

## Electronic Supplementary Information

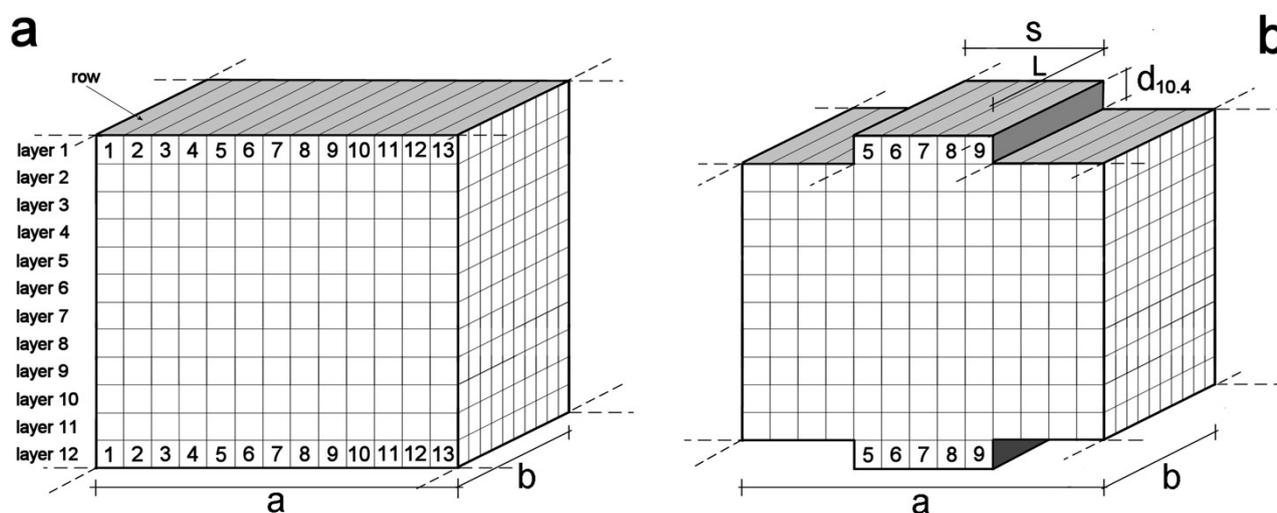
### A new computational strategy to calculate the edge energy of a relaxed step. Calcite ( $\text{CaCO}_3$ ) as a case study

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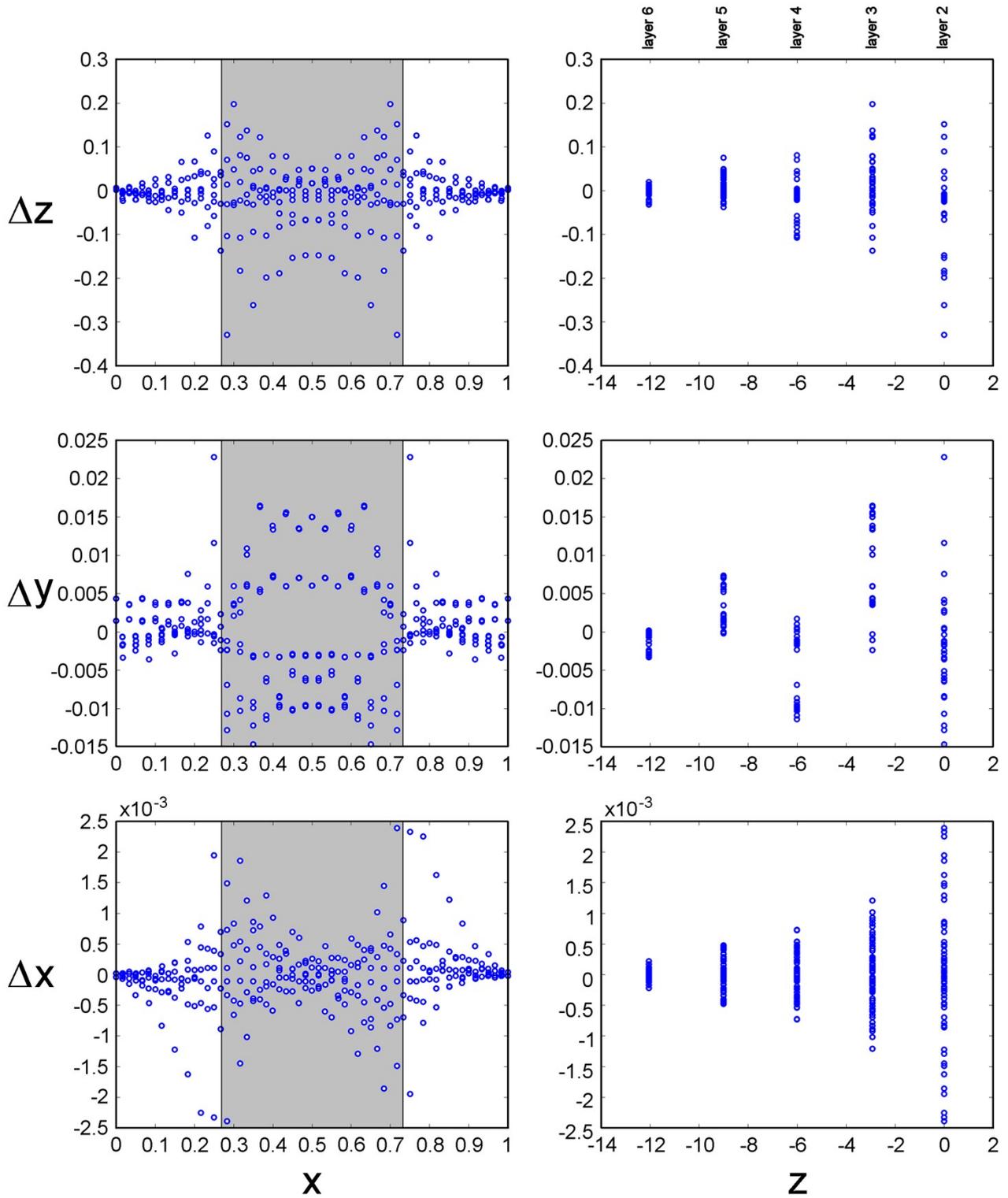
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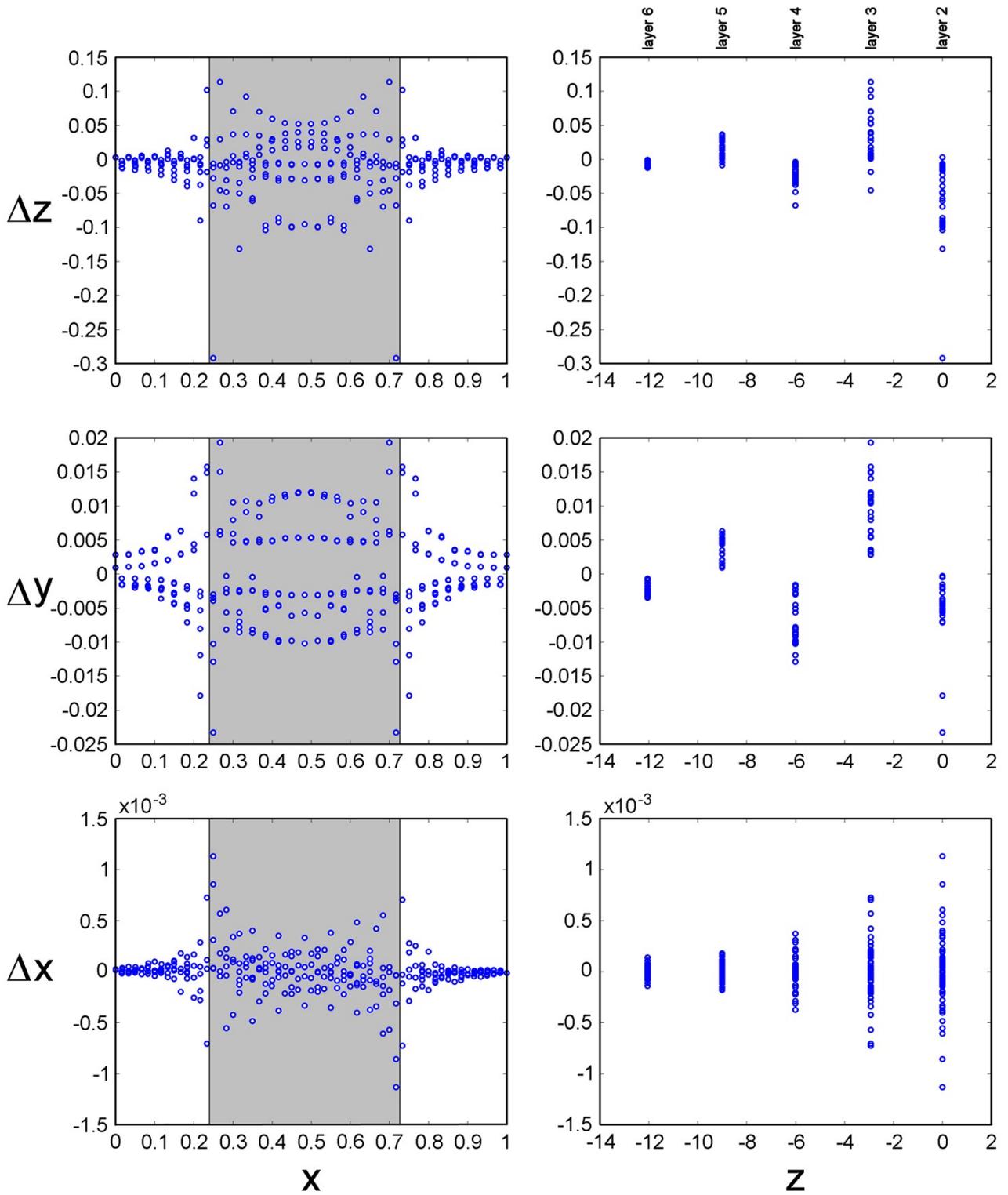
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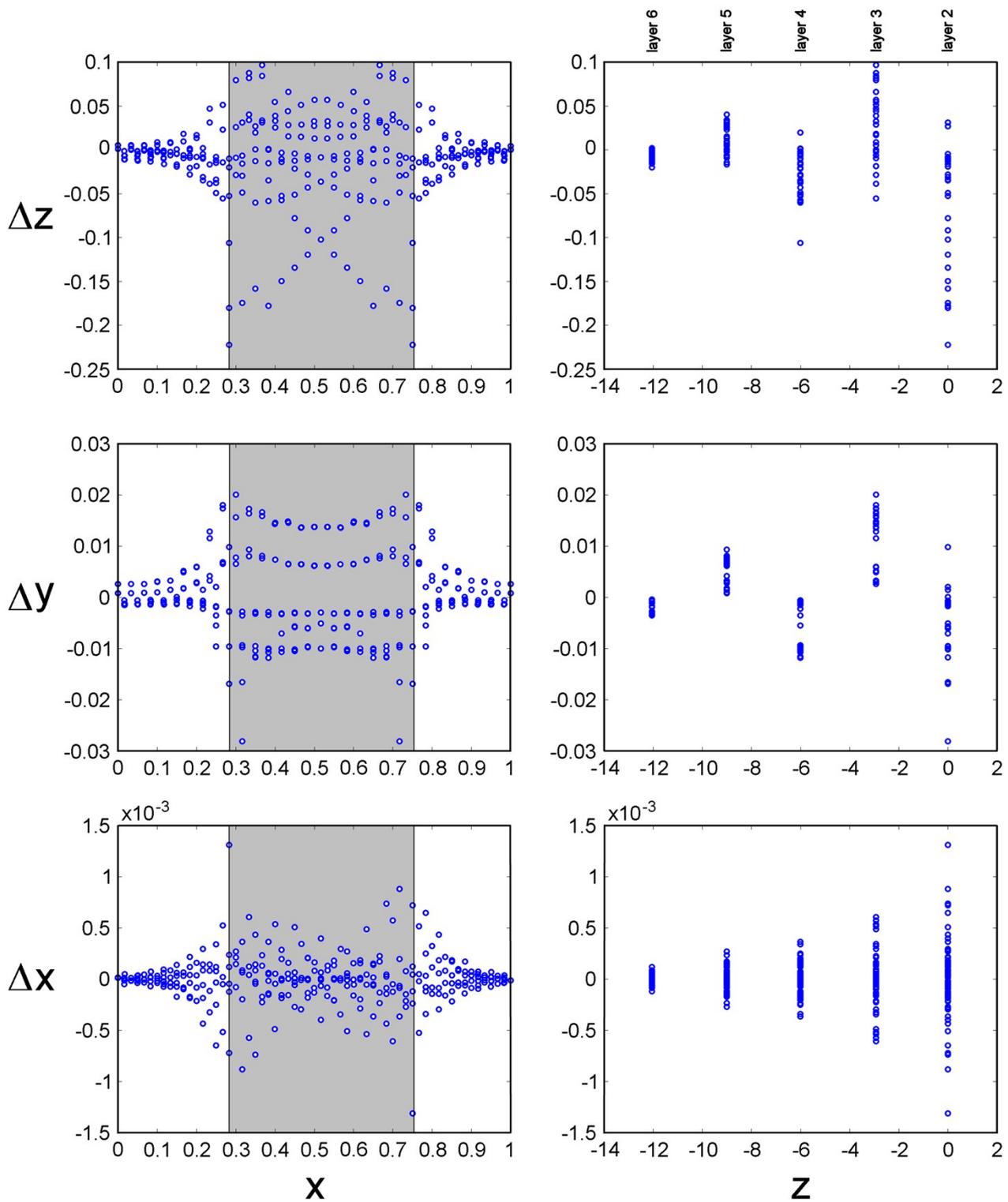
**Figure S1.** Kossel's crystal is used to exemplify the construction of two steps of height  $d_{10.4}$  