

Bright and efficient red emitting electroluminescent devices containing a ternary europium complex with greater than 6% external quantum efficiency

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1. Synthesis of Binary hydrated complexes

1.1. [Eu(btfa)₃(H₂O)₂] and [Eu(nta)₃(H₂O)₂]

Binary hydrated [Eu(btfa)₃(H₂O)₂] and [Eu(nta)₃(H₂O)₂] complexes (**Chart S1**) were synthesized by the conventional method.¹ Briefly, EuCl₃.6H₂O (Eu- 2.39 g, 6.57 mmol) aqueous solution was added dropwise through a dropping funnel to a solution of sodium salt of β-diketone (2.0 g, 19.97 mmol). The precipitate formed was filtered, washed with a copious amount of deionized water and dried in vacuum over P₄O₁₀ and re-crystallized from DCM.

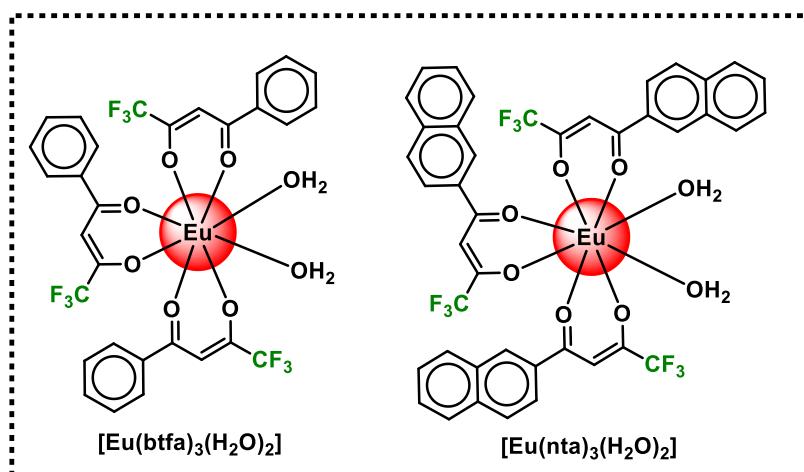


Chart S1: Chemical structures of binary hydrated [Eu(btfa)₃(H₂O)₂] and [Eu(nta)₃(H₂O)₂] complexes

2. Theoretical Judd–Ofelt (J-O) intensity parameters (Ω_λ) ($\lambda = 2, 4$ and 6)

The theoretical intensity parameters derived from the Judd-Ofelt theory² were calculated by the following expression³:

$$\Omega_\lambda^{calc} = (2\lambda + 1) \sum_t^{\lambda-1, \lambda+1(odd)} \sum_{p=-t}^{t(all)} \frac{|B_{\lambda tp}|^2}{(2t + 1)} \quad \text{Eq. S1}$$

$$B_{\lambda tp} = \frac{2}{\Delta E} \langle r^{t+1} \rangle \theta(t, \lambda) \gamma_p^t - \left[\frac{(\lambda + 1)(2\lambda + 3)}{2\lambda + 1} \right]^{1/2} \langle r^\lambda \rangle (1 - \sigma_\lambda) \langle f \| C^{(\lambda)} \| f \rangle \Gamma_p^t \delta_{t, \lambda+1} \quad \text{Eq. S2}$$

$$\gamma_p^t = \left(\frac{4\pi}{2t+1} \right)^{\frac{1}{2}} e^2 \sum_j \rho_j (2\beta_j)^{t+1} \frac{g_j}{R_j^{t+1}} Y_p^{t*}(\theta_j, \phi_j) \quad \text{Eq. S3}$$

$$\Gamma_p^t = \left(\frac{4\pi}{2t+1} \right)^{\frac{1}{2}} \sum_j \frac{\alpha_j}{R_j^{t+1}} Y_p^{t*}(\theta_j, \phi_j) \quad \text{Eq. S4}$$

The distance from atom j coordinated directly to the lanthanide ion (R_j) together with the corresponding angular coordinates (θ_j and ϕ_j) show the dependency of the theoretical intensity parameters on the complex structure. Eq. S2 contains the contribution from the forced electric dipole and dynamic coupling mechanisms. The theoretical Ω_λ have been calculated by adjusting the charge factors (g_j) and polarizabilities (α_j), Eq. S3 and S4, respectively, in order to reproduce the experimental values of Ω_2 and Ω_4 . The complete procedure used to calculate Ω_λ is widely discussed in reference.⁴

The QDC model⁴ implemented into LUMPAC⁵ postulates that the g_j are obtained from the product between adjustable parameters (Q) and each ZDO (Zero Differential Overlap) electronic density (q_j) of each atom j coordinated directly to the lanthanide ion. Similarly, the QDC model postulates that the α_j are calculated using two adjustable parameters (D and C)

$$g_j = Q \cdot q_j \quad \text{Eq. S5}$$

$$\alpha_j = SE_j \cdot D + C \quad \text{Eq. S6}$$

The ZDO electronic density and the electrophilic superdelocalizability (SE) for any atom μ of the complex are calculated by

$$q_\mu = 2 \sum_{i'}^{\text{occ.}} \sum_p^{N_\mu} \left| c_{pi'}^\mu \right|^2 \quad \text{Eq. S7}$$

$$SE_\mu = 2 \sum_{i'}^{\text{occ.}} \sum_p \sum_q \frac{c_{pi'}^\mu c_{qi'}^\mu}{\varepsilon_i'} \quad \text{Eq. S8}$$

where i' runs through all the occupied molecular orbitals of the complex, p runs through all atomic orbitals, $c_{pi'}^\mu$ is the corresponding linear coefficient, and ε_i is the energy of the occupied molecular orbital i .

The theoretical radiative decay rate for europium is given by

$$A_{rad} = \frac{32e^2\pi^3\chi}{3\hbar(2J+1)} \sum_{\lambda=2,4,6} \nu[{}^5D_0 \rightarrow {}^7F_{J=\lambda}]^3 \Omega_\lambda \left| \left\langle {}^5D_0 \left| U^{(\lambda)} \right| {}^7F_{J=\lambda} \right\rangle \right|^2 + \frac{32\pi^3 n^3 \nu[{}^5D_0 \rightarrow {}^7F_1]^3}{3\hbar} S_{md}$$
Eq. S9

where e is the elementary charge; $2J+1$ is the degeneracy of the initial state, in this case 5D_0 , and therefore $J=0$. χ is the Lorentz local-field correction term given by $\chi = n(n^2 + 2)^2 / 9$, in this work value of refractive index n equal to 1.424 was considered. $\nu[{}^5D_0 \rightarrow {}^7F_J]$ are the energies of the barycenters of the respective transitions. The magnetic dipole strength of the ${}^5D_0 \rightarrow {}^7F_1$ transition is theoretically evaluated as being $S_{md} = 9.6 \times 10^{-42}$ esu²cm²⁶.

