

# Explanation of the Conductivity Difference of Half-Heusler Transparent Conductors by Ionization Energy

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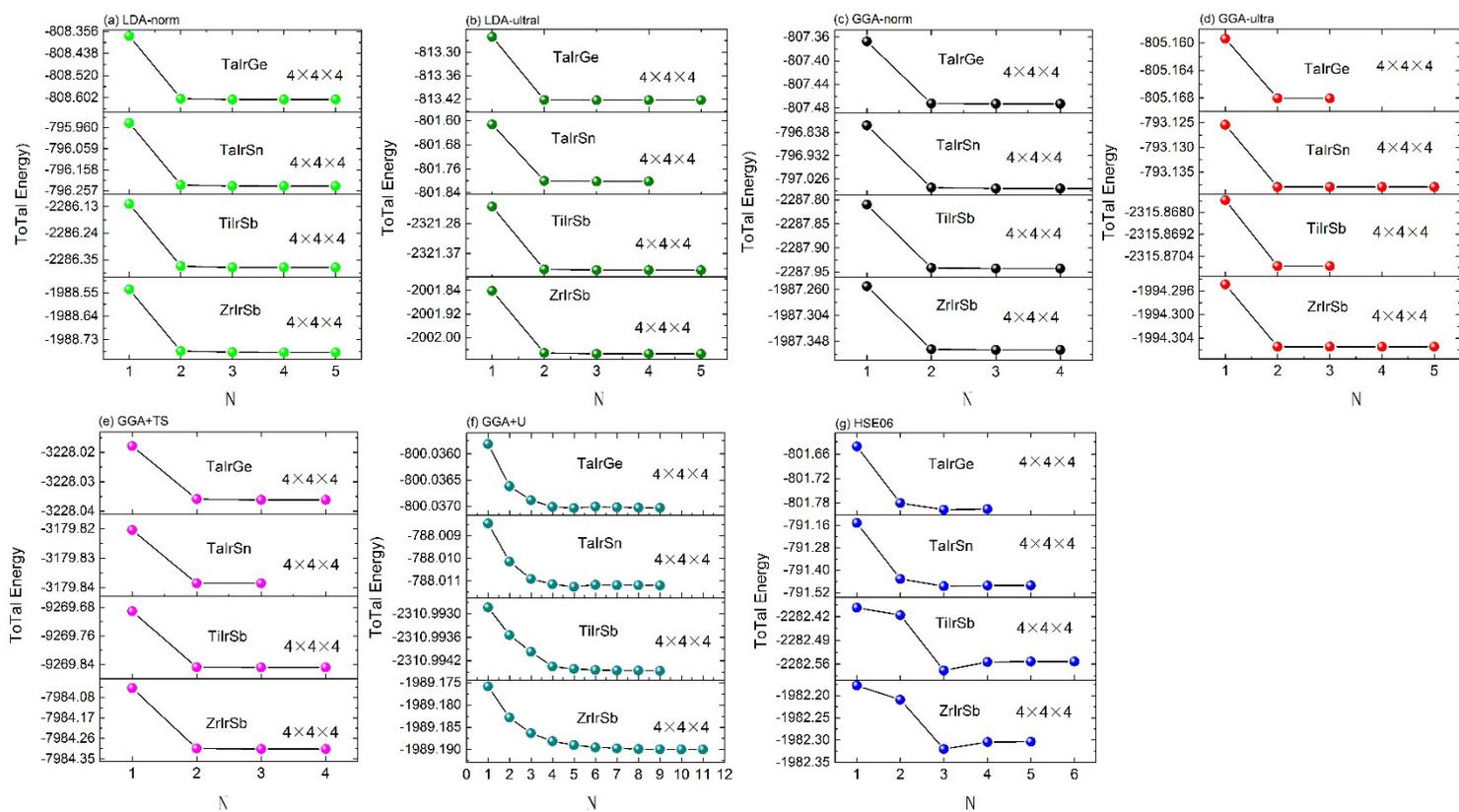
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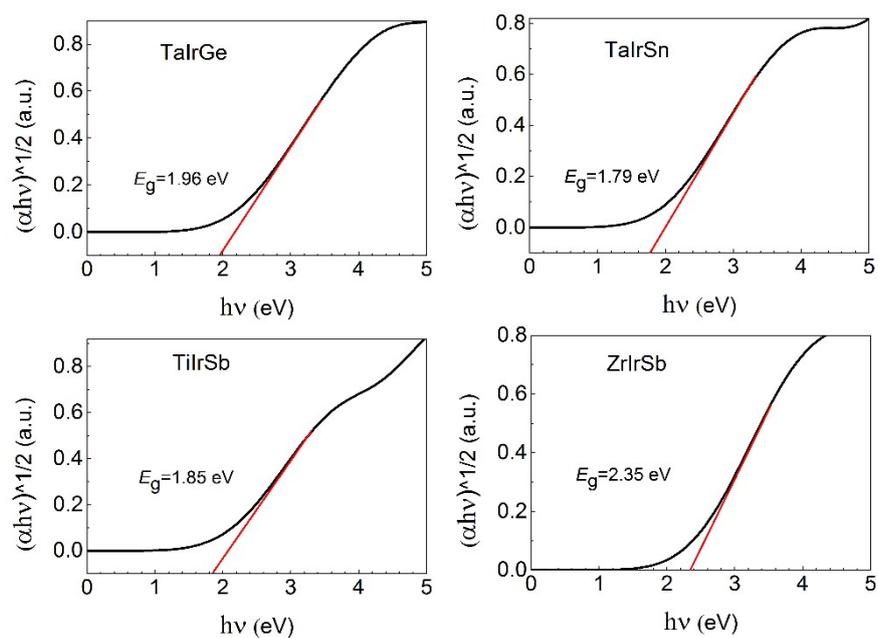
