

Supporting Information

Phase Transformation, Charge Transfer, and Ionic Diffusion of $\text{Na}_4\text{MnV}(\text{PO}_4)_3$ in Sodium-Ion Batteries: A Combined First-principles and Experimental Study

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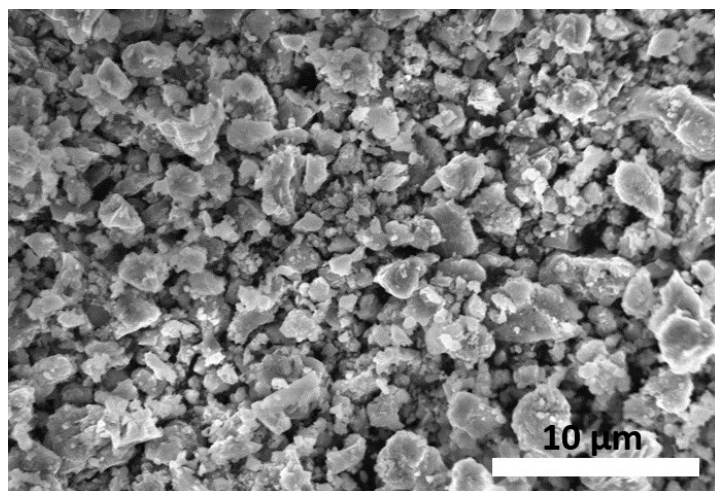


Fig. S1. SEM image of the Na₄MnV(PO₄)₃ material.

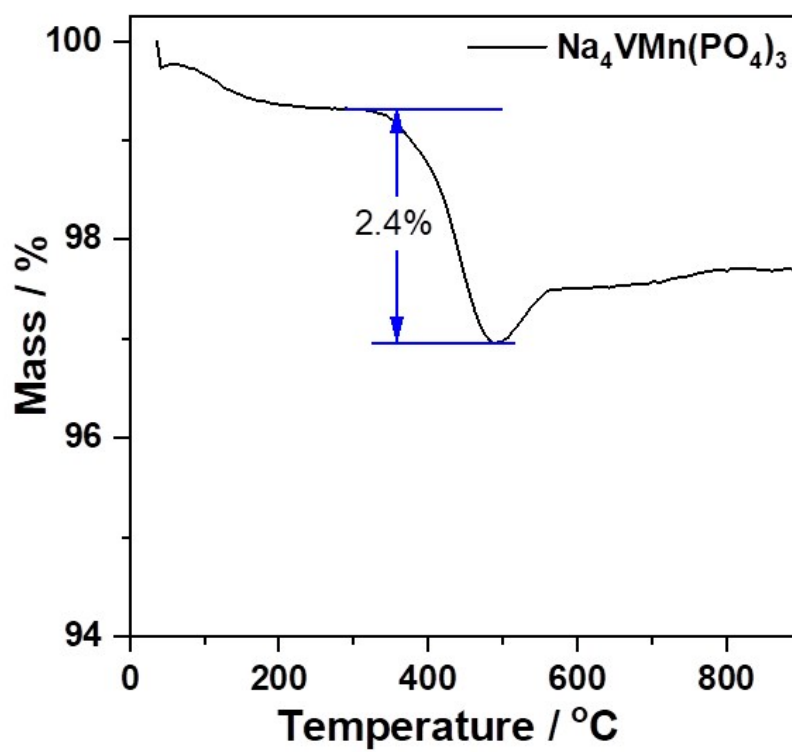


Fig. S2. TG curve of the Na₄MnV(PO₄)₃ material heated in O₂.