3. Theoretical Quantum Yield

The PLQY (q) is defined as the ratio of the number of emitted photons by the lanthanide ion to the number of absorbed photons by the ligand.

$$q = \frac{A_{rad} \eta_{{}^5D_0}}{\varphi \eta_{S_0}}$$
Eq. S10

where the terms η_{S_0} and $\eta_{{}^5D_0}$ correspond to the energetic population of the S_0 and 5D_0 states, respectively. φ is the absorption rate from the fundamental singlet to the excited singlet of the ligand. The normalized population of a given level j considered in the energy transfer modeling, η_j , are obtained from an equations system in the steady-state approximation.

$$\frac{d\eta_j}{dt} = -\sum_{i \neq j} W_{ji} \eta_j + \sum_{i \neq j} W_{ij} \eta_i$$
Eq. S11

where W_{ij} is the transfer rate from level i to level j , with the transition rates from and to the same state are zero. In the steady-state approximation $\frac{d\eta_j}{dt} = 0$, allowing that the set of algebraic equations derived from Eq. S11 can be solved analytically. The emission quantum yield for the complexes were calculated with LUMPAC 1.4.0.⁵

4. Full EL Device structures

4.1 Single EML Device based on Eu-1

Device 1: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-1** (3 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

Device 2: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-1** (4 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

Device 3: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-1** (5 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

4.2 Double EML Device based on Eu-1

Device 4: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-1** (3 wt%): TcTa (10 nm)/**Eu-1** (3 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

Device 5: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-1** (4 wt%): TcTa (10 nm)/**Eu-1** (4 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

Device 6: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-1** (5 wt%): TcTa (10 nm)/**Eu-1** (5 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

4.3 Single EML Device based on Eu-2

Device 1: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-2** (3 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

Device 2: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-2** (4 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

Device 3: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-2** (5 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

4.4 Double EML Device based on Eu-2

Device 4: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-2** (3 wt%): TcTa (10 nm)/**Eu-2** (3 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

Device 5: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-2** (4 wt%): TcTa (10 nm)/**Eu-2** (4 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

Device 6: ITO/HAT-CN (6 nm)/HAT-CN (0.2 wt%): TAPC (50 nm)/**Eu-2** (5 wt%): TcTa (10 nm)/**Eu-2** (5 wt%): 26DCzPPy (10 nm)/Tm3PyP26PyB (60 nm)/LiF (1 nm)/Al (100 nm)

Table S1. Corrected emission intensity relative to $^5D_0 \rightarrow ^7F_1$ transition, Barycenter, %contribution of each transition of **Eu-1** and **Eu-2** in DCM solution at RT

	Corrected emission Intensity relative to $^5D_0 \rightarrow ^7F_1$ transition					
	\int_{0-0}	\int_{0-1}	\int_{0-2}	\int_{0-3}	\int_{0-4}	\int_{total}
Eu-1						
Corrected intensity ^a	0.24	1.00	18.89	0.63	2.06	22.82
Barycenter (cm ⁻¹)	17253.59	16883.65	16214.77	15310.25	14338.68	
%contribution	1.05%	-	82.77%	2.76%	9.02%	
Eu-2						
Corrected intensity ^a	0.23	1.00	20.42	0.61	2.21	24.47
Barycenter (cm ⁻¹)	17261.37	16881.43	16218.07	15322.58	(14337.79)	
%contribution	[0.93%]	-	[83.44%]	[2.49%]	[9.03%]	

^arelative to the MD $^5D_0 \rightarrow ^7F_1$ transition

Table S2. Sparkle/RM1 model ZDO electronic densities (q) and electrophilic superdelocalizabilities (SE), by considering the B3LYP/SVP/MWB52 geometry, for each atom directly coordinated to Eu^{3+} , in complexes **Eu-1** and **Eu-2**, together with corresponding charge factors (g) and polarizabilities (α) from the fitting. Calculated electric dipole intensity parameters ($\Omega_{\lambda}^{\text{FED}}$) for both complexes

Ligand Atom	Eu-1				Ligand Atom	Eu-2			
	$Q = 0.0169 \text{ au}^{-1}$	$D = 40.58 \text{ au}^{-1} \cdot \text{\AA}^3$	$C = 19.32 \text{ \AA}^3$	$D/C = 2.10 \text{ au}^{-1}$		$Q = 0.0319 \text{ au}^{-1}$	$D = 42.32 \text{ au}^{-1} \cdot \text{\AA}^3$	$C = 20.41 \text{ \AA}^3$	$D/C = 2.07 \text{ au}^{-1}$
	q (au)	SE (au)	g	α (\AA^3)		q (au)	SE (au)	g	α (\AA^3)
O(DPEPO)	6.8450	-0.4289	0.1160	1.9161	O(DPEPO)	6.8477	-0.4163	0.2187	2.7914
O(DPEPO)	6.8338	-0.4360	0.1158	1.6286	O(DPEPO)	6.8325	-0.4376	0.2182	1.8937
O(btfa1)	6.3177	-0.4089	0.1070	2.7268	O(nta1)	6.3191	-0.4194	0.2018	2.6610
O(btfa)	6.3435	-0.4347	0.1075	1.6815	O(nta1)	6.3427	-0.4484	0.2026	1.4357
O(btfa2)	6.3395	-0.4184	0.1074	2.3415	O(nta2)	6.3447	-0.4309	0.2026	2.1759
O(btfa2)	6.3447	-0.4614	0.1075	0.5954	O(nta2)	6.3242	-0.4677	0.2020	0.6177
O(btfa3)	6.3367	-0.2841	0.1074	7.7923	O(nta3)	6.3396	-0.3013	0.2025	7.6614
O(btfa3)	6.3313	-0.2341	0.1073	9.8193	O(nta3)	6.3401	-0.2370	0.2025	10.3838
	$\Omega_2^{\text{FED}} = 0.0001 \times 10^{-20} \text{ cm}^2$					$\Omega_2^{\text{FED}} = 0.0005 \times 10^{-20} \text{ cm}^2$			
	$\Omega_4^{\text{FED}} = 0.0022 \times 10^{-20} \text{ cm}^2$					$\Omega_4^{\text{FED}} = 0.0079 \times 10^{-20} \text{ cm}^2$			
	$\Omega_6^{\text{FED}} = 0.0049 \times 10^{-20} \text{ cm}^2$					$\Omega_6^{\text{FED}} = 0.0167 \times 10^{-20} \text{ cm}^2$			

Table S3. Singlet and triplet excited states energy and corresponding distance from the Eu(III) nucleus to the electronic barycenter of the ligand donor state (R_L) for the different RM1 geometries considered for the **Eu-1** and **Eu-2** complexes

Complex	$R_{L,sing.} (\text{\AA})$	$E_{sing.} (\text{cm}^{-1})$	$R_{L,trip.} (\text{\AA})$	$E_{trip.} (\text{cm}^{-1})$
INDO/S-CIS // RM1				
Eu-1				
Eu-1-1	3.97	36058.9	4.90	20720.2
Eu-1-2	3.81	35713.3	4.69	20721.7
Eu-1-3	4.30	35983.9	4.89	20896.7
Eu-1-4	4.28	36604.6	3.98	21038.4
Eu-1-5	4.51	36227.7	4.69	20969.0
Eu-1-6	4.25	36402.8	4.49	20935.9
Eu-1-7	4.08	35751.6	4.25	20865.5
Eu-1-8	4.35	36122.6	4.60	20890.1
Eu-2				
Eu-2-1	5.25	34962.9	5.49	20959.6
Eu-2-2	4.87	35752.2	5.95	22009.4
Eu-2-3	4.91	35883.7	5.52	21166.7
Eu-2-4	5.57	36389.0	5.49	21058.1
Eu-2-5	5.34	36956.9	5.54	21203.7
Eu-2-6	5.45	36321.3	5.69	21120.7
Eu-2-7	5.16	36546.1	5.47	21180.7
Eu-2-8	5.27	36884.1	5.50	21128.2

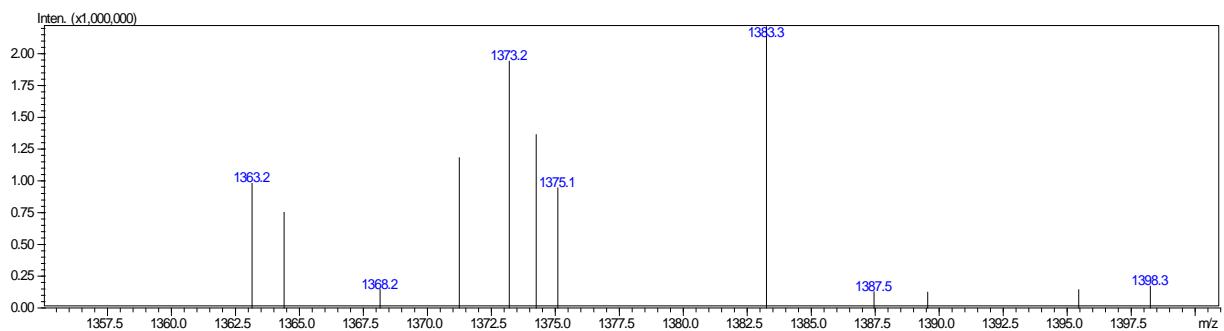


Fig. S1. Positive mode ESI-MS spectrum of **Eu-1** complex in acetone solution.

