

## Electronic Supplementary Information

### Role of Free Volumes and Segmental Dynamics on Ion Conductivity of PEO/LiTFSI Solid Polymer Electrolytes Filled with SiO<sub>2</sub> Nanoparticles: A Positron Annihilation and Broadband Dielectric Spectroscopy Study

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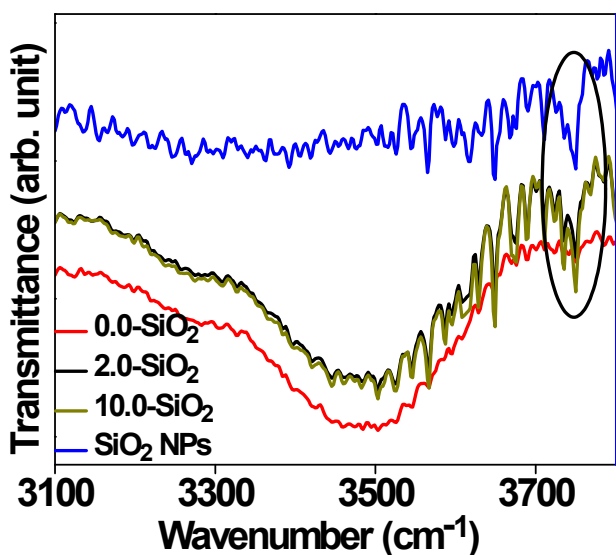
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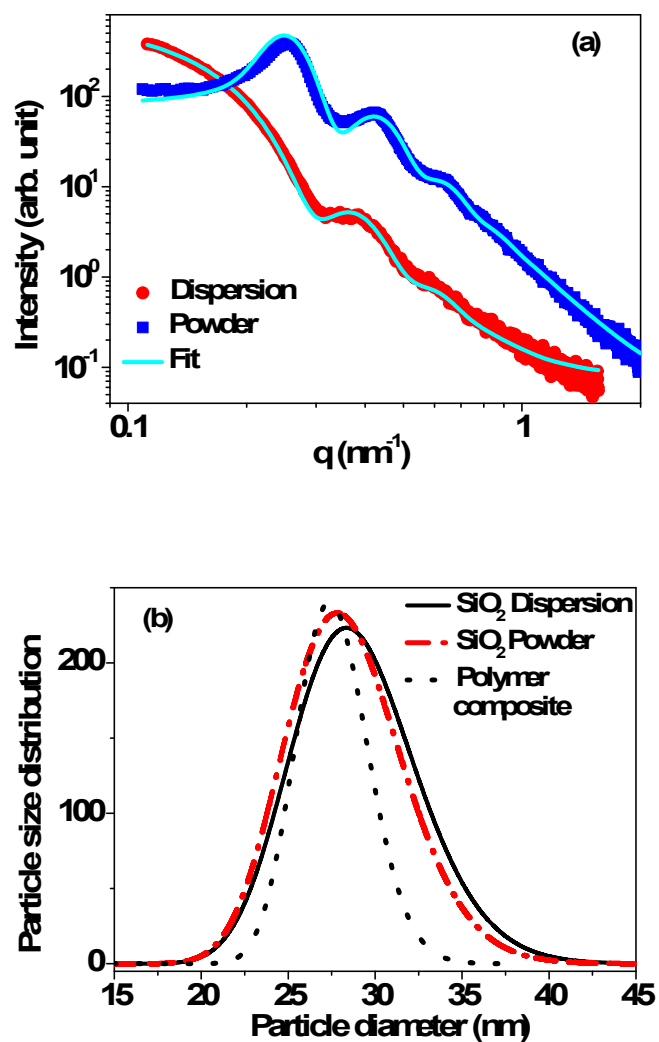
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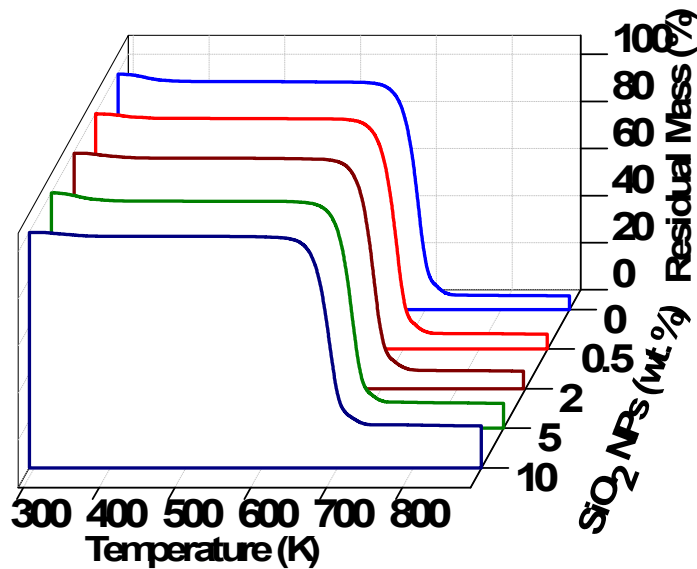
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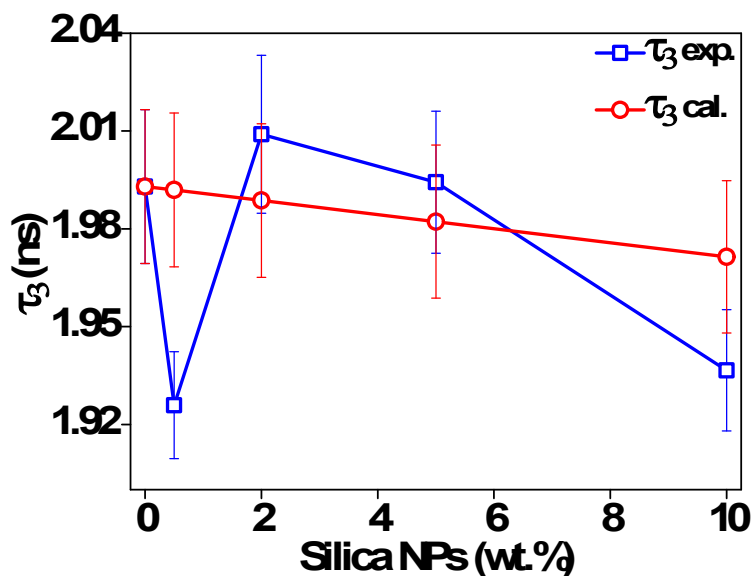
**Figure S1:** FTIR spectra of SiO<sub>2</sub> NPs and SPEs showing band in the range of 3740-3750 cm<sup>-1</sup> corresponding to silanol groups.



