

Supplementary information (SI) for Role of Magnetization on Catalytic Pathways of Non-Oxidative Methane Activation on Neutral Iron Carbide Clusters[†]

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1 Choice of exchange-correlation functional

DFT functional - PBE,¹ BP86,^{2,3} BPW91,^{2,4} OPBE,⁵ M06L,⁶ B3LYP(*) (15% Hartree-Fock exact exchange),⁷ and TPSSh⁸ - and basis sets - 6-311++G(2d,2p),⁹ def2TZVP,^{10,11} def2QZVP,¹⁰ S6-31G*,¹² and TZVP¹³ - were considered.

First, we calculated the order of spin state energy of singlet, triplet, quintet, and septet for FeC diatomic cluster. We found that when the calculation is initiated with singlet state ($\hat{S}^2 = 0$), it ends up in a contaminated state for all functionals and basis sets (see Table S1). Hybrid and meta-GGA functionals (B3LYP(*), TPSSh, and M06L) give more spin contamination than the GGA functionals (Table S1). Except for B3LYP(*) and M06L, when calculations initiated with triplet spin state ($\hat{S}^2 = 2$), it ended up in state with \hat{S}^2 value within 10% error compared to the starting \hat{S}^2 (Table S2). Quintet and septet shows almost no contamination (Table S3 and S4). The order of spin states is similar in all the cases. The relative energies of the states vary. However, the triplet is the ground spin state for the FeC cluster.

To benchmark the DFT methods against the reaction mechanism, it is essential to examine the functionals and the basis sets for the bond dissociation energy (BDE) of FeC, C₂ and C-H bond in CH₄. The BDEs of FeC are shown in Table S5. All the functionals overestimated the BDE of FeC. The BDE of FeC is most accurately described by M06L followed by TPSSh for almost all the basis sets (Table S5). In combination with def2TZVP, M06L and TPSSh show the 1.19% and 2.08% error in BDE of FeC. It can be noticed that there is not much difference due to change in the basis set except for S6-31G*, which increases the error in BDE (Table S5). Therefore, we considered only the def2TZVP basis set for further calculations. We also calculated Fe-C bond length using def2TZVP and found that all functional give percentage error in bond length up to 2.34% (Table S6). In terms of Fe-C bond length, all functional perform well. Notably, B3LYP(*) give largest error in BDE (see Table S5).

BDE of C₂ and C-H are also calculated only for def2TZVP. Table S7 shows that, in C-H

BDE, the maximum error is given by BP86 (7.16%) and the least error by BPW91 (3.64%). PBE, OPBE, M06L, and TPSSh give errors of 4.85%, 5.43%, 6%, and 5.61%, respectively. All the functionals behave reasonably well for C-H BDE as well. However, TPSSh shows the smallest error for C₂ BDE (0.48%) whereas PBE, OPBE, and M06L show the error of 11.9%, 8.2%, and 6.05%, respectively (see Table S8). Since the considered iron carbide clusters involve Fe-C and C-C bonds, TPSSh is the best functional due to its very small percentage error in Fe-C and C₂ BDE. OPBE is a computationally cheaper functional suggested in the literature for accuracy of spin states, which also perform well except for the Fe-C BDE in the present context. As a reasonable compromise between computational expense and accuracy, we propose using OPBE to obtain equilibrium geometries and correcting their energy with TPSSh. Applying this approach to the calculation of FeC BDE we found that the percentage error decreases from 20.35% (OPBE) to 3% (TPSSh/OPBE) (Table S9). We further compared the methane activation mechanism on the FeC cluster (as shown in Figure 1 in the main text) calculated by optimizations using TPSSh and M06L (Table S11) with the one in which energy is calculated using TPSSh and M06L on the OPBE optimized structures (Table S11). It is found that the type of spin crossovers are maintained in all these cases. The key difference is that M06L shows a stronger adsorption energy (-0.20 eV) than both OPBE (0 eV) and TPSSh (-0.02 eV) (Table S11). Consequently, the C-H activation barrier is higher (0.81 eV) in the M06L case. However, the energy levels for the transition state in M06L and OPBE are nearly equal. On the other hand, when OPBE geometry is used to calculate the reaction path energy with M06L (i.e. M06L/OPBE) and TPSSh (i.e. TPSSh/OPBE), it is found that activation barriers are comparable in M06L/OPBE and TPSSh/OPBE. The adsorption energy in M06L becomes positive from negative, whereas that in the TPSSh case is similar to previously obtained by optimization by TPSSh. To calculate the adsorption energy, it is important to account for the dispersion correction. The adsorption energies of all the clusters presented in this chapter are corrected by dispersion correction. The relevant discussion is provided in the upcoming section. Interestingly, TPSSh and OPBE

yielded similar geometries (Table S11). Therefore, the reaction path energy calculated by TPSSh/OPBE is as good as the reaction path is calculated by TPSSh optimization. In this work, we have used OPBE for geometry optimization for all the further calculations, and then energies are corrected by TPSSh. To account for the weak interactions in adsorption of methane GD3BJ dispersion corrections further correct the adsorption energies.

We also tested these functionals on a trinuclear cluster (Fe_3C) to calculate the order of spin states starting from $S = 0$ to $S = 9$. Undectet ($S = 5$) state is found to be the ground state for Fe_3C cluster. On ignoring the spin-contaminated solutions, nonet ($S = 4$) and septet ($S = 3$) are the first and second excited spin states, respectively. Exceptionally, M06L shows tridectet ($S = 6$) as a second excited state instead of septet inconsistent with the literature.¹⁴ This further justifies the choice of TPSSh over M06L in this case.

Table S1: Expectation value of total spin operator $\langle \hat{S}^2 \rangle$ obtained when calculation is initiated with singlet state for FeC cluster. The expected value of $\langle \hat{S}^2 \rangle$ is zero.

Functional	Basis set				
	6-311++G(2d,2p)	def2QZVP	def2TZVP	S6-31G*	TZVP
B3LYP(*)	2.3	4.0	4.0	2.0	4.4
PBE	0.5	0.5	0.5	0.5	0.6
BP86	0.5	0.5	0.5	0.4	0.5
BPW91	0.6	0.5	0.5	0.5	0.6
M06L	3.0	2.7	2.6	2.6	3.0
OPBE	1.2	1.2	1.2	1.1	1.4
TPSSh	3.0	2.9	2.9	2.7	3.2

Table S2: Percentage spin contamination obtained when calculation is initiated with triplet state for FeC cluster.

Functional	Basis set				
	6-311++G(2d,2p)	def2QZVP	def2TZVP	S6-31G*	TZVP
B3LYP(*)	4.40	13.70	12.66	2.97	17.85
PBE	0.34	0.31	0.30	0.28	0.37
BP86	0.28	0.26	0.25	0.23	0.31
BPW91	0.43	0.39	0.37	0.33	0.46
M06L	6.51	9.69	7.87	7.14	16.44
OPBE	1.19	1.07	1.03	0.95	1.32
TPSSh	6.48	5.99	5.54	4.82	7.46

Table S3: Percentage spin contamination obtained when calculation is initiated with quintet state for FeC cluster.