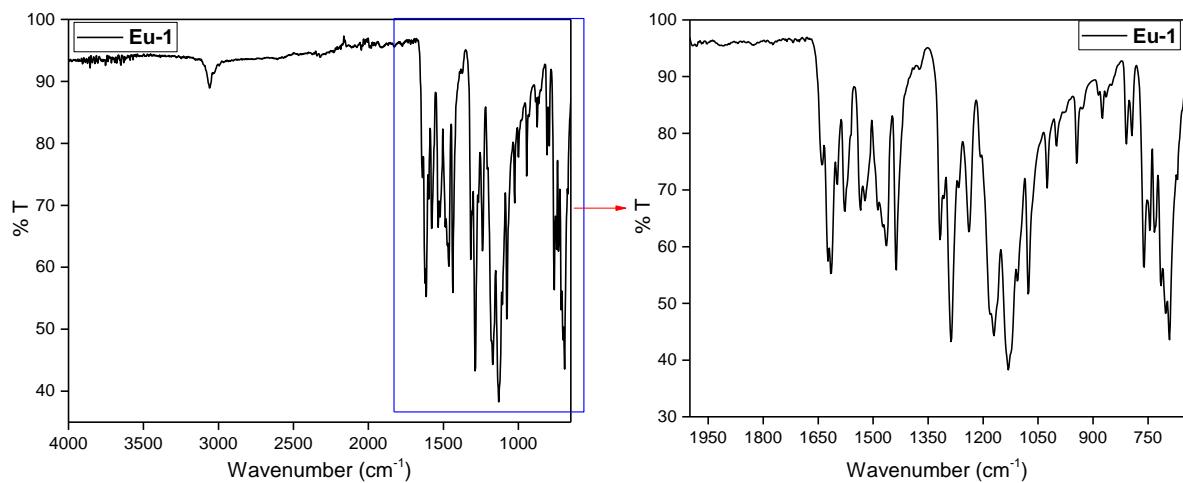


Fig. S2. FTI-R spectrum of solid **Eu-1** complex with its expansion from $2000 - 650\text{ cm}^{-1}$

1.

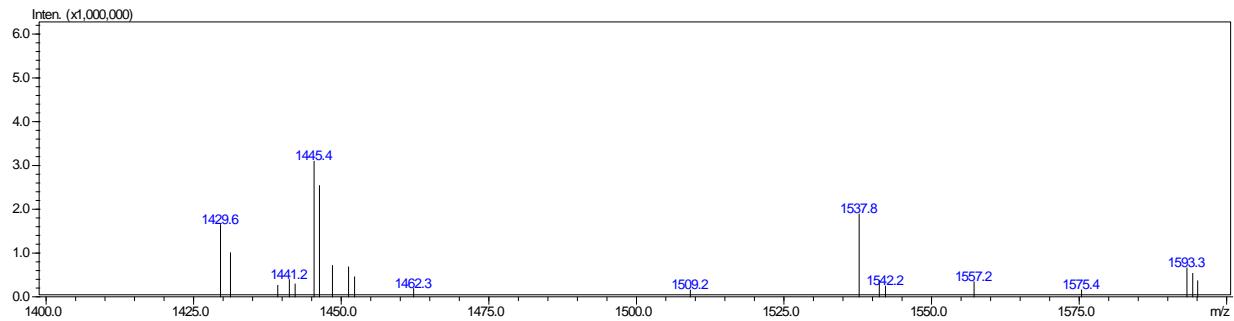


Fig. S3. Positive mode ESI-MS spectrum of **Eu-2** complex in acetone solution.

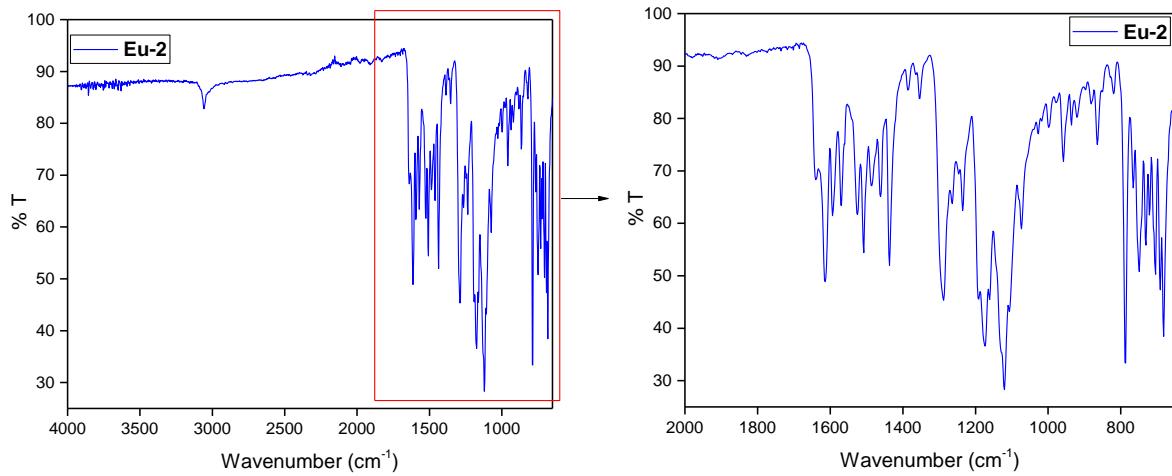


Fig. S4. FTIR spectra of solid **Eu-2** complex with its expansion from 2000 – 650 cm⁻¹.

