

Electronic Supplementary Information for

**Molecular Mechanisms of Thermal Instability in Hybrid Perovskite Light
Absorbers for Photovoltaic Solar Cells**

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S1. The analysis of radial distribution function and coordination numbers

In order to explore the microstructural evolution of bulk MAPbI₃ during melting process, we calculate radial distribution functions (RDFs) of Pb-I and I-I pairs for MAPbI₃ at different temperatures (T). For equilibrated MAPbI₃ at 300 K, **Figure S1(a)** shows two sharp RDF peaks of Pb-I pairs located at $r = 3.08$ and 7.0 \AA , which represent I atoms in the octahedra connecting with center Pb atoms, and those in adjacent octahedra. With the increase of T , it can be seen in **Figure S1(b)** that both peaks become broadened meaning the large stretching of PbI₆ octahedra, but RDFs still maintain similar shapes up to $T = 1052$ K. We thus set the location of RDF valley right after the first RDF peak as Pb-I bond length cutoff, namely $r_{\text{Pb-I}} = 4.5 \text{ \AA}$, which is then utilised for detecting Pb-I bonds in defective MAPbI₃. When gradually reaching melting point $T_m \sim 1052$ K, there is a sharp increase of first RDF peak, associated with the disappearance of the second RDF peak. Such variation in the trend for both RDF peaks demonstrates the crystalline-to-liquid phase transition, which is consistent with the calculation of translational order parameter η . Namely, the split of regular PbI₆ octahedra and formation of partial ones (i.e. PbI₄ and PbI₅) results in the enhanced first RDF peak of Pb-I pairs. Meanwhile, the lost medium-range order, as presented by the broken of PbI₆ octahedral network, leads to a significant reduction in the second RDF peak of Pb-I pairs. The RDFs of I-I pairs also show similar variation trend. As T increases, they have much broadened first peaks. This means wider range of I-I distances in PbI₆ octahedra, indicating much severer distortion of PbI₆ away from their regular shapes. When approaching T_m , the missing second and third RDFs peaks confirm again the existence of the short-range I-I order rather than the medium-range order.

S2 Phonon density of states and band structure calculations at finite temperature

To predict phonon density of states (DOS) and band structures at finite temperature, the dynamical matrix is first determined from MD simulations based on fluctuation-dissipation theory as implemented in LAMMPS. The simulation model has $N = 10 \times 10 \times 10$ unit cells (MAPbI₃ as one unit cell in this study), and each unit cell has three real space vectors, \mathbf{a}_1 , \mathbf{a}_2 and \mathbf{a}_3 . Based on the fluctuation-dissipation theory, the force constant coefficients are given by^{1,2}

$$\Phi_{k\alpha,k'\beta}(\mathbf{q}) = k_B T \mathbf{G}_{k\alpha,k'\beta}^{-1}(\mathbf{q}) \quad (5)$$

where \mathbf{q} is a reciprocal vector; \mathbf{G} is the Green's functions coefficients given by

$$\mathbf{G}_{k\alpha,k'\beta}(\mathbf{q}) = \langle \mathbf{u}_{k\alpha}(\mathbf{q}) \cdot \mathbf{u}_{k'\beta}^*(\mathbf{q}) \rangle \quad (6)$$

where $\langle \dots \rangle$ represents an ensemble average; $\mathbf{u}_{k\alpha}(\mathbf{q}) = \sum_l \mathbf{u}_{lk\alpha} \exp(i\mathbf{q} \cdot \mathbf{r}_l)$ is the α component of the atomic displacement for the k th atom in the unit cell in the reciprocal space at \mathbf{q} . In practice, \mathbf{G} can also be measured based on the following expression

$$\mathbf{G}_{k\alpha,k'\beta}(\mathbf{q}) = \langle \mathbf{R}_{k\alpha}(\mathbf{q}) \cdot \mathbf{R}_{k'\beta}^*(\mathbf{q}) \rangle - \langle \mathbf{R}_{k\alpha}(\mathbf{q}) \rangle \cdot \langle \mathbf{R}_{k'\beta}^*(\mathbf{q}) \rangle \quad (7)$$

where \mathbf{R} is the instantaneous positions of atoms, and $\langle \mathbf{R} \rangle$ is the averaged atomic positions. Once the force constant matrix is given, the dynamical matrix \mathbf{D} can be obtained by

$$\mathbf{D}_{k\alpha,k'\beta}(\mathbf{q}) = (m_k m_{k'})^{-\frac{1}{2}} \Phi_{k\alpha,k'\beta}(\mathbf{q}) \quad (8)$$

If the dynamical matrix \mathbf{D} is known, its eigenvalues are exactly the phonon frequencies at \mathbf{q} . Therefore, you can predict the phonon band structures along certain reciprocal path. In addition, the phonon DOS can be obtained by integrating all \mathbf{q} over the Brillouin zone.