Functional	Basis set				
	6-311++G(2d,2p)	def2QZVP	def2TZVP	S6-31G*	TZVP
B3LYP(*)	0.08	0.17	0.17	0.06	0.20
PBE	0.03	0.03	0.17	0.02	0.03
BP86	0.02	0.03	0.03	0.02	0.03
BPW91	0.03	0.04	0.02	0.03	0.04
M06L	0.27	0.26	0.03	0.18	0.20
OPBE	0.06	0.06	0.14	0.04	0.06
TPSSh	0.19	0.20	0.06	0.16	0.22

Table S4: Percentage spin contamination obtained when calculation is initiated with septet state for FeC cluster.

Functional	Basis set				
	6-311++G(2d,2p)	def2QZVP	def2TZVP	S6-31G*	TZVP
B3LYP(*)	0.0	0.0	0.0	0.0	0.0
PBE	0.0	0.0	0.0	0.0	0.0
BP86	0.0	0.0	0.0	0.0	0.0
BPW91	0.0	0.0	0.0	0.0	0.0
M06L	0.0	0.0	0.0	0.0	0.0
OPBE	0.0	0.0	0.0	0.0	0.0
TPSSh	0.0	0.0	0.0	0.0	0.0

Table S5: Percentage error in bond dissociation energy (BDE) of FeC diatomic cluster. The reference energy of the BDE was adopted from ref.¹⁵

Functional	Basis set				
	6-311++G(2d,2p)	def2QZVP	def2TZVP	S6-31G*	TZVP
B3LYP(*)	10.81	137.45	125.09	13.72	122.12
BP86	28.25	29.23	28.87	30.90	28.27
BPW91	24.25	25.23	24.85	26.93	24.94
M06L	1.12	0.57	1.19	3.46	0.41
OPBE	19.78	20.95	20.35	22.86	19.35
PBE	29.04	30.07	29.67	31.93	28.85
TPSSh	1.74	2.66	2.08	15.36	1.23

Table S6: Percentage error in Fe-C bond length of FeC using variety of functionals with def2TZVP basis set. The reference bond length was adopted from ref.¹⁶

Functional	Bond length	
	Fe-C (Å)	% error
B3LYP(*)	1.61	0.83
BP86	1.56	-2.33
BPW91	1.56	-2.20
M06L	1.60	0.60
OPBE	1.56	-2.24
PBE	1.56	-2.34
TPSSh	1.58	-0.69
Expt. ¹⁶	1.59	-

Table S7: Percentage error in C-H bond dissociation energy (BDE) of methane using variety of functionals with def2TZVP basis set. The reference energy of the BDE was adopted from ref.¹⁵

Functional	BDE	% error
B3LYP(*)	4.84	6.27
BP86	4.88	7.16
BPW91	4.72	3.64
M06L	4.82	6.00
OPBE	4.80	5.43
PBE	4.77	4.85
TPSSh	4.81	5.61
Expt. ¹⁵	4.55	-

Table S8: Percentage error in bond dissociation energy (BDE) of C₂ using variety of functionals with def2TZVP basis set. The reference energy of the BDE was adopted from ref.¹⁵

Functional	BDE	% error
B3LYP-star	6.36	3.09
BP86	6.80	10.27
BPW91	6.69	8.40
M06L	6.54	6.05
OPBE	6.68	8.19
PBE	6.90	11.89
TPSSh	6.20	0.49
expt. ¹⁵	6.17	-

Table S9: Percentage error in Fe-C bond dissociation energy on the geometry optimized by OPBE using variety of functionals with def2TZVP basis set. The reference energy of the BDE was adopted from ref.¹⁵

Functional	BDE	% error
B3LYP(*)	3.95	0.03
BP86	5.15	30.37
BPW91	4.99	26.35
M06L	4.03	1.92
OPBE	4.81	21.77
PBE	5.18	31.18
TPSSh	4.07	3.06
Expt. ¹⁵	3.95	-

Table S10: Methane binding energies calculated with TPSSh and TPSSh+GD2BJ.

Cluster	TPSSh + GD3BJ	TPSSh
FeC	-0.001	0.01
FeC ₂	-0.41	-0.33
FeC ₃	-0.60	-0.51
Fe ₃ C	-0.01	-0.001
Fe ₃ C ₃	-0.02	-0.003
Fe ₃ C ₆	-0.02	-0.001
Fe ₃ C ₉	-0.03	-0.004
Fe ₃ C ₆ -iso	-0.06	-0.01
Fe ₃ C ₉ -iso	-0.01	0.0001

Table S11: The methane activation reaction mechanism on FeC cluster calculated using three different functionals. The complete reaction path is calculated geometry and transition state optimizations in all three functionals. The spin state of every structure presented have less 10% spin contamination. Bold numbers represent the lowest energy spin state for corresponding state. For explanation of energy term see main text.

State	OPBE			M06L			TPSSh		
	Triplet	Quintet	Septet	Triplet	Quintet	Septet	Triplet	Quintet	Septet
IS	0.00	0.87	2.16	0.00	0.76	1.64	0.00	0.88	1.76
I1	0.00	0.85	2.15	-0.20	0.55	1.15	-0.02	0.84	1.43
TS1	0.62	1.37	3.06	0.60	1.84	1.97	0.71	1.97	2.74
I2	-0.19	-0.38	0.42	-0.61	-0.92	-0.30	-0.38	-0.62	-0.23
FS	1.88	2.19	3.59	1.59	1.89	3.09	1.55	1.86	2.72
E _B	-0.003			-0.205			-0.016		
E _{Act}	0.621			0.808			0.731		
E _{Evol}	2.571			2.808			2.480		
E _{Evol} ^{eff}	2.263			2.515			2.173		
E _R	1.880			1.595			1.555		
				M06L/OPBE			TPSSh/OPBE		
IS	0.00	0.87	2.16	0.00	0.77	1.65	0.00	0.88	1.78
I1	0.00	0.85	2.15	0.01	0.77	1.65	0.00	0.88	1.77
TS1	0.62	1.37	3.06	0.63	1.25	2.60	0.72	1.43	2.75
I2	-0.19	-0.38	0.42	-0.58	-0.84	-0.28	-0.37	-0.59	-0.19
FS	1.88	2.19	3.59	1.61	1.91	3.12	1.56	1.88	2.78
E _B	-0.003			0.008			-0.002		
E _{Act}	0.621			0.626			0.719		
E _{Evol}	2.517			2.748			2.462		
E _{Evol} ^{eff}	2.263			2.449			2.151		
E _R	1.880			1.612			1.565		

2 Spin contamination along the reaction path

Table S12: Percentage spin contamination of all the structure along the reaction mechanism on mononuclear clusters.

