

## Supplementary Information

### Oxide-ion diffusion in brownmillerite-type $\text{Ca}_2\text{AlMnO}_{5+\delta}$ from first-principles calculations

Ushio Matsumoto,<sup>\*a,b,c</sup> Akihide Kuwabara,<sup>\*\*a</sup> Craig A. J. Fisher,<sup>a</sup> Hiroki Moriwake<sup>a</sup> and Isao Tanaka<sup>a,c</sup>

<sup>a</sup> Nanostructures Research Laboratory, Japan Fine Ceramics Center, 2-4-1 Mutsuno, Atsuta-ku, Nagoya 456-8587, Japan.

<sup>b</sup> Digital Innovation Center, Furukawa Electric Co., Ltd., 4-3 Okano 2, Nishi-ku, Yokohama 220-0073, Japan.

<sup>c</sup> Department of Materials Science and Engineering, Kyoto University, Kyoto 505-8501, Japan.

\* Email: ushio\_matsumoto@jfcc.or.jp

\*\* Email: kuwabara@jfcc.or.jp

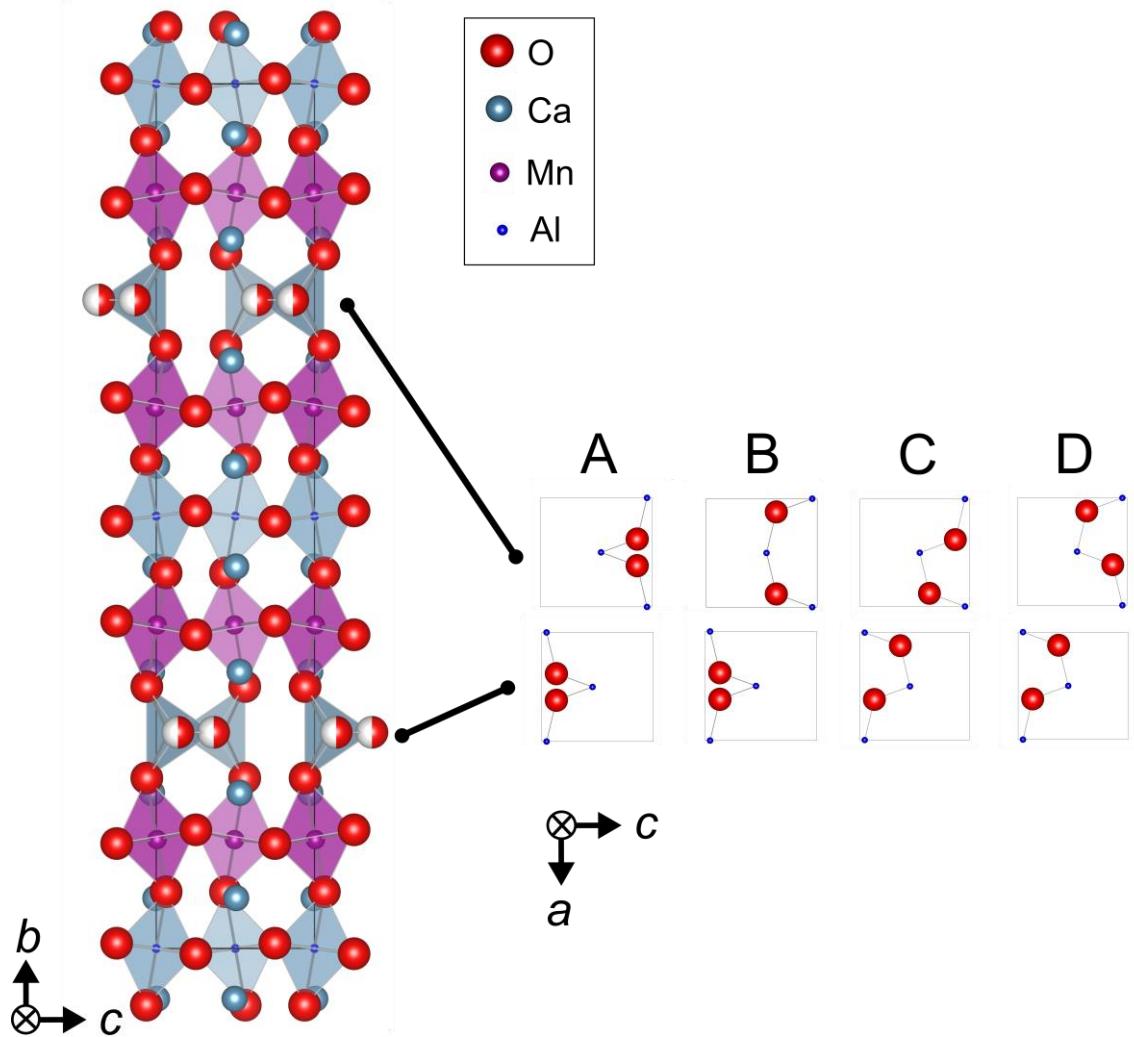


Figure S1 Four possible configurations (A-D) of Al and O atoms in  $\text{AlO}_4$  layers of  $\text{Ca}_2\text{AlMnO}_{5.5}$  corresponding to partial occupancies of 1/2. Grey lines indicate the unit cell.

Table S1 Relative energies,  $\Delta E$ , of four  $\text{AlO}_4$  layer configurations in  $\text{Ca}_2\text{AlMnO}_{5.5}$  with respect to configuration D.

Config.	$\Delta E$ (eV/f.u.)
A	0.2824
B	0.2820
C	0.0002
D	0.0000

