Supporting information for

Site Dependent Catalytic Water Dissociation on Anisotropic Buckled Black Phosphorous Surface

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1. Stepwise Collective Variables (CVs)

Our defined collective variables are in the form of a coordination number among the reactive species and reactive sites. For step 1, CV1 and CV2 represent the CN between $P_a(a=ZZ/AC/bulk)-O_a$ and O_a-O_{ext} as depicted in Figure 2(a). For step 2, the CVs (Figure 2(b)) represent the decreasing and increasing CN among O_b -H_a. and O_a -H_a, respectively. Figures 2(c) and 2(d) represent the direct and indirect mechanism of step 3. In the direct mechanism, CV1 and CV2 represent the O_a -O_c CN and O_c -O_e CN, here O_e belongs to the spectator water molecule. For the indirect mechanism, the water molecule is the nucleophile and OH⁻ is the external proton abstractor, following which O_e belongs to the OH⁻ and O_c belongs to the water molecule. Hence CV1 and CV2 are depicted as CN among O_a -O_c and O_e -H_c respectively.

2. Step 1 [OH* formation]: Site Dependent Reactivity

We choose 3 different sites for observation, namely zigzag, armchair, and bulk. The closest water molecules properly oriented towards the mentioned sites are selected. A basic medium of 1M allows us to add 1 NaOH to the system, preventing the overpopulation of OH- and keeping surface oxidation under check. The OH- acts as the reactive species, prepared by removing one of the protons away from the OHand the system neutrality is maintained by adding one Na⁺. Direct adsorption of OH⁻ leaves us with one probable choice of collective variable, i.e., the coordination number between P_a (a=ZZ/AC/Bulk) and O_a . The second CV is defined considering the non-bonded distance between the oxygen (O_{ext}) of an external water molecule and O_a. No wall potentials are added as the solver properly explores the product state. CV1 and CV2 range between 0 to 1 and 1 to 0, respectively. The external water molecule is kept static at its position so that a fixed cutoff distance can be maintained throughout the metadynamics simulation. The simulations are run for 500 steps, with Gaussian hills worth 0.45 kcal mol⁻¹ being added every 10 NVT steps. The gamma function for well-tempered metadynamics is 15. The OH* adsorption free energy barriers, obtained by exploring the contour plots from well-tempered metadynamics run, are minimum for ZZ, with a value of 3.69 kcal mol⁻¹, followed by AC and bulk with values 4.11 and 5.09 kcal mol⁻¹. The contour plot along with different reactive states of step 1 are depicted in Figure S1(a-d), (e-h), and (i-l) for ZZ, AC, and bulk sites, respectively.



Figure S1. Represents the reactant, transition state, product, and surface contour plot obtained from the metadynamics simulation of the first step of the OER catalyzed by bi-layer BP centered at (a-d) ZZ, (e-h) AC, and (i-l) bulk.

Table S1. The fixed distance cutoff, p, q defined for CV1 and CV2 along with the Gaussian hill parameters, and the free energy barrier obtained for the first step of the OER catalyzed by BP.

	CV1		CV2			Hill height	Frequency	γ	Scale	ΔG (kcal mol ⁻¹)	
	Р	q	do	р	q	do	(kcai moi)				
ZZ	8	18	2.5	10	22	4.0	0.45	10	15	0.1	3.69
AC	8	18	2.6	10	22	4.0	0.45	10	15	0.1	4.11
Bulk	8	18	2.6	10	22	3.6	0.45	10	15	0.1	5.09

3. Step 2 [O* formation]: Site Dependent Reactivity

OH* formation is followed by the proton abstraction by the reactive OH⁻ and formation of O*. As a proton transfer step, it is bound to be less energy demanding, already proven by the gas phase calculation of heterogeneous catalyst mediated OER^{1,2}. Our previous studies on undoped and doped graphene-based catalysis study using Langevin metadynamics results in the second and 4th OER step to be the least energy-demanding as they involve simple thermodynamically susceptible proton transfer³. Among the

two CVs defined, CV1 represents the CN between O_b and H_a , taking values within 0 to 1 for non-bonded to the covalently bonded system. CV2 is denoted for O_a and H_a CN and ranges within 1-0. The electronic and physical parameters set for well-tempered metadynamics are provided in Table S2. As expected, the proton transfer barriers for ZZ, AC, and bulk are calculated to be 1.21, 2.16, 1.81 kcal mol⁻¹, quite smallscale as compared to step 1 and step 3. The reactant, transition state, product. and the free energy plot obtained by weighing the two CVs are depicted in Figure S2(a-d), (e-h), and (i-l) for ZZ, AC, and bulk sites, respectively.



Figure S2. Represents the reactant, transition state, product, and surface contour plot obtained from the metadynamics simulation of the second step of the OER catalyzed by bi-layer BP centered at (a-d) ZZ, (e-h) AC, and (i-l) bulk.

Тε	able	S2.	The f	ixed	distan	ce cuto	ff, p,	q de	fined	for	CV1	and	CV2	along	with	the	Gaussia	n hill
pa	aram	ete	rs, and	d the	free er	nergy ba	rrier	obta	ined	for t	he se	cond	l step	of the	OER	cata	lyzed by	BP.