Cluster	State	Multiplicities		
		Triplet	Quintet	Septet
FeC ₁	IS	3.51	.14	0
	I1	3.50	.14	0
	TS1	.31	.04	0
	I2	.88	.01	0
	FS	.44	0	0
FeC ₂	IS	1.20	0	0
	I1	1.33	0	0
	TS1	.12	.01	0
	I2	.07	0	0
	FS	.01	0	0
FeC ₃	IS	.48	.02	.01
	I1	.61	.01	.01
	TS1	2.46	.02	0
	I2	3.62	.03	0
	FS	.06	0	0

Table S13: Percentage spin contamination of all the structure along the reaction mechanism on trinuclear clusters.

State		Multiplicities	
Fe_3C	Septet	Nonet	Undectet
	IS	.193	.12
	I1	.88	.12
	I2	1.37	.17
	FS	.76	.07
Fe_3C_3	Septet	Nonet	Undectet
	IS	.24	.10
	I1	.24	.10
	TS1	.24	.06
	I2	.48	.14
Fe_3C_6	Septet	Nonet	Undectet
	IS	2.59	.21
	I1	1.47	.21
	TS1	.84	.04
	I2	1.25	.26
Fe_3C_9	Septet	Nonet	Undectet
	IS	1.06	.44
	I1	1.06	.44
	TS1	.92	.05
	I2	1.06	.05
	FS	.59	.02

Table S14: Percentage spin contamination of all the structure along the reaction mechanism on high energy isomers of Fe_3C_9 and Fe_3C_6 trinuclear clusters.

State		Multiplicities		
		Nonet	Undectet	Tridectet
Fe_3C_6 -iso	IS	.09	.02	0
	I1	.08	.02	0
	TS1	.08	.01	0
	I2	.10	.03	0
	FS	.06	.01	0
Fe_3C_9 -iso		Septet	Nonet	Undectet
	IS	3.12	.59	.21
	I1	4.40	.59	.21
	TS1	1.25	.68	.18
	I2	1.04	.36	.14
	FS	1.10	.26	.07

3 Mulliken spin densities

Table S15: Mulliken spin densities of all the structure along the reaction mechanism on all clusters.

	State	Fe	C	H	Unpaired electrons
FeC					
Triplet					
	IS	2.91	-0.91		2.00
	I1	2.91	-0.91	0.00	2.00
	TS1	2.12	-0.07	-0.05	2.00
	I2	2.59	-0.67	0.08	2.00
	FS	3.43	-0.48	0.05	3.00
Quintet					
	IS	3.91	0.09		4.00
	I1	3.91	0.08	0.01	4.00
	TS1	3.58	0.40	0.02	4.00
	I2	3.39	0.57	0.04	4.00
	FS	3.84	1.17	-0.01	5.00
Septet					
	IS	3.82	2.18		6.00
	I1	3.81	2.18	0.00	6.00
	TS1	3.71	2.34	-0.05	6.00
	I2	4.11	1.89	0.00	6.00
	FS	5.05	1.96	-0.01	7.00

	State	Fe	C	H	Unpaired electrons
FeC₂					
Triplet					
	IS	2.54	-0.54		2.00
	I1	2.55	-0.54	0.00	2.00
	TS1	1.99	0.06	-0.05	2.00
	I2	2.13	-0.14	0.02	2.00
	FS	2.94	0.07	-0.01	3.00
Quintet					
	IS	3.38	0.62		4.00
	I1	3.31	0.68	0.01	4.00
	TS1	3.23	0.85	-0.07	4.00
	I2	4.07	-0.09	0.02	4.00
	FS	4.96	0.04	-0.01	5.00
Septet					
	IS	4.92	1.08		6.00
	I1	4.92	1.08	0.00	6.00
	TS1	4.21	1.43	0.35	6.00
	I2	4.16	1.60	0.24	6.00
	FS	5.21	1.73	0.06	7.00
FeC₃					
Triplet					
	IS	2.26	-0.26		2.00
	I1	2.29	-0.28	-0.01	2.00
	TS1	2.60	-0.61	0.01	2.00
	I2	2.75	-0.77	0.02	2.00
	FS	2.78	0.21	0.01	3.00
Quintet					
	IS	3.73	0.27		4.00
	I1	2.88	1.11	0.01	4.00
	TS1	2.94	1.08	-0.02	4.00
	I2	3.35	0.62	0.03	4.00
	FS	3.51	1.50	-0.01	5.00
Septet					
	IS	3.85	2.15		6.00
	I1	3.64	2.37	-0.01	6.00
	TS1	3.91	2.11	-0.03	6.00
	I2	4.09	1.93	-0.02	6.00
	FS	5.09	1.96	-0.05	7.00

	State	Fe	C	H	Unpaired electrons
Fe₃C					
Septet					
	IS	6.46	-0.46		6.00
	I1	6.54	-0.49	-0.05	6.00
	TS1	6.86	-0.78	-0.08	6.00
	I2	6.47	-0.48	0.01	6.00
	FS	7.37	-0.38	0.00	7.00
Nonet					
	IS	8.81	-0.81		8.00
	I1	8.82	-0.80	-0.02	8.00
	TS1	8.74	-0.68	-0.06	8.00
	I2	8.53	-0.54	0.02	8.00
	FS	9.26	-0.25	-0.01	9.00
Undectet					
	IS	10.42	-0.42		10.00
	I1	10.41	-0.42	0.00	10.00
	TS1	10.17	-0.14	-0.03	10.00
	I2	10.26	-0.29	0.03	10.00
	FS	11.13	-0.17	0.04	11.00
Fe₃C₃					
Septet					
	IS	6.54	-0.54		6.00
	I1	6.54	-0.54	0.00	6.00
	TS1	6.71	-0.70	-0.01	6.00
	I2	7.14	-1.17	0.03	6.00
	FS	7.74	-0.74	0.00	7.00
Nonet					
	IS	8.12	-0.12		8.00
	I1	8.12	-0.13	0.00	8.00
	TS1	8.07	-0.07	0.00	8.00
	I2	8.59	-0.62	0.04	8.00
	FS	9.44	-0.44	0.00	9.00
Undectet					
	IS	9.93	0.07		10.00
	I1	9.93	0.07	0.00	10.00
	TS1	9.98	0.02	0.00	10.00
	I2	9.96	-0.01	0.05	10.00
	FS	10.46	0.52	0.02	11.00