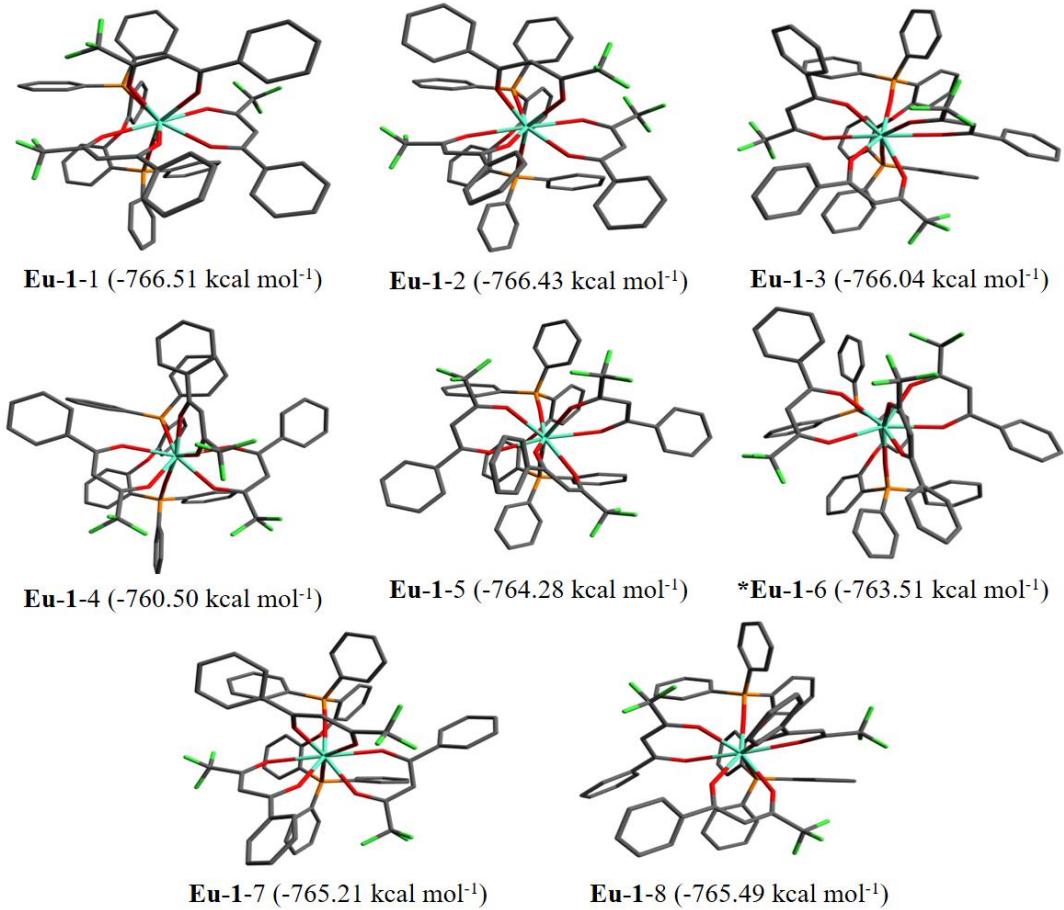


Fig. S5. Geometries optimized at the RM1 level of theory for different structural possibilities considered for **Eu-1**. The values in the parentheses are the heat of formation for each structure calculated with RM1. *Conformation of the starting structure (CSD CODE 1942486).

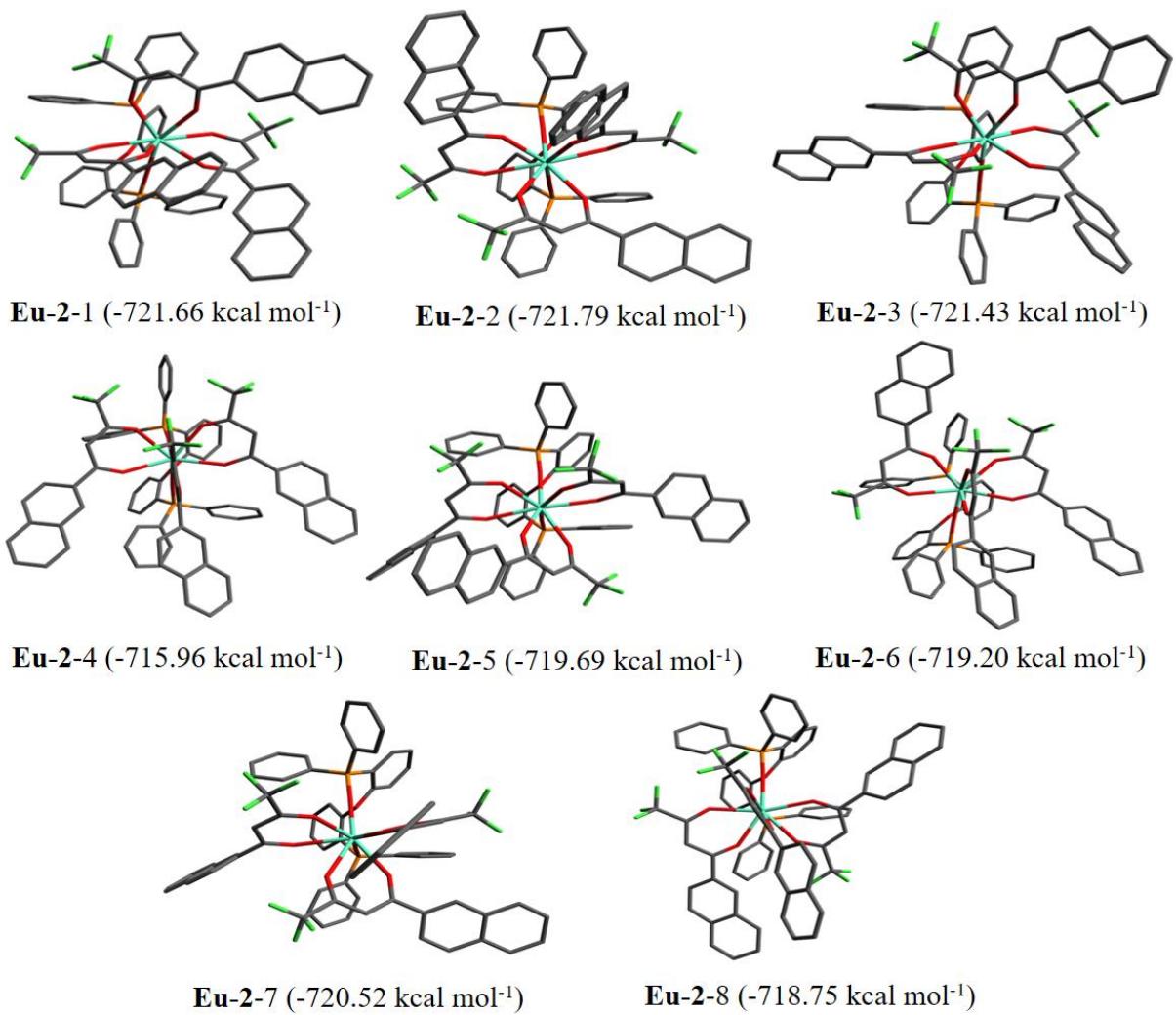


Fig. S6. Geometries optimized at the RM1 level of theory for different structural possibilities considered for **Eu-2** complex. The values in the parentheses are the heat of formation for each structure calculated with RM1.

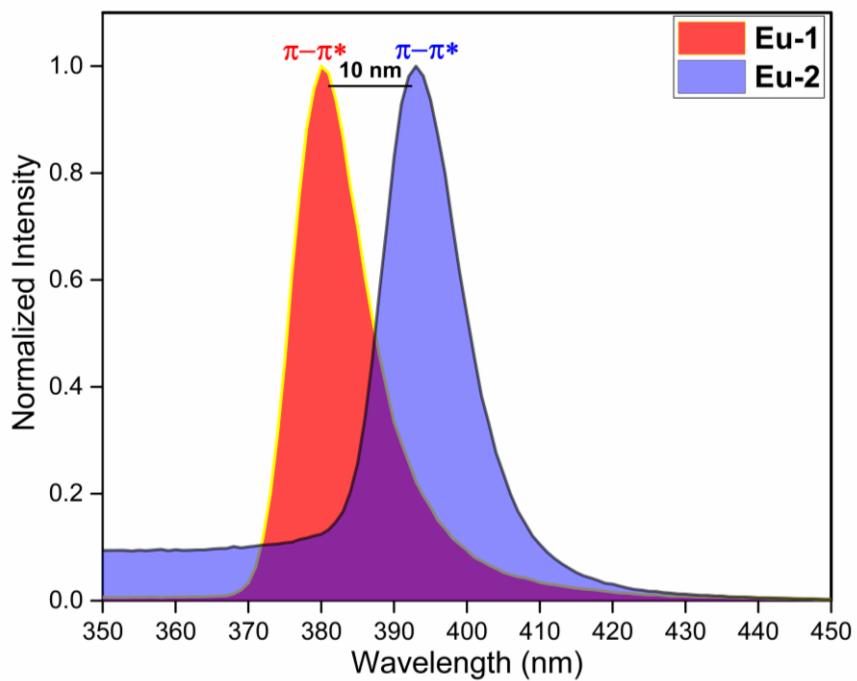


Fig. S7. Excitation spectra of the **Eu-1** and **Eu-2** complexes in DCM solution at RT.