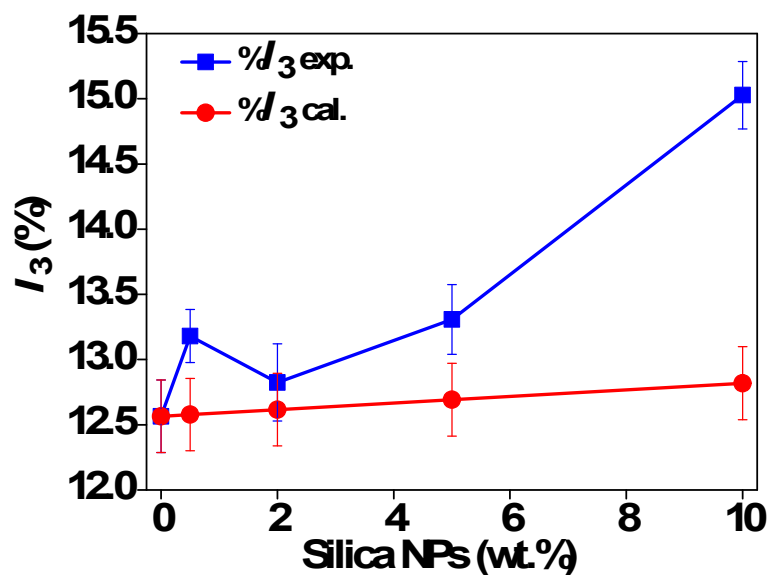
**Figure S2:** (a) The SAXS profile of the 2 wt.% silica dispersion and the dried silica nanopowder are depicted. The SAXS profiles have been fitted using eq. 6 in the manuscript (b) particle size distribution is estimated from both the profiles as well as estimated in the composite SPE.



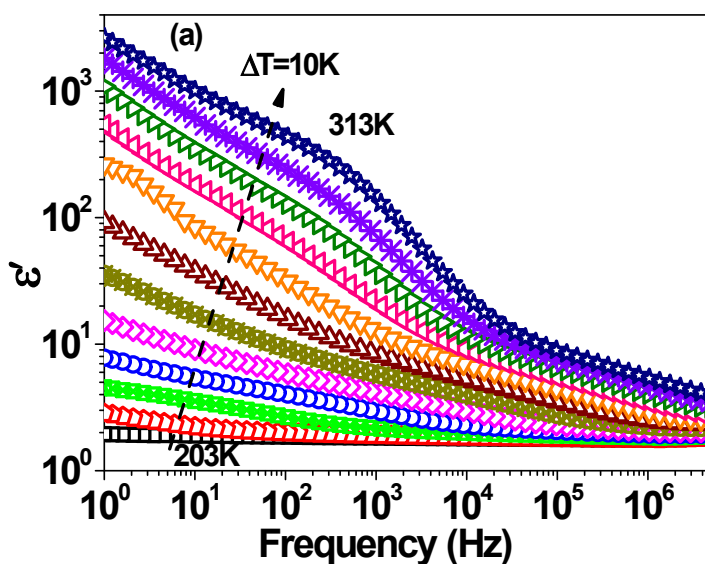
**Figure S3:** TGA curves of PEO based electrolytes with different loadings of SiO<sub>2</sub> NPs (0.0 -10.0 wt.%).

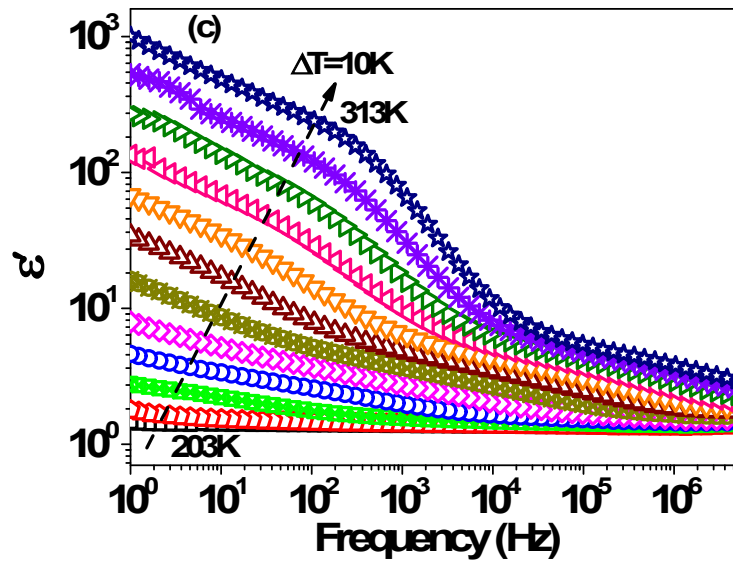
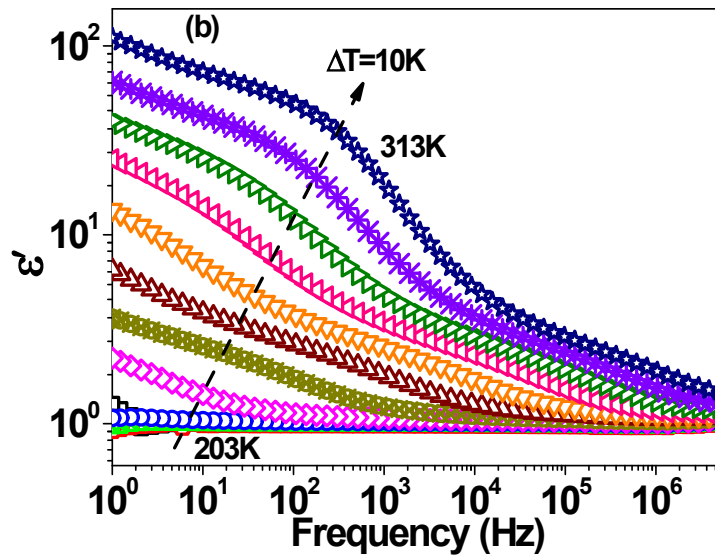