For phonon dispersion calculation in this work, the $1 \times 1 \times 1$ MAPbI₃ unit cell is expanded to $10 \times 10 \times 10$ supercell to construct the perfect simulation model. Defective $1 \times 1 \times 1$ MAPbI₃ unit cells with I and MA vacancies (vacancy concentration $k_V = 2.5\%$) are expanded by $6 \times 6 \times 6$ to construct corresponding defective simulation models.

Table S1. The detailed potential parameters for all intra-/inter-molecular interactions in hybrid perovskite MAPbI₃ from the potential MYP1.³

Buckingham Potential			
Ion Pairs	A (kcal/mol)	ρ (Å)	C (kcal/mol·Å⁶)
Pb – Pb	397000.0	0.28	25370.0
I – I	41319.0	0.46	10838.0
Pb – I	158565.0	0.32	11760.0
Pb – C	12566186.2765653	0.15	0.0
Pb – N	12566186.2765653	0.15	0.0
I – C	43412.8729434772	0.325	0.0
I – N	43412.8729434772	0.325	0.0
Lennard-Jones Potential			
Ion Pairs	ϵ (kcal/mol)	σ (Å)	
C – C	0.1094	3.39967	
N – N	0.1700	3.25000	
HC – HC (-C)	0.0157	1.96000	
H+ – H+ (-N)	0.0157	1.06908	
Pb – HC (-C)	0.0140	2.70999	
Pb – H+ (-N)	0.0140	2.26454	
I – HC (-C)	0.0574	3.10000	
I – H+ (-N)	0.0574	2.75000	
Ion Type	Partial charges q		
Pb	+1.401200		
I	-0.700600		
N	-0.699800		
C	+0.460200		
HC (-C)	-0.003600		
H+ (-N)	+0.317000		