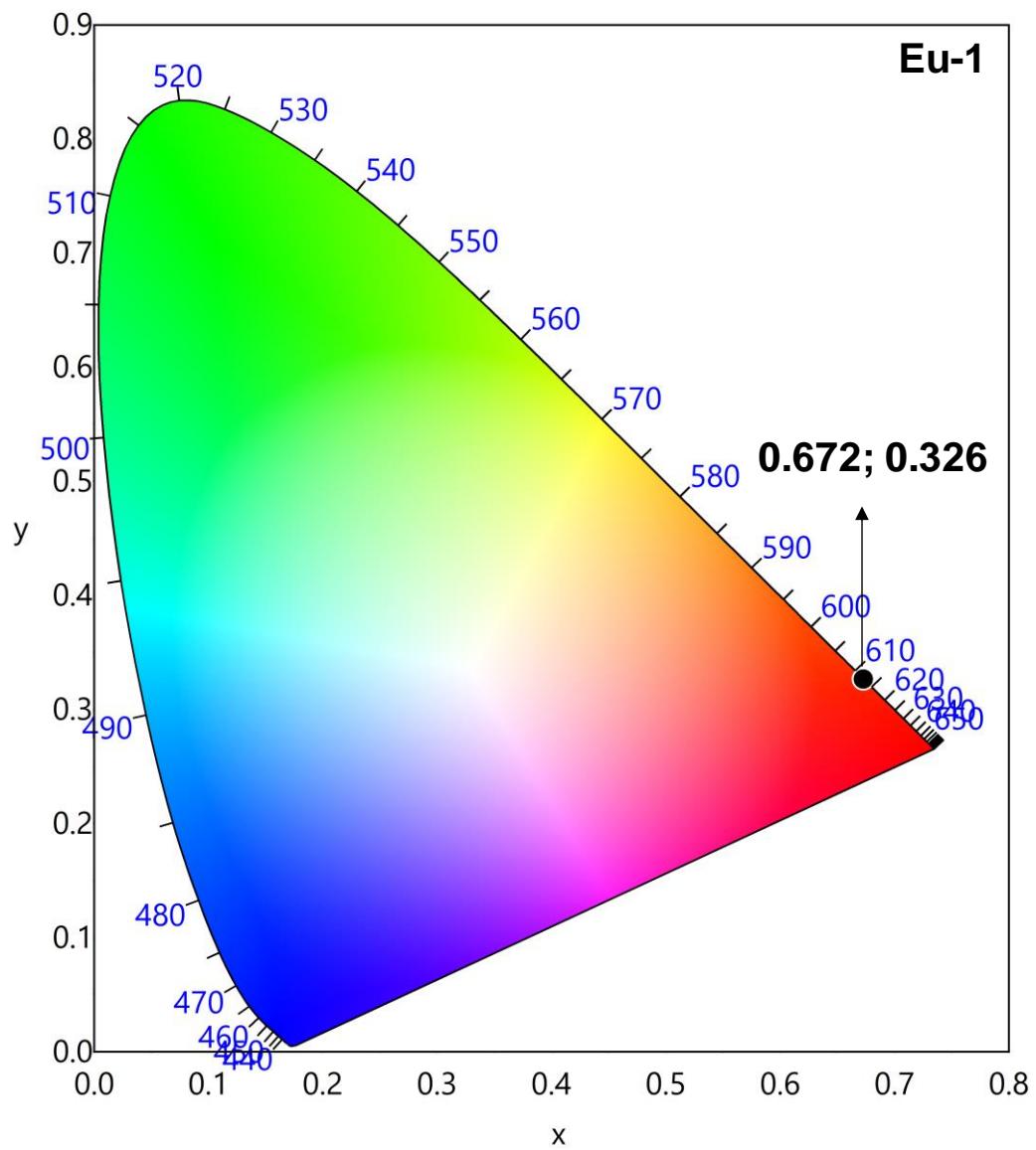


Fig. S8. International Commission on Illumination (CIE) 1931 chromaticity diagram of **Eu-1** showing the observed color in DCM solution at RT.

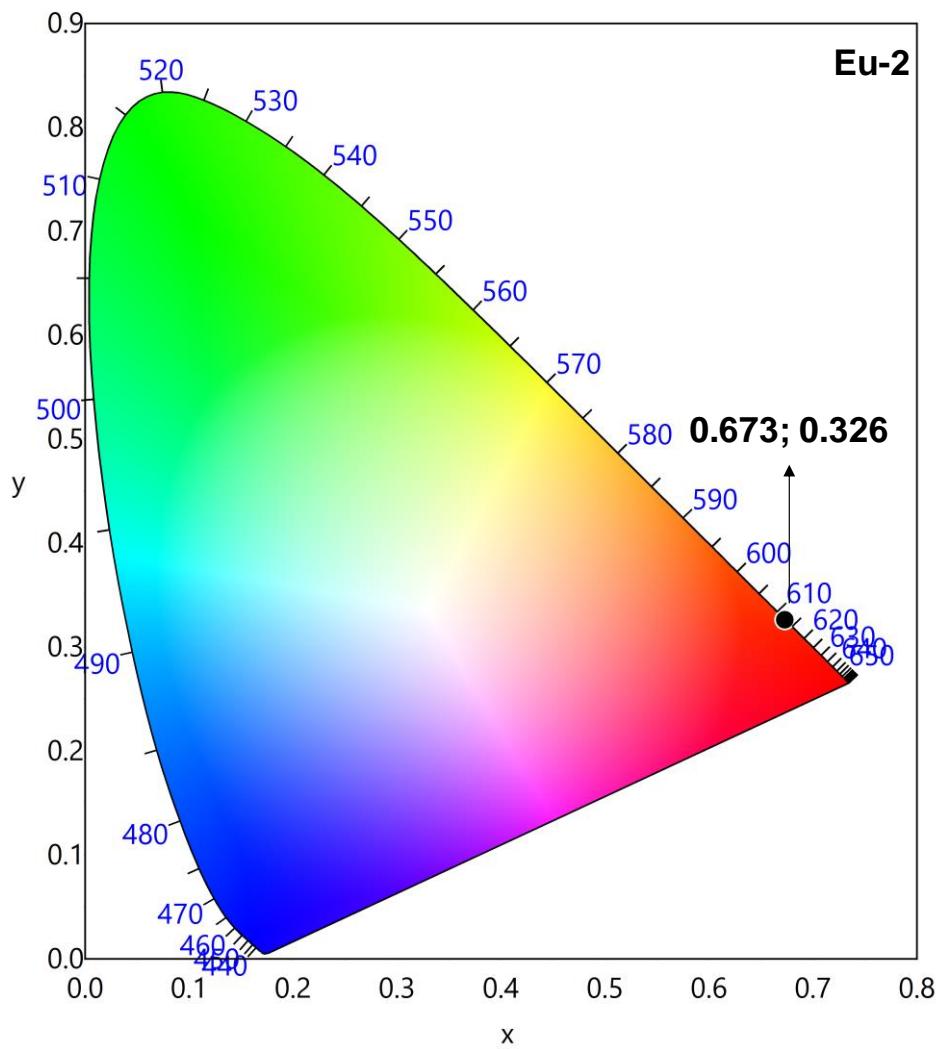


Fig. S9. 1931 CIE chromaticity diagram of **Eu-2** showing the observed color in DCM solution at RT.