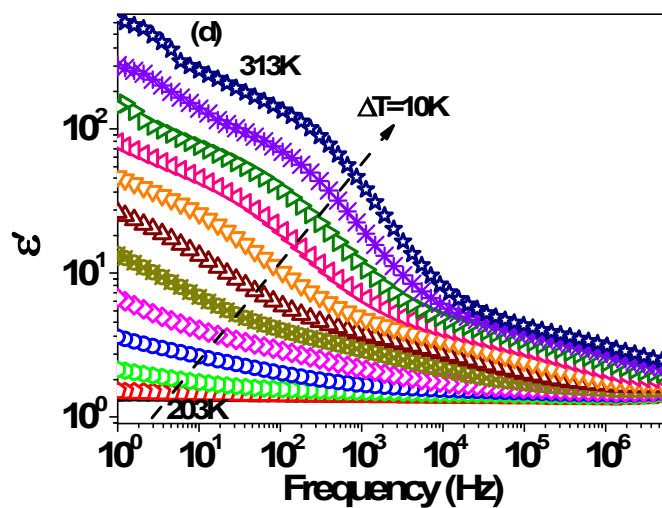
**Figure S4:** *o*-Ps lifetime as a function of SiO<sub>2</sub> NPs loading. The red circle symbol shows the calculated *o*-Ps lifetime considering SPEs as mixture of PEO-5wt.% LiTFSI and SiO<sub>2</sub> NPs using eq.  $\tau_{\text{cal}} = x\tau_{\text{silica}} + (1-x)\tau_{\text{silica-0}}$ , where  $x$  is the weight fraction of SiO<sub>2</sub> NPs in the electrolyte. Lines are guide to the eye.



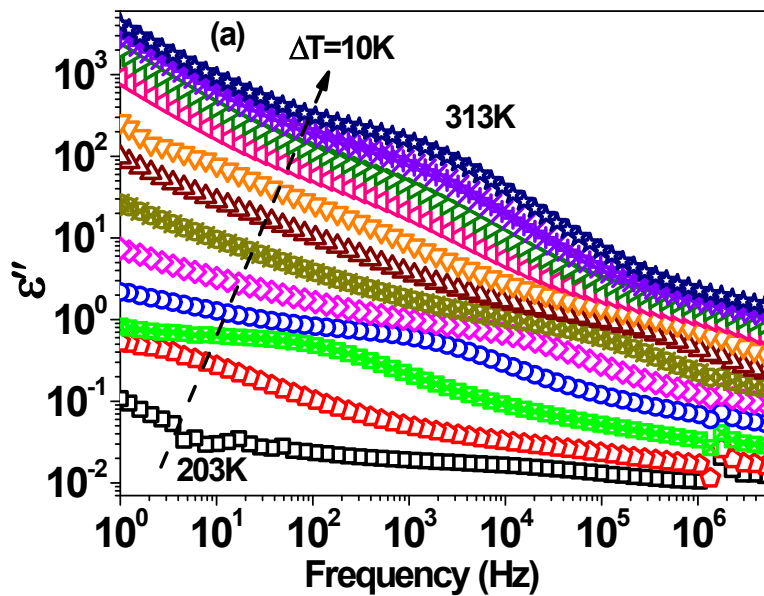
**Figure S5:** *o*-Ps intensity as a function of SiO<sub>2</sub> NPs loading. The red circle symbol shows the calculated *o*-Ps lifetime considering SPEs as mixture of PEO-5wt.% LiTFSI and SiO<sub>2</sub> NPs using eq.  $I_{cal} = xI_{silica+} + (1-x)I_{silica-0}$ , where  $x$  is the weight fraction of SiO<sub>2</sub>NPs in the electrolyte. Lines are guide to the eye.

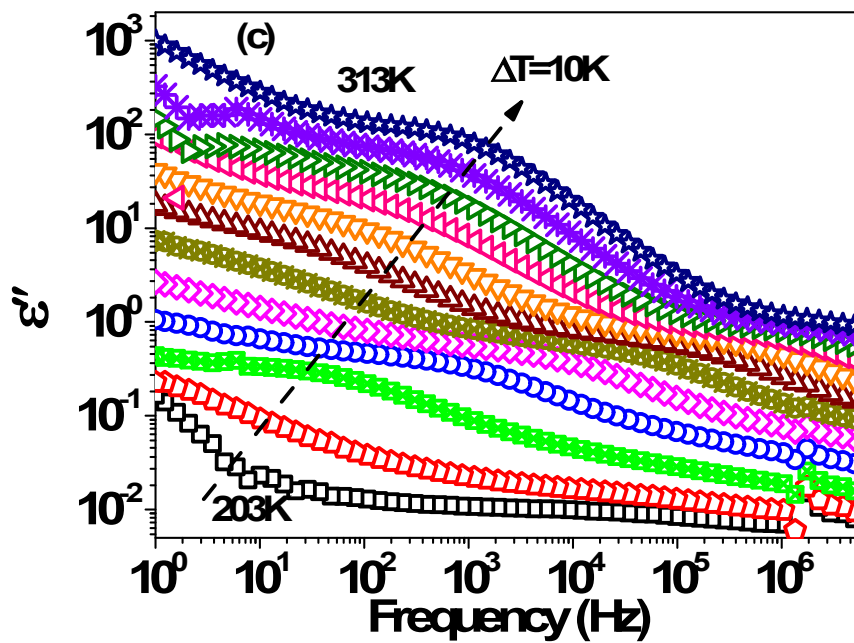
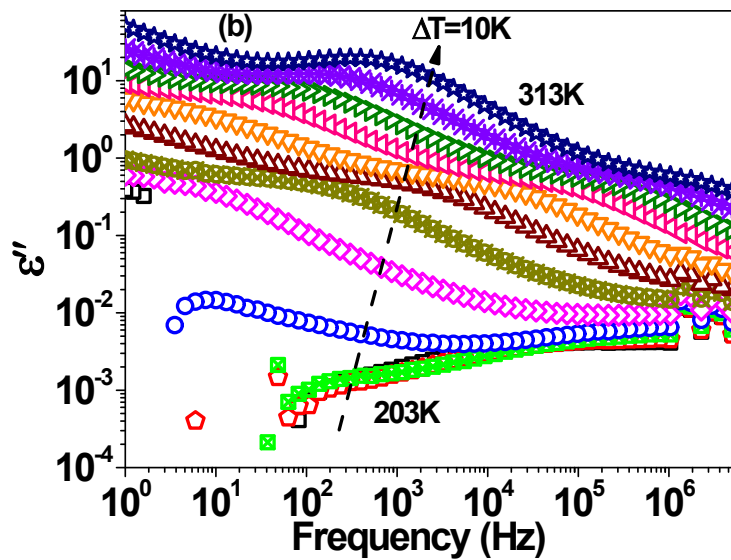