on the top and bottom crystal surface of a slab of calcite for performing quantum-mechanical geometry optimizations. (a) Twelve-layers (10.4) slab is cut from the optimized bulk structure of calcite. (b) Steps delimited by two  $[uvw]$  edges parallel to cell parameter  $b$  are generated by deleting rows 1-4 and 10-13 in the layers 1 and 12.  $S$  and  $L$  are the width and length of the step, respectively. Top and bottom surfaces of the slab (with step) are be put in relation by either an inversion center or a mirror plane to cancel out the dipole moment and allowing quantum-mechanical calculations.



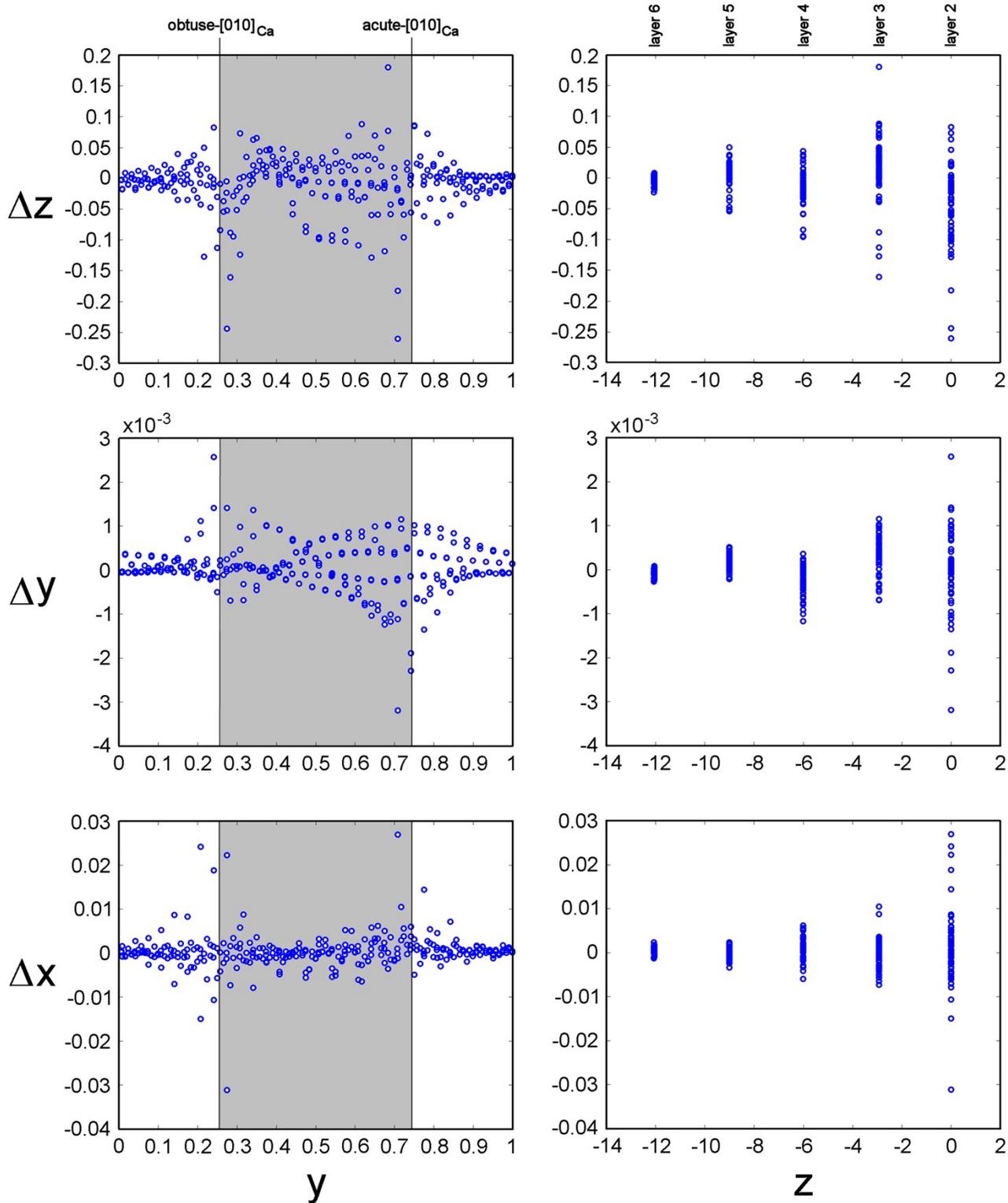