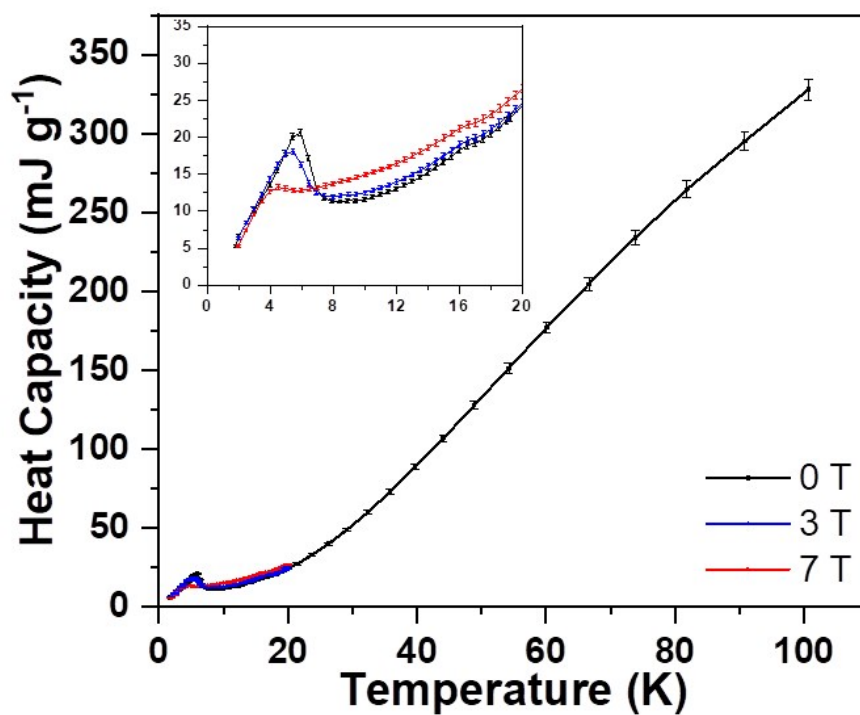


Fig. S3. Heat capacity curve of the $\text{Na}_4\text{MnV}(\text{PO}_4)_3$ material.

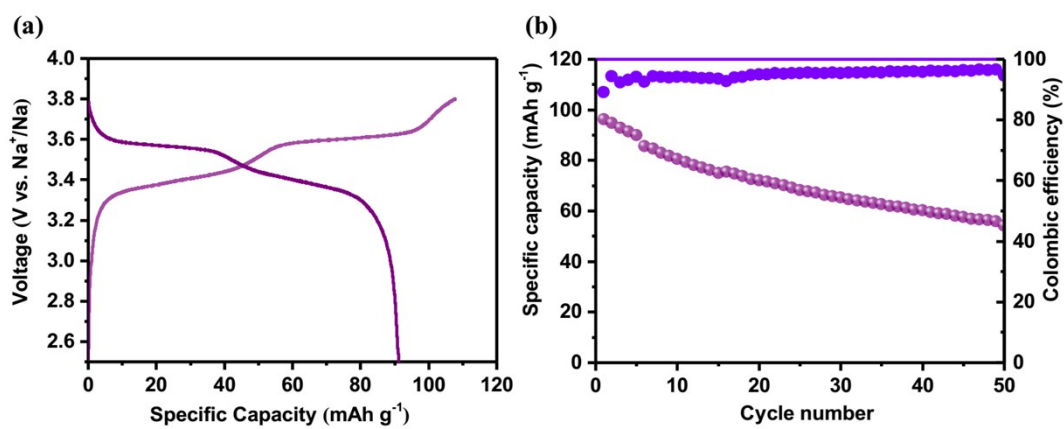


Fig. S4. The charge-discharge profiles and cycling performance of $\text{Na}_4\text{MnV}(\text{PO}_4)_3$ at the current density of $3 \text{ mA} \cdot \text{g}^{-1}$ (a-b, respectively).