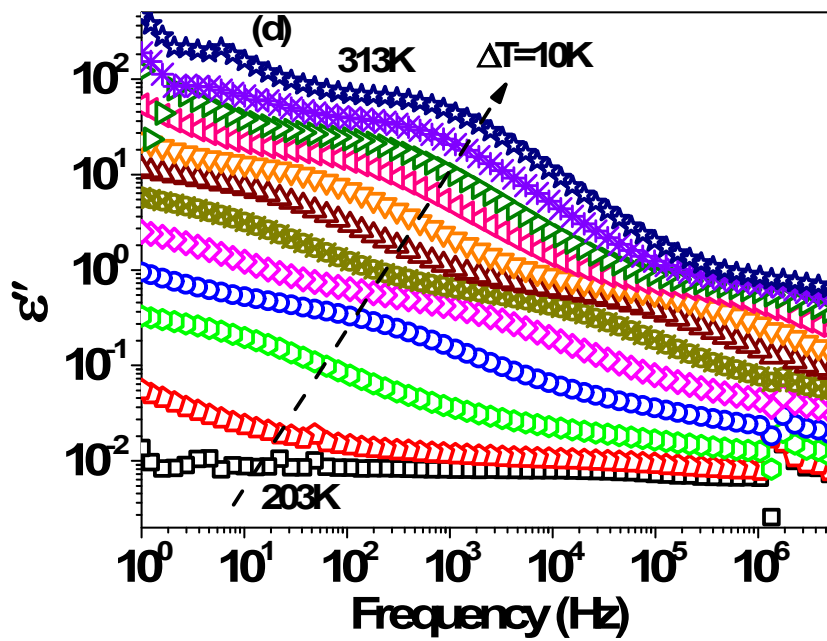




**Figure S6:** Real part ( $\epsilon'$ ) of the complex permittivity of (a) 0.0-SiO<sub>2</sub> (b) 0.5-SiO<sub>2</sub> (c) 2.0-SiO<sub>2</sub> (d) 10.0-SiO<sub>2</sub> SPEs.

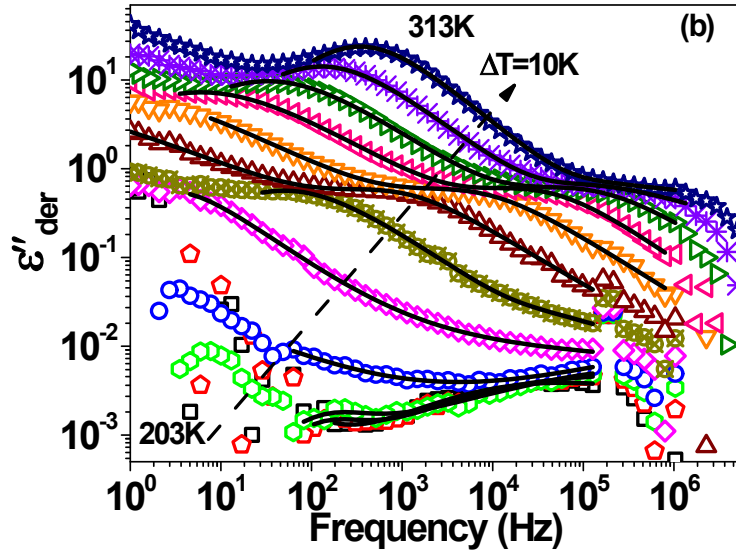
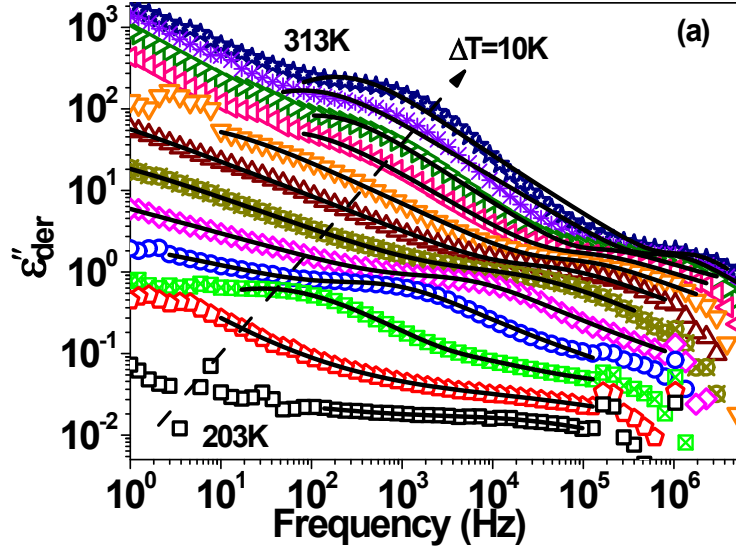


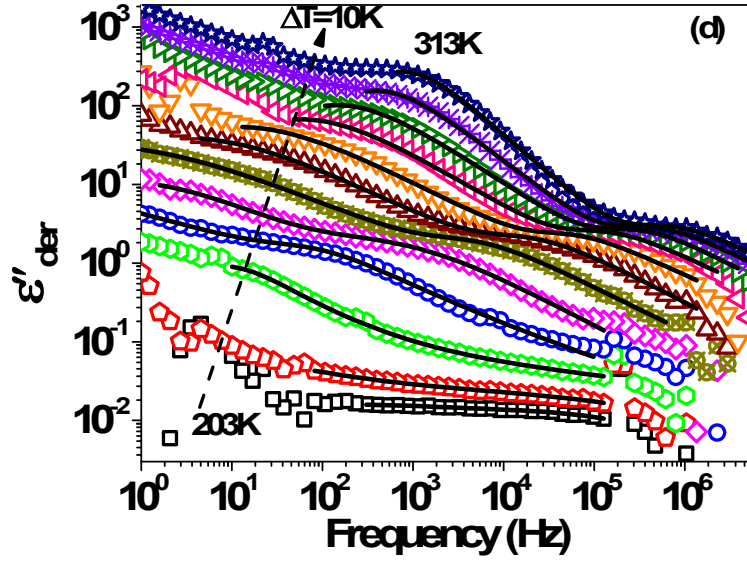
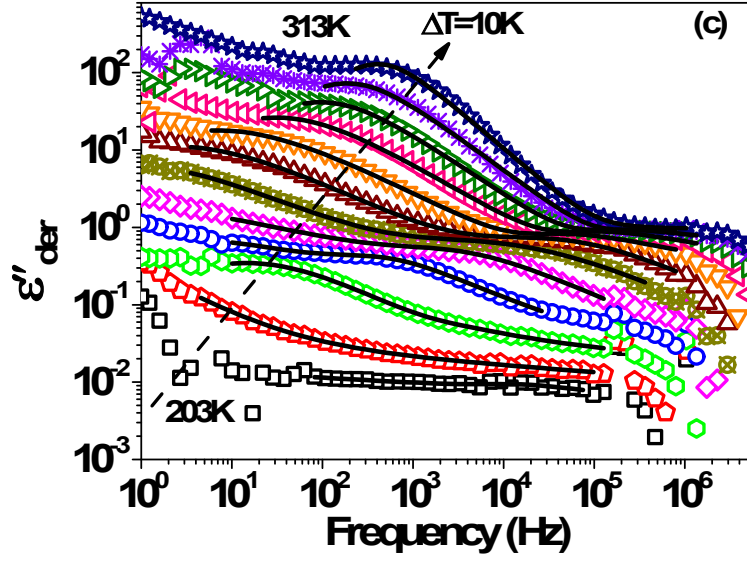


