Supporting Information

Metallic C₅N Monolayer as Efficient Catalyst for Accelerating Redox Kinetics of Sulfur in Lithium-Sulfur Batteries

Zhihao Wang ^{a,†}, Zhihao Zeng ^{a,†}, Wei Nong ^a, Zhen Yang ^b, Chenze Qi

^b, Zhengping Qiao ^{a,*}, Yan Li ^{a,*} and Chengxin Wang ^a

^a State key Laboratory of Optoelectronic Materials and Technologies, School of Materials Science and Engineering, Sun Yat-Sen (Zhongshan) University, Guangzhou 510275, People's Republic of China

^b Zhejiang Key Laboratory of Alternative Technologies for Fine Chemicals Process,
College of Chemistry and Chemical Engineering, Shaoxing University, Shaoxing,
312000, PR China

* Corresponding Author. E-mail: cesqzp@mail.sysu.edu.cn (Zhengping Qiao)

* Corresponding Author. E-mail: liyan266@mail.sysu.edu.cn (Yan Li)

[†] These authors contributed equally.

Content

Note1.Computational details	2
Data1. For Section 3.1	3
Data2. For Section 3.2	5
Reference	15

Note1.Computational details

The adsorption energy (E_{ads}) of adsorbates were obtained by following formula:

$$E_{ads} = E_{total} - E_{substrate} - E_{adsorbate} \tag{1}$$

where E_{total} , $E_{substrate}$ and $E_{adsorbate}$ denoted the total energy of adsorbed system, substrate, and isolated adsorbate, respectively. Considering the definition, the lower the E_{ads} , the stronger the interaction between the substrate and adsorbate is.

The cohesive energy (E_{coh}) of both phases C₅N is calculated by $E_{coh} = (E_{C5N} - 5E_C - E_N)/6$, where E_{C5N} , E_C and E_N are the energy of C₅N per formula, energies of isolated C and N atoms, respectively, and 6 represents the total number of atoms in C₅N formula.

The Gibbs free energy of Li_2S_n and S_8 are calculated by

$$G = E_{DFT} + E_{ZPE} - TS \tag{2}$$

where E_{DFT} , E_{ZPE} , and S stand for the total energy obtained by DFT simulation, zeropoint energy, and the entropy, respectively. The zero-point energies of LiPs and S₈ cluster were obtained from vibrational frequency calculations and could be determined as $\text{ZPE} = \frac{1}{2} \sum_{i} hv_{i}$, here h and v_{i} are Planck constant and vibrational frequencies, respectively. T is the standard room temperature (298.15 K).

The elementary reaction steps for sulfur reduction[1] are considered as:

$$S_{8} + 16Li^{+} \rightarrow S_{8}^{*} + 16Li^{+} \#(3)$$

$$S_{8}^{*} + 16Li^{+} + 2e^{-} \rightarrow Li_{2}S_{8}^{*} + 14Li^{+} \#(4)$$

$$Li_{2}S_{8}^{*} + 14Li^{+} + 2e^{-} \rightarrow Li_{2}S_{6}^{*} + Li_{2}S_{2} + 12Li^{+} \#(5)$$

$$Li_{2}S_{6}^{*} + Li_{2}S_{2} + 12Li^{+} + 2e^{-} \rightarrow Li_{2}S_{4}^{*} + 2Li_{2}S_{2} + 10Li^{+} \#(6)$$

$$Li_{2}S_{4}^{*} + 2Li_{2}S_{2} + 10Li^{+} + 2e^{-} \rightarrow Li_{2}S_{2}^{*} + 3Li_{2}S_{2} + 8Li^{+} \#(7)$$
$$Li_{2}S_{2}^{*} + 3Li_{2}S_{2} + 8Li^{+} + 8e^{-} \rightarrow Li_{2}S^{*} + 7Li_{2}S\#(8)$$

The energy of a single Li ion and an electron $(Li^+ + e^-)$ pair was treated as the energy of a single Li atom from its crystalline phase. The adsorbate with an asterisk "*" refers to the state of being adsorbed, whereas the isolated state does not have a star mark.

