

**Ground and Excited Electronic Structures of Metal  
Encapsulated Nanocages: The Cases of Endohedral  $M@C_{20}H_{20}$   
( $M = K, Rb, Ca, Sr$ ) and  $M@C_{36}H_{36}$  ( $M = Na, K, Rb$ )**

*Isuru R. Ariyaratna*

**Supporting Information**

Department of Chemistry and Biochemistry, Auburn University,  
Auburn, AL 36849, USA

Current Address: Department of Chemical Engineering, Massachusetts Institute of Technology,  
Cambridge, MA, 02139, USA









									1301.9	1303.6	1298.7	1300.7	1291.9	1294.4
									1305.9	1306.5	1299.4	1301.7	1292.9	1295.4
									1306.1	1307.7	1299.5	1302.4	1293.1	1295.7
									1306.4	1309.6	1301.3	1305.2	1296.5	1300.8
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									1323.0	1329.2	1319.4	1323.0	1318.6	1321.2
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									1331.1	1334.9	1327.9	1331.8	1324.0	1328.0
									1332.8	1337.5	1330.3	1333.6	1328.1	1330.2
									1337.5	1338.4	1332.1	1333.8	1328.7	1331.4
									1337.5	1339.0	1334.0	1336.3	1331.1	1333.6
									1337.7	1340.5	1334.6	1337.4	1331.4	1333.8
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									1367.9	1372.1	1364.3	1366.3	1358.4	1360.2
									1371.0	1373.1	1365.9	1366.6	1359.1	1360.7
									1372.8	1373.4	1365.9	1368.0	1360.0	1361.3
									1373.1	1373.8	1367.2	1368.3	1360.6	1361.3
									1373.7	1375.5	1368.1	1369.3	1361.1	1362.3
									1375.6	1376.0	1369.8	1371.5	1363.2	1364.3
									1377.0	1378.7	1372.0	1372.8	1366.7	1368.8
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									1385.0	1386.2	1378.7	1380.2	1369.7	1373.0
									1385.3	1388.6	1380.5	1383.0	1371.4	1374.4
									1391.9	1393.8	1384.6	1388.2	1374.0	1375.4
									1399.7	1401.2	1387.3	1388.7	1375.3	1377.0
									1401.1	1401.4	1387.4	1388.9	1375.5	1377.6
									1402.3	1407.9	1389.1	1391.2	1378.9	1380.3
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									1411.4	1413.2	1394.6	1397.9	1385.4	1387.0
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									1416.9	1418.2	1400.7	1402.5	1389.6	1391.3
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									1442.0	1449.5	1402.3	1403.7	1394.4	1397.0
									2968.8	3032.9	2993.7	3041.3	3000.4	3044.4
									2971.2	3033.3	2995.3	3041.8	3002.5	3045.0
									2980.0	3046.5	3001.1	3052.0	3004.1	3053.2
									2982.0	3047.4	3002.9	3052.3	3006.7	3054.2
									2985.0	3048.1	3004.5	3054.4	3006.8	3055.3
									2990.1	3051.1	3006.4	3055.2	3009.7	3056.9
									2991.8	3052.5	3007.4	3056.2	3010.8	3057.3
									2992.4	3054.3	3009.3	3057.5	3011.4	3058.1
									2993.9	3056.4	3009.6	3060.0	3012.8	3061.4
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									3007.4	3065.0	3020.4	3068.3	3021.7	3069.3
									3009.4	3067.5	3021.3	3071.0	3023.4	3071.9
									3009.6	3071.2	3023.3	3077.4	3025.5	3078.0
									3011.7	3075.8	3024.3	3080.7	3025.6	3081.0
									3012.1	3077.6	3025.7	3081.2	3031.1	3081.4
									3013.2	3078.5	3026.8	3081.4	3031.4	3081.7
									3016.3	3078.6	3029.2	3082.3	3032.3	3082.7
									3016.5	3079.5	3029.2	3083.0	3036.8	3082.8
									3018.6	3080.9	3030.4	3083.1	3037.6	3084.2
									3019.8	3081.9	3032.0	3085.4	3038.0	3086.1
									3024.7	3083.4	3033.3	3087.3	3038.4	3087.4
									3027.5	3087.5	3038.0	3092.6	3038.9	3093.3
									3028.5	3090.8	3039.2	3094.6	3039.7	3093.8
									3028.6	3090.9	3040.0	3094.7	3039.9	3095.3
									3028.7	3093.1	3040.5	3096.9	3040.8	3098.2
									3042.3	3095.9	3044.6	3098.4	3045.2	3098.6
									3043.5	3097.4	3047.8	3101.2	3045.4	3102.1
									3043.9	3098.6	3048.0	3102.7	3046.7	3103.8
									3044.6	3106.8	3053.7	3109.6	3050.9	3109.2
									3049.8	3108.4	3059.0	3109.8	3057.5	3109.4
									3053.3	3110.5	3059.2	3113.3	3065.3	3112.6
									3053.3	3110.9	3062.0	3115.0	3069.2	3114.1
									3060.8	3137.8	3084.0	3135.3	3090.9	3129.7
									3069.0	3138.9	3086.8	3136.6	3091.1	3131.7

**Table S4.** Vertical electron attachment energies (eV) and pole strengths (in parentheses) of  $\text{K@C}_{20}\text{H}_{20}^+$ , at neutral  $\text{K@C}_{20}\text{H}_{20}$  geometry (optimized at B3LYP/aug-cc-pVTZ level) obtained from diagonal electron propagator methods using cc-pVTZ (K, C) and d-aug-cc-pVTZ (H). All valence electrons are correlated.

