ReaxFF-MPNN Machine Learning Potential: A Combination of

Reactive Force Field and Message Passing Neural Networks

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-Supporting Information-

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1. Energy terms used in ReaxFF-MPNN

We use bond energy, three-body bond angle energy, four-body torsion energy, and long-range energy such as H-bond energy, van der Waals energy, and Coulomb energy. The over/under coordinate and lone pair energy terms are not used in the ReaxFF-MPNN as shown in (s1).

$$E_{total} = E_{bond} + E_{val} + E_{pen} + E_{coa} + E_{tors} + E_{conj} + E_{H-bond} + E_{vdWaals} + E_{od}$$
(s1)

2. Bond energy in ReaxFF-MPNN

We have considered two forms of bond energy formula and the two kinds of bond energy in ReaxFF-MPNN are expressed by formula (s2) and (s3).

$$E^{bond}_{ij} = -D^{\sigma}_{e} \cdot f^{E_{bond}}_{NN} \left(BO^{\sigma}_{ij}, BO^{\pi}_{ij}, BO^{\pi\pi}_{ij} \right) \cdot BO_{ij}$$
(s2)

$$E^{bond}_{ij} = -D^{\sigma}_{e} \cdot f^{E_{bond}}_{NN} (\Delta_{i} - BO_{ij}, \Delta_{j} - BO_{ij}, BO_{ij}) \cdot BO_{ij}$$
(s3)

Where D_e^{σ} is adjusting parameters, and $f_{NN}^{E_{bond}}$ is a neural network. Typically, a neural network function can be expressed by (s4).

$$f_{NN}(X) = \sigma(W \cdot \cdots \sigma(W \cdot \sigma(W \cdot X + b) + b) + \cdots + b)$$
(s4)

 σ represents the activation function, and in this work, we use the sigmoid activation function as in formula (s5).

$$\sigma(X) = \frac{1}{1 + e^{-X}} \tag{s5}$$

The X represents the input vector, W and b represent the *weight* and *bias* of the neural network.

3. Bond order in *ReaxFF-MPNN*

The initial bond order is $BO^{t=0}(BO^{t=0}_{\sigma} + BO^{t=0}_{\pi} + BO^{t=0}_{\pi\pi})$ which is computed from ReaxFF uncorrected bond order $BO'(BO'_{\sigma} + BO'_{\pi} + BO'_{\pi\pi})$ with neural network functions.

$$BO_{\sigma}^{t=0} = f_{NN}^{\sigma} (BO_{\sigma}')$$
(s6)

$$BO_{\pi}^{t=0} = f_{NN}^{\pi} (BO_{\pi})$$
(s7)

$$BO_{\pi\pi}^{t=0} = f_{NN}^{\pi\pi} (BO_{\pi\pi})$$
(s8)

We use $BO^{t=1}(BO^{t=1}_{\sigma} + BO^{t=1}_{\pi} + BO^{t=1}_{\pi\pi})$ as the final bond state, the $BO^{t=1}$ is computed by formula (s9).

$$BO_{ij}^{t=1} = f_{NN}^{message} \left(\Delta_{i}^{t=0} - BO_{ij}^{t=0}, \Delta_{i}^{t=0} - BO_{ij}^{t=0}, BO_{ij}^{t=0} \right) \odot BO^{t=0}$$
(s9)

where \bigcirc denote the element multiplication, and \triangle is calculated by the formula (s10).

$$\Delta_i = \sum_{j \in N_i} BO_{ij} \tag{s10}$$

4. The bond energy curve of the NN bond of structure $NO_2N(CH_3)_2$ and $NO_2NCH_3CH_2$ NH₂ from DFT calculations



Figure s1. The structure of (a) NO₂N(CH₃)₂ and (b) NO₂NCH₃CH₂ NH₂.



Figure s2. The bond energy versus distance between N_1 - N_2 of the structure of $NO_2N(CH_3)_2$ and $NO_2NCH_3CH_2NH_2$ calculated by SIESTA with PBE functional and double- ζ polarize basis set as shown in Figure s1(a) and Figure s2(b), respectively.

5. A neural network taper function for vdW interaction

ReaxFF uses a distance-corrected Morse-potential and a shielded interaction to provide nuclear repulsion. A 7th order polynomial taper correction function developed by de Vos Burchart is employed to avoid energy discontinuities. We have tested a new neural network taper function instead of the polynomial taper function with parameter adjustable (the new VDW function is given in formula s11). The comparison of neural network taper function and polynomial taper function is provided in Figure s3.

$$E_{vdWaals} = f_{NN}^{Taper} \cdot D_{ij} \cdot \left\{ exp \left[\alpha_{ij} \cdot \left(1 - f_{13} \frac{(r_{ij})}{r_{vdW}} \right) \right] - 2 \cdot exp \left[\frac{1}{2} \cdot \alpha_{ij} \cdot \left(1 - f_{13} \frac{(r_{ij})}{r_{vdW}} \right) \right] \right\}$$
(s11)



Figure s3. The plot of the ReaxFF taper function developed by Burchart et. al. (blue circle) and the neural network taper function (red square error bar).