Supporting Material

Dynamics of nuclear recoil: QM-BOMD simulations of model systems following β -decay

Rasmus Fromsejer,^a Kurt V. Mikkelsen^a and Lars Hemmingsen^a

^aDepartment of Chemistry, University of Copenhagen, Universitetsparken 5, 2100 København Ø, Denmark. E-mail: rf@chem.ku.dk, kmi@chem.ku.dk, lhe@chem.ku.dk



Figure S1: Decay scheme of ¹¹¹Ag. The dark blue arrows indicate the decay pathway used in ¹¹¹Ag γ - γ perturbed angular correlation spectroscopy. The nuclear spin, energy and half-life of relevant energy levels and percentage probability of relevant pathways is shown.



Figure S2: Trajectory of the ratio of the total energy E relative to the start energy E_0 for the PBE0-D3-MD and PM7-MD simulations. $E_{rec} = 500 \text{ kJ/mol}, \Delta t = 0.5 \text{ fs}, E_{therm} = 0.$



Figure S3: Comparison of power spectral data as function of wavenumber for the Cd-S4 bond from the PBE0-D3-MD and PM7-MD simulations of model 1: (A) $E_{rec} = 0 \text{ kJ/mol trajectories}$, (B) $E_{rec} = 500 \text{ kJ/mol trajectories}$. $\Delta t = 0.5 \text{ fs}$, $E_{therm} = 0 \text{ kJ/mol}$.



Figure S4: PM7 optimized structure of acetone-model 1 interaction.

Method	r(Cd-O)
PM7	2.33
PM6	3.34
PBE0-D3	2.53
CAM-B3LYP	2.50
$\omega B97 XD$	2.51
M062X	2.46

Table S4: Cadmium-carbonyl oxygen bond-lengths (in Ångström) in optimized structures of acetone-model 1 interaction. The def2-TZVP basis-set was used for the DFT calculations.



Figure S5: Model 2 structure with additional water acting as hydrogen bond donor. Hydrogen bond distance 1.75 Å.



Figure S6: PM7-MD trajectories of selected inter-atomic distances in model 2 with additional water acting as hydrogen bond donor (non-frozen) (fig. S4). Recoil perpendicular to S-Cd-S plane, $E_{rec} = 500 \text{ kJ/mol}$. $E_{therm} = 0$, $\Delta t = 0.5 \text{ fs}$.



Figure S7: PM7-MD trajectories of selected inter-atomic distances in model 2 (frozen). $E_{rec} = 0 \text{ kJ/mol}, E_{therm} = 0, \Delta t = 0.5 \text{ fs.}$



Figure S8: PM7-MD trajectories of selected inter-atomic distances in model 3 (non-frozen) with ¹¹¹Ag(I) occupying metal-site. $E_{rec} = 0 \text{ kJ/mol}, E_{therm} = 0, \Delta t = 0.5 \text{ fs}.$



Figure S9: PM7-MD trajectories of selected inter-atomic distances in model 3 (frozen). $E_{rec} = 0 \text{ kJ/mol}, E_{therm} = 0, \Delta t = 0.5 \text{ fs.}$



Figure S10: PM7-MD trajectories of selected inter-atomic distances in model 3 (non-frozen). $E_{rec} = 0 \text{ kJ/mol}, E_{therm} = 0, \Delta t = 0.5 \text{ fs.}$

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Model 1 Cartesian coordinates in Bohr optimized with PBE0
C 139.269436 39.71156743 152.2386652
S 142.0145635 41.52114447 151.2296157
C 149.3805925 36.2529399 145.9639661
S 146.1495428 36.77231408 144.9059463
Cd(Iso=111) 144.1057683 39.03239424 148.1690571
H 138.0676421 40.93262521 153.3974149
H 138.1475907 39.05409774 150.6364515
H 150.4821762 35.51933693 144.3745308
H 150.2737829 38.000447 146.6013593
H 149.4916858 34.87337568 147.4976337
H 139.7883037 38.07060875 153.381305

11

Model 1 Cartesian coordinates in Bohr optimized with PM7 C 139.6919466 39.01566071 151.5537566 S 142.2281479 41.33473245 151.2810692 C 150.0355508 35.92047852 145.8093676 S 147.3366441 37.5605717 144.4514105 Cd(Iso=111) 144.9278104 39.62377454 147.8396892 H 137.8982187 40.0599233 151.3799019 H 139.6966709 37.60913766 150.0177874 H 150.7959765 34.6309295 144.3336806 H 151.558292 37.27881356 146.2296426 H 149.4916876 34.87338135 147.4976488 H 139.7883226 38.07060875 153.3813107