	State	Fe	C	H	Unpaired electrons
Fe₃C₆					
Septet					
	IS	7.55	-1.55		6.00
	I1	7.41	-1.40	-0.01	6.00
	TS1	7.37	-1.30	-0.07	6.00
	I2	7.24	-1.26	0.02	6.00
	FS	8.12	-1.14	0.01	7.00
Nonet					
	IS	8.69	-0.69		8.00
	I1	8.69	-0.69	0.00	8.00
	TS1	8.12	-0.05	-0.07	8.00
	I2	8.82	-0.87	0.05	8.00
	FS	9.27	-0.26	-0.01	9.00
Undectet					
	IS	9.44	0.56		10.00
	I1	9.44	0.56	0.00	10.00
	TS1	9.33	0.70	-0.03	10.00
	I2	9.62	0.35	0.03	10.00
	FS	9.92	1.08	0.00	11.00
Fe₃C₉					
Septet					
	IS	7.14	-1.14		6.00
	I1	7.15	-1.15	0.00	6.00
	TS1	7.06	-1.07	0.01	6.00
	I2	7.25	-1.29	0.04	6.00
	FS	8.15	-1.16	0.00	7.00
Nonet					
	IS	9.12	-1.12		8.00
	I1	9.13	-1.13	0.00	8.00
	TS1	8.25	-0.26	0.01	8.00
	I2	8.08	-0.10	0.02	8.00
	FS	8.76	0.26	-0.01	9.00
Undectet					
	IS	9.41	0.59		10.00
	I1	9.41	0.59	0.00	10.00
	TS1	9.27	0.72	0.01	10.00
	I2	9.35	0.60	0.05	10.00
	FS	9.98	1.00	0.02	11.00

	State	Fe	C	H	Unpaired electrons
Fe₃C₆-iso					
Nonet					
	IS	8.05	-0.05		8.00
	I1	8.05	-0.06	0.00	8.00
	TS1	8.06	-0.08	0.02	8.00
	I2	8.33	-0.35	0.02	8.00
	FS	9.13	-0.12	-0.01	9.00
Undectet					
	IS	9.57	0.43		10.00
	I1	9.57	0.42	0.00	10.00
	TS1	9.42	0.57	0.01	10.00
	I2	9.65	0.32	0.02	10.00
	FS	10.37	0.65	-0.02	11.00
Tridectet					
	IS	10.87	1.13		12.00
	I1	10.87	1.13	0.00	12.00
	TS1	10.81	1.19	0.00	12.00
	I2	10.81	1.17	0.02	12.00
	FS	11.49	1.48	0.03	13.00
Fe₃C₉-iso					
Septet					
	IS	8.00	-2.00		6.00
	I1	8.23	-2.23	0.00	6.00
	TS1	7.44	-1.44	0.00	6.00
	I2	7.24	-1.27	0.03	6.00
	FS	8.47	-1.47	0.00	7.00
Nonet					
	IS	8.98	-0.98		8.00
	I1	8.99	-0.99	0.00	8.00
	TS1	8.90	-0.94	0.04	8.00
	I2	8.36	-0.35	-0.01	8.00
	FS	9.04	-0.02	-0.02	9.00
Undectet					
	IS	9.52	0.48		10.00
	I1	9.53	0.47	0.00	10.00
	TS1	9.52	0.46	0.02	10.00
	I2	9.37	0.61	0.02	10.00
	FS	9.65	1.37	-0.02	11.00

4 Geometries of intermediates and transition states in all spin channels

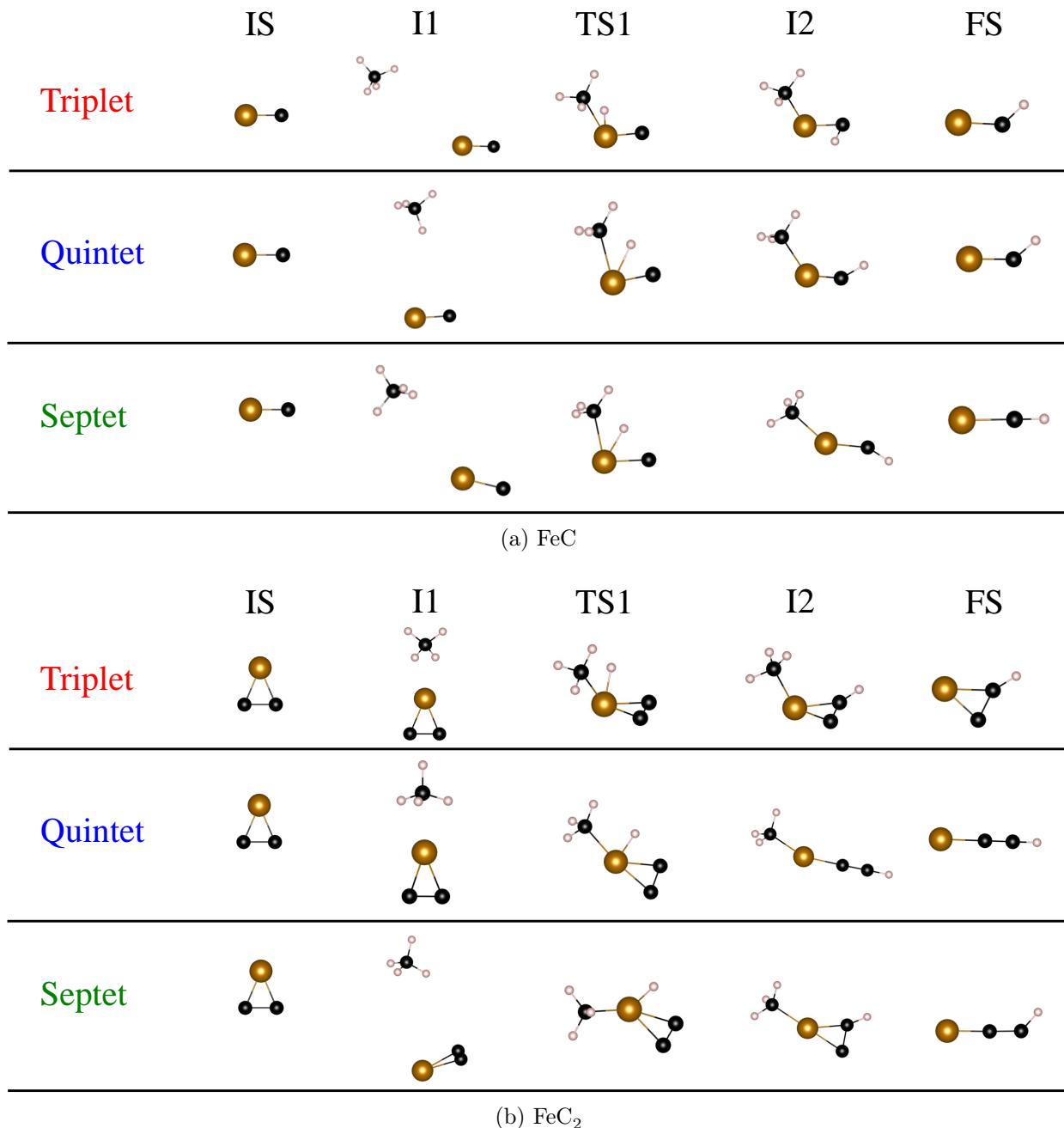


Figure S1: Continued to next page...