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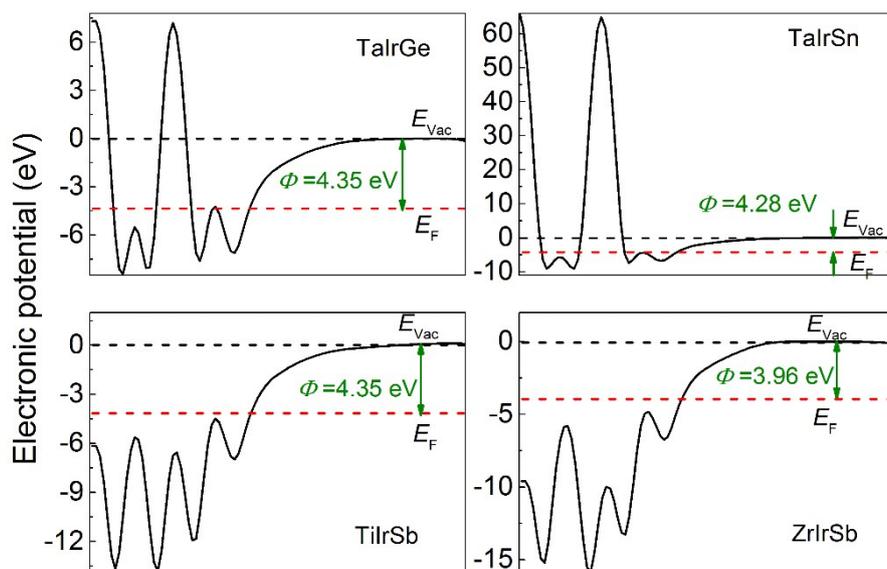
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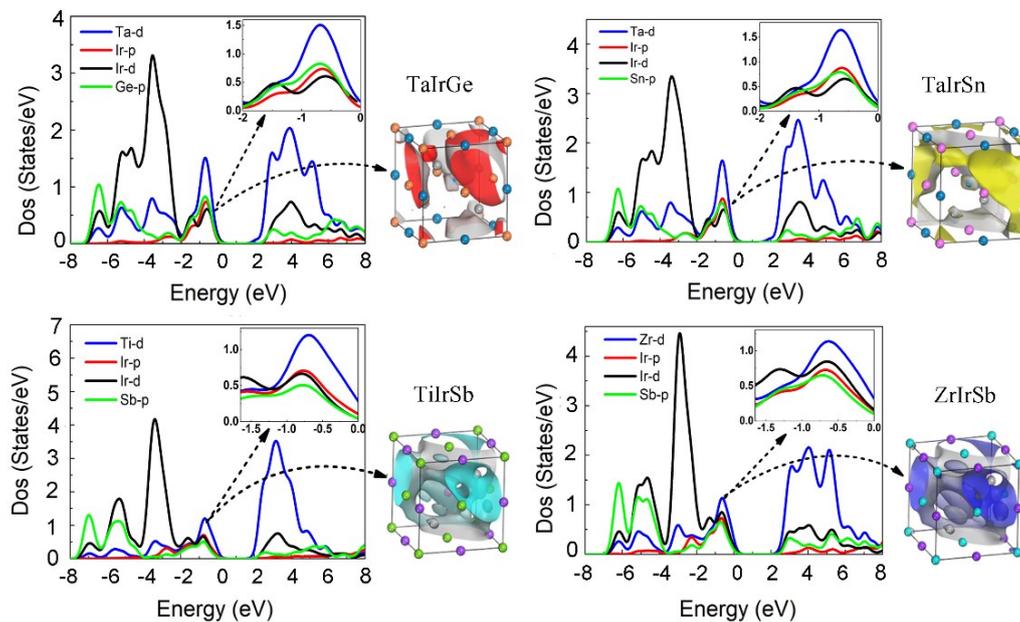
**Figure S1.** Calculated total energy as a function of N for ABX compounds with LDA, GGA, GGA+TS, GGA+U and HSE06 functional for testing the convergence of the k-point mesh.



