## Electronic Supplementary Information for

## Development of a Coupled Geophysical-Geothermal Scheme for Quantification of Hydrates in Gas Hydrate-Bearing Permafrost Sediments

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The following data are available at Mendeley Data, <u>https://doi.org/10.17632/2zf6dsxkfw.1</u>:

- 1. Detailed experimental conditions and measured elastic wave velocities and ETC values at different effective overburden pressures (Section 4.1).
- 2. Detailed predicted and experimental saturations of the co-existing phases together with the PT conditions used for testing the performance of the coupled geophysical-geothermal scheme (Section 4.3).

## **Supporting Information**

**Table S1.** ETC and ETC ratio at unfrozen and frozen conditions, predicted to investigate sensitivity of the modified ETC model to the saturation and pore-scale habit of hydrates.

**Table S2.** ETC and elastic wave velocities determined by the rock-physics model (EMT-C) at frozen conditions, predicted to investigate sensitivity of the modified ETC model to the unfrozen water saturation at different hydrates distribution patterns.

**Table S3.** ETC and ETC ratio at unfrozen conditions and frozen conditions, predicted to investigate sensitivity of the modified ETC model to the hydrate-forced heave.

Table S1. ETC and ETC ratio at unfrozen and frozen conditions, predicted to investigate sensitivity of the modified ETC model to the saturation and pore-scale habit of hydrates.

ETC and ETC Ratio at Unfrozen Conditions									
No	σ	S <sub>h</sub>	Sw	Sq	ETC	ETC Ratio			
INO.	(-)	(-)	(-)	(-)̈́	(W/m.K)	(-)			
				4=N/2					
	-	0.00	0.60	0.40	2.319	1.000			
1	1	0.04	0.56	0.40	2.246	0.968			
2	5	0.20	0.40	0.40	2.020	0.871			
3	10	0.39	0.21	0.40	1.918	0.827			
4	15	0.52	0.08	0.40	1.904	0.821			
5	20	0.60	0.00	0.40	1.903	0.821			
				4=N/4					
	-	0.00	0.60	0.40	2.319	1.000			
6	1	0.02	0.58	0.40	2.298	0.991			
7	5	0.10	0.50	0.40	2.225	0.959			
8	10	0.21	0.39	0.40	2.151	0.927			
9	15	0.33	0.27	0.40	2.100	0.905			
10	20	0.51	0.09	0.40	2.074	0.894			
11	25	0.55	0.05	0.40	2.068	0.892			
			/	4=N/6					
	-	0.00	0.60	0.40	2.319	1.000			
12	1	0.01	0.59	0.40	2.311	0.996			
13	5	0.05	0.55	0.40	2.280	0.983			
14	10	0.10	0.50	0.40	2.247	0.969			
15	15	0.16	0.44	0.40	2.221	0.957			
16	20	0.27	0.33	0.40	2.202	0.949			
17	25	0.39	0.21	0.40	2.190	0.944			
18	30	0.41	0.19	0.40	2.184	0.942			
19	35	0.42	0.18	0.40	2.181	0.941			
			/	4=N/8					
	-	0.00	0.60	0.40	2.319	1.000			
20	1	0.01	0.60	0.40	2.316	0.999			
21	5	0.02	0.58	0.40	2.302	0.992			
22	10	0.05	0.55	0.40	2.287	0.986			
23	15	0.08	0.52	0.40	2.273	0.980			
24	20	0.13	0.47	0.40	2.262	0.975			
25	25	0.22	0.38	0.40	2.253	0.971			
26	30	0.28	0.32	0.40	2.247	0.969			
27	35	0.30	0.30	0.40	2.244	0.968			
28	40	0.31	0.29	0.40	2.242	0.967			

ETC and ETC Ratio at Frozen Conditions									
Ne	σ	Sh	Si	Suw	Sa	ETC	ETC Ratio		
INO	(-)	(-)	(-)	(-)	(-)	(W/m.K)	(-)		
A=N/2									
	-	0.00	0.57	0.10	0.33	3.571	1.000		
1	1	0.05	0.52	0.10	0.33	3.179	0.890		
2	5	0.21	0.36	0 10	0.33	2 355	0.659		
3	10	0.38	0.19	0.10	0.33	2 059	0.577		
4	15	0.52	0.05	0.10	0.33	2 022	0.566		
5	20	0.57	0.00	0.10	0.33	2 0 1 9	0.565		
		0.01	0.00	A=N	/4	2.010	0.000		
	-	0.00	0.57	0.10	0.33	3.571	1.000		
6	1	0.03	0.54	0.10	0.33	3.370	0.944		
7	5	0.12	0.45	0.10	0.33	2 887	0.808		
. 8	10	0.24	0.33	0.10	0.33	2 579	0 722		
9	15	0.39	0.18	0.10	0.33	2 401	0.672		
10	20	0.52	0.05	0.10	0.33	2 334	0.654		
11	25	0.54	0.03	0.10	0.33	2 324	0.651		
		0.0.	0.00	A=N	/6	2.02.			
	-	0.00	0.57	0.10	0.33	3.571	1.000		
12	1	0.01	0.56	0.10	0.33	3.473	0.973		
13	5	0.06	0.51	0.10	0.33	3.241	0.908		
14	10	0.12	0.45	0.10	0.33	3.096	0.867		
15	15	0.20	0.37	0.10	0.33	2.992	0.838		
16	20	0.33	0.24	0.10	0.33	2.911	0.815		
17	25	0.42	0.15	0.10	0.33	2.858	0.800		
18	30	0.44	0.14	0.10	0.33	2.834	0.794		
19	35	0.44	0.13	0.10	0.33	2.820	0.790		
				A=N	/8				
	-	0.00	0.57	0.10	0.33	3.571	1.000		
20	1	0.01	0.56	0.10	0.33	3.526	0.987		
21	5	0.04	0.53	0.10	0.33	3.401	0.952		
22	10	0.07	0.50	0.10	0.33	3.320	0.930		
23	15	0.12	0.45	0.10	0.33	3.265	0.914		
24	20	0.19	0.38	0.10	0.33	3.212	0.899		
25	25	0.29	0.28	0.10	0.33	3.164	0.886		
26	30	0.32	0.25	0.10	0.33	3.138	0.879		
27	35	0.33	0.24	0.10	0.33	3.123	0.875		
28	40	0.34	0.23	0.10	0.33	3.113	0.872		