	CV1		CV2			Hill height	Frequency	y γ Scale		ΔG (kcal mol ⁻¹)	
	р	q	do	Р	q	do	(kcai moi)				
ZZ	8	18	1.6	8	18	1.6	0.40	5	15	0.1	1.21
AC	8	18	1.6	8	18	1.9	0.40	5	15	0.1	2.16
Bulk	8	18	1.5	8	18	1.6	0.40	5	15	0.1	1.81

			Mech	anism 1			Mechanism 2							
	CV1 CN [Oa-Oc]				CV2 CN [Oa-O) _{e]}		CV1 CN [Oa-	Oc]	CV2 CN [He-Oe]				
	р	q	do	р	q	do	р	q	do	Р	Q	do		
ZZ	8	18	2.2	10	22	4.0	8	18	2.2	8	18	2.1		
AC	8	18	2.3	10	22	4.2	8	18	2.2	8	18	2.0		
Bulk	8	18	2.3	10	22	4.1	8	18	2.2	8	18	1.9		

Table S3. The bonded and non-bonded parameters p, q, and fixed distance cutoff used for two collective variables in two different mechanisms.

Table S4. Different Gaussian hill parameters and free energy barriers along with standard deviation obtained from 3 different runs for the third step of OER at the zigzag, armchair, and bulk site. All the parameters are tabulated for mechanisms 1 and 2.

Mechanism		Hill height	Frequency	K (kca	l mol ⁻¹)	γ	Scale	ΔG (kcal mol ⁻¹)		$\overline{x} \pm \sigma$		
1		(kcal mol ⁻¹)		[CV1]	[CV2]							
	Set 1	1.25	5	4.0	-	15	0.1	7.18				
ZZ	Set 2	1.75	7	4.0	-	15	0.1	7.60		7.59±0.	33	
	Set 3	2.25	9	4.0	-	15	0.1	7.99				
	Set 1	1.25	5	4.0	-	20	0.1	9.04				
AC	Set 2	1.75	7	4.0	-	20	0.1	9.02		9.04±0	.01	
	Set 3	2.25	9	4.0	-	20	0.1	9.06				
	Set 1	1.25	5	8.0	-	20	0.1	12.81				
Bulk	Set 2	1.75	7	8.0	-	20	0.1	12.68		12.80±0.09		
	Set 3	2.25	9	8.0	-	20	0.1	12.91				
Mech	anism	Hill height	Frequency	K (kcal mol ⁻¹)		γ	Scale	∆G1	$\overline{x} \pm \sigma$	∆ <i>G</i> 2	$\overline{x} \pm \sigma$	
:	2	(kcal mol [¬])		[CV1]	[CV2]			(kcal mol^{-1})		(kcal mol ⁻¹)		
	Set 1	1.25	5	4.0	4.0	15	0.1	1.24	1.81	6.24	5.74	
ZZ	Set 2	1.75	7	5.0	5.0	15	0.1	1.89	±0.44	5.73	±0.49	
	Set 3	2.25	9	5.0	6.0	15	0.1	2.31		5.25		
	Set 1	1.25	5	14.0	10.0	25	0.1	5.11	4.87	4.26	4.28	
AC	Set 2	1.75	7	16.0	11.0	25	0.1	4.88	±0.24	4.23	±0.08	
	Set 3	2.25	9	16.0	12.0	25	0.1	4.62		4.36		
	Set 1	1.50	5	16.0	10.0	25	0.1	3.26	3.38	8.50	8.25	
Bulk	Set 2	2.00	7	18.0	11.0	25	0.1	3.49	±0.11	8.12	±0.22	
	Set 3	2.50	9	18.0	11.0	25	0.1	3.39		8.13		

4. Free Energy Plot of third Step [OOH* formation]



Figure S3. Represent the 1D plot of free energy barrier in terms of individual CVs as obtained from the metadynamics simulation of step 3 of OER following (a-f) mechanism 1 and (g-l) mechanism 2 taking place at ZZ, AC, and bulk site.

5. Rate Constant

The elementary steps of the OER reactions follow first-order reaction kinetic. The rate of reaction of an elementary reaction is given as⁴,

$$k = Ae^{\frac{E_a}{k_bT}} = \frac{k_b t}{h} \frac{Q^{TS}}{Q} e^{\frac{E_a}{k_bT}}$$

where k = the rate constant in s⁻¹, $k_b =$ Boltzmann constant in eV K⁻¹, T = reaction temperature in K, $E_a =$ is the activation barrier in eV. The partition functions of the transition states and the ground states are given as Q_{TS} and Q. In the rate equation $\frac{k_b t}{h} \frac{Q^{TS}}{Q}$ is the prefactor A, chosen to be 10⁻³ s⁻¹ for all elementary reactions⁴. We can directly use the rate equation to calculate the rate constant for the rate determining step of OER. The rate constants for the 3rd step of OER, catalyzed by BP at the ZZ site, are calculated for mechanism 1 and 2. The rate constant for the formation of the hydroperoxo species through mechanism 1 and mechanism 2 is 2956.92 x 10⁴ s⁻¹, 2811.90 x 10⁴ s⁻¹, respectively.

Table S4. Comparative table for the activation energy of the rate determining step of OER, obtained from metadynamics simulation, catalyzed by undoped graphene⁵, doped graphene³, and BP.

	Involved Mechanism	ΔG [kcal mol ⁻¹]			
Undoped graphene	Mechanism 1	21.19±0.51			
N-doped graphene	Mechanism 1	18.23 ± 0.48			
P-doped graphene	Mechanism 1	17.88 ± 0.76			
B-doped graphene	Mechanism 1	15.97 ±0.51			
S-doped graphene	Mechanism 1	14.73 ±0.92			
BP	Mechanism 1	7.59 ±0.33			
DI	Mechanism 2	7.62±0.11			

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