**Figure S2.**  $\Delta X$ ,  $\Delta Y$  and  $\Delta Z$  as a function of  $X$  (fractional coordinates) and  $Z$  (cartesian coordinates,  $\text{\AA}$ ) for the  $[4\bar{2}1]_{\text{Ca}}$  step on (10.4) surface. In the left column, the grey area indicates the location of the step along  $X$ . In the right column,  $Z = 0$  is the  $d_{10.4}$  layer just below the step (i.e., layer 2) and  $Z \sim -12 \text{ \AA}$  is the last layer in region 1 (i.e., layer 6).



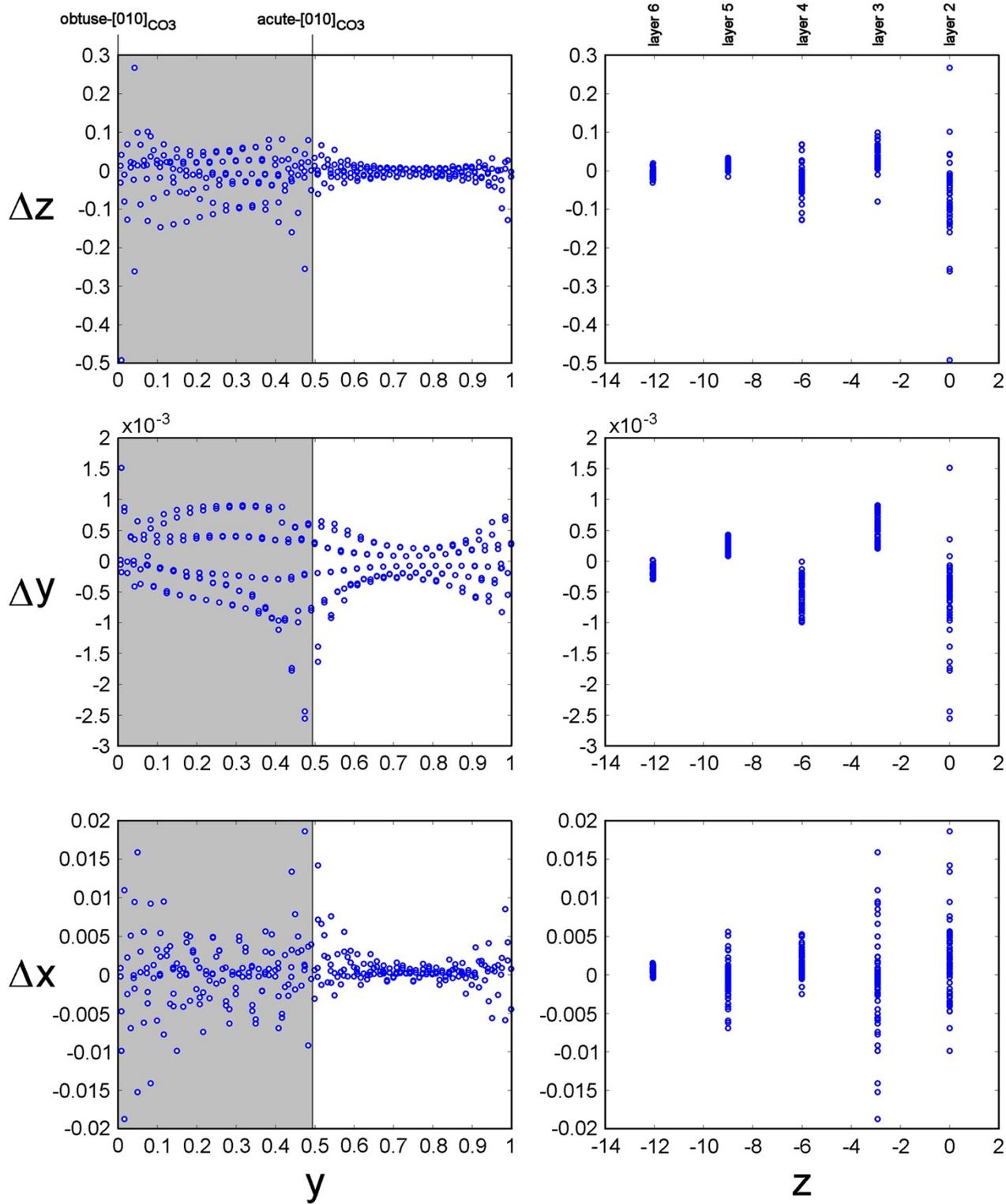