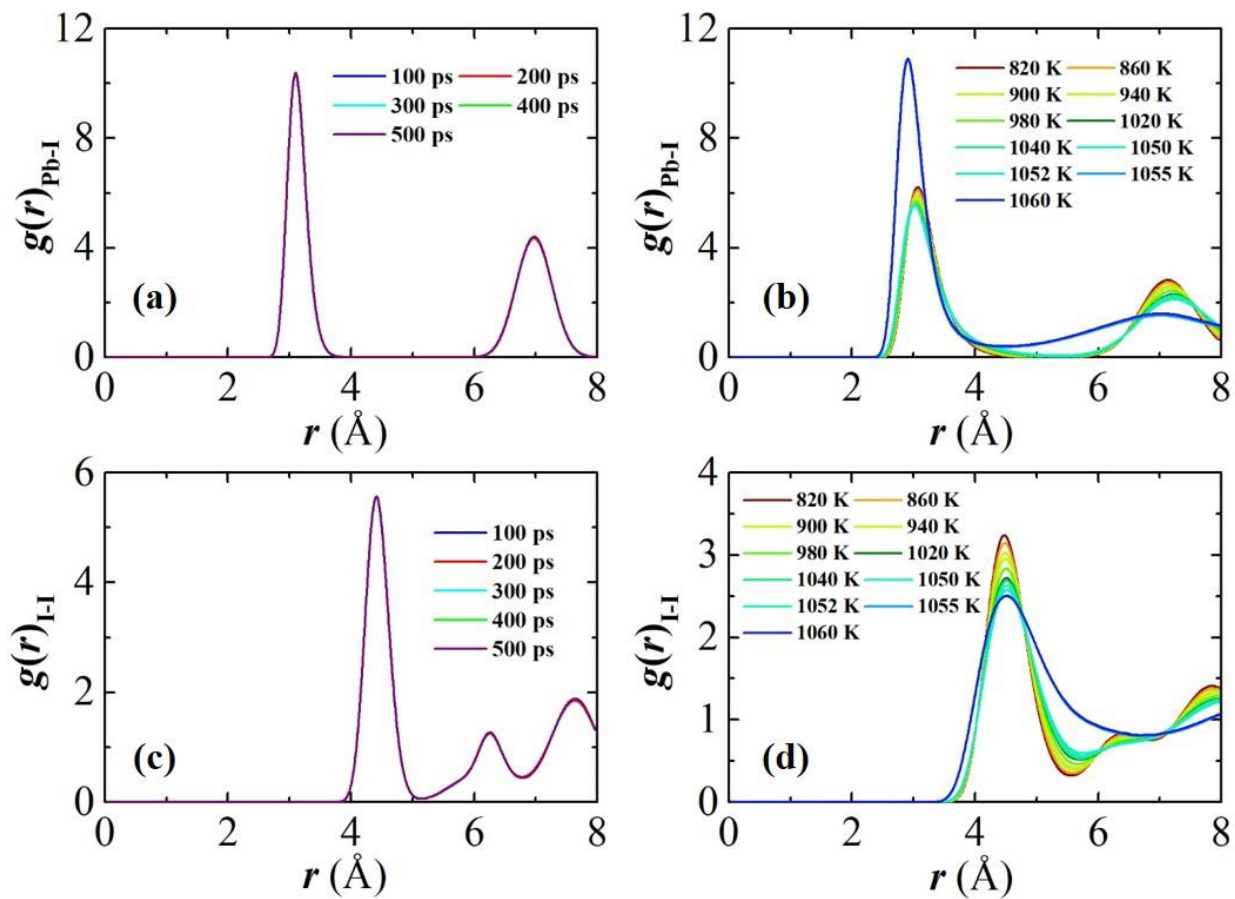


Figure S1. Radial distribution functions (RDFs) of atom pairs in pristine MAPbI₃ bulk crystal. (a-b) The RDFs of Pb-I pairs in MAPbI₃ (a) equilibrated at 300 K, and (b) heated up to the melting point $T_m \approx 1052.5$ K. (c-d) The RDFs of I-I pairs in MAPbI₃ (a) equilibrated at 300 K, and (b) heated up to the melting point $T_m \approx 1052.5$ K.

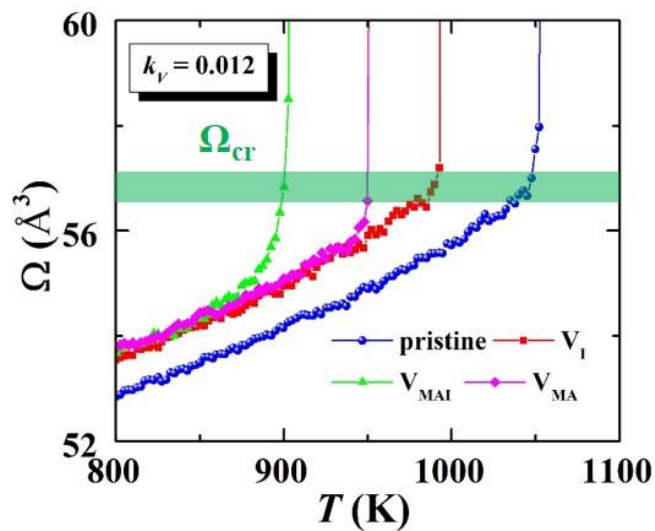


Figure S2. The mean atomic volume (Ω) of pristine and defective MAPbI₃ bulk crystals as a function of temperature (T). Three types of point defects, including I (V_I), MA⁺ (V_{MA}), and MAI⁰ (V_{MAI}) vacancies with a concentration of 0.012 are considered. The green bar highlights the critical mean atomic values Ω_{cr} when the melting of simulation models is initiated.