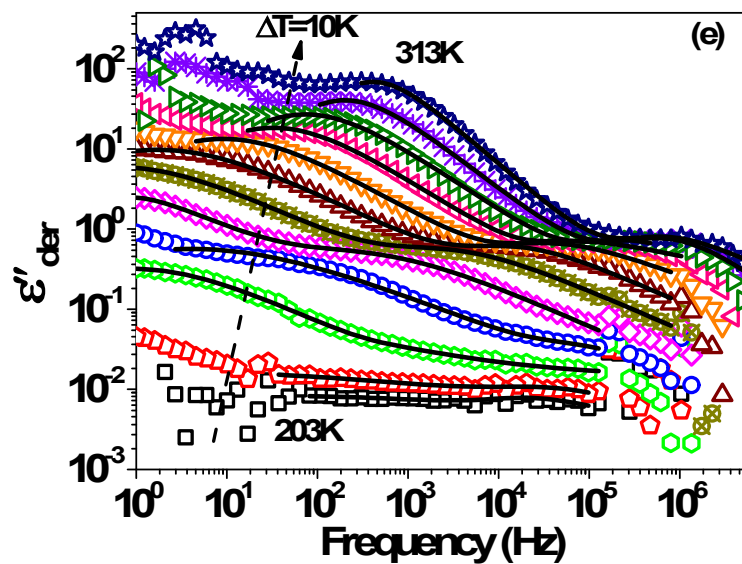


**Figure S7:** Imaginary part ( $\epsilon''$ ) of the complex permittivity of (a) 0.0-SiO<sub>2</sub> (b) 0.5-SiO<sub>2</sub> (c) 2.0-SiO<sub>2</sub> (d) 10.0-SiO<sub>2</sub> SPEs.

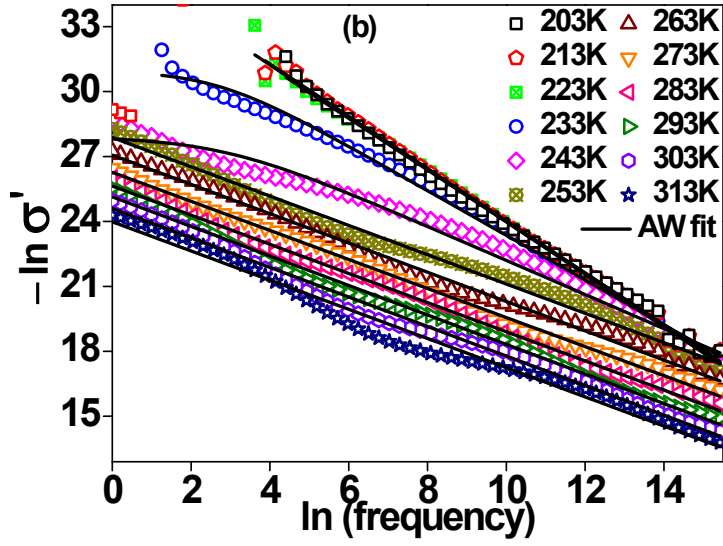
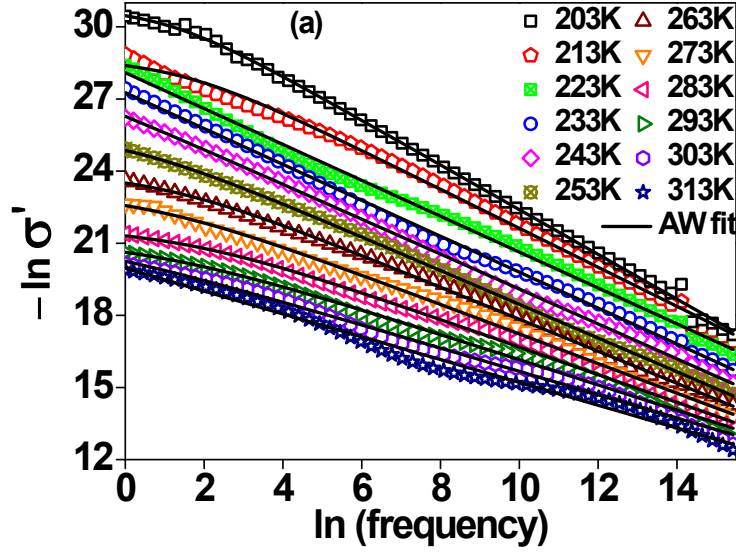


