

# Enhancing the Performance of Supercapacitors through Constructing “Mini Parallel-Plate Capacitor” in Electrode with High Dielectric Constant Materials

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## S1. Chemicals

FeCl<sub>3</sub> · 6H<sub>2</sub>O, V<sub>2</sub>O<sub>5</sub>, SnCl<sub>4</sub> · 5H<sub>2</sub>O, tetrabutyl titanate (TBT), Urea, SDS, CTAB, HCl, ethylene glycol (EG), KOH, H<sub>2</sub>O<sub>2</sub>, NaBr, H<sub>2</sub>C<sub>2</sub>O<sub>4</sub> and ethanol were purchased from Sinopharm Chemical Reagent Co., Ltd. (Shanghai). All those reagents were analytical grade. NH<sub>3</sub>, N<sub>2</sub> purchased from Deyang special Gas Co., Ltd. (Jinan, China).

## S2. Synthetic Methods

**Preparation of acid treated carbon fiber:** In a typical procedure, a piece of carbon fiber cloth (1.5 cm × 4cm) was subsequently cleaned with DI water and ethanol under ultrasonic, and dried in an oven. Then, the freshly cleaned CF was added into a stainless-steel autoclave (100mL) containing commercially available concentrated HNO<sub>3</sub> (50 mL) and DI water (15 mL), and was hold at 120 °C for 12 h. Then, the resulted CF was washed thoroughly with DI water until the pH is close to 7.

**Synthesis of FeO<sub>x</sub>N<sub>y</sub> nanorods:** a Teflonlined stainless-steel autoclave with a capacity of 50 mL was filled with 30 mL of an aqueous solution containing 0.4 g ferric chloride (FeCl<sub>3</sub>·6H<sub>2</sub>O), 0.2 g urea, and 0.02 g sodium lauryl sulfate (SDS). A 1.5 cm × 4 cm piece of clean carbon fiber treated with air plasma was immersed in the precursor solution in an autoclave. The autoclave was heated at 100 °C for 12 h and then cooled to room temperature. Hydroxides grown on the carbon fiber were washed with deionized water and ethanol and dried at 60 °C in air. The asprepared FeOOH samples were further thermally annealed at 350 °C under NH<sub>3</sub> atmosphere for 2 h at the heating rate of 2 °C min<sup>-1</sup>. For comparison, the Fe<sub>2</sub>O<sub>3</sub> samples was obtained by annealed at 350 °C under nitrogen (N<sub>2</sub>) atmosphere for 2 h. Powder samples of Fe<sub>2</sub>O<sub>3</sub> were prepared by the same method.

**Synthesis of VO<sub>x</sub>N<sub>y</sub> nanorods:** first, 0.9 g of V<sub>2</sub>O<sub>5</sub> powder and 1.35 g of H<sub>2</sub>C<sub>2</sub>O<sub>4</sub> powder were dissolved with 30 mL of distilled water at 75 °C for 12h. 10 ml of the above solution was transferred into a 50 mL Teflon lined stainless steel autoclave. Then 1 mL of 30% H<sub>2</sub>O<sub>2</sub> and 20 mL of ethanol were added and kept continuously stirring for about 30 min; then, one piece of acid treated clean carbon fiber (1.5 cm × 4 cm) was immersed into the reaction solution. The autoclave liners were kept at 180 °C for 3 h and then the sample was collected and rinsed with ethanol and distilled water. The obtained hydroxide array growth on the carbon cloth was washed with deionized (DI) water, ethanol and dried at 60 °C. Following the as-prepared samples were further thermally annealed at 550 °C under ammonia (NH<sub>3</sub>) atmosphere for 1 h with the heating rate of 3°C min<sup>-1</sup>, during the heating and cooling process use N<sub>2</sub> atmosphere protection.

For comparison, the VO<sub>2</sub> samples was obtained by annealed at 550°C under nitrogen (N<sub>2</sub>) atmosphere for 2 h. Powder samples of VO<sub>2</sub> were prepared by the same method.

**Synthesis of SnO<sub>x</sub>N<sub>y</sub> nanorods:** first, 0.927 g of NaBr powder were dissolved with 3 mL of distilled water in beaker A and stirred 0.5 hour. Identically, 0.1 g of SnCl<sub>4</sub>·5H<sub>2</sub>O were dissolved with 20 mL of glacial acetic acid in beaker B and stirred 0.5 hour. Then, the solution in beaker A and beaker B was mixed and stirred for 0.5 hour to form mixed solution. After that, the above solution was transferred into a 50 mL Teflon lined stainless steel autoclave and 3 mL of ethanol (Et) were added and kept continuously stirring for about 0.5 hour; then, one piece of acid treated clean carbon fiber (1.5 cm × 4 cm) was immersed into the reaction solution. The autoclave liners was kept at 200 °C for 24 h and then the obtained hydroxide array growth on the carbon fiber was washed with deionized (DI) water, ethanol and dried at 60°C. Following the as-prepared samples were further thermally annealed at 475°C under ammonia (NH<sub>3</sub>) atmosphere for 4 h with the heating rate of 3 °C min<sup>-1</sup>, during the heating and cooling process use N<sub>2</sub> atmosphere protection. For comparison, the SnO<sub>2</sub> samples was obtained by annealed at 475 °C under nitrogen (N<sub>2</sub>) atmosphere for 4 h. Powder samples of SnO<sub>2</sub> were prepared by the same method.

### **S3. Materials Characterization**

The morphology and phase structure of the samples were investigated with FESEM (Hitachi-4800), HRTEM (JEM 2100F), XRD (Bruker D8 Advance), XPS (Philips Tecnai Twin-20U), and Raman (Horiba Jobin Yvon), respectively.

## S4. Electrochemical Tests

The electrochemical characterizations of the CM and the CMM were tested using a three-electrode system on a CHI660E electrochemical workstation (Shanghai Chen Hua Instruments Co., China). In the test system, the self-supported binder-free CM and CMM were used as the work electrode, with a platinum sheet (2 cm × 2 cm) as a counter electrode and Hg/HgO as a reference electrode, in 6.0 M KOH aqueous solution.

All the electrochemical measurements with galvanostatic charge/discharge (GCD), cyclic voltammetry (CV), and electrochemical impedance spectroscopy (EIS) techniques were conducted in three-electrode system. For detail, CV and GCD curves were collected at -1 V to 0 V against Hg/HgO by varying the scan rate from 5 mV s<sup>-1</sup> to 100 mV s<sup>-1</sup> and current density from 0.1 A g<sup>-1</sup> to 10 A g<sup>-1</sup>, respectively. Alternating current EIS spectra were collected within a frequency range of 10<sup>-2</sup> Hz – 10<sup>5</sup> Hz at the open circuit voltage with AC amplitude of 5 mV.

For three-electrode cells, specific capacity derived from GCD discharge curves was calculated as:

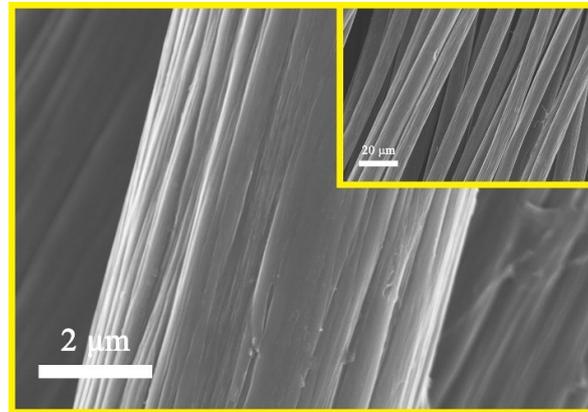
$$C(F/g) = I \int (1/V(t))dt$$

where I is the applied constant-current density, t is the discharge time, and V(t) is the potential as a function of t.