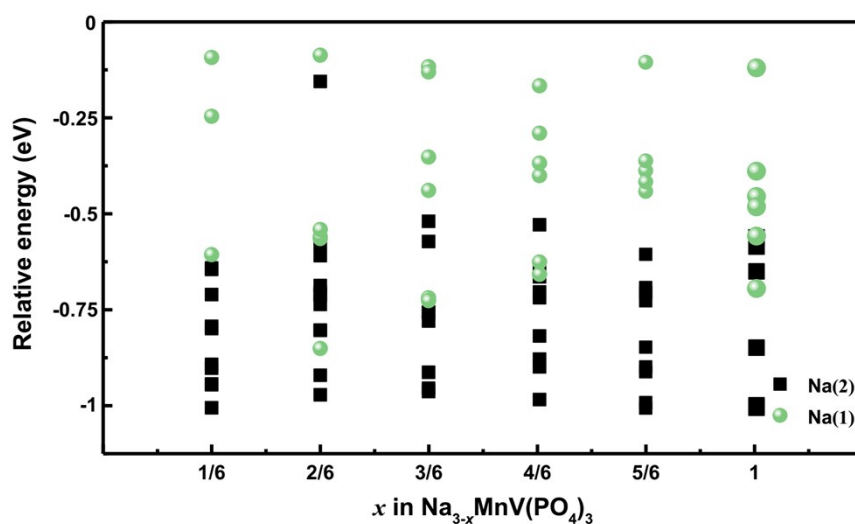


Fig. S5. Calculated relative energies of $\text{Na}_{3-x}\text{MnV}(\text{PO}_4)_3$ in different structural forms: $\text{Na(1)Na(2)}_{2-x}\text{MnV}(\text{PO}_4)_3$ (black) and $\text{Na(1)}_{1-x}\text{Na(2)}_2\text{MnV}(\text{PO}_4)_3$ (green).

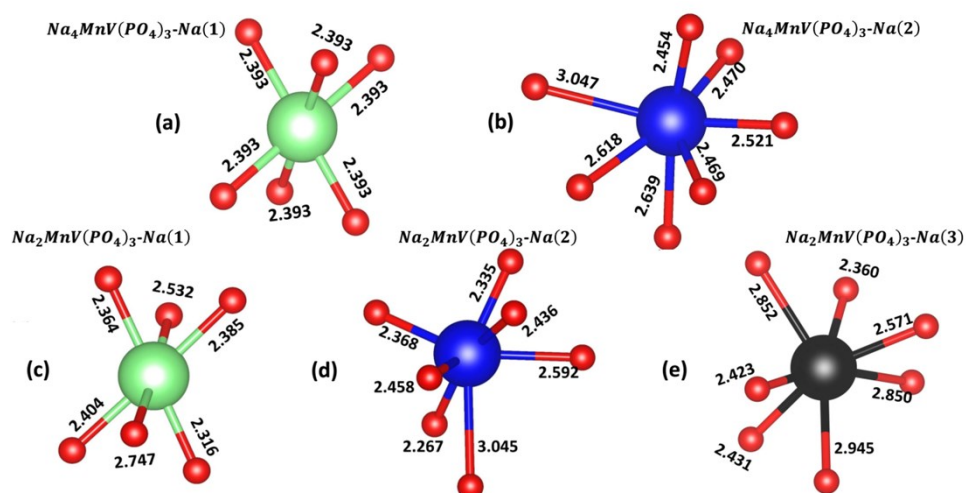


Fig. S6. Bond lengths of Na–O. Na(1) and Na(2) in $\text{Na}_4\text{MnV}(\text{PO}_4)_3$ (a–b, respectively). Na(1), Na(2), and Na(3) in $\text{Na}_2\text{MnV}(\text{PO}_4)_3$ (c–e, respectively).

