# Infrequent Metadynamics Study of Rareevent Electrostatic Channeling 

Yan Xie, Scott Calabrese Barton
Department of Chemical Engineering and Materials Science, Michigan State University, East Lansing, MI, 48824, USA. E-mail: scb@msu.edu

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## S1 Definition of Infrequent Metadynamics Basins

In the committor analysis of infrequent metadynamics, we defined 19 possible triple association basins, besides $d_{246}$, based on the assumption that the nearby index difference of the three indexes of $d_{i j k}$ should not be greater than 2 . For instance, $d_{123}, d_{124}, d_{135}$ and $d_{134}$ are possible, but not $d_{125}$ or $d_{145}$. Therefore, these basins below are all assumed to be possible triple association basins: $d_{123}, d_{124}, d_{134}, d_{135}, d_{234}, d_{235}, d_{245}, d_{246}, d_{345}, d_{346}, d_{356}, d_{357}, d_{456}$, $d_{457}, d_{467}, d_{468}, d_{567}, d_{568}, d_{578}$, and $d_{678}$.


Fig. S1 Schematic of the KMC model.


Fig. S2 Association state probability of G6P on the poly-lysine bridge.


Fig. S3 Electrostatic energy between G6P and the poly-arginine bridge.


Fig. S4 (a) Example biased distribution of $x_{1}$ of all the US windows at $I S=0 \mathrm{mM}$, temperature 300 K . (b) Example 2D energy plot of G6P desorption energy from the triple association on the poly-arginine peptide. Data above the yellow cutoff line was used for calculation of the PMF. (c) The projection of desorption energy on $x_{1}$ at $I S=0 \mathrm{mM}$, temperature 300 K .


Fig. S5 Product concentration versus time at IS $=120 \mathrm{mM}$ in the KMC model.


Fig. S6 Probability distribution of the number of adsorbed intermediates on the poly-lysine bridge and polyarginine bridge.

Table S1. Energy barriers and rate constants

| IS | $G_{\text {hop }}$ | $\Delta G_{\text {des }}$ | $\Delta G$ | $\frac{k_{\text {hop }}}{k_{\text {des }}}$ | $\frac{k_{\text {ads }}}{k_{\text {des }}} \times 10^{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| mM | $\mathrm{kJ} / \mathrm{mol}$ | $\mathrm{kJ} / \mathrm{mol}$ | $\mathrm{kJ} / \mathrm{mol}$ |  |  |
| 0 | 25.1 | 47.4 | 22.3 | 7515 | 179 |
| 20 | 25.1 | 45.6 | 20.5 | 3652 | 87 |
| 40 | 25.1 | 42.6 | 17.5 | 1096 | 26 |
| 70 | 25.1 | 41.2 | 16.1 | 625 | 15 |
| 120 | 25.1 | 36.7 | 11.6 | 103 | 2.5 |

IS: ionic strength
$G_{\text {hop }}, k_{\text {hop }}$ : energy barrier and rate constant of hopping on the bridge from one triple association to an adjacent triple association
$\Delta G_{d e s}, k_{d e s}$ : energy barrier and rate constant of desorption from triple association $\Delta G$ : the energy difference between hopping and desorption $\Delta G=G_{d e s}-G_{h o p}$

Table S2. KMC parameters

| Region | Parameter | Value |
| :---: | :---: | :---: |
| System | $c_{H K-G 6 P D H}$, cascade concentration, $\mathrm{mol} \mathrm{L}^{-1}$ | $8 \times 10^{-9}$ |
|  | Vol, reaction volume, L | $2.1 \times 10^{-14}$ |
|  | $c_{\text {sub }}$, substrate concentration for $\mathrm{HK}, \mathrm{mol} \mathrm{L}^{-1}$ | 2 |
| HK | $k_{c a t}^{H K}$, TOF of HK, molec s ${ }^{-1}$ | 0.7 |
|  | $k_{\text {des }}^{H K}$, desorption rate on $\mathrm{HK}, \mathrm{s}^{-1}$ | 0.07 |
|  | $k_{\text {ads }}^{H K}$, absorption rate on $\mathrm{HK}, \mathrm{s}^{-1}$ | $7.7 \times 10^{4}$ |
|  | $k_{\text {hop }}^{1 b}$, hopping rate from HK to bridge, $\mathrm{s}^{-1}$ | $k_{\text {hop }}$ |
|  | $K_{M, 1}^{H K}$, Michaelis constant of HK, mM | $10^{-5}$ |
| Bridge | $k_{\text {hop }}$, hopping rate on bridge, $\mathrm{s}^{-1}$ | $k_{c a t}^{H K} \times 100=70$ |
|  | $k_{\text {des }}$, desorption rate on bridge, $\mathrm{s}^{-1}$ | $\frac{k_{\text {hop }}}{k_{\text {hop }} / k_{\text {des }}}$ |
|  | $k_{\text {ads }}$, adsorption rate on bridge, $\mathrm{s}^{-1} \mathrm{~mol}^{-1} \mathrm{~L}$ | $k_{\text {des }} \times\left(k_{\text {hop }} / k_{\text {des }}\right)$ |
| G6PDH | $k_{\text {hop }}^{b 2}$, hopping rate from bridge to G6PDH, $\mathrm{s}^{-1}$ | $k_{\text {hop }}$ |
|  | $k_{\text {cat }}^{\mathrm{G} 6 \mathrm{PDH}}$, TOF of G6PDH, molec s ${ }^{-1}$ | 6.2 |
|  | $k_{\text {des }}^{\mathrm{G6PDH}}$, desorption rate on G6PDH, $\mathrm{s}^{-1}$ | 0.62 |
|  | $k_{\text {ads }}^{\mathrm{G} 6 \mathrm{PDH}}$, absorption rate on G6PDH, $\mathrm{s}^{-1}$ | $1.3 \times 10^{6}$ |
|  | $K_{M, 2}$, Michaelis constant of G6PDH, mM | $5.4 \times 10^{-6}$ |

* The value of $k_{\text {hop }} / k_{\text {des }}$ is from Table S1.