Final State ( $I_h$ )	Vertical electron attachment energies and pole strengths			
	KT	D2 (PS)	P3 (PS)	P3+ (PS)
$1^2\text{A}_g$	-1.765	-2.153 (0.985)	-2.115 (0.986)	-2.120 (0.985)
$1^2\text{T}_{1u}$	-1.547	-1.855 (0.988)	-1.831 (0.988)	-1.834 (0.988)
$1^2\text{H}_g$	-1.200	-1.412 (0.992)	-1.399 (0.991)	-1.400 (0.991)
$1^2\text{T}_{2u}$	-0.807	-0.953 (0.994)	-0.943 (0.994)	-0.944 (0.994)
$1^2\text{G}_u$	-0.782	-0.880 (0.996)	-0.877 (0.996)	-0.878 (0.996)
$2^2\text{A}_g$	-0.738	-0.994 (0.990)	-0.961 (0.991)	-0.965 (0.991)
$2^2\text{T}_{1u}$	-0.664	-0.889 (0.991)	-0.864 (0.992)	-0.867 (0.992)
$1^2\text{G}_g$	-0.398	-0.441 (0.998)	-0.441 (0.998)	-0.441 (0.998)
$2^2\text{H}_g$	-0.364	-0.610 (0.990)	-0.587 (0.991)	-0.590 (0.991)
$2^2\text{T}_{2u}$	0.062	-0.338 (0.985)	-0.291 (0.986)	-0.296 (0.986)
$2^2\text{G}_u$	0.097	-0.126 (0.991)	-0.115 (0.991)	-0.116 (0.991)

**Table S5.** Vertical electron attachment energies (eV) and pole strengths (in parentheses) of  $\text{Rb@C}_{20}\text{H}_{20}^+$  at neutral  $\text{Rb@C}_{20}\text{H}_{20}$  geometry, obtained from diagonal electron propagator methods using cc-pVTZ (C), d-aug-cc-pVTZ (H), and cc-pVTZ-PP (Rb) (Rb: 28 ECP). All valence electrons are correlated.

Final state ( $I_h$ )	Vertical electron attachment energies and pole strengths			
	KT	D2 (PS)	P3 (PS)	P3+ (PS)
$1^2\text{A}_g$	-1.738	-2.100 (0.986)	-2.060 (0.987)	-2.065 (0.987)
$1^2\text{T}_{1u}$	-1.530	-1.827 (0.988)	-1.796 (0.989)	-1.800 (0.988)
$1^2\text{H}_g$	-1.198	-1.408 (0.992)	-1.390 (0.992)	-1.392 (0.992)
$1^2\text{T}_{2u}$	-0.808	-0.956 (0.994)	-0.942 (0.994)	-0.944 (0.994)
$1^2\text{G}_u$	-0.781	-0.881 (0.996)	-0.876 (0.996)	-0.876 (0.996)
$2^2\text{A}_g$	-0.735	-0.969 (0.991)	-0.936 (0.992)	-0.940 (0.992)
$2^2\text{T}_{1u}$	-0.651	-0.880 (0.991)	-0.849 (0.992)	-0.853 (0.992)
$1^2\text{G}_g$	-0.399	-0.444 (0.998)	-0.442 (0.998)	-0.442 (0.998)
$2^2\text{H}_g$	-0.377	-0.612 (0.991)	-0.585 (0.991)	-0.588 (0.991)
$2^2\text{T}_{2u}$	0.056	-0.347 (0.985)	-0.289 (0.986)	-0.297 (0.986)
$2^2\text{G}_u$	0.092	-0.129 (0.991)	-0.113 (0.991)	-0.114 (0.991)

**Table S6.** Vertical electron attachment energies (eV) and pole strengths (in parentheses) of  $\text{Ca@C}_{20}\text{H}_{20}^{2+}$  at neutral  $\text{Ca@C}_{20}\text{H}_{20}^+$  geometry, obtained from diagonal electron propagator methods using cc-pVTZ (Ca, C) and d-aug-cc-pVTZ (H). All valence electrons are correlated.