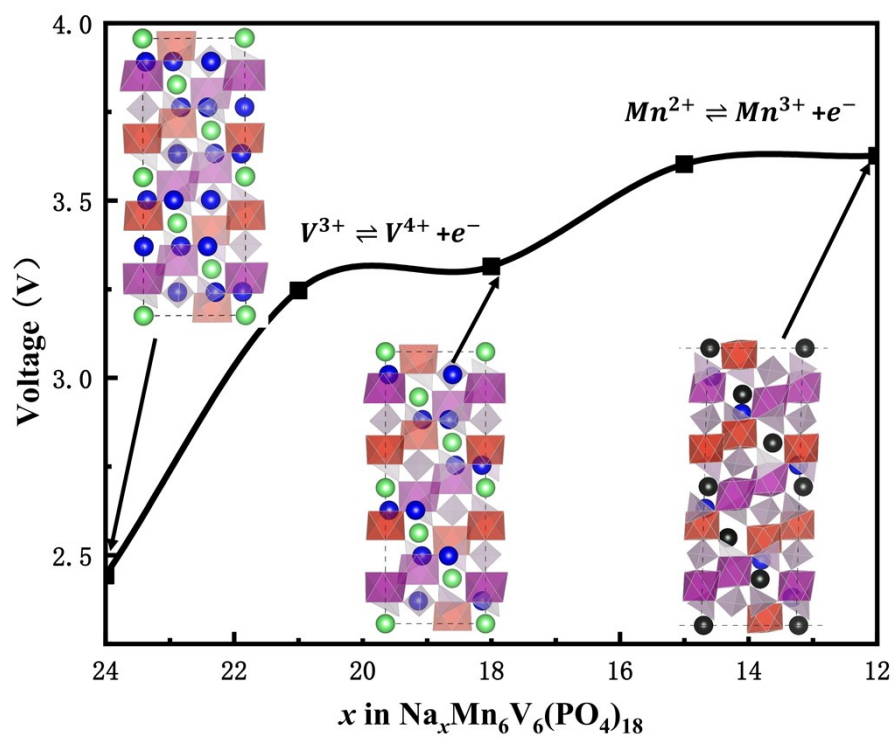


Fig. S7. Calculated voltage profile of Na₄MnV(PO₄)₃.