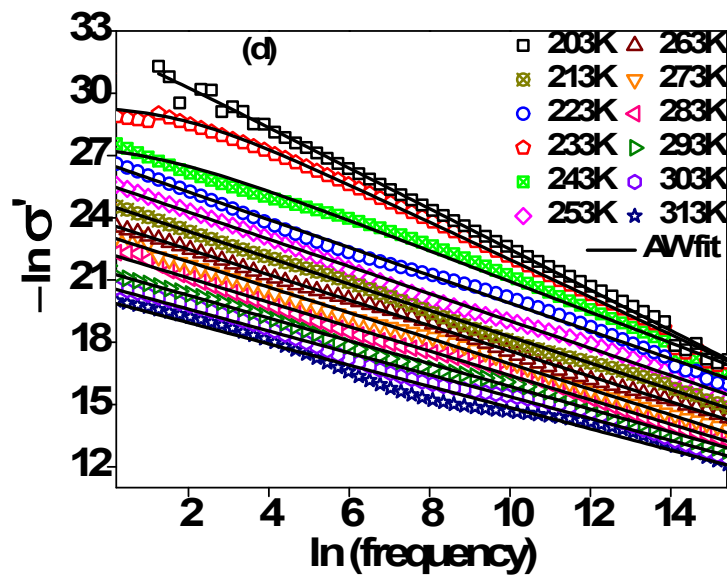
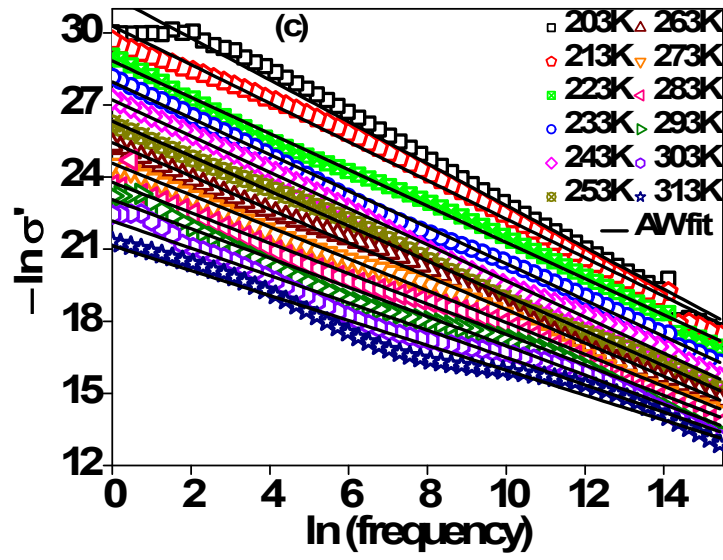


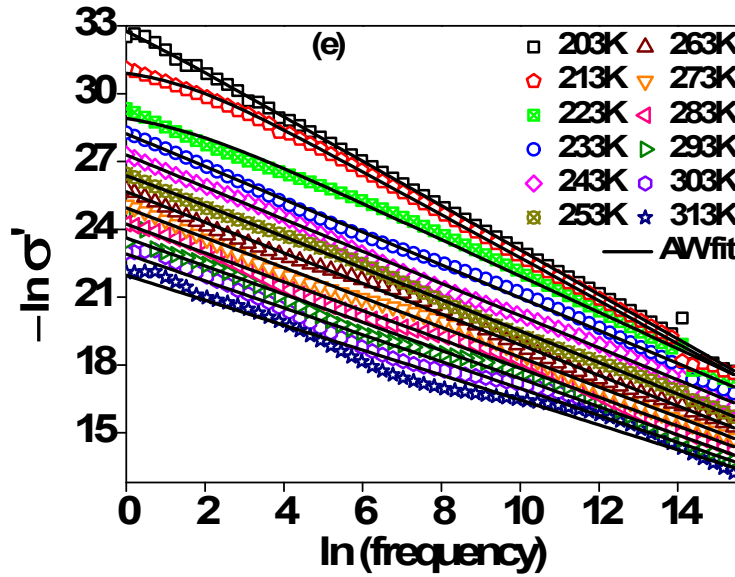




**Figure S8:**  $\epsilon''_{\text{der}}$  curves of (a) 0.0-SiO<sub>2</sub> (b) 0.5-SiO<sub>2</sub> (c) 2.0-SiO<sub>2</sub> (d) 5.0-SiO<sub>2</sub> (e) 10.0-SiO<sub>2</sub> SPEs.







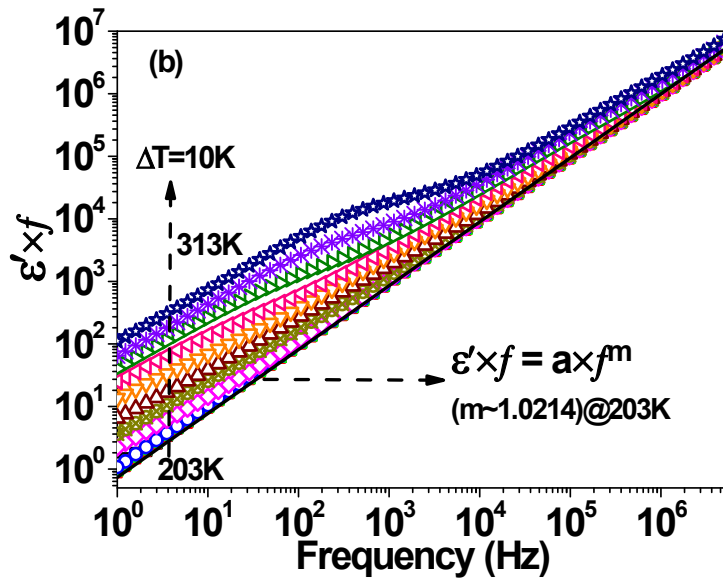
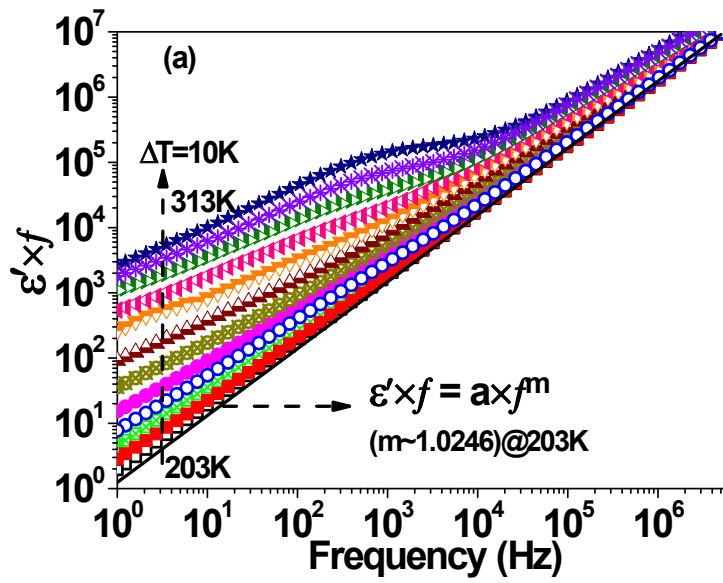
**Figure S9:** Negative log-log plot of ac conductivity ( $\sigma'$ ) for (a) 0.0-SiO<sub>2</sub> (b) 0.5-SiO<sub>2</sub> (c) 2.0-SiO<sub>2</sub> (d) 5.0-SiO<sub>2</sub> (e) 10.0-SiO<sub>2</sub> SPEs. Solid line shows fit using Almond-West (AW) formalism.