Table S1. The k-meshes used for different types of calculations related to H-C₅N.

		J 1	5
k-point	structural relaxation	Self-consistent field	Density of states
Primitive cell	7×7×1	11×11×1	13×13×1
Super cell	$2 \times 2 \times 1$	$5 \times 5 \times 1$	-
Nanoribbon	1×9×1	1×15×1	1×15×1

Table S2. The k-meshes used for different types of calculations related to $O-C_5N$.

k-mesh	structural relaxation	Self-consistent field	Density of states
Primitive cell	5×25×1	5×25×1	6×30×1
Super cell	2×6×1	3×9×1	-
Nanoribbon	6×1×1	$8 \times 1 \times 1$	$10 \times 1 \times 1$

Data1. For Section 3.1



Fig. S1. Variations of temperature and energy against time for MD simulations of the H- C_5N monolayer, and the inset shows the side view of the snapshot of the atomic configuration. The simulation is run at 300 K for 6 ps with a time step of 3 fs.



Fig. S2. Variations of temperature and energy against time for MD simulations of the O- C_5N monolayer, and the inset shows the side view of the snapshot of the atomic configuration. The simulation is run at 300 K for 6 ps with a time step of 3 fs.



Fig. S3. Fully relaxed C₅N with another atomic arrangement from the literature[2]. Our simulation results give rise to the lattice constants of a = 3.66 Å and b = 8.88 Å and the cohesive energy of -7.20 eV for this configuration, which are in accordance with the previous report.

Table S3. The charge transfers between adsorbates and $O-C_5N$. The positive value means the charge transfer from adsorbates to $O-C_5N$ and the negative value represent the reverse direction of charge transfer.

LiPs	charge transfer/e
Li ₂ S	-1.147
Li_2S_2	0.218
Li_2S_4	0.027
Li_2S_6	0.015
Li_2S_8	0.008
S	-0.050

Data2. For Section 3.2



Fig. S4. Optimized structures of H-A-C1N1-C2N0 (a), H-A-C2N0-C2N0-1 (b), H-A-C2N0-C2N0-2 (c), H-Z-C2N1-C3N0-1 (d), H-Z-C3N0-C2N1 (e), H-Z-C2N1-C3N0-2 (f). We use -1/-2 to identify the two nanoribbons terminated with the same types of edge atoms but with different atomic arrangements. Taking H-A-C1N1-C2N0 (a) as example, it denotes the nanoribbon with armchair edges derived from H-C₅N with successive edge atoms of one C atom and one N atom at the left side and two C atoms and single N atom at the right side of the ribbon, respectively. In general, H-A-CmNn-CpNq (m, n, p and q = integer) denotes that there exist m C atoms and n N atoms at left side and p C atoms and q N atoms at right side of the ribbon with armchair edge obtained from the H-C₅N.



Fig. S5. Optimized structures of O-A-C5N1-C5N1-1 (g), O-Z-C6N0-C4N2 (h), O-Z-C3N0-C3N0-1 (i), O-Z-C3N0-C3N0-2 (j) and O-A-C5N1-C5N1-2 (k).

Different Nanoribbon	$E_{ m ads}/ m eV$
H-A-C2N0-C2N0-1	-0.64
H-A-C2N0-C2N0-1	-0.76
H-A-C2N0-C2N0-2	-0.83
H-A-C2N0-C2N0-2	-0.81
H-Z-C2N1-C3N0-1	-0.23
H-Z-C2N1- C3N0 -1	-0.22
H-Z-C2N1-C3N0-2	-0.23
O-A-C5N1-C5N1-1	-0.60
H-Z-C3N0-C2N1	-0.21
H-Z-C3N0-C2N1	-0.46
O-Z-C6N0-C4N2	-0.39
O-Z-C6N0-C4N2	-0.49
O-Z-C3N0-C3N0-1	-0.71
O-Z-C3N0- C3N0 -1	-0.73
O-Z-C3N0-C3N0-2	-0.87
O-Z-C3N0-C3N0-2	-0.76
O-A-C5N1-C5N1-2	-0.74
H-A-C1N1-C2N0	-1.03
H-A-C1N1-C1N1	-1.07
O-Z-C2N0-C0N2	-1.72

Table S4. Adsorption energies of Li_2S_6 on different nanoribbons. Bolded CmNn present the situation that LiPs adsorb on that side of nanoribbon.