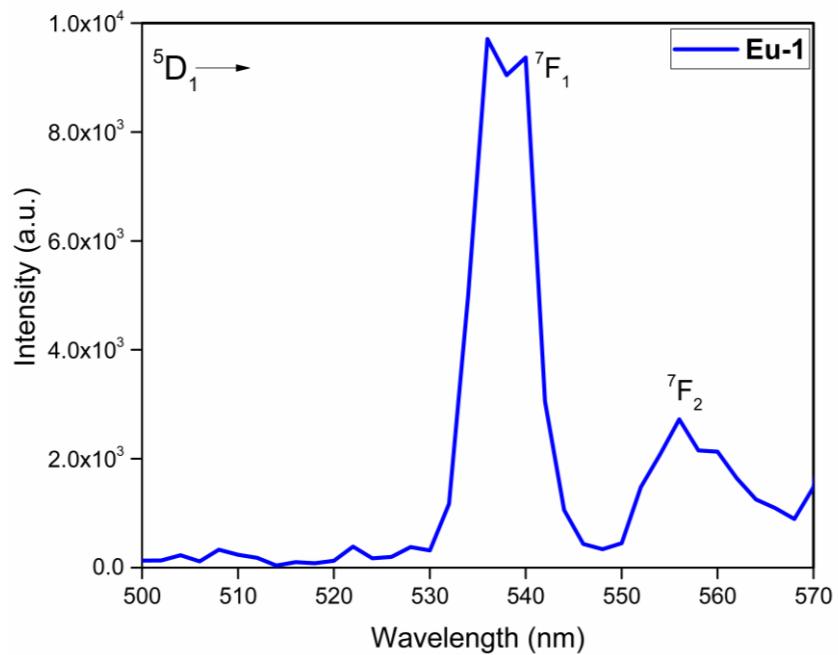


Fig. S10. Magnification of the region between 500 – 570 nm displaying ${}^5D_1 \rightarrow {}^7F_{1-2}$ transitions at RT for **Eu-1** complex.

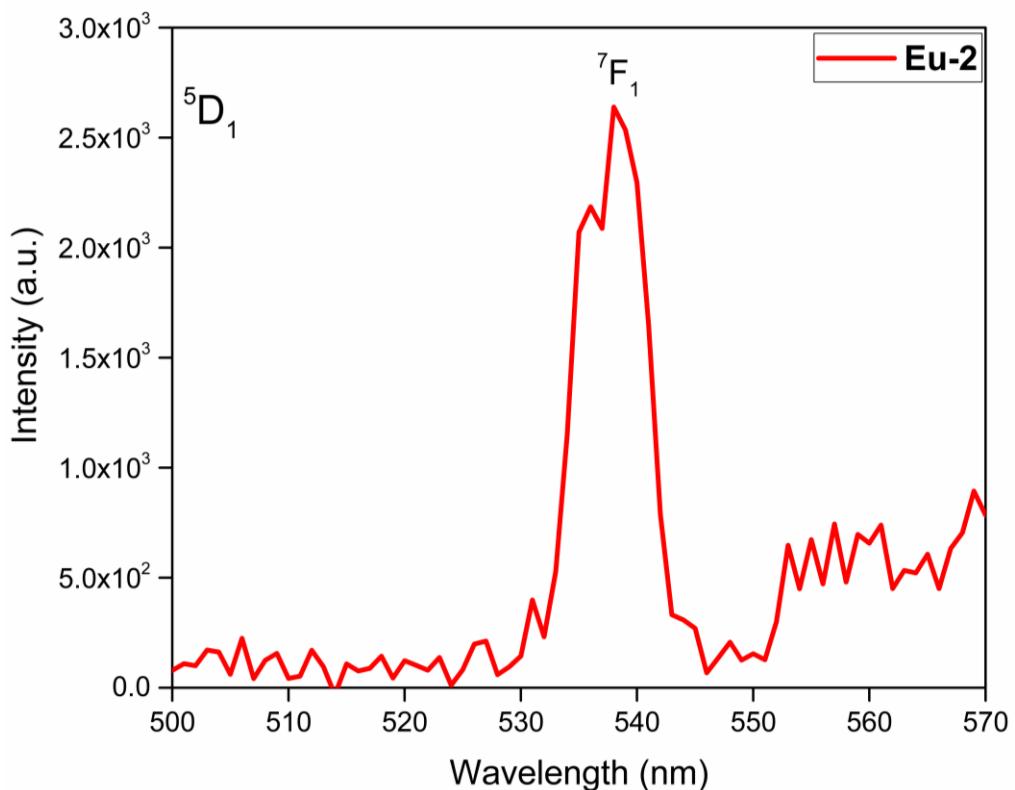


Fig. S11. Magnification of the region between 500 – 570 nm displaying ⁵D₁ → ⁷F₁ transitions at RT for **Eu-2** complex.

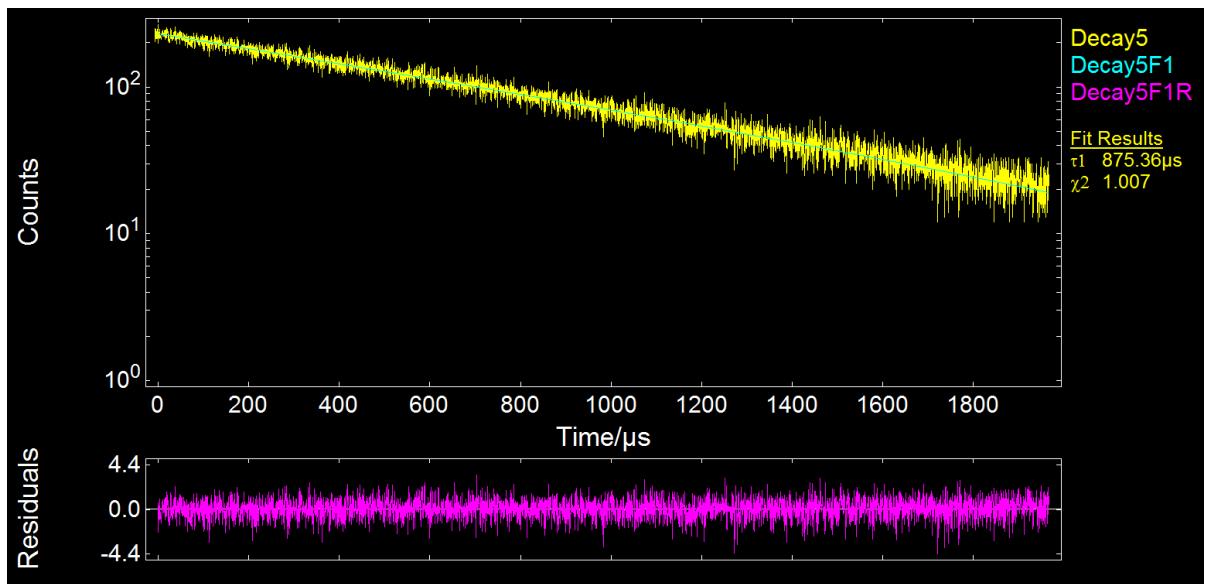


Fig. S12. Decay curve of Eu-1 with fitted curve and observed luminescence lifetime in DCM at RT.