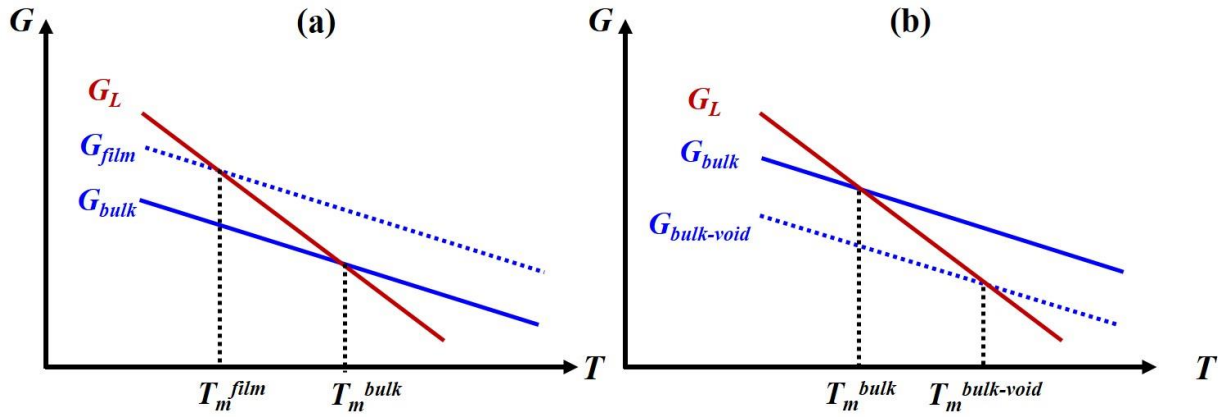


Figure S3. Schematic free energy diagram of the material melting of (a) thin films with free surfaces and (b) bulk crystals with nanovoids. See the main text for details. G_L , G_{bulk} , G_{film} and $G_{bulk-void}$ denotes the free energy of liquid phase, bulk crystals, thin films and bulk crystals with nanovoids. T_m^{bulk} , T_m^{film} and $T_m^{bulk-void}$ denote the melting temperatures of bulk crystals, thin films and bulk crystals with nanovoids.