125

Model 2 Cartesian coordinates in Bohr partially optimized with PM7 N 137.4147947 36.2608314 154.4250914 C 139.7781956 37.65588381 154.1499926 C 140.2325197 39.74853236 156.0819256 D 138.4961186 41.1261067 156.7735445 C 139.6919674 39.01575331 151.5537377 S 142.228146 41.33473812 151.2811164 N 142.6062669 39.99792328 156.9738744 C 143.4018472 41.90844948 158.81823 C 144.5526904 44.23092272 157.5067601 0 143.3886191 45.35908913 155.8400218 C 145.3369247 40.48737553 160.3942614 C 146.6786302 38.99449389 158.4157183 C 144.5186734 37.97593159 156.7981129 N 151.722409 33.49524765 149.312587 C 149.3646697 34.38026113 148.1811305 C 147.6447602 32.20243129 147.394859 0 148.178997 30.86687312 145.5636031 C 150.0354676 35.92039915 145.8094545 S 147.3366933 37.56056981 144.4514388 N 145.5447889 31.8211016 148.7781082 C 143.7098726 29.81042559 148.2471028 C 142.4664329 30.11845092 145.6695165 0 141.6765274 28.27407836 144.4903275 C 141.7842418 30.09577421 150.3862726 C 143.3281479 31.13701323 152.4989862 C 144.9306337 33.09476936 151.1761781 N 142.2850192 32.46738033 144.8059136 C 141.0888226 33.01540086 142.3851746 C 142.5609192 31.91935979 140.1609672 0 141.5366877 30.47938859 138.6472966 C 140.7770178 35.88967409 142.0280164 C 139.3238185 36.98760489 144.2843493 C 139.3616131 36.428246 139.5657035 C 139.1386254 39.85053788 144.307026 N 152.6331568 44.23848162 147.8238042 C 150.0952548 43.58085698 148.67985 C 148.245213 45.79561584 148.6193788 0 146.1230508 45.53483365 147.6990822 C 150.2029692 42.48103645 151.3462534 0 151.5616822 40.18123992 151.3405842 N 146.8260288 47.60786306 141.3722815 C 145.1876364 45.78427748 140.1175035 C 142.4834404 46.00915487 141.1190582 0 140.6541856 45.80317474 139.6866459 C 146.1362788 43.05551315 140.5181254 C 144.3467102 41.19224333 139.2425603 C 148.7856747 42.77205426 139.4390918

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Model 3 in Cartesian coordinates in Bohr partially optimized with PM7 N -23.591339 35.199926 1.241550 C -24.360458 32.595884 0.589595 C -24.400142 32.055422 -2.326253 0 -23.965505 29.916252 -3.259777 C -26.956941 32.206600 1.891616 0 -29.084773 33.591769 1.071475 H -24.880132 36.256283 2.169405 H -23.219063 31.295752 1.706423 H -26.781197 32.493838 3.923071 H -27.459608 30.269631 1.407846 H -29.226502 35.058197 2.131611 N -17.980743 29.075324 -3.972204 C -17.801219 26.516635 -3.163401 C -19.280874 24.991626 -5.109819 0 -18.489079 23.056547 -5.962085 C -18.713956 25.938379 -0.453534 C -18.593014 23.160482 0.421409 C -17.111469 27.387799 1.547686 H -19.263867 30.228057 -3.152063 H -15.811337 26.013968 -3.348594 H -20.671713 26.548760 -0.257003 H -19.481185 21.977513 -1.012893 H -16.712737 22.342230 0.234326 H -19.481185 22.822221 2.248774 H -17.419494 29.394688 1.198086 Н -17.557444 26.794425 3.469537 H -15.119698 27.138355 1.084703 N -21.675157 25.688935 -5.733429 C -23.355123 24.294317 -7.519220 C -22.211839 23.899365 -10.174285 0 -22.315774 21.847122 -11.219303 C -25.959166 25.700273 -7.880157 C -27.722280 24.111014 -9.488314 C -30.570097 24.764859 -9.038559 C -32.476831 23.610237 -10.935844 N -35.084653 24.073219 -10.091137 H -22.521754 26.835999 -4.465423 Н -23.948497 22.523644 -6.651835 H -25.775862 27.601338 -8.653055

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