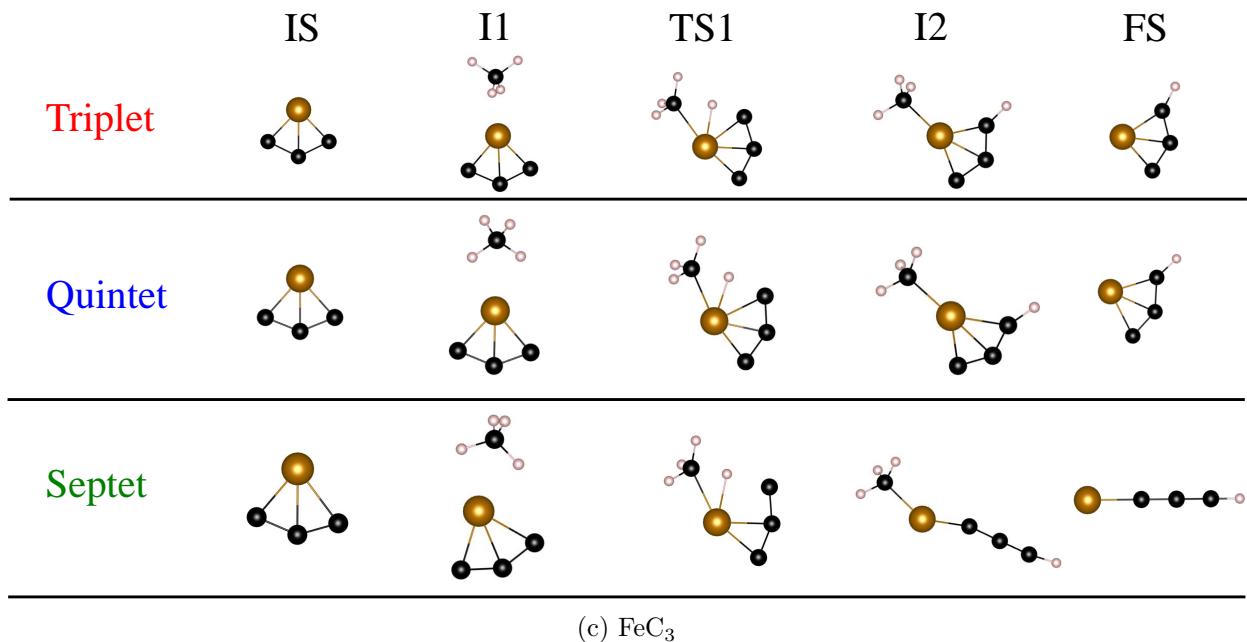
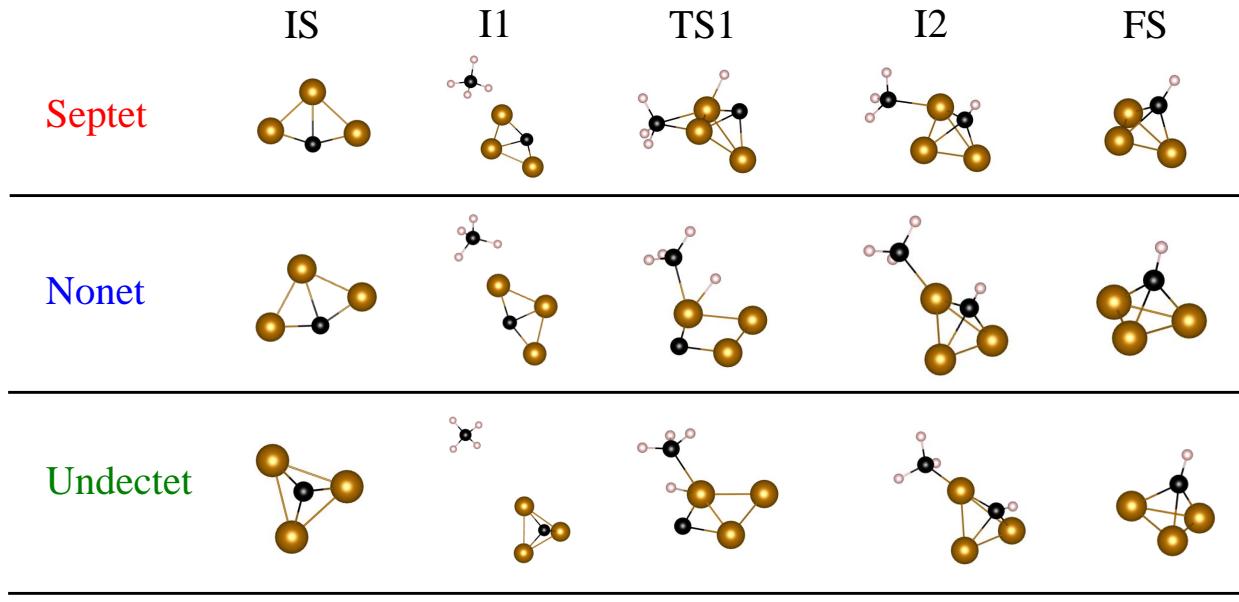
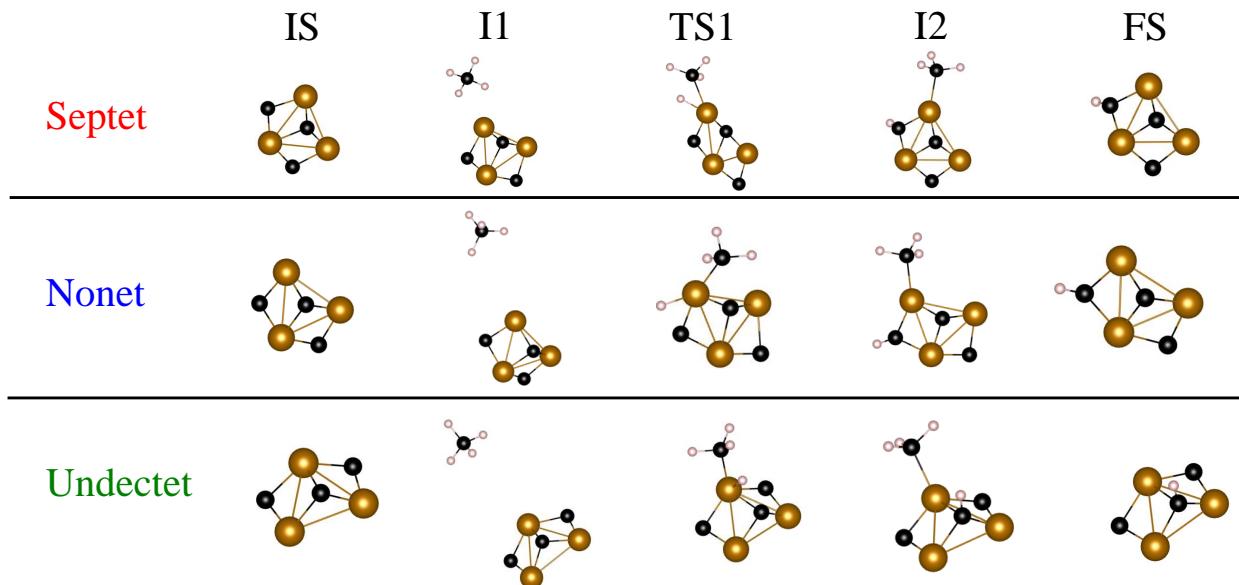