Table S2 Positional parameters and site occupancies in unit cells of Ca<sub>2</sub>AlMnO<sub>5</sub> (space group *Ibm2*,  $a = 5.501 \text{ \AA}$ ,  $b = 14.79 \text{ \AA}$ ,  $c = 5.250 \text{ \AA}$ ).

Atom	Wyckoff symbol	Fractional atomic coordinates			Site occupancy
		<i>x</i>	<i>y</i>	<i>z</i>	
Ca1	8 <i>c</i>	0.5278	0.1115	0.0099	1.0
Mn1	4 <i>a</i>	0.0000	0.0000	-0.0001	1.0
Al1	4 <i>b</i>	0.0709	0.2500	0.0395	1.0
O1	8 <i>c</i>	0.2462	0.0143	0.2519	1.0
O2	8 <i>c</i>	0.9283	0.1476	0.9676	1.0
O3	4 <i>b</i>	0.3596	0.2500	0.8767	1.0
X	4 <i>b</i>	0.6721	0.2500	0.1693	
Y	4 <i>b</i>	0.9153	0.7500	0.7057	

Table S3 Positional parameters and site occupancies in unit cells of Ca<sub>2</sub>AlMnO<sub>5.5</sub> (space group *Imma*,  $a = 5.280 \text{ \AA}$ ,  $b = 29.12 \text{ \AA}$ ,  $c = 5.390 \text{ \AA}$ ).

Atom	Wyckoff symbol	Fractional atomic coordinates			Site occupancy
		<i>x</i>	<i>y</i>	<i>z</i>	
Ca1	8 <i>h</i>	0.9971	0.0582	0.5055	1.0
Ca2	8 <i>h</i>	0.0051	0.3206	0.5305	1.0
Mn1	8 <i>h</i>	0.9976	0.1260	0.0083	1.0
Al1	4 <i>a</i>	0.9972	0.0000	0.0000	1.0
Al2	8 <i>i</i>	0.0495	0.2500	0.0769	0.5
O1	8 <i>g</i>	0.2474	0.9931	0.2499	1.0
O2	8 <i>g</i>	0.2491	0.1394	0.2469	1.0
O3	8 <i>g</i>	0.2496	0.6206	0.2475	1.0
O4	8 <i>h</i>	0.9963	0.0656	0.0703	1.0
O5	8 <i>h</i>	0.9892	0.3031	0.9372	1.0
O6	8 <i>i</i>	0.8862	0.2500	0.3668	0.5