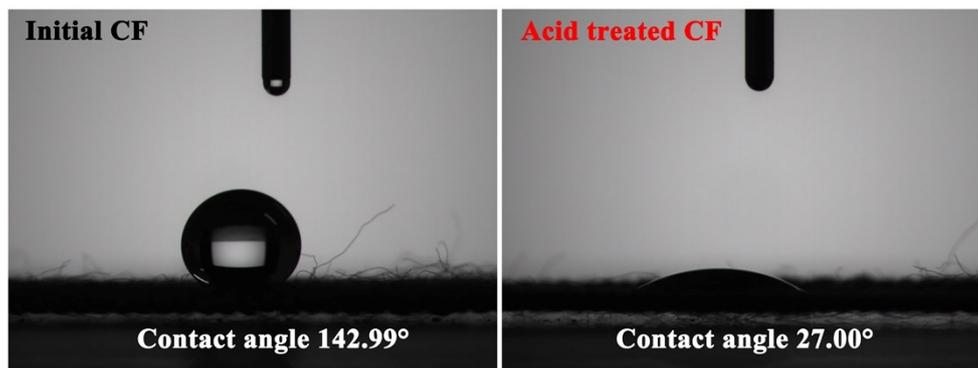
Dielectric constant test of metal oxide materials: The metal oxide powder of the corresponding crystal type and morphology is pressed into a small wafer with an area of 1.37 mm<sup>2</sup> and a certain thickness (0.75~1.37 mm) by a tablet press, and its capacitance and dielectric loss are measured by Impedance analyzer (Agilent-4294A).

Then, the dielectric constant of the metal oxide is obtained from the measured capacitance.

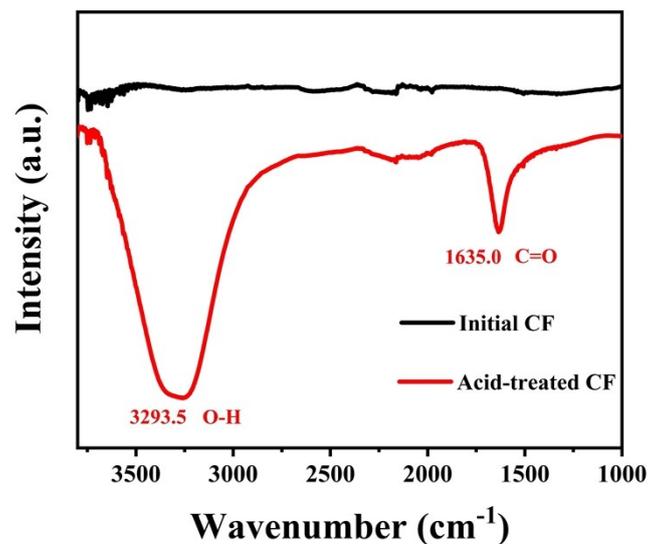
### S5. Supplementary Figures S1–S19



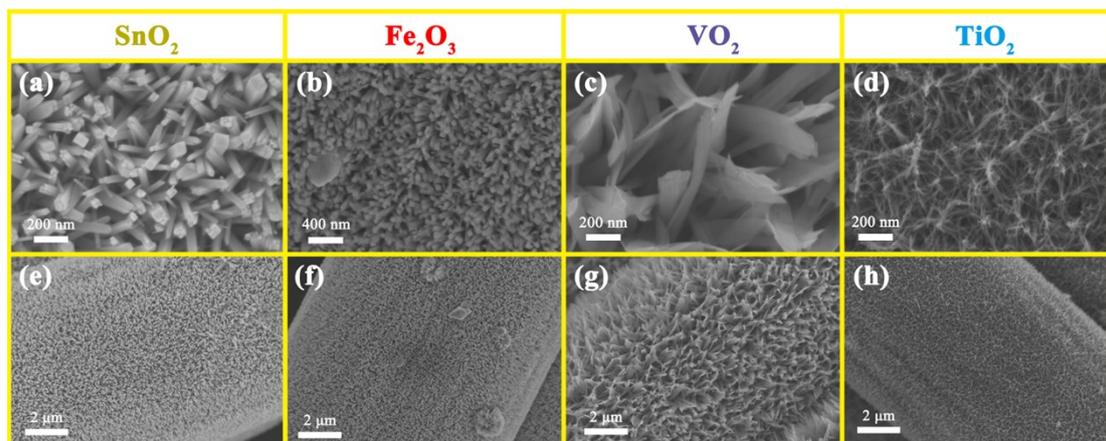
**Figure S1.** SEM image of acid treated clean carbon fiber.



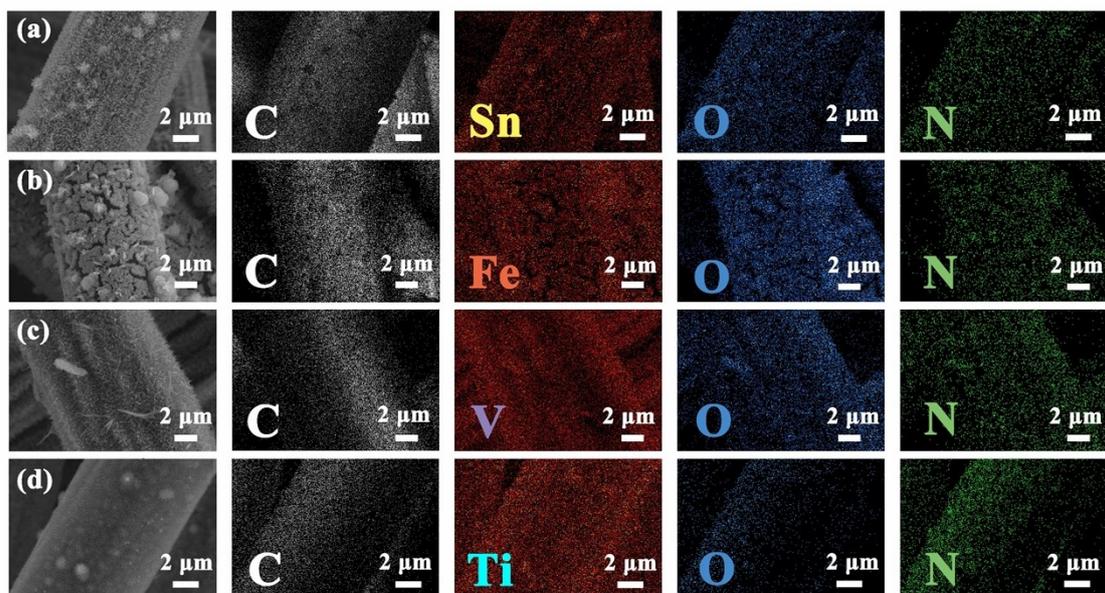
**Figure S2.** Water contact angles of CF and acid treated clean CF.



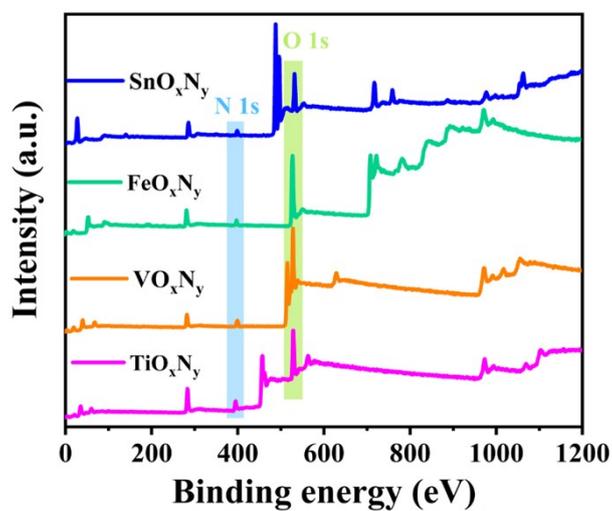
**Figure S3.** Fourier transform infrared spectroscopy (FTIR) spectra of CF and acid treated clean CF.