Figure S1: Geometries of all the intermediates and transition states in all three spin channels studied for the reaction on mononuclear clusters. The spin multiplicity of the FS state is one unit higher in all spin channels (i.e., quartet in triplet channel, sextet in quintet channel, etc.) due to the evolution of the methyl radical.



(a) Fe_3C



(b) Fe_3C_3

Figure S2: Continued to next page...

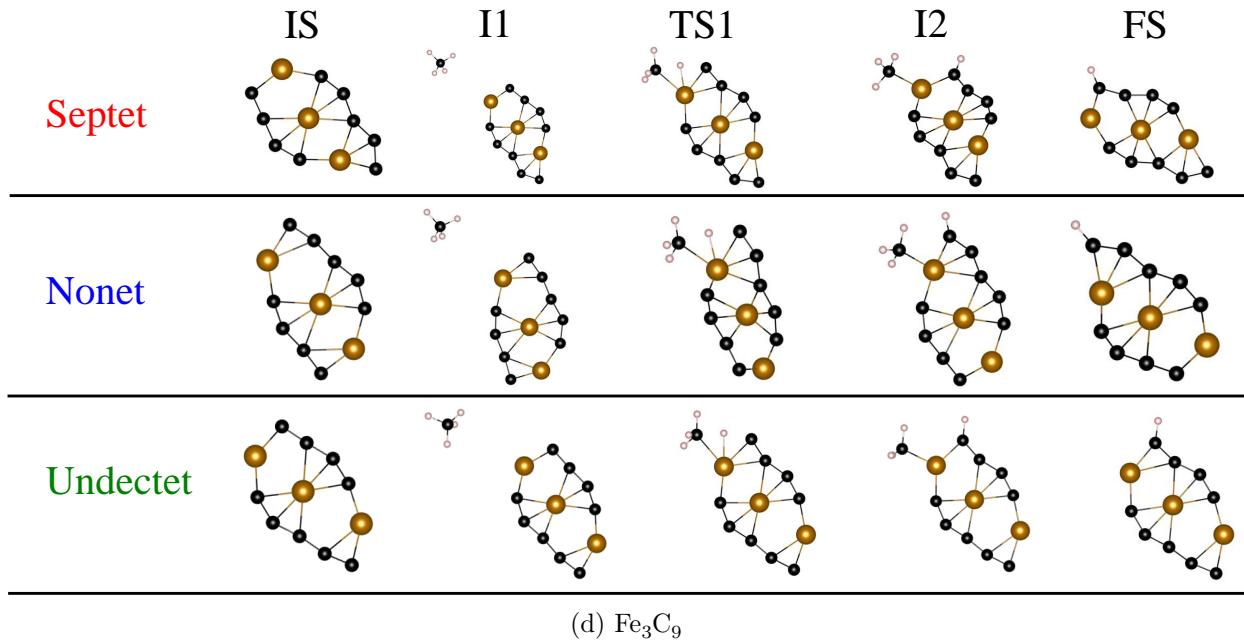
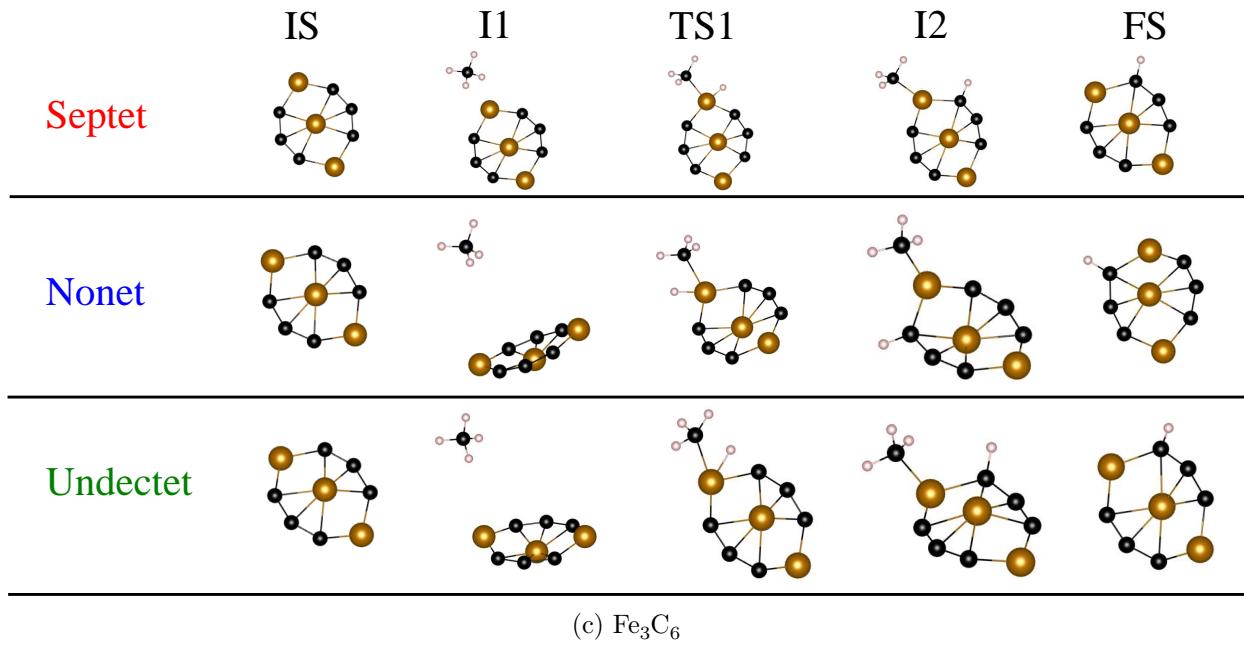
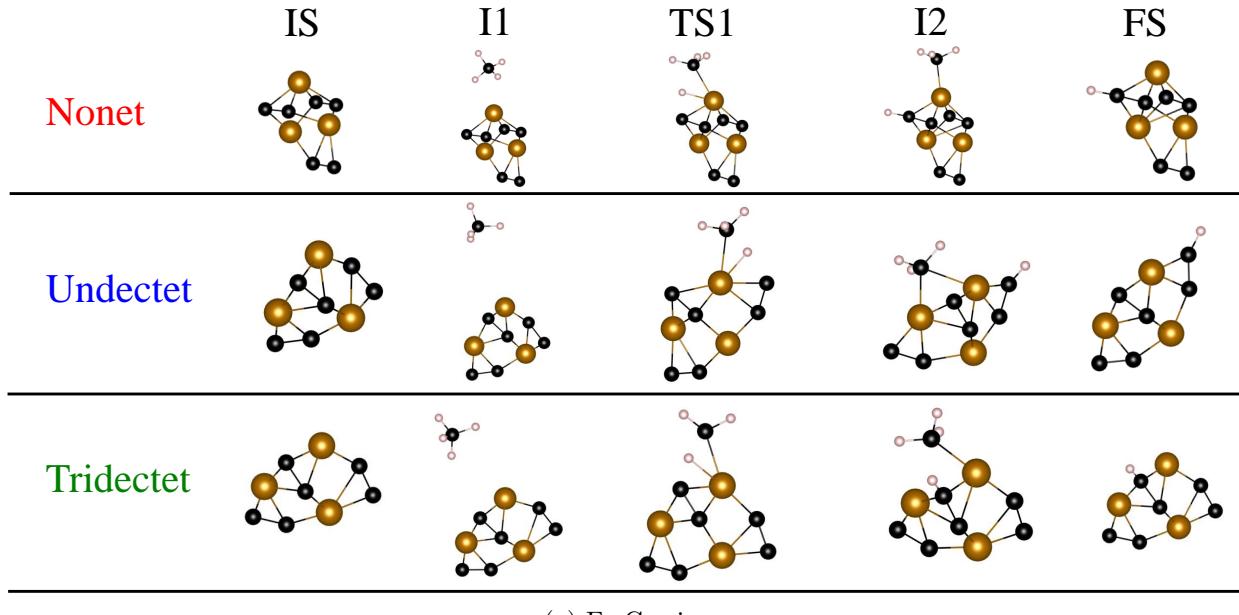
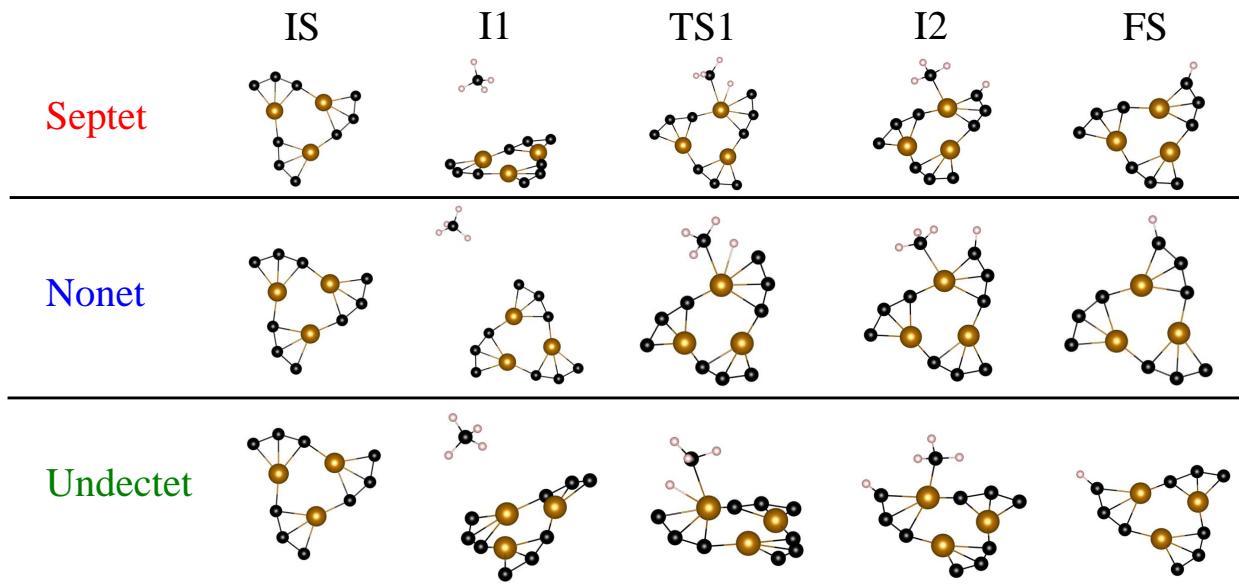