**Figure S3.**  $\Delta X$ ,  $\Delta Y$  and  $\Delta Z$  as a function of  $X$  (fractional coordinates) and  $Z$  (cartesian coordinates, Å) for the  $[4^2 1]_{\text{CO}_3(\text{A})}$  step on (10.4) surface. In the left column, the grey area indicates the location of the step along  $X$ . In the right column,  $Z = 0$  is the  $d_{10.4}$  layer just below the step (i.e., layer 2) and  $Z \sim -12$  Å is the last layer in region 1 (i.e., layer 6).



**Figure S4.**  $\Delta X$ ,  $\Delta Y$  and  $\Delta Z$  as a function of  $X$  (fractional coordinates) and  $Z$  (cartesian coordinates, Å) for the  $[4^2\bar{1}]_{\text{CO}_3(\text{B})}$  step on (10.4) surface. In the left column, the grey area indicates the location of the step along  $X$ . In the right column,  $Z = 0$  is the  $d_{10.4}$  layer just below the step (i.e., layer 2) and  $Z \sim -12$  Å is the last layer in region 1 (i.e., layer 6).



**Figure S5.**  $\Delta X$ ,  $\Delta Y$  and  $\Delta Z$  as a function of  $X$  (fractional coordinates) and  $Z$  (cartesian coordinates, Å) for the  $[010]_{Ca}$  step on  $(10.4)$  surface. In the left column, the grey area indicates the location of the step along  $Y$ . In the right column,  $Z = 0$  is the  $d_{10.4}$  layer just below the step (i.e., layer 2) and  $Z \sim -12$  Å is the last layer in region 1 (i.e., layer 6).



**Figure S6.**  $\Delta X$ ,  $\Delta Y$  and  $\Delta Z$  as a function of  $X$  (fractional coordinates) and  $Z$  (cartesian coordinates, Å) for the  $[010]_{\text{CO}_3}$  step on (10.4) surface. In the left column, the grey area indicates the location of the step along  $Y$ . In the right column,  $Z = 0$  is the  $d_{10.4}$  layer just below the step (i.e., layer 2) and  $Z \sim -12$  Å is the last layer in region 1 (i.e., layer 6).