## Supporting information for "The Dirac half-semimetal and quantum anomalous Hall effect in two-dimensional Janus $Mn_2X_3Y_3$ (X, Y = F, Cl, Br, I)"

Ping Li<sup>1,2,\*</sup> and Zhi-Xin Guo<sup>1,†</sup>

<sup>1</sup>State Key Laboratory for Mechanical Behavior of Materials,

Center for Spintronics and Quantum System, School of Materials Science and Engineering,

Xi'an Jiaotong University, Xi'an, Shaanxi, 710049, China

<sup>2</sup>Key Laboratory for Computational Physical Sciences (Ministry of Eduction), Fudan University, Shanghai, 200433, China

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- 5. Figure S4 the energy and k contribution of  $Mn_2Cl_3Br_3$  to the spin up bands.

<sup>\*</sup> pli@xjtu.edu.cn

<sup>†</sup> zxguo08@xjtu.edu.cn

TABLE S1. Different magnetic configuration of the total energy E (meV/cell) (relative to the FM state).

	$\mathbf{FM}$	AFM-N	AFM-ZZ	AFM-C-I	AFM-C-II	AFM-C-III
$Mn_2F_3Cl_3$	0.00	295.68	340.53	381.75	521.53	428.99
$\mathrm{Mn_2F_3Br_3}$	0.00	314.88	428.90	572.70	428.94	610.94
$\mathrm{Mn_2F_3I_3}$	0.00	335.04	221.51	216.81	192.54	257.94
$\mathrm{Mn_2Cl_3Br_3}$	0.00	446.40	257.06	446.08	389.98	397.44
${\rm Mn_2Cl_3I_3}$	0.00	456.00	270.80	299.35	261.60	345.70
$Mn_2Br_3I_3 \\$	0.00	463.68	224.51	366.95	324.76	329.23



FIG. S1. Total energy fluctuations of the Mn<sub>2</sub>X<sub>3</sub>Y<sub>3</sub> monolayer during 3 ps MD simulation at 300 K.



FIG. S2. Phonon dispersion curves of the Mn<sub>2</sub>Cl<sub>3</sub>Br<sub>3</sub>.



FIG. S3. The calculated spin-polarized band structures of  $Mn_2F_3Br_3$ ,  $Mn_2F_3I_3$ , and  $Mn_2Cl_3I_3$ . Spin up and spin down bands are plotted as magenta and blue curves, respectively.



FIG. S4. Energy and k contribution of  $Mn_2Cl_3Br_3$  for Cl p-resolved, Br p-resolved and Mn d-resolved to the spin up bands.