Figure S2: Geometries of all the intermediates and transition states in all three spin channels studied for the reaction on trinuclear clusters. The spin multiplicity of the FS state is one unit higher in all spin channels (i.e., octet in septet channel, dectet in nonet channel, etc.) due to the evolution of the methyl radical.



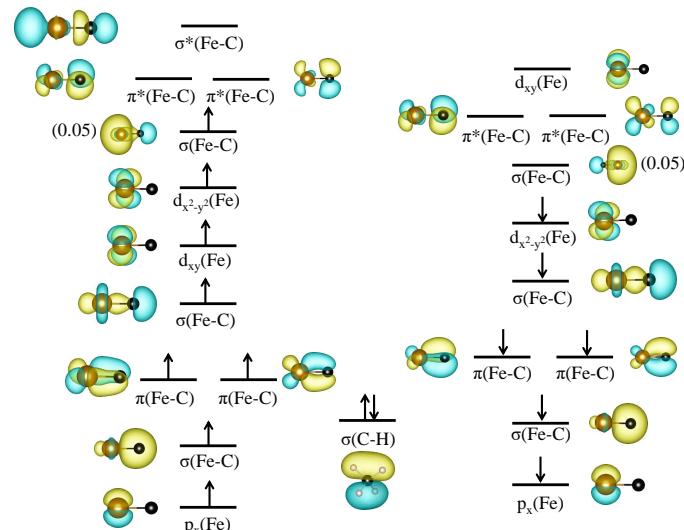
(a) $\text{Fe}_3\text{C}_6\text{-iso}$



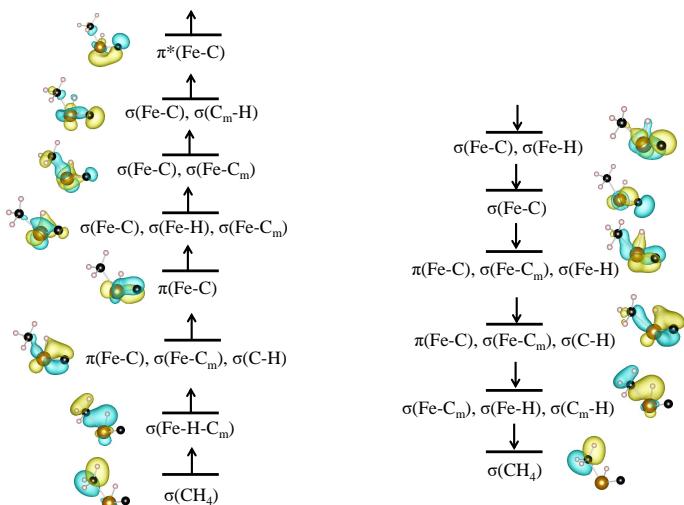
(b) $\text{Fe}_3\text{C}_9\text{-iso}$

Figure S3: Geometries of all the intermediates and transition states in all three spin channels studied for the reaction on high energy isomers of $\text{Fe}_3\text{C}_6\text{-iso}$ and $\text{Fe}_3\text{C}_9\text{-iso}$ clusters. The spin multiplicity of the FS state is one unit higher in all spin channels (i.e., octet in septet channel, dectet in nonet channel, etc.) due to the evolution of the methyl radical.