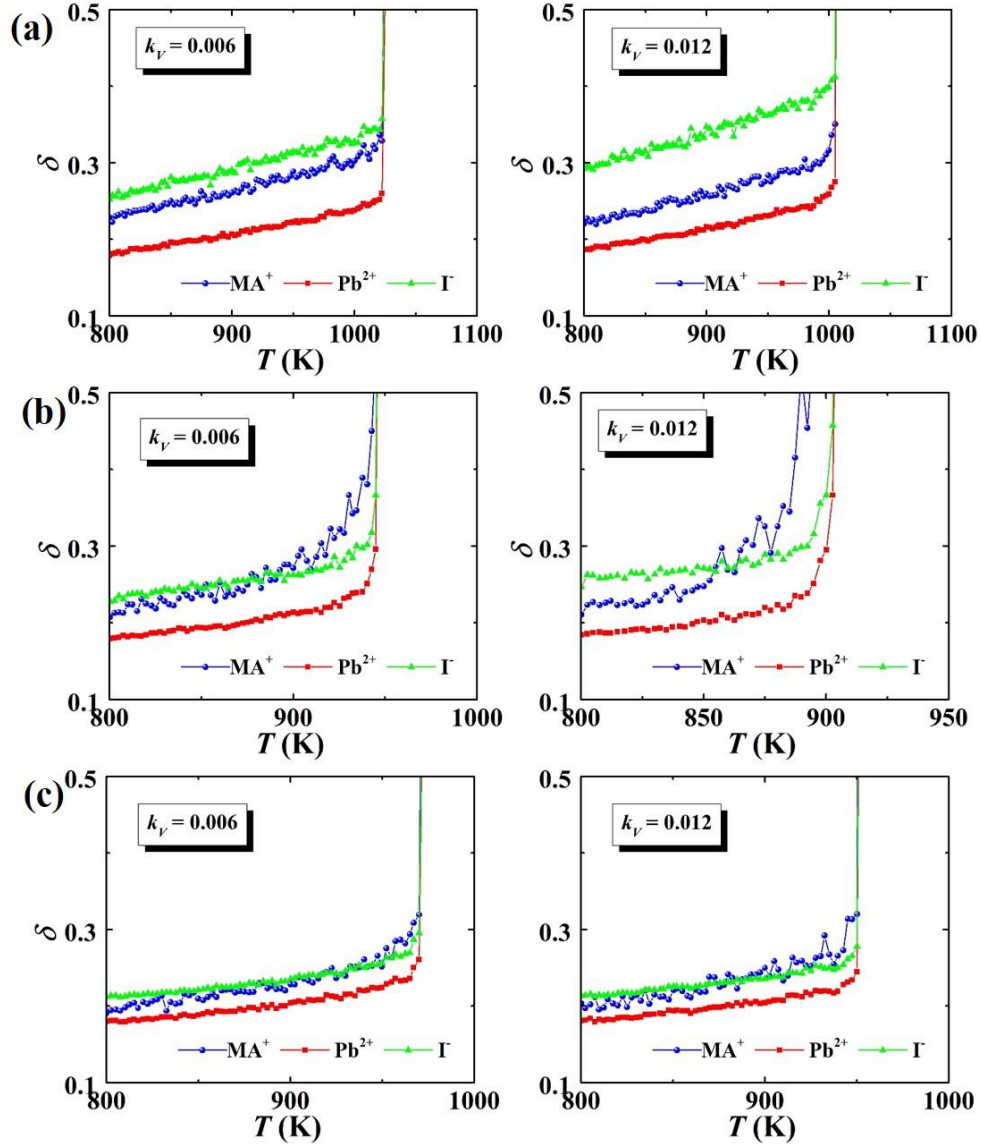


Figure S4. The Lindemann ratio of MA^+ , Pb^{2+} and I ions in bulk MAPbI_3 with (a) I , (b) MAI^0 and (c) MA^+ vacancies at vacancy concentration $k_V = 0.006$ and $k_V = 0.012$ as a function of temperature T .

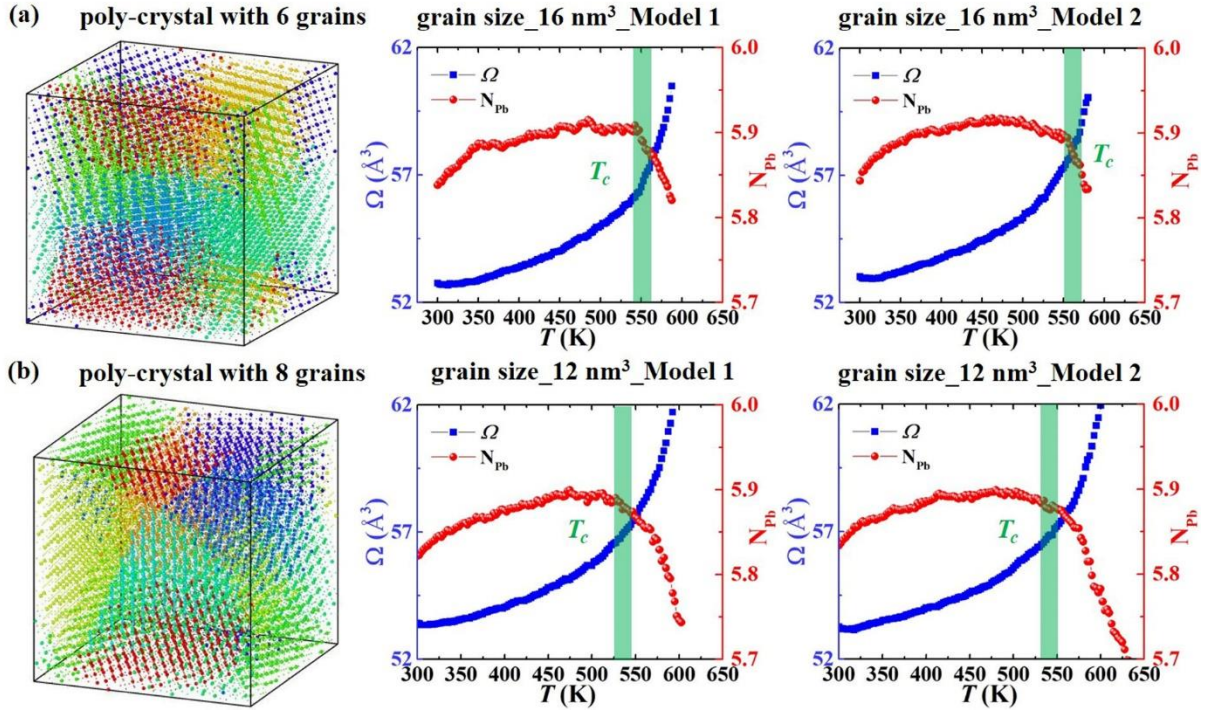


Figure S5. Atomistic configurations, as well as the mean atomic volume (Ω) and averaged coordination number of Pb ions (N_{Pb}) as a function of temperature for randomly oriented polycrystalline MAPbI₃ with the grain sizes of (a) 16 nm³, and (b) 12 nm³. Two different polycrystalline models with the same number of grains are simulated separately. The grain numbers of polycrystalline MAPbI₃ crystals are represented by different colors in the first column of figures.

References

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