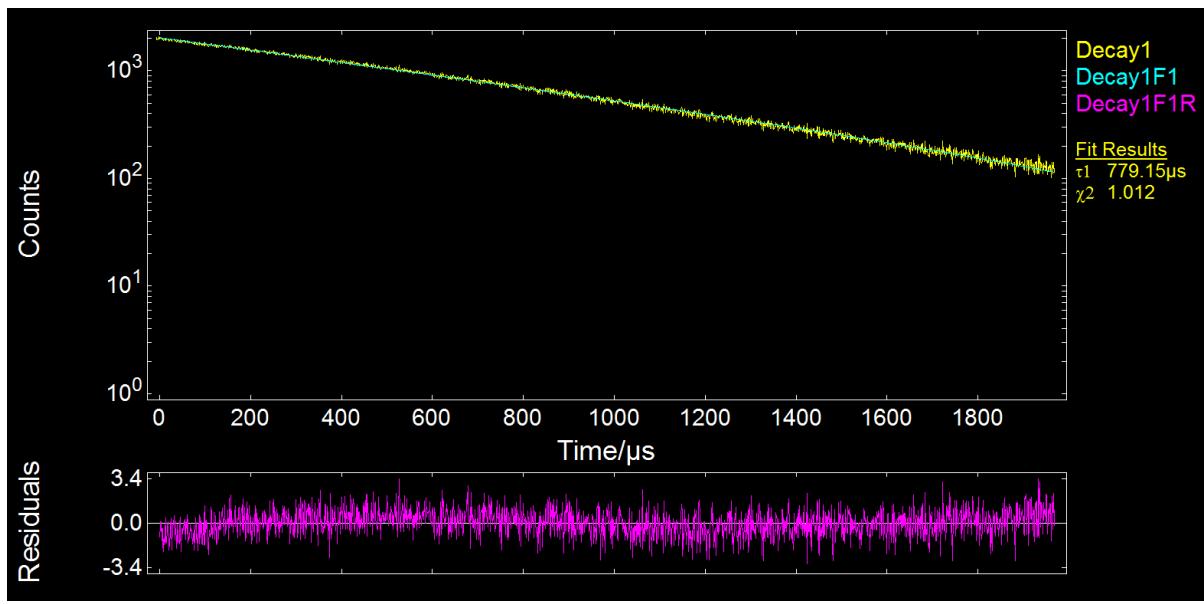


Fig. S13. Decay curve of **Eu-2** with fitted curve and observed luminescence lifetime in DCM at RT.

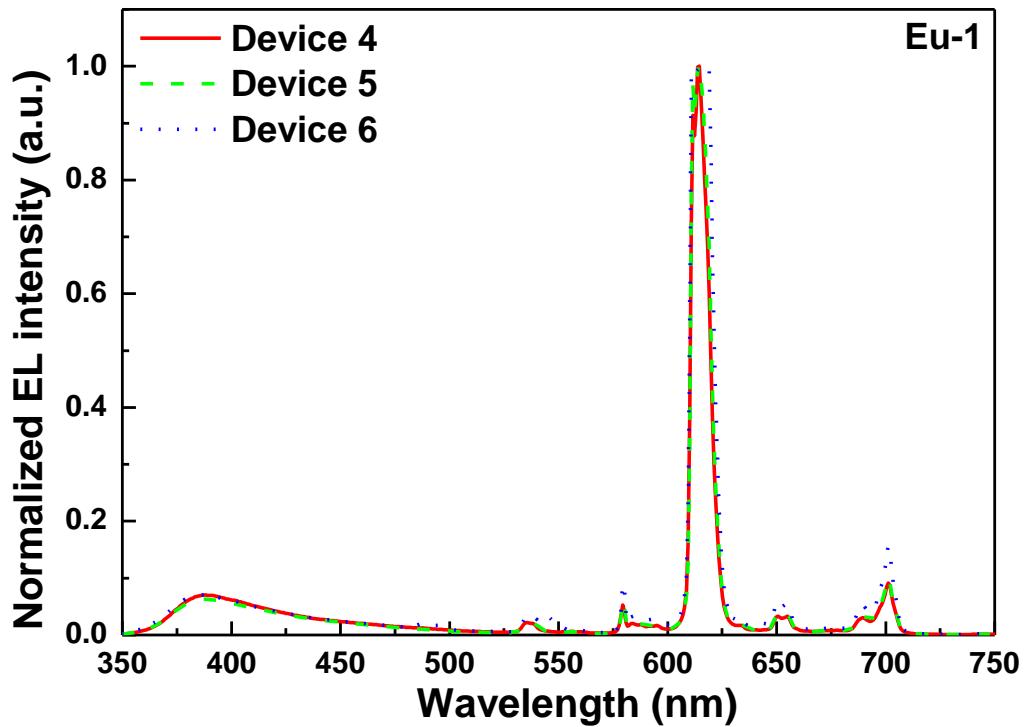


Fig. S14. Normalized EL spectra of the double-EML devices **4**, **5** and **6** of **Eu-1** operating at 10 mA/cm^2 .

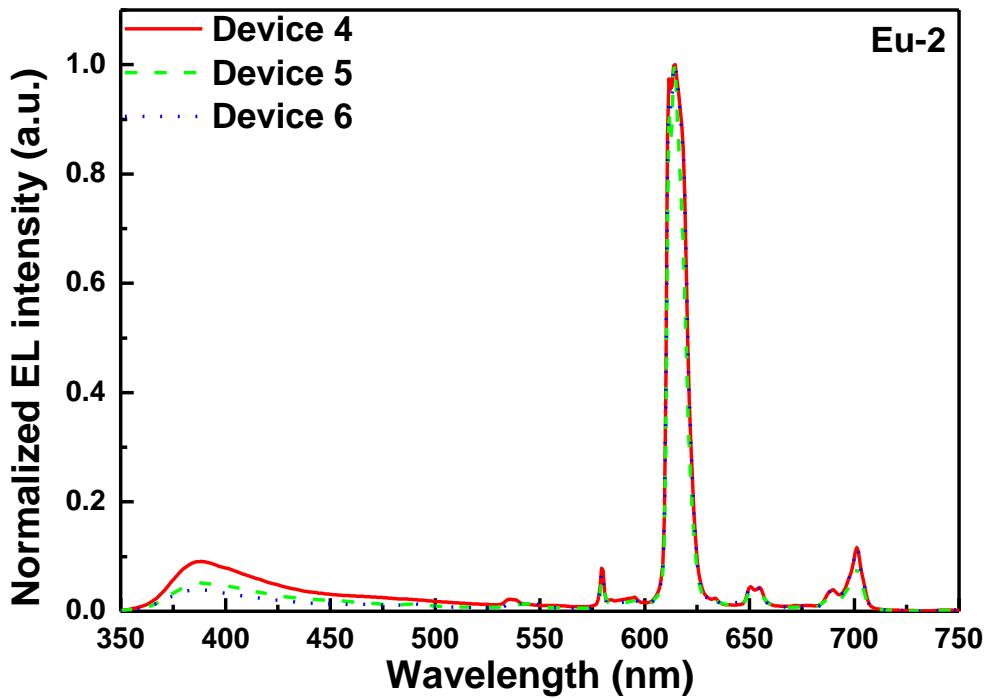


Fig. S15. Normalized EL spectra of the double-EML devices 4, 5 and 6 of Eu-2 operating at 10 mA/cm^2 .