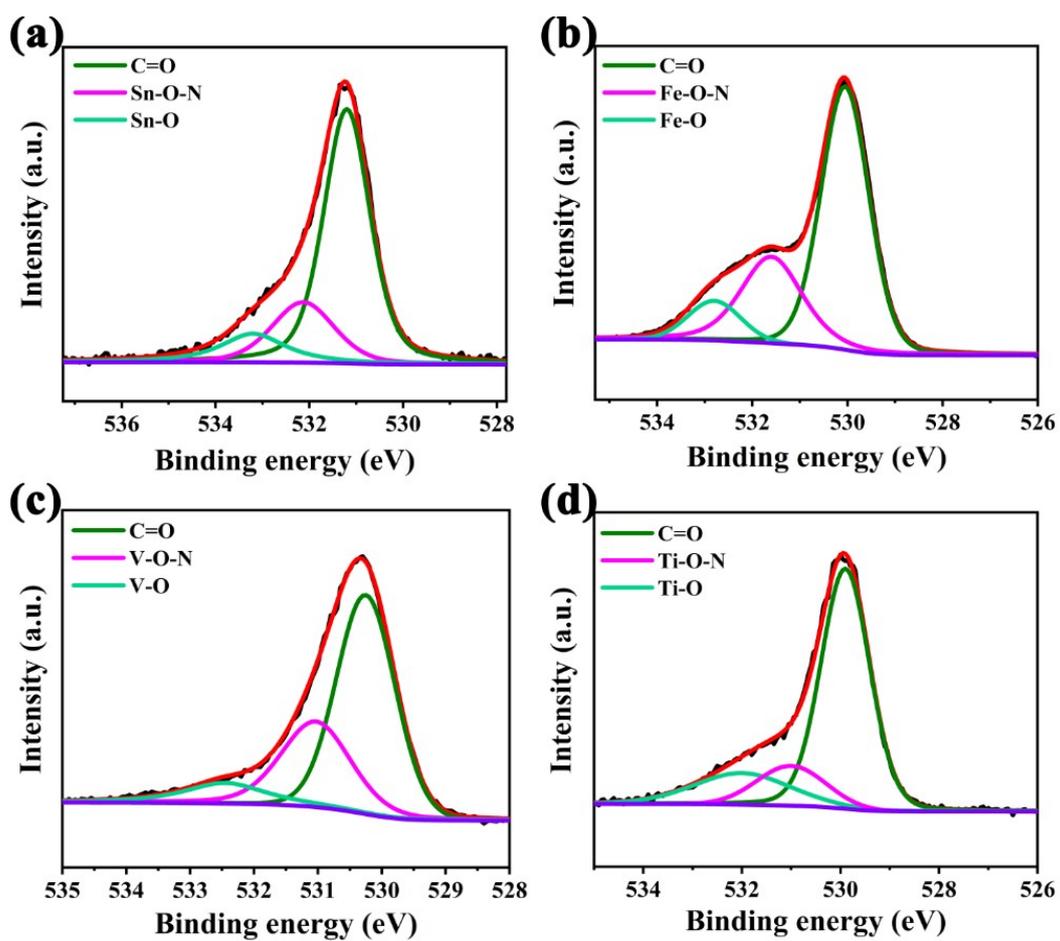
**Figure S4.** SEM images of the corresponding (a, e)  $\text{SnO}_2$ , (b, f)  $\text{Fe}_2\text{O}_3$ , (c, g)  $\text{VO}_2$  and  $\text{TiO}_2$  (d, h) hydroxide precursors used for preparing metal oxynitride nanorods at different magnification.



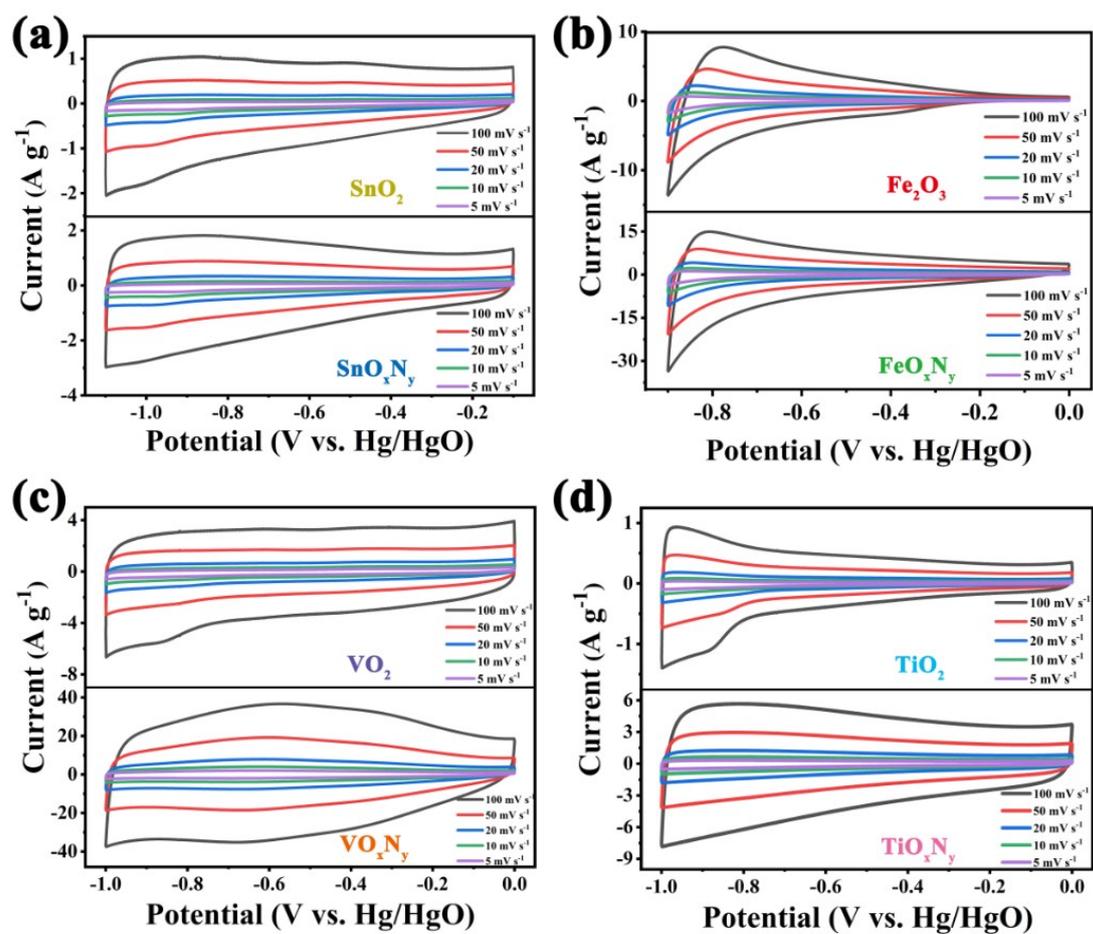
**Figure S5.** Elemental mapping images of the as-prepared  $\text{SnO}_x\text{N}_y$  (a),  $\text{FeO}_x\text{N}_y$  (b),  $\text{VO}_x\text{N}_y$  (c) and  $\text{TiO}_x\text{N}_y$  (d) samples.