Table S5. The variation in bond length (Δd) and bond angle (ΔA) after LiPs adsorbed on O-Z-C2N0-**C0N2** nanoribbon. Herein, the variations are calculated as the difference between that of adsorbed LiPs and isolated LiPs. The subscripts, Li-S, S-S and Li-S-Li, in $\Delta d_{\text{Li-S}}$, $\Delta d_{\text{S-S}}$ and $\Delta A_{\text{Li-S-Li}}$ stand for Li-S and S-S bonds as well as Li-S-Li angle in Li₂S, respectively.

LiPs	$\Delta d_{ ext{Li-S}}(ext{Å})$	$\Delta d_{\text{S-S}}(\text{\AA})$	$\Delta A_{\text{Li-S-Li}}(^{\circ})$
Li ₂ S	0.25	-	44.34
Li_2S_2	0.27	0.23	-
Li_2S_4	0.16	0.04	-
Li_2S_6	-0.05	0.01	-
Li_2S_8	0.03	0.02	-
S ₈	-	0.00	-

entre entre.			
LiPs	$\Delta d_{ ext{Li-S}}(ext{Å})$	$\Delta d_{ ext{S-S}}(ext{Å})$	$\Delta A_{\text{Li-S-Li}}(^{\circ})$
Li ₂ S	0.17	-	13.37
Li_2S_2	0.02	-0.10	-
Li_2S_4	0.12	-0.01	-
Li_2S_6	0.00	-0.01	-
Li_2S_8	-0.02	0.00	-
S_8	-	0.00	-

Table S6. The variations in bond length and bond angle after LiPs adsorbed on H-A-C1N1-C2N0.

Table S7. The variations in bond length and bond angle after LiPs adsorbed on H-A-C1N1-C1N1.

LiPs	$\Delta d_{ ext{Li-S}}(ext{Å})$	$\Delta d_{\text{S-S}}(\text{\AA})$	$\Delta A_{\text{Li-S-Li}}(^{\circ})$
Li ₂ S	0.16	-	9.41
Li_2S_2	0.08	-0.11	-
Li_2S_4	0.12	-0.01	-
$L_{i2}S_6$	0.10	-0.01	-
Li_2S_8	-0.03	-0.01	-
S ₈	-	0.00	-



Fig. S6. Optimized structures of Li_2S_6 adsorbed on the five kinds of nanoribbons.



Fig. S7. Optimized structures of Li_2S_6 adsorbed on the four kinds of nanoribbons.



Fig. S8. Optimized structure of Li_2S_6 adsorbed on the O-A-C5N1-C5N1-2 nanoribbon.



Fig. S9. Optimized structures of LiPs adsorbed on the H-A-C1N1-C2N0 nanoribbon, and corresponding E_{ads} .



Fig. S10. Optimized structures of LiPs adsorbed on the O-Z-C2N0-C0N2 nanoribbon, and corresponding E_{ads} .



Fig. S11. Optimized structures of Li_2S_6 adsorbed on the O-Z-C2N0-C0N2 nanoribbon, and corresponding E_{ads} .

Reference

- [1] Q. He, B. Yu, H. Wang, M. Rana, X. Liao, and Y. Zhao, Oxygen defects boost polysulfides immobilization and catalytic conversion: First-principles computational characterization and experimental design, Nano Res. 13 (2020) 2299-2307.
- [2] D. Wang, H. Li, L. Zhang, Z. Sun, D. Han, L. Niu, and J. Zhao, 2D Nitrogen-Containing Carbon Material C₅N as Potential Host Material for Lithium Polysulfides: A First-Principles Study, Adv. Theory Simul. 2 (2018) 1800165-1800172.