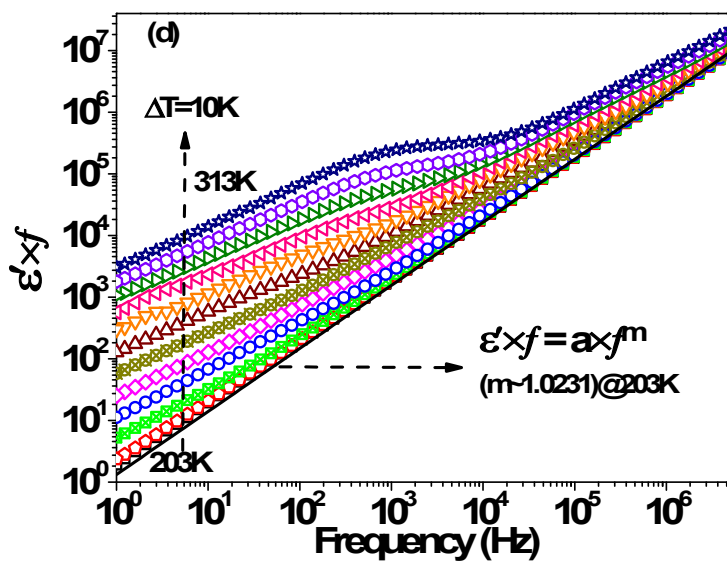
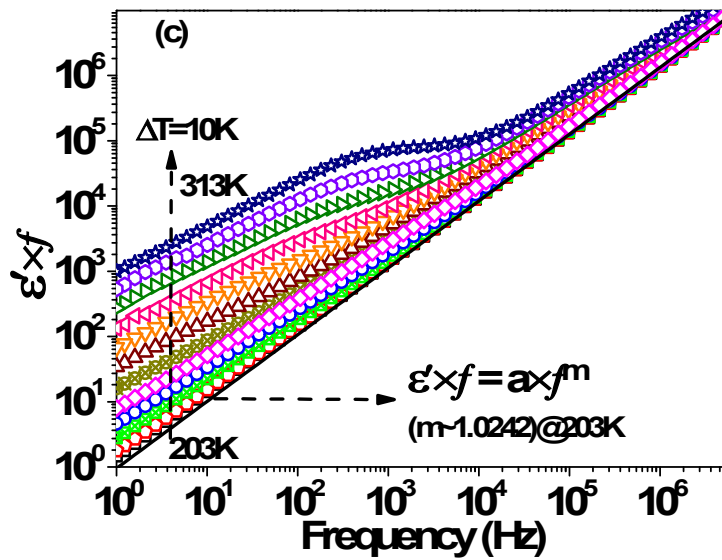
### Kramer-Krönig approach [S1]:

The mathematical expression for Kramer-Krönig approach is given by eq. S1.

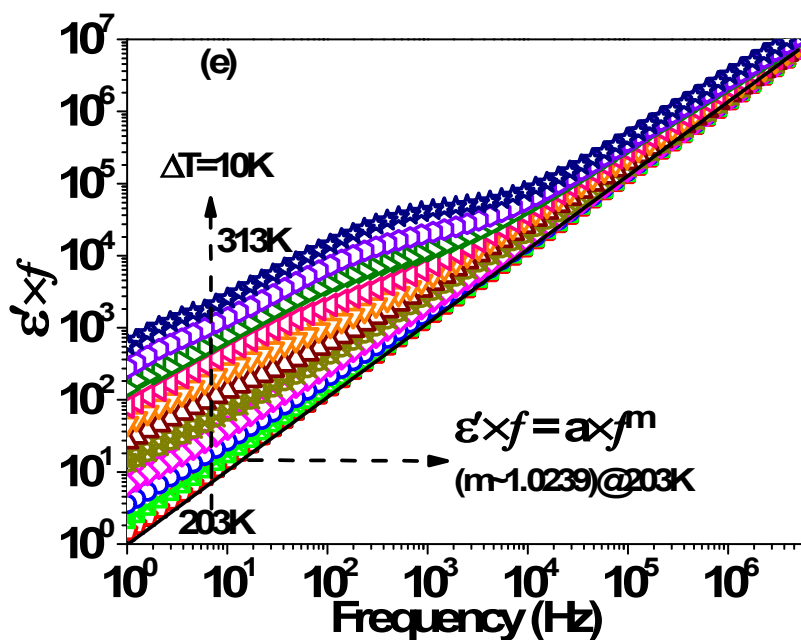
$$\varepsilon'f = af^m \text{ (S1)}$$

The exponent 'm' is weak temperature dependent parameter. Nearly unity value of the exponent shows NCL behaviour and fractional values shows dominance of UDR. Figure S8 shows the variation of ( $\varepsilon'f$ ) with frequency. Fitting the spectra as per eq.S1 results in approximate unity values in and around lower temperatures ~203 K showing the dominance of NCL in low temperature range. The exponent 'm' decreases with increasing temperature indicating the dominance of UDR in high temperature range. It may also be noted that 'm' values is almost similar for different silica loading showing that it is only temperature dependent irrespective of the filler concentration. Considering the frequency dependence, the linear region showing NCL extends over entire frequency region at lower temperature while this linear region shifts to higher frequencies on increasing temperature.