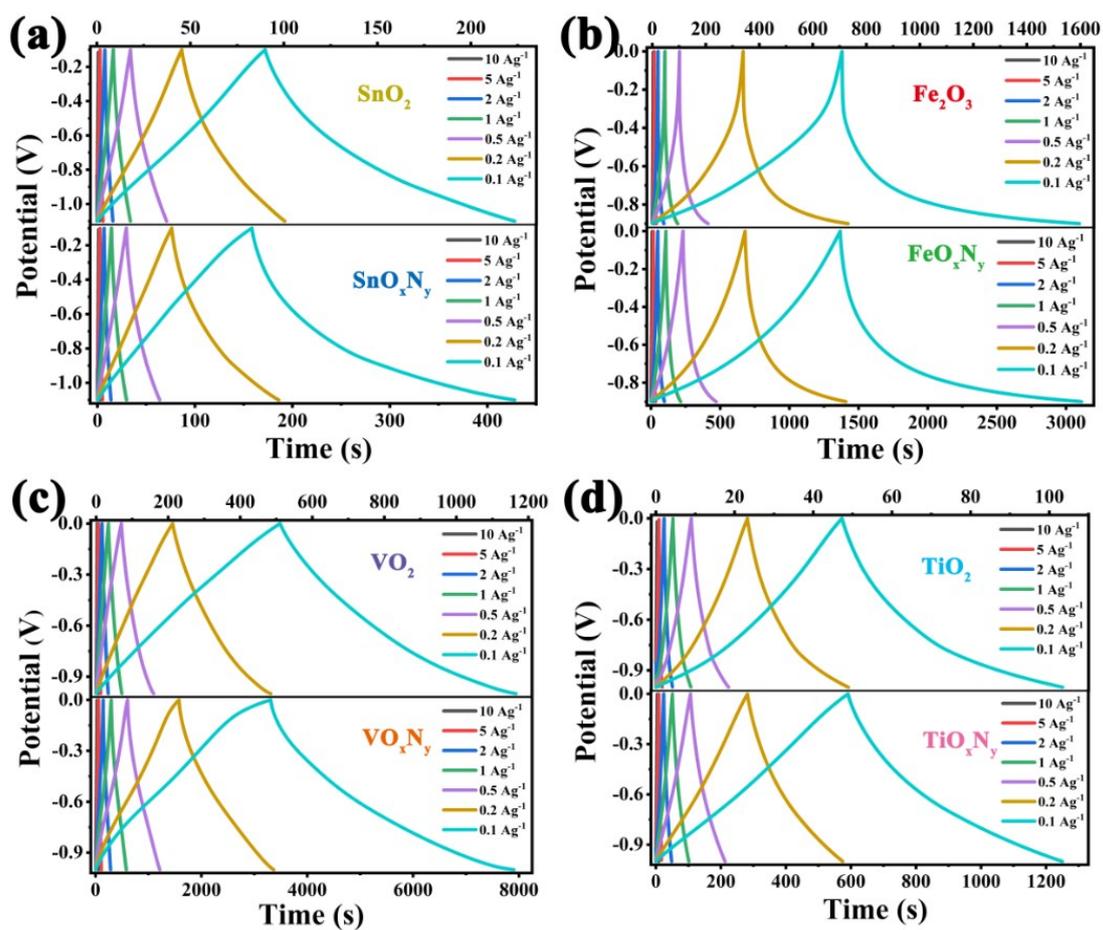
**Figure S6.** The XPS spectra of survey spectra.



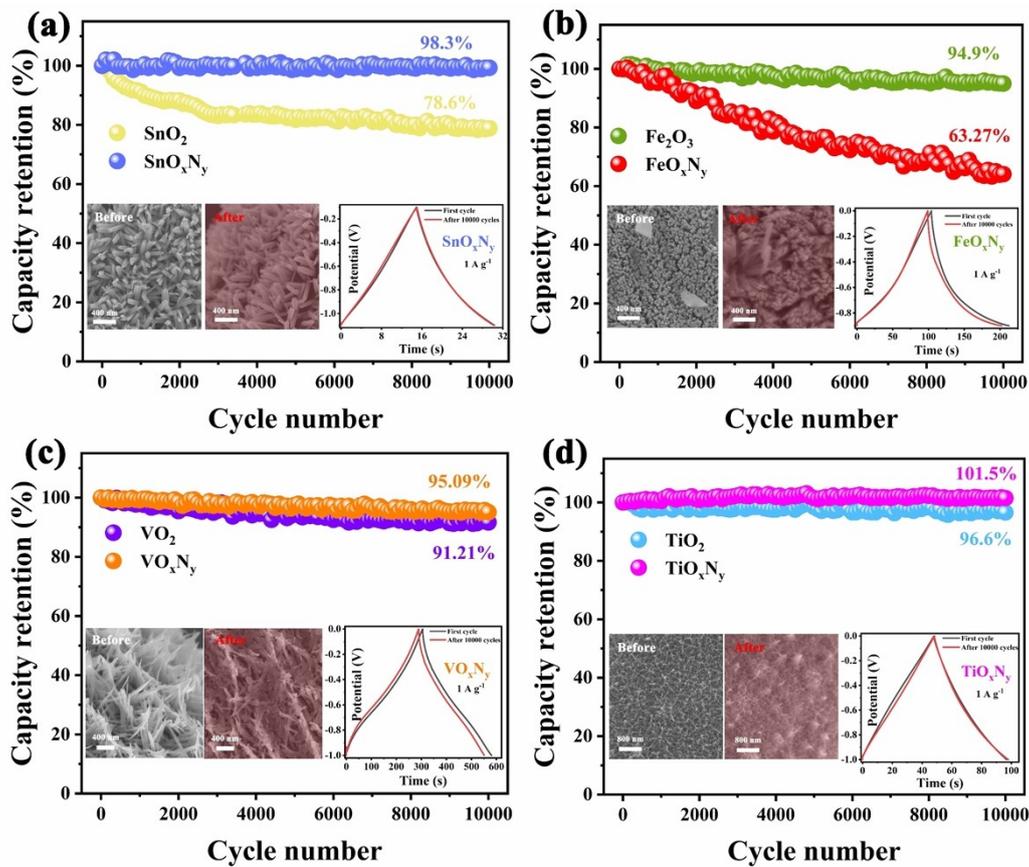
**Figure S7.** Corresponding high-resolution O 1s spectra of SnO<sub>x</sub>N<sub>y</sub> (a), FeO<sub>x</sub>N<sub>y</sub> (b), VO<sub>x</sub>N<sub>y</sub> (c) and TiO<sub>x</sub>N<sub>y</sub> (d), respectively.



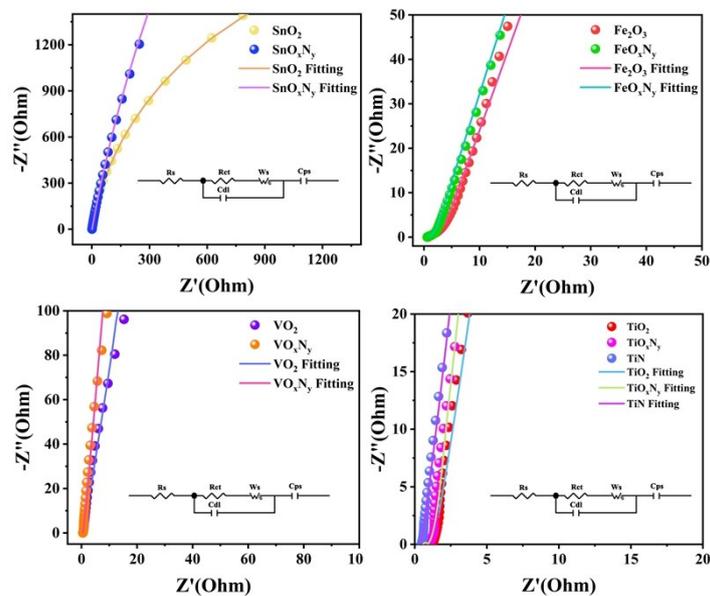
**Figure S8.** The CV curves at increasing scan rates of the  $\text{SnO}_2$  and  $\text{SnO}_x\text{N}_y$  (a),  $\text{Fe}_2\text{O}_3$  and  $\text{FeO}_x\text{N}_y$  (b),  $\text{VO}_2$  and  $\text{VO}_x\text{N}_y$  (c),  $\text{TiO}_2$  and  $\text{TiO}_x\text{N}_y$  (d) electrodes.