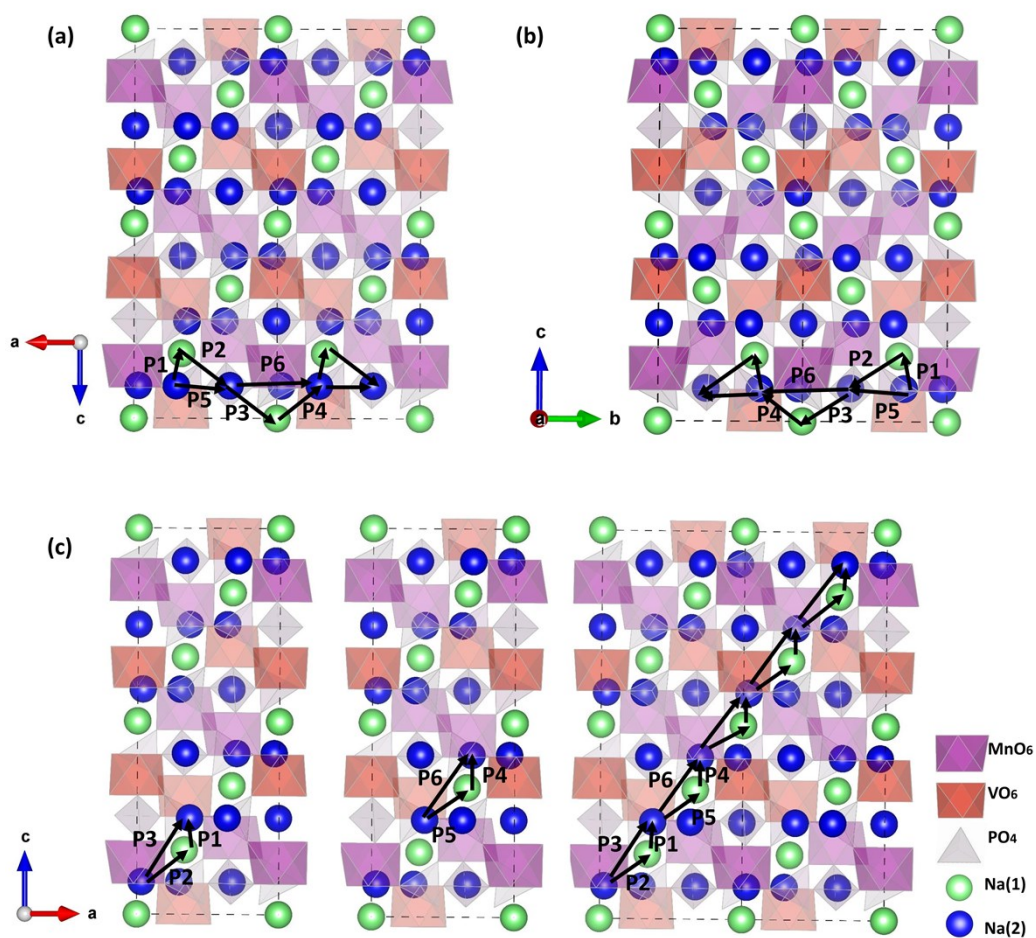


Fig. S8. Possible migration pathways for Na^+ in $\text{Na}_4\text{MnV}(\text{PO}_4)_3$ viewed from the $[100]$, and $[010]$ directions (a–b, respectively). (c) Schematic representation of possible Na^+ migration pathways in the $\text{Na}_4\text{MnV}(\text{PO}_4)_3$ framework from the view of $[001]$ planes and spiral 1D diffusion pathway along the c -axis.

Table S1. Structural parameters of the $\text{Na}_4\text{MnV}(\text{PO}_4)_3$ material based on the Rietveld refinement results.

Space group: $R\bar{3}c$		$Z=6$			
$a=8.9398(2) \text{ \AA}$; $c=21.5317(7) \text{ \AA}$;		$V=1490.26(7) \text{ \AA}^3$			
Atom	Wyckoff site	X	Y	Z	Occupancy
O(1)	36f	0.1918(6)	-0.0193(6)	0.1933(2)	1
O(2)	36f	0.1881(5)	0.1761(5)	0.0848(2)	1
Mn	12c	0	0	0.1498(1)	0.5
V	12c	0	0	0.1498(1)	0.5
P	18e	0.2988(3)	0	0.25	1
Na(1)	6b	0	0	0	1
Na(2)	18e	0.6414(4)	0	0.25	0.98(1)

Table S2. Calculated relative energies of the $\text{Na(1)Na(2)}_{3-x}\text{MnV(PO}_4)_3$ and $\text{Na(1)}_{1-x}\text{Na(2)}_3\text{MnV(PO}_4)_3$ structures.

Concentration	$\text{Na(1)}_{1-x}\text{Na(2)}_3\text{MnV(PO}_4)_3$ (eV/f.u.)	$\text{Na(1)Na(2)}_{3-x}\text{MnV(PO}_4)_3$ (eV/f.u.)
$x = 0$	-844.46	-845.12
$x = 0.5$	-833.35	-834.91
$x = 1.0$	-820.62	-821.32

Table S3. Na^+ migration energy barriers of $\text{Na}_4\text{MnV(PO}_4)_3$ along the [100] direction.

	Diffusion direction	Activation energy (eV)
P1	$\text{Na(1)} \leftrightarrow \text{Na(2)}$	0.380
P2	$\text{Na(1)} \leftrightarrow \text{Na(2)}$	0.300
P3	$\text{Na(1)} \leftrightarrow \text{Na(2)}$	0.390
P4	$\text{Na(1)} \leftrightarrow \text{Na(2)}$	0.390
P5	$\text{Na(1)} \leftrightarrow \text{Na(2)}$	1.320
P6	$\text{Na(1)} \leftrightarrow \text{Na(2)}$	1.174

Table S4. Na⁺ migration energy barriers of Na₄MnV(PO₄)₃ along the [010] direction.

	Diffusion direction	Activation energy (eV)
P1	Na(1) ↔ Na(2)	0.380
P2	Na(1) ↔ Na(2)	0.356
P3	Na(1) ↔ Na(2)	0.389
P4	Na(1) ↔ Na(2)	0.389
P5	Na(1) ↔ Na(2)	1.305
P6	Na(1) ↔ Na(2)	1.124

Table S5. Na⁺ migration energy barriers of Na₄MnV(PO₄)₃ along the [001] direction.

	Diffusion direction	Activation energy (eV)
P1	Na(1) ↔ Na(2)	0.317
P2	Na(1) ↔ Na(2)	0.328
P3	Na(1) ↔ Na(2)	1.343
P4	Na(1) ↔ Na(2)	0.380
P5	Na(1) ↔ Na(2)	1.373
P6	Na(1) ↔ Na(2)	1.074