**ETC and ETC Ratio at Frozen Conditions** 

**Table S2.** ETC and elastic wave velocities determined by the rock-physics model (EMT-C) at frozen conditions, predicted to investigate sensitivity of the modified ETC model to the unfrozen water saturation at different hydrates distribution patterns.

ETC											
No.	S <sub>uw</sub> (-)	S <sub>h</sub> (-)	ETC (W/m.K)	No.	S <sub>uw</sub> (-)	S <sub>h</sub> (-)	ETC (W/m.K)	No.	S <sub>uw</sub> (-)	S <sub>h</sub> (-)	ETC (W/m.K)
A=N/8											
1	0.00	0.00	3.929	1	0.03	0.00	3.839	1	0.09	0.00	3.670
2	0.00	0.12	3.567	2	0.03	0.12	3.479	2	0.09	0.12	3.312
3	0.00	0.25	3.495	3	0.03	0.25	3.407	3	0.09	0.25	3.240
4	0.00	0.36	3.426	4	0.03	0.36	3.342	4	0.09	0.36	3.180
	A=N/6										
1	0.00	0.00	3.929	1	0.03	0.00	3.839	1	0.09	0.00	3.670
2	0.00	0.12	3.402	2	0.03	0.12	3.317	2	0.09	0.12	3.153
3	0.00	0.25	3.269	3	0.03	0.25	3.183	3	0.09	0.25	3.016
4	0.00	0.36	3.209	4	0.03	0.36	3.123	4	0.09	0.36	2.955
A=N/4											
1	0.00	0.00	3.929	1	0.03	0.00	3.839	1	0.09	0.00	3.670
2	0.00	0.12	3.154	2	0.03	0.12	3.078	2	0.09	0.12	2.936
3	0.00	0.25	2.789	3	0.03	0.25	2.716	3	0.09	0.25	2.581
4	0.00	0.36	2.672	4	0.03	0.36	2.599	4	0.09	0.36	2.462

Elastic wave velocities									
No	$S_{h}$	VP	VS						
INO.	(-)	(km/s)	(km/s)						
	S <sub>uw</sub> =0.00								
1	0.00	3.94	2.23						
2	0.12	3.94	2.23						
3	0.25	3.94	2.23						
4	0.36	3.94	2.23						
	Su	w=0.03							
1	0.00	3.92	2.21						
2	0.12	3.92	2.21						
3	0.25	3.92	2.21						
4	0.36	3.92	2.21						
	S <sub>uw</sub> =0.09								
1	0.00	3.87	2.19						
2	0.12	3.87	2.19						
3	0.25	3.87	2.19						
4	0.36	3.87	2.19						

**Table S3.** ETC and ETC ratio at unfrozen conditions and frozen conditions, predicted to investigate sensitivity of the modified ETC model to the hydrate-forced heave.

No	р	S <sub>h</sub>	Sw	Sg	ETC	ETC Ratio				
110.	(LL)	(-)	(-)	(-)	(W/m.K)	(-)				
h = 2 LL										
1	48	0.60	0.00	0.40	1.185	0.623				
2	32	0.60	0.00	0.40	1.554	0.817				
3	16	0.60	0.00	0.40	1.830	0.962				
-	0	0.60	0.00	0.40	1.903	1.000				
	h = 4 LL									
4	48	0.60	0.00	0.40	1.001	0.526				
5	32	0.60	0.00	0.40	1.444	0.759				
6	16	0.60	0.00	0.40	1.811	0.952				
-	0	0.60	0.00	0.40	1.903	1.000				
	h = 6 LL									
7	48	0.60	0.00	0.40	0.911	0.479				
8	32	0.60	0.00	0.40	1.384	0.727				
9	16	0.60	0.00	0.40	1.796	0.944				
-	0	0.60	0.00	0.40	1.903	1.000				

ETC and ETC Ratio at Unfrozen Conditions

## **ETC and ETC Ratio at Frozen Conditions**

No	р	Sh	Si	$S_{uw}$	Sg	ETC	ETC Ratio
NO.	(LL)	(-)	(-)	(-)	(-)	(W/m.K)	(-)
h = 2 LL							
1	48	0.10	0.42	0.08	0.40	1.419	0.400
2	32	0.10	0.42	0.08	0.40	2.172	0.612
3	16	0.10	0.42	0.08	0.40	3.245	0.915
-	0	0.10	0.42	0.08	0.40	3.546	1.000
				h = 4	LL		
4	48	0.10	0.42	0.08	0.40	1.128	0.318
5	32	0.10	0.42	0.08	0.40	1.978	0.558
6	16	0.10	0.42	0.08	0.40	3.214	0.906
-	0	0.10	0.42	0.08	0.40	3.546	1.000
				h = 6	LL		
7	48	0.10	0.42	0.08	0.40	1.004	0.283
8	32	0.10	0.42	0.08	0.40	1.888	0.532
9	16	0.10	0.42	0.08	0.40	3.189	0.899
_	0	0.10	0.42	0.08	0.40	3.546	1.000