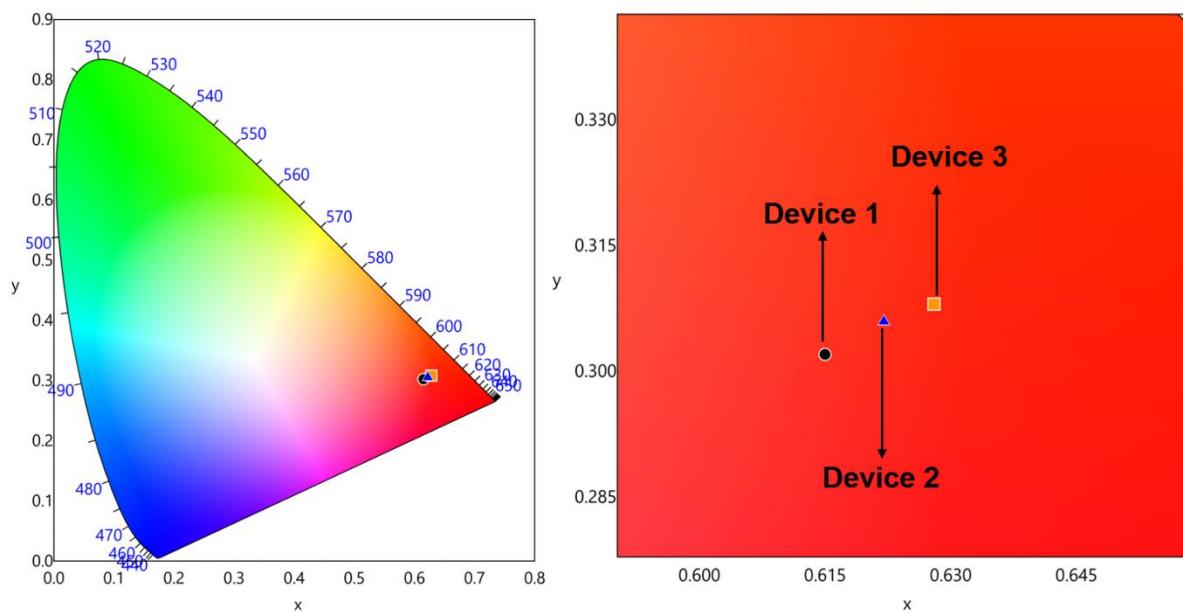


Fig. S16. CIE 1931 chromaticity diagrams of single EML devices **1**, **2** and **3** of **Eu-2** with magnified view operating at 10 mA/cm^2 .

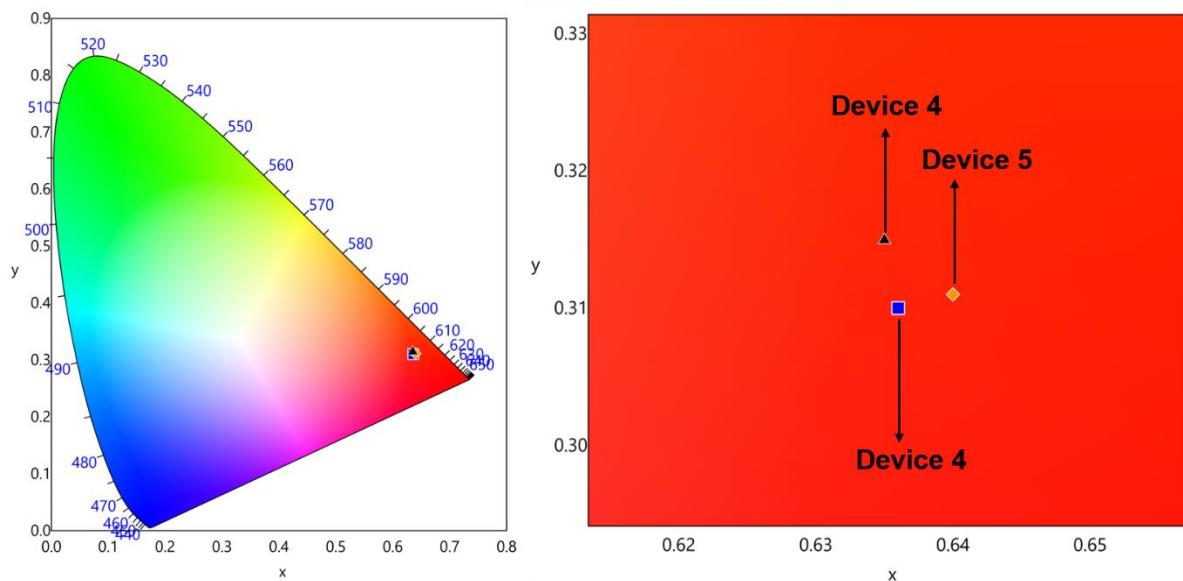


Fig. S17. CIE 1931 chromaticity diagrams of single EML devices **4**, **5** and **6** of **Eu-1** with magnified view operating at 10 mA/cm^2 .

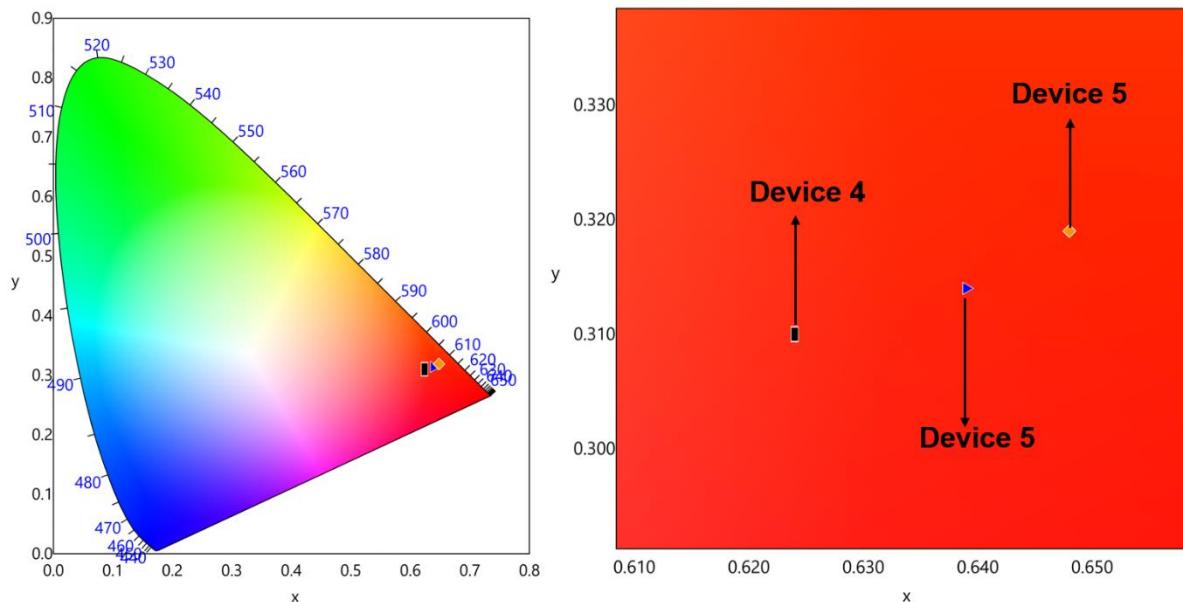


Fig. S18. CIE 1931 chromaticity diagrams of single EML devices **4**, **5** and **6** of **Eu-2** with magnified view operating at 10 mA/cm^2 .

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