Final state ( $I_h$ )	Vertical electron attachment energies and pole strengths			
	KT	D2 (PS)	P3 (PS)	P3+ (PS)
$1^2A_g$	-4.417	-5.210 (0.972)	-5.098 (0.974)	-5.113 (0.974)
$1^2T_{1u}$	-4.068	-4.743 (0.975)	-4.663 (0.977)	-4.672 (0.976)
$1^2H_g$	-3.563	-4.153 (0.979)	-4.078 (0.980)	-4.088 (0.980)
$1^2T_{2u}$	-3.082	-3.765 (0.976)	-3.670 (0.978)	-3.683 (0.978)

**Table S7.** Vertical electron attachment energies (eV) and pole strengths (in parentheses) of  $\text{Na@C}_{36}\text{H}_{36}^+$  at neutral  $\text{Na@C}_{36}\text{H}_{36}$  geometry, obtained from diagonal electron propagator methods using cc-pVDZ (Na, C) and d-aug-cc-pVDZ (H). All valence electrons are correlated.

Final state ( $D_2$ )	Vertical electron attachment energies and pole strengths			
	KT	D2 (PS)	P3 (PS)	P3+ (PS)
$1^2A$	-1.723	-2.490 (0.972)	-2.356 (0.975)	-2.375 (0.975)
$1^2B_1$	-1.463	-1.887 (0.984)	-1.855 (0.983)	-1.859 (0.983)
$1^2B_2$	-1.444	-1.882 (0.983)	-1.846 (0.983)	-1.850 (0.983)
$1^2B_3$	-1.365	-1.800 (0.983)	-1.757 (0.984)	-1.762 (0.984)
$2^2B_3$	-1.118	-1.392 (0.989)	-1.380 (0.988)	-1.382 (0.988)
$2^2A$	-1.115	-1.385 (0.989)	-1.373 (0.989)	-1.375 (0.989)
$2^2B_2$	-1.081	-1.341 (0.990)	-1.333 (0.989)	-1.334 (0.989)
$2^2B_1$	-1.075	-1.343 (0.989)	-1.334 (0.989)	-1.335 (0.989)
$3^2A$	-1.072	-1.350 (0.989)	-1.340 (0.988)	-1.341 (0.988)

**Table S8.** Vertical electron attachment energies (eV) and pole strengths (in parentheses) of  $\text{K@C}_{36}\text{H}_{36}^+$  at neutral  $\text{K@C}_{36}\text{H}_{36}$  geometry, obtained from diagonal electron propagator methods using cc-pVDZ (K, C) and d-aug-cc-pVDZ (H). All valence electrons are correlated.

Final state ( $D_2$ )	Vertical electron attachment energies and pole strengths			
	KT	D2 (PS)	P3 (PS)	P3+ (PS)
$1^2A$	-1.636	-2.228 (0.978)	-2.150 (0.979)	-2.161 (0.979)
$1^2B_1$	-1.430	-1.812 (0.985)	-1.785 (0.985)	-1.788 (0.985)
$1^2B_2$	-1.425	-1.823 (0.985)	-1.794 (0.984)	-1.797 (0.984)
$1^2B_3$	-1.350	-1.750 (0.985)	-1.717 (0.984)	-1.721 (0.984)
$2^2B_3$	-1.122	-1.394 (0.989)	-1.379 (0.989)	-1.381 (0.989)
$2^2A$	-1.118	-1.388 (0.989)	-1.374 (0.989)	-1.375 (0.989)
$2^2B_1$	-1.084	-1.352 (0.990)	-1.340 (0.989)	-1.342 (0.989)
$2^2B_2$	-1.084	-1.346 (0.990)	-1.335 (0.989)	-1.336 (0.989)
$3^2A$	-1.073	-1.340 (0.990)	-1.330 (0.989)	-1.331 (0.989)



**Table S9.** Vertical electron attachment energies (eV) and pole strengths (in parentheses) of  $\text{Rb@C}_{36}\text{H}_{36}^+$  at neutral  $\text{Rb@C}_{36}\text{H}_{36}$  geometry, obtained from diagonal electron propagator methods using cc-pVDZ (C), d-aug-cc-pVDZ (H), and cc-pVDZ-PP (Rb) (Rb: 28 ECP). All valence electrons are correlated.

Final state ( $D_2$ )	Vertical electron attachment energies and pole strengths			
	KT	D2 (PS)	P3 (PS)	P3+ (PS)
$1^2\text{A}$	-1.617	-2.167 (0.979)	-2.098 (0.980)	-2.107 (0.980)
$1^2\text{B}_1$	-1.414	-1.777 (0.986)	-1.751 (0.985)	-1.754 (0.985)
$1^2\text{B}_2$	-1.413	-1.795 (0.985)	-1.766 (0.985)	-1.770 (0.985)
$1^2\text{B}_3$	-1.345	-1.720 (0.986)	-1.692 (0.985)	-1.695 (0.985)
$2^2\text{B}_3$	-1.116	-1.404 (0.989)	-1.385 (0.988)	-1.388 (0.988)
$2^2\text{A}$	-1.113	-1.399 (0.989)	-1.381 (0.988)	-1.383 (0.988)
$2^2\text{B}_1$	-1.083	-1.365 (0.989)	-1.350 (0.988)	-1.352 (0.988)
$2^2\text{B}_2$	-1.082	-1.355 (0.989)	-1.341 (0.989)	-1.343 (0.989)
$3^2\text{A}$	-1.072	-1.347 (0.989)	-1.334 (0.988)	-1.335 (0.989)