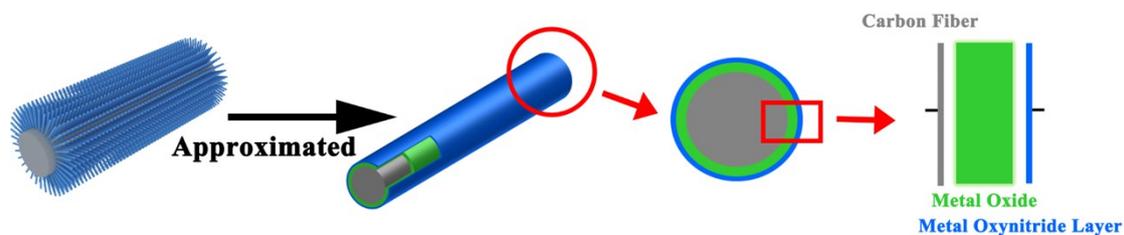
**Figure S9.** The GCD curves at increasing current density of the  $\text{SnO}_2$  and  $\text{SnO}_x\text{N}_y$  (a),  $\text{Fe}_2\text{O}_3$  and  $\text{FeO}_x\text{N}_y$  (b),  $\text{VO}_2$  and  $\text{VO}_x\text{N}_y$  (c),  $\text{TiO}_2$  and  $\text{TiO}_x\text{N}_y$  (d) electrodes.



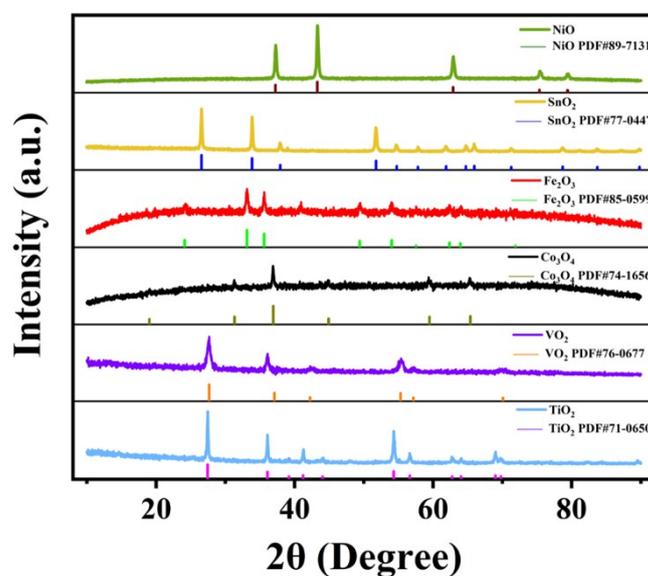
**Figure S10.** Charge/discharge cycling performance of CM electrodes and CMM electrodes, insets figures are SEM images and GCD curves before and after 10000 cycles.



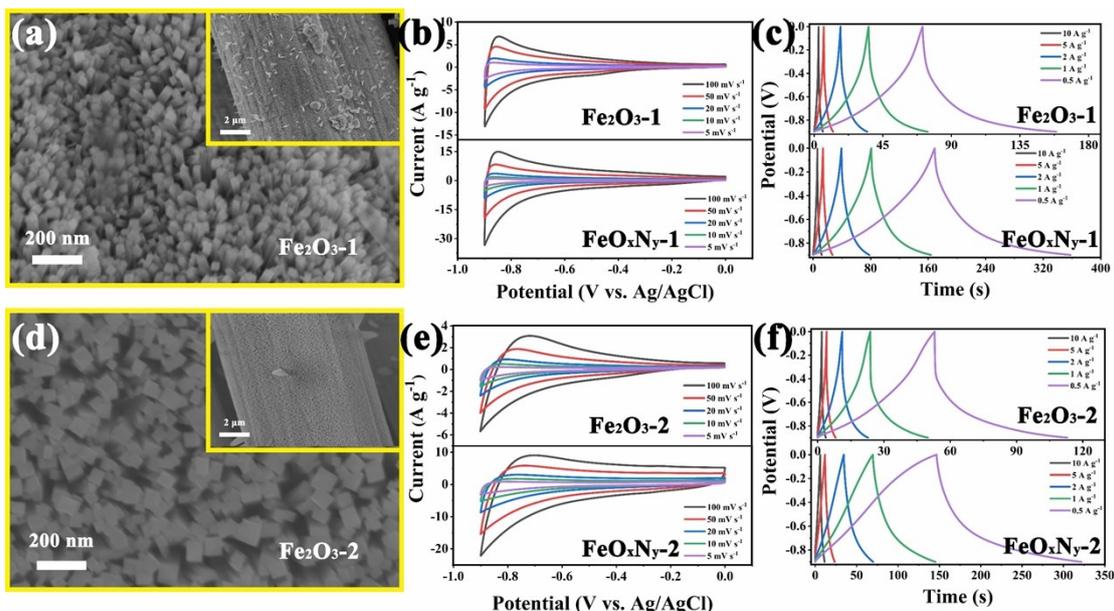
**Figure S11.** Nyquist plots of the electrodes, with inset showing the equivalent circuit model.



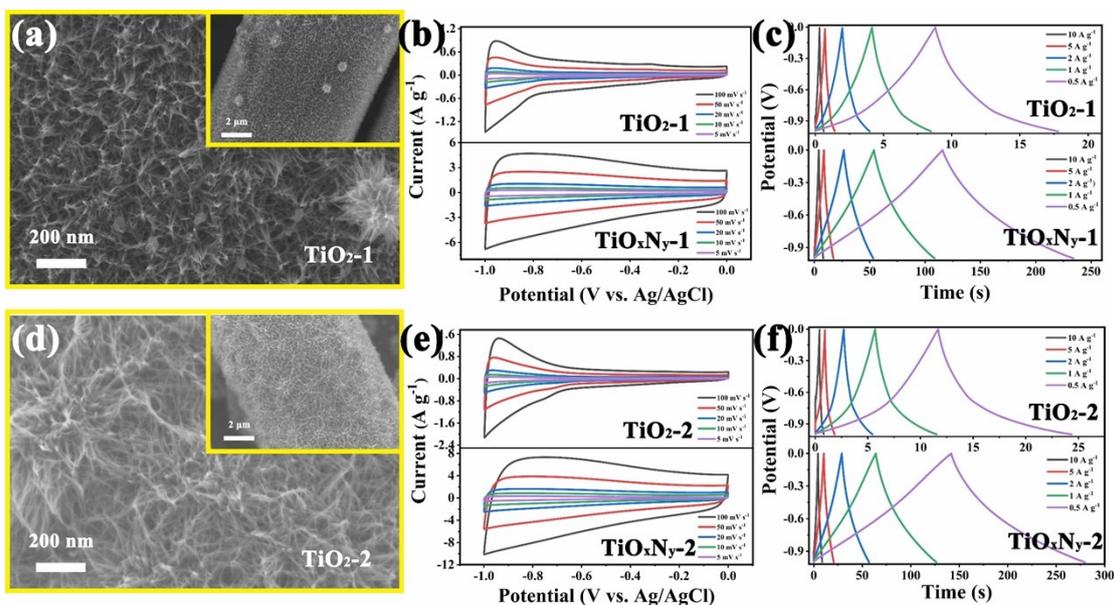
**Figure S12.** Metal oxynitride nanorods on each carbon fiber can be approximated to a coaxial mini parallel-plate capacitor, form a sandwich structure.