**Figure S2.** The determination of indirect band gaps of ABX compounds (HSE06).



**Figure S3.** Calculated electrostatic potentials ABX system with slab with a width of 7 layers.



**Figure S4.** Partial density of states (PDOS) of TaIrGe, TaIrSn, TiIrSb, and ZrIrSb within HSE06. The corresponding modulus of the crystalline orbital near the valence band edge, and isovalue of  $5 \times 10^{-2}$  a.u is adopted

Table S1 The calculated lattice constants of TaIrGe, TaIrSn, TiIrSb and ZrIrSb along with the previous reported values.

	$a$ (LDA-ultra)	$a$ (LDA-norm)	$a$ (GGA-ultra)	$a$ (GGA-norm)	$a$ (GGA+TS)	$a$ (GGA+U)	$a$ (HSE06)	Ref. [9]
TaIrGe	5.893	5.861	6.059	5.914	6.002	6.039	5.852	6.026
	-2.21%	-2.74%	0.55%	-1.86%	-0.40%	0.22%	-2.89%	
TaIrSn	6.085	6.043	6.273	6.054	6.206	6.253	5.997	6.233
	-2.37%	-3.05%	0.64%	-2.87%	-0.43%	0.32%	-3.79%	
TiIrSb	6.010	5.980	6.148	6.032	6.093	6.159	5.881	6.169
	-2.58%	-3.06%	-0.34%	-2.22%	-1.23%	-0.16%	-4.67%	
ZrIrSb	6.200	6.189	6.334	6.246	6.275	6.327	6.106	6.372
	-2.70%	-2.87%	-0.60%	-1.98%	-1.52%	-0.71%	-4.17%	

Table S2 The calculated band gaps using different functional along with the previously experimental and theoretical results.

$E_g(E_g^{dir})$	GGA	GGA+TS	GGA+U	HSE06	Exp. <sup>[9, 18]</sup>	HSE06 <sup>[9]</sup>	HSE06 <sup>[18]</sup>
TaIrGe	1.20	1.19	1.62 (2.68)	1.84 (3.19)	3.36 <sup>[18]</sup>	1.62 (2.49)	1.74 (3.1)
TaIrSn	1.16	1.16	1.54 (2.24)	1.75 (2.77)	2.4 <sup>[9]</sup>	1.55 (2.26)	1.61 (2.33)
TiIrSb	0.98	1.01	1.41 (2.16)	1.81 (2.64)	2.4 <sup>[9]</sup>	1.63 (2.39)	1.69 (2.51)
ZrIrSb	1.61	1.65	1.82 (2.43)	2.22 (3.12)	3.2 <sup>[9]</sup>	1.91 (2.25)	2.06 (2.38)

**Table S3.** The effective masses of holes at VBM, Sub-VBM (sub-maximum of valence bands), and CBM.

System	VBM-L	VBM-R	Sub-VBM-L	Sub-VBM-R	CBM-L	CBM-R
TaIrGe	0.78	0.83	0.41	0.92	0.51	0.36
TaIrSn	0.76	0.92	0.41	1.04	0.57	0.43
TiIrSb	2.23	0.72	5.85	1.01	0.81	0.67
ZrIrSb	2.21	0.65	2.62	0.90	0.75	0.46