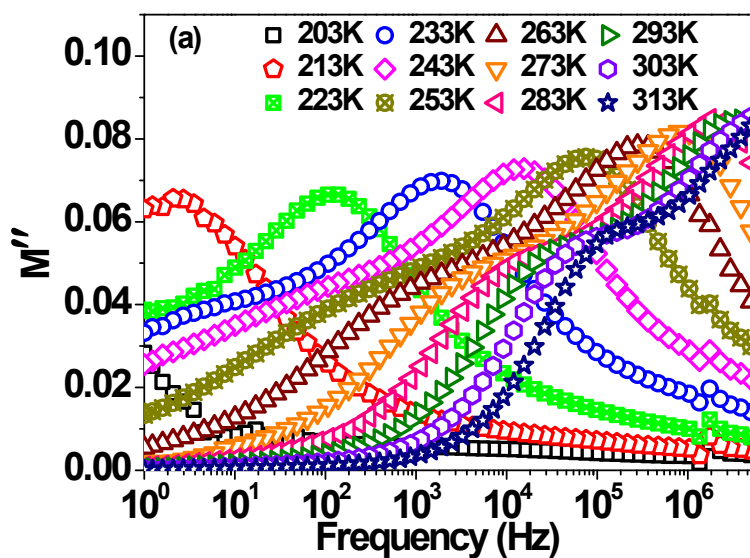


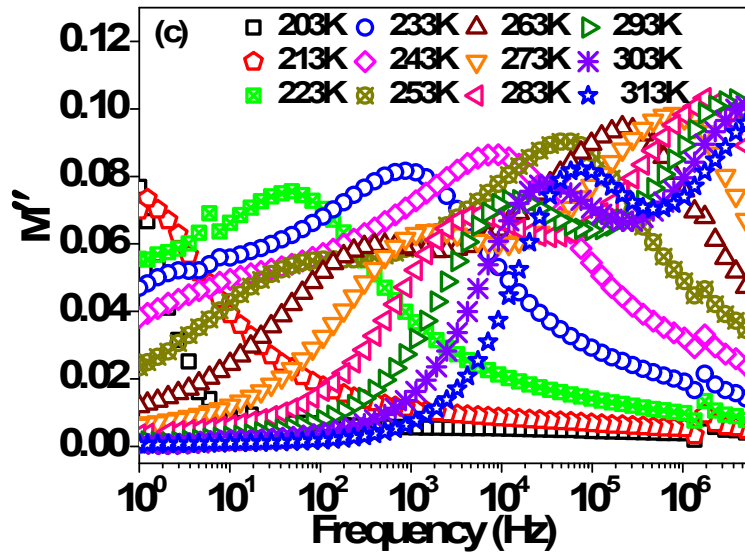
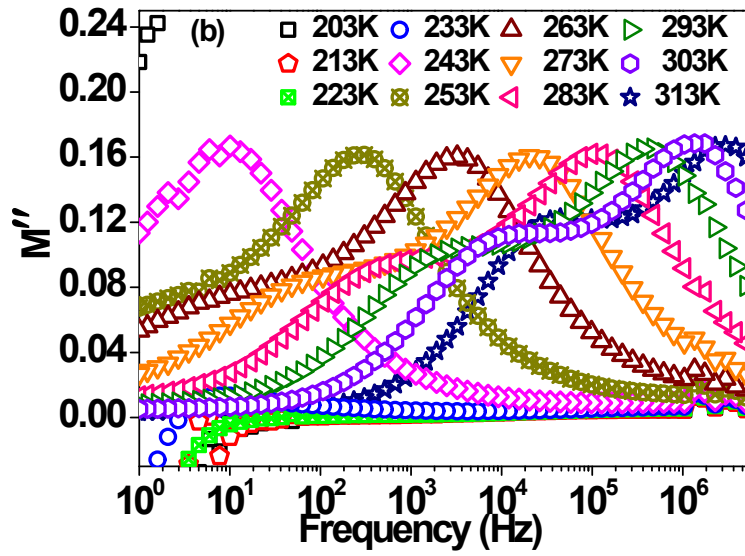


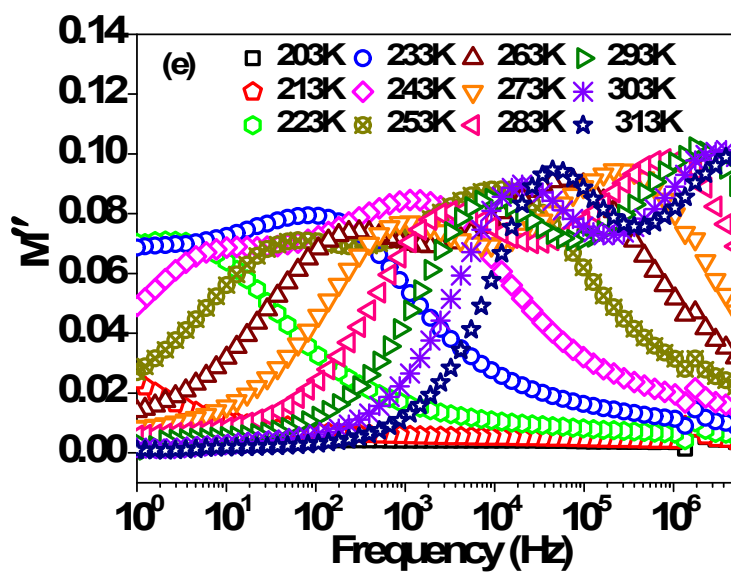
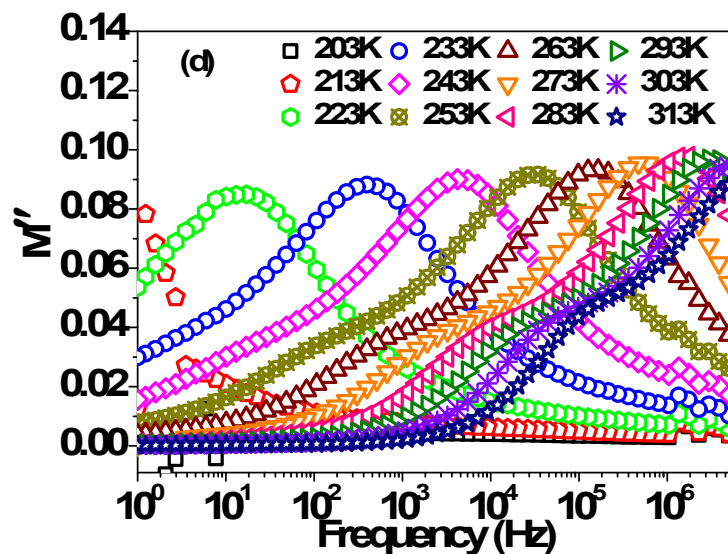




**Figure S10:** Kramer-Krönig formalism applied to (a) 0.0-SiO<sub>2</sub> (b) 0.5-SiO<sub>2</sub> (c) 2.0-SiO<sub>2</sub> (d) 5.0-SiO<sub>2</sub> (e) 10.0-SiO<sub>2</sub> SPEs.







**Figure S11:** Imaginary part of the Modulus,  $M''(f)$  of (a) 0.0-SiO<sub>2</sub> (b) 0.5-SiO<sub>2</sub> (c) 2.0-SiO<sub>2</sub> (d) 5.0-SiO<sub>2</sub> (e) 10.0-SiO<sub>2</sub> SPEs.

## REFERENCES

S1. T. Dam, S. S. Jena and D. K. Pradhan, *Phys. Chem. Chem. Phys.*, 2016, **18**, 19955-19965.