**Figure S13.** XRD patterns of the metal oxides powder.

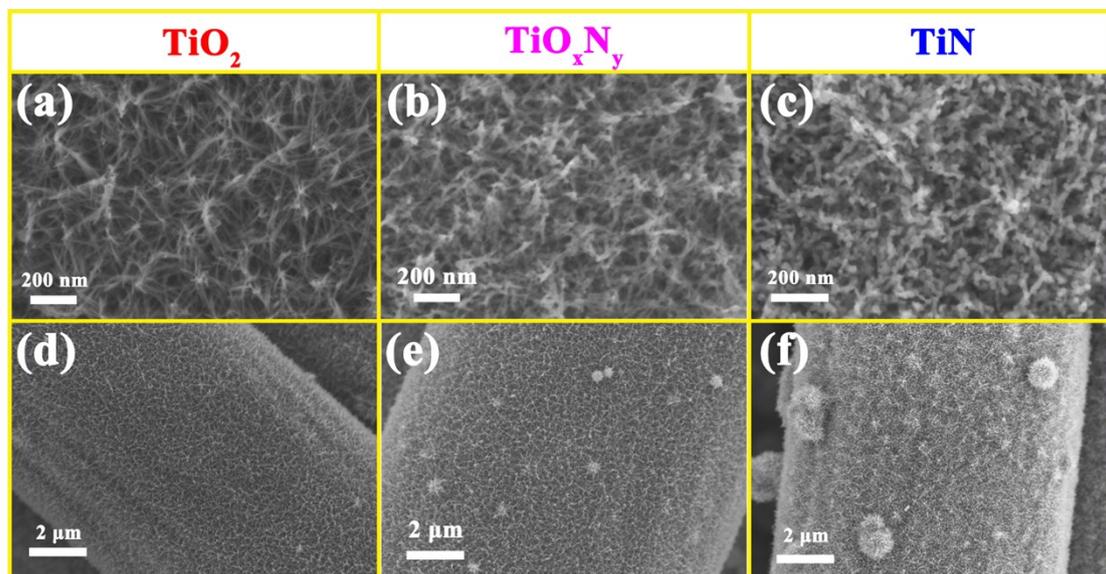


**Figure S14.** (a) SEM images of  $\text{Fe}_2\text{O}_3$ -1 (small ‘A’ value); (b) CV curves of  $\text{Fe}_2\text{O}_3$ -1 and  $\text{FeO}_x\text{N}_y$ -1; (c) GCD curves of  $\text{Fe}_2\text{O}_3$ -1 and  $\text{FeO}_x\text{N}_y$ -1; (d) SEM images of  $\text{Fe}_2\text{O}_3$ -2 (large ‘A’ value); (e) CV curves of  $\text{Fe}_2\text{O}_3$ -2 and  $\text{FeO}_x\text{N}_y$ -2; (f) GCD curves of  $\text{Fe}_2\text{O}_3$ -2 and  $\text{FeO}_x\text{N}_y$ -2.

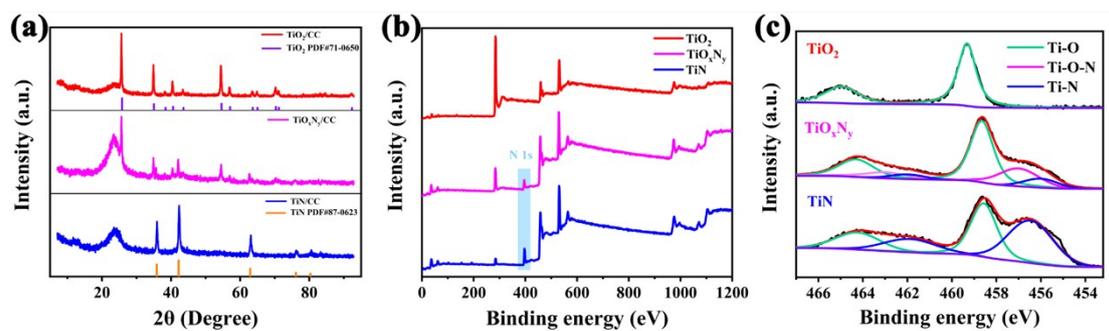


**Figure S15.** (a) SEM images of  $\text{TiO}_2$ -1 (small ‘d’ value); (b) CV curves of  $\text{TiO}_2$ -1 and  $\text{TiO}_x\text{N}_y$ -1; (c) GCD curves of  $\text{TiO}_2$ -1 and  $\text{TiO}_x\text{N}_y$ -1; (d) SEM images of  $\text{TiO}_2$ -2 (large ‘d’ value); (e) CV curves of  $\text{TiO}_2$ -2 and  $\text{TiO}_x\text{N}_y$ -2; (f) GCD curves of  $\text{TiO}_2$ -2 and  $\text{TiO}_x\text{N}_y$ -2.

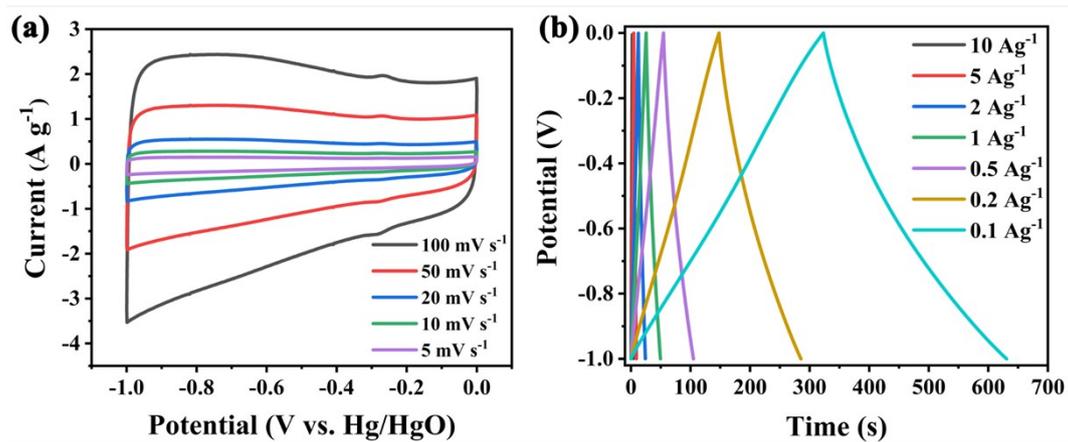
‘d’ value); (e) CV curves of  $\text{TiO}_2$ -2 and  $\text{TiO}_x\text{N}_y$ -2; (f) GCD curves of  $\text{TiO}_2$ -2 and  $\text{TiO}_x\text{N}_y$ -2.



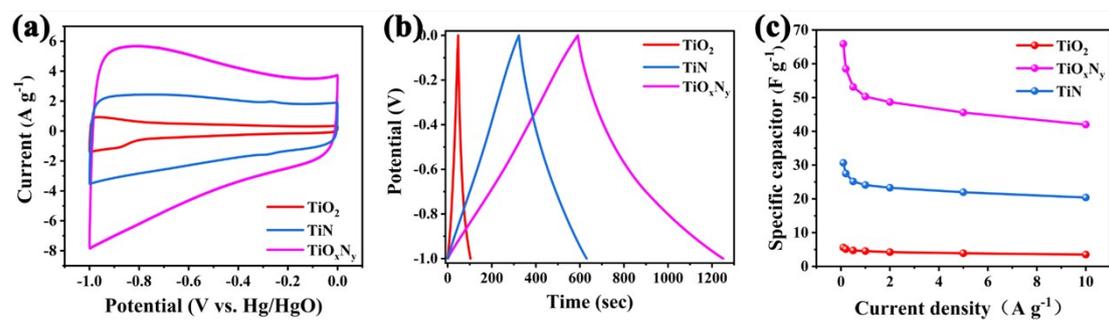
**Figure S16.** SEM images of the corresponding (a, d)  $\text{TiO}_2$ , (b, e)  $\text{TiO}_x\text{N}_y$ , (c, f)  $\text{TiN}$  at different magnification.



**Figure S17.** XRD patterns and XPS spectra of the  $\text{TiO}_2$ ,  $\text{TiO}_x\text{N}_y$  and  $\text{TiN}$ .



**Figure S18.** The CV and GCD curves at increasing scan rates and current density of the TiN.



**Figure S19.** The CV, GCD and as a function of current density of the  $\text{TiO}_2$ ,  $\text{TiO}_x\text{N}_y$  and TiN electrodes.

