6	-1.2	-24	-52.2	87	10
Bi nanoparticles/Bi ₂ O ₃ nanosheets	0.5 M NaHCO ₃	-0.75	-0.85	-6	(Mass loading not provided)	~100	11
BiNS	0.5 M NaHCO ₃	-1.3 V vs SCE	-1.5 V vs SCE	-14	-3.5	95	12
Eutectic Bi-Sn	0.1 M KHCO ₃	-0.9	-1.1	-13	-10.1	78	13
Bi nanosheets	0.1 M KHCO ₃	-0.5	-1.1	-16.5	-8.25	86	14

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