## S6. Supplementary Table S1-S11

**Table S1.** The specific capacity at increasing current density of CM and CMM (M=Sn, Fe, V and Ti) electrodes.

Current density	0.1 A g <sup>-1</sup>	0.2 A g <sup>-1</sup>	0.5 A g <sup>-1</sup>	1 A g <sup>-1</sup>	2 A g <sup>-1</sup>	5 A g <sup>-1</sup>	10 A g <sup>-1</sup>
SnO <sub>2</sub>	13.35	11.00	9.68	9.13	8.54	8.00	7.40
SnO <sub>x</sub> N <sub>y</sub>	26.97	21.96	17.05	15.47	13.98	12.90	12.40
Multiple	2.02	2.00	1.76	1.69	1.64	1.61	1.68
Fe <sub>2</sub> O <sub>3</sub>	98.86	87.12	59.17	52.57	47.57	41.56	37.33
FeO <sub>x</sub> N <sub>y</sub>	193.34	162.08	133.31	118.11	105.33	89.89	77.22
Multiple	1.96	1.86	2.25	2.24	2.21	2.16	2.07
VO <sub>2</sub>	68.24	55.08	45.01	39.40	36.00	34.05	33.20
VO <sub>x</sub> N <sub>y</sub>	459.72	358.14	304.29	286.56	275.66	266.41	261.68
Multiple	6.73	6.50	6.76	7.27	7.66	7.82	7.88
TiO <sub>2</sub>	5.61	5.134	4.73	4.56	4.24	3.90	3.50
TiO <sub>x</sub> N <sub>y</sub>	65.90	58.50	53.15	50.30	48.66	45.55	42.00
Multiple	11.75	11.39	11.25	11.03	11.48	11.68	12.00

**Table S2.** Rs and Rct values of CM electrodes and CMM electrodes.

	SnO <sub>2</sub>	SnON	Fe <sub>2</sub> O <sub>3</sub>	FeON	VO <sub>2</sub>	VON	TiO <sub>2</sub>	TiON	TiN
Rs (Ω)	0.68	0.65	0.61	0.58	0.51	0.49	0.61	0.59	0.44
Rct (Ω)	0.66	0.32	0.83	0.45	0.52	0.23	1.06	0.29	0.026

**Table S3.** Resistivity and conductivity of CM electrodes and CMM electrodes.

	L (cm)	S (cm <sup>2</sup> )	R (Ω)	ρ (Ω cm <sup>2</sup> m <sup>-1</sup> )	σ (S cm <sup>-1</sup> )
Fe <sub>2</sub> O <sub>3</sub> /CF	1.51	0.01768	1025.307	0.120049	8.329915
FeO <sub>x</sub> N <sub>y</sub> /CF	1.506	0.01855	358.3033	0.044134	22.65845
SnO <sub>2</sub> /CF	1.512	0.01584	929.7187	0.097399	10.26704

<b>SnO<sub>x</sub>N<sub>y</sub>/CF</b>	1.511	0.01734	523.343	0.060058	16.65056
<b>VO<sub>2</sub>/CF</b>	1.498	0.01716	1040.405	0.119181	8.390579
<b>VO<sub>x</sub>N<sub>y</sub>/CF</b>	1.495	0.01656	875.3968	0.096967	10.31278
<b>TiO<sub>2</sub>/CF</b>	1.502	0.0189	1131.838	0.142422	7.021401
<b>TiO<sub>x</sub>N<sub>y</sub>/CF</b>	1.505	0.01925	247.5031	0.031657	31.58822

**able S4.** Dielectric constant and dielectric loss of NiO.

Frequency	D (mU)	Cp (pF)	d (mm)	A (mm <sup>2</sup> )	$\epsilon_0$	$\epsilon_r$
1K Hz	420	0.255	1.37	1.37	8.85*10 <sup>-12</sup>	28.814
2K Hz	320	0.232	1.37	1.37	8.85*10 <sup>-12</sup>	26.215
5K Hz	290	0.213	1.37	1.37	8.85*10 <sup>-12</sup>	24.068
10K Hz	288	0.2	1.37	1.37	8.85*10 <sup>-12</sup>	22.599
20K Hz	248	0.182	1.37	1.37	8.85*10 <sup>-12</sup>	20.565
50K Hz	171	0.167	1.37	1.37	8.85*10 <sup>-12</sup>	18.870
100K Hz	133	0.154	1.37	1.37	8.85*10 <sup>-12</sup>	17.401
200K Hz	125	0.143	1.37	1.37	8.85*10 <sup>-12</sup>	16.158
500K Hz	141	0.133	1.37	1.37	8.85*10 <sup>-12</sup>	15.028
1M Hz	174	0.125	1.37	1.37	8.85*10 <sup>-12</sup>	14.124
2M Hz	206	0.12	1.37	1.37	8.85*10 <sup>-12</sup>	13.559
5M Hz	233	0.113	1.37	1.37	8.85*10 <sup>-12</sup>	12.768
10M Hz	235	0.107	1.37	1.37	8.85*10 <sup>-12</sup>	12.090
20M Hz	226	0.101	1.37	1.37	8.85*10 <sup>-12</sup>	11.412
50M Hz	200	0.097	1.37	1.37	8.85*10 <sup>-12</sup>	10.960
80M Hz	185	0.093	1.37	1.37	8.85*10 <sup>-12</sup>	10.508

**Table S5.** Dielectric constant and dielectric loss of SnO<sub>2</sub>.

Frequency	D (mU)	Cp (pF)	d (mm)	A (mm <sup>2</sup> )	$\epsilon_0$	$\epsilon_r$
1K Hz	257	0.511	0.85	1.37	8.85*10 <sup>-12</sup>	35.824
2K Hz	238	0.475	0.85	1.37	8.85*10 <sup>-12</sup>	33.300
5K Hz	214	0.437	0.85	1.37	8.85*10 <sup>-12</sup>	30.636
10K Hz	201	0.417	0.85	1.37	8.85*10 <sup>-12</sup>	29.234
20K Hz	188	0.383	0.85	1.37	8.85*10 <sup>-12</sup>	26.851
50K Hz	145	0.352	0.85	1.37	8.85*10 <sup>-12</sup>	24.677
100K Hz	122	0.316	0.85	1.37	8.85*10 <sup>-12</sup>	22.153
200K Hz	119	0.289	0.85	1.37	8.85*10 <sup>-12</sup>	20.261
500K Hz	120	0.275	0.85	1.37	8.85*10 <sup>-12</sup>	19.279
1M Hz	128	0.251	0.85	1.37	8.85*10 <sup>-12</sup>	17.597

2M Hz	133	0.24	0.85	1.37	$8.85 \times 10^{-12}$	16.825
5M Hz	163	0.222	0.85	1.37	$8.85 \times 10^{-12}$	15.564
10M Hz	182	0.207	0.85	1.37	$8.85 \times 10^{-12}$	14.512
20M Hz	206	0.194	0.85	1.37	$8.85 \times 10^{-12}$	13.601
50M Hz	180	0.183	0.85	1.37	$8.85 \times 10^{-12}$	12.829
80M Hz	162	0.18	0.85	1.37	$8.85 \times 10^{-12}$	12.619

**Table S6.** Dielectric constant and dielectric loss of Fe<sub>2</sub>O<sub>3</sub>.

Frequency	D (mU)	Cp (pF)	d (mm)	A (mm <sup>2</sup> )	$\epsilon_0$	$\epsilon_r$
1K Hz	208	0.438	1.27	1.37	$8.85 \times 10^{-12}$	45.879
2K Hz	179	0.404	1.27	1.37	$8.85 \times 10^{-12}$	42.318
5K Hz	158	0.37	1.27	1.37	$8.85 \times 10^{-12}$	38.756
10K Hz	140	0.336	1.27	1.37	$8.85 \times 10^{-12}$	35.195
20K Hz	130	0.306	1.27	1.37	$8.85 \times 10^{-12}$	32.052
50K Hz	148	0.276	1.27	1.37	$8.85 \times 10^{-12}$	28.910
100K Hz	132	0.246	1.27	1.37	$8.85 \times 10^{-12}$	25.768
200K Hz	122	0.226	1.27	1.37	$8.85 \times 10^{-12}$	23.673
500K Hz	116	0.205	1.27	1.37	$8.85 \times 10^{-12}$	21.473
1M Hz	112	0.185	1.27	1.37	$8.85 \times 10^{-12}$	19.378
2M Hz	123	0.175	1.27	1.37	$8.85 \times 10^{-12}$	18.331
5M Hz	133	0.164	1.27	1.37	$8.85 \times 10^{-12}$	17.178
10M Hz	142	0.163	1.27	1.37	$8.85 \times 10^{-12}$	17.074
20M Hz	135	0.153	1.27	1.37	$8.85 \times 10^{-12}$	16.026
50M Hz	130	0.146	1.27	1.37	$8.85 \times 10^{-12}$	15.293
80M Hz	127	0.138	1.27	1.37	$8.85 \times 10^{-12}$	14.455

**Table S7.** Dielectric constant and dielectric loss of Co<sub>3</sub>O<sub>4</sub>.

Frequency	D (mU)	Cp (pF)	d (mm)	A (mm <sup>2</sup> )	$\epsilon_0$	$\epsilon_r$
1K Hz	186	0.898	0.85	1.37	$8.85 \times 10^{-12}$	62.955
2K Hz	170	0.781	0.85	1.37	$8.85 \times 10^{-12}$	54.753
5K Hz	132	0.693	0.85	1.37	$8.85 \times 10^{-12}$	48.583
10K Hz	103	0.623	0.85	1.37	$8.85 \times 10^{-12}$	43.676
20K Hz	85	0.56	0.85	1.37	$8.85 \times 10^{-12}$	39.259
50K Hz	73	0.519	0.85	1.37	$8.85 \times 10^{-12}$	36.385
100K Hz	62	0.475	0.85	1.37	$8.85 \times 10^{-12}$	33.300
200K Hz	53	0.437	0.85	1.37	$8.85 \times 10^{-12}$	30.636
500K Hz	48	0.411	0.85	1.37	$8.85 \times 10^{-12}$	28.814

1M Hz	58	0.376	0.85	1.37	$8.85 \times 10^{-12}$	26.360
2M Hz	60	0.357	0.85	1.37	$8.85 \times 10^{-12}$	25.028
5M Hz	71	0.354	0.85	1.37	$8.85 \times 10^{-12}$	24.818
10M Hz	75	0.34	0.85	1.37	$8.85 \times 10^{-12}$	23.836
20M Hz	62	0.326	0.85	1.37	$8.85 \times 10^{-12}$	22.855
50M Hz	58	0.317	0.85	1.37	$8.85 \times 10^{-12}$	22.224
80M Hz	55	0.314	0.85	1.37	$8.85 \times 10^{-12}$	22.013

**Table S8.** Dielectric constant and dielectric loss of VO<sub>2</sub>.

Frequency	D (mU)	Cp (pF)	d (mm)	A (mm <sup>2</sup> )	$\epsilon_0$	$\epsilon_r$
1K Hz	102	1.692	0.75	1.37	$8.85 \times 10^{-12}$	104.6641
2K Hz	83	1.469	0.75	1.37	$8.85 \times 10^{-12}$	90.86973
5K Hz	70	1.307	0.75	1.37	$8.85 \times 10^{-12}$	80.84869
10K Hz	62	1.2	0.75	1.37	$8.85 \times 10^{-12}$	74.22987
20K Hz	57	1.138	0.75	1.37	$8.85 \times 10^{-12}$	70.39466
50K Hz	52	1.084	0.75	1.37	$8.85 \times 10^{-12}$	67.05431
100K Hz	48	1.035	0.75	1.37	$8.85 \times 10^{-12}$	64.02326
200K Hz	42	0.992	0.75	1.37	$8.85 \times 10^{-12}$	61.36336
500K Hz	43	0.958	0.75	1.37	$8.85 \times 10^{-12}$	59.26018
1M Hz	48	0.93	0.75	1.37	$8.85 \times 10^{-12}$	57.52815
2M Hz	50	0.907	0.75	1.37	$8.85 \times 10^{-12}$	56.10541
5M Hz	62	0.887	0.75	1.37	$8.85 \times 10^{-12}$	54.86824
10M Hz	75	0.864	0.75	1.37	$8.85 \times 10^{-12}$	53.4455
20M Hz	86	0.855	0.75	1.37	$8.85 \times 10^{-12}$	52.88878
50M Hz	73	0.84	0.75	1.37	$8.85 \times 10^{-12}$	51.96091
80M Hz	68	0.824	0.75	1.37	$8.85 \times 10^{-12}$	50.97117

**Table S9.** Dielectric constant and dielectric loss of TiO<sub>2</sub>.

Frequency	D (mU)	Cp (pF)	d (mm)	A (mm <sup>2</sup> )	$\epsilon_0$	$\epsilon_r$
1K Hz	88	1.486	1.06	1.37	$8.85 \times 10^{-12}$	129.915
2K Hz	72	1.356	1.06	1.37	$8.85 \times 10^{-12}$	118.550
5K Hz	64	1.242	1.06	1.37	$8.85 \times 10^{-12}$	108.583
10K Hz	51	1.137	1.06	1.37	$8.85 \times 10^{-12}$	99.404
20K Hz	42	1.05	1.06	1.37	$8.85 \times 10^{-12}$	91.798
50K Hz	36	0.982	1.06	1.37	$8.85 \times 10^{-12}$	85.853
100K Hz	32	0.92	1.06	1.37	$8.85 \times 10^{-12}$	80.432
200K Hz	28	0.877	1.06	1.37	$8.85 \times 10^{-12}$	76.673

500K Hz	36	0.835	1.06	1.37	$8.85 \times 10^{-12}$	73.001
1M Hz	45	0.811	1.06	1.37	$8.85 \times 10^{-12}$	70.903
2M Hz	53	0.782	1.06	1.37	$8.85 \times 10^{-12}$	68.367
5M Hz	60	0.759	1.06	1.37	$8.85 \times 10^{-12}$	66.357
10M Hz	64	0.737	1.06	1.37	$8.85 \times 10^{-12}$	64.433
20M Hz	75	0.718	1.06	1.37	$8.85 \times 10^{-12}$	62.772
50M Hz	61	0.7	1.06	1.37	$8.85 \times 10^{-12}$	61.198
80M Hz	55	0.687	1.06	1.37	$8.85 \times 10^{-12}$	60.062

**Table S10.** The specific capacitance at increasing current density of  $\text{Fe}_2\text{O}_3$  and  $\text{FeO}_x\text{N}_y$  electrodes with different ‘A’ values.

Current density	0.5 A g <sup>-1</sup>	1 A g <sup>-1</sup>	2 A g <sup>-1</sup>	5 A g <sup>-1</sup>	10 A g <sup>-1</sup>
$\text{Fe}_2\text{O}_3$ -1	48.73	43.07	38.96	34.02	30.65
$\text{FeO}_x\text{N}_y$ -1	104.89	92.17	86.08	72.99	64.73
Multiple	2.15	2.14	2.21	2.15	2.11
$\text{Fe}_2\text{O}_3$ -2	33.32	28.99	25.88	22.48	20.09
$\text{FeO}_x\text{N}_y$ -2	97.3	84.04	79.03	64.66	58.06
Multiple	2.92	2.90	3.05	2.88	2.89

**Table S11.** The specific capacitance at increasing current density of  $\text{TiO}_2$  and  $\text{TiO}_x\text{N}_y$  electrodes with different ‘d’ values.

Current density	0.5 A g <sup>-1</sup>	1 A g <sup>-1</sup>	2 A g <sup>-1</sup>	5 A g <sup>-1</sup>	10 A g <sup>-1</sup>
$\text{TiO}_2$ -1	4.50	4.33	4.00	3.55	3.10
$\text{TiO}_x\text{N}_y$ -1	59.12	54.79	53.15	42.90	39.80
Multiple	13.13	12.65	13.29	12.08	13.84
$\text{TiO}_2$ -2	6.35	5.84	5.47	4.58	4.00
$\text{TiO}_x\text{N}_y$ -2	68.87	62.29	56.03	50.93	43.13
Multiple	10.85	10.67	10.24	11.12	10.78