5 Orbital diagrams

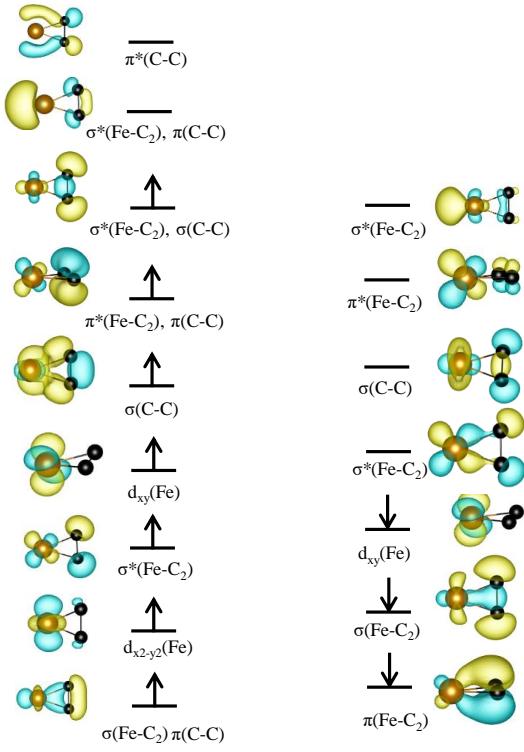


(a) IS

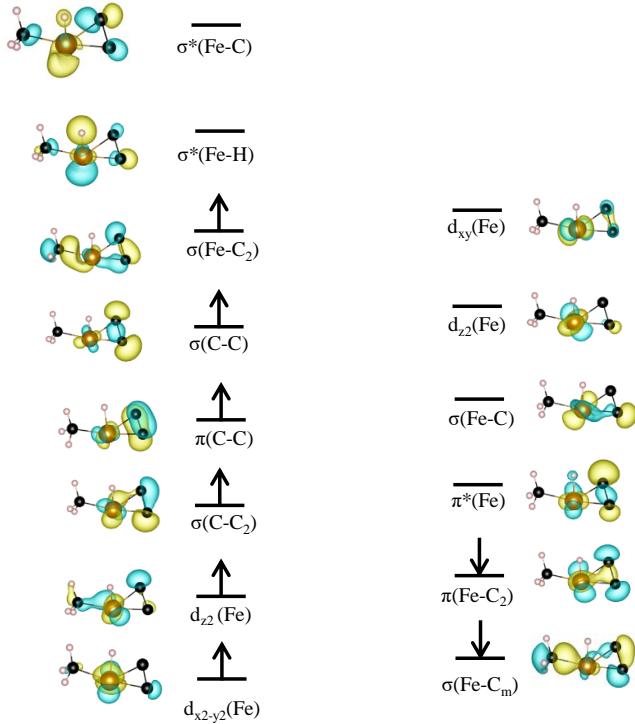


(b) TS1

Figure S4: Kohn-Sham orbital diagram of methane activation process on diatomic FeC cluster for IS and TS1. The up and down arrows represent the alpha and beta spin electrons. The isosurface value used is $0.07 \text{ } a_0^{-3}$ except alpha-HOMO and beta-LUMO in (a) where the isosurface value of $0.05 \text{ } a_0^{-3}$ as specified in parenthesis near the corresponding orbitals.

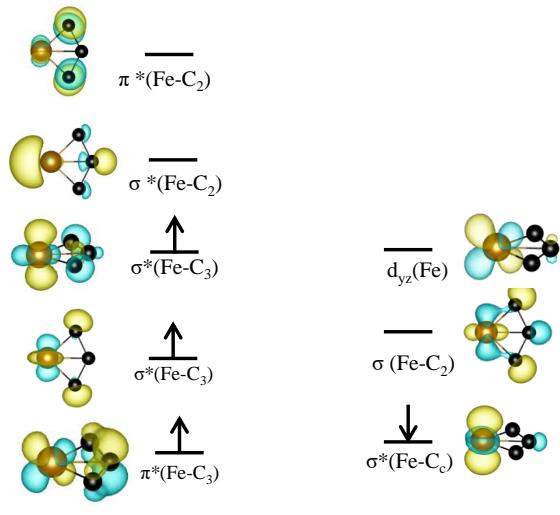


(a) IS

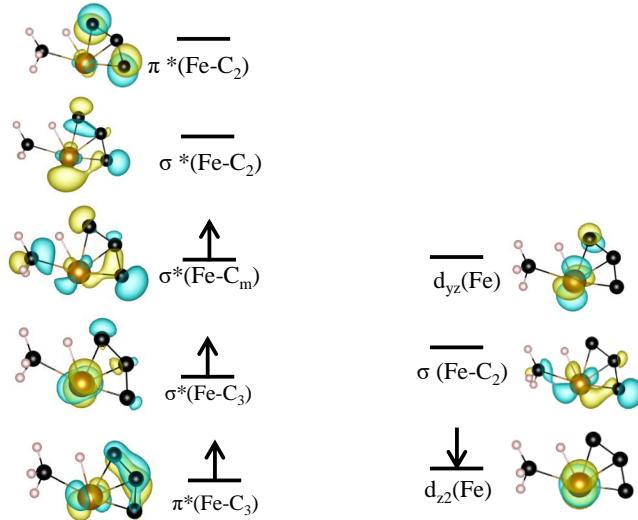


(b) TS1

Figure S5: Kohn-Sham orbital diagram of methane activation process on triatomic FeC_2 cluster for IS and TS1. The up and down arrows represent the alpha and beta spin electrons. The isosurface value used is 0.07 a_0^{-3} . ²⁴



(a) IS



(b) TS1

Figure S6: Kohn-Sham orbital diagram of methane activation process on FeC_3 cluster for IS and TS1. The up and down arrows represent the alpha and beta spin electrons. The isosurface value used is 0.07 a_0^{-3} .

6 The H-transfer in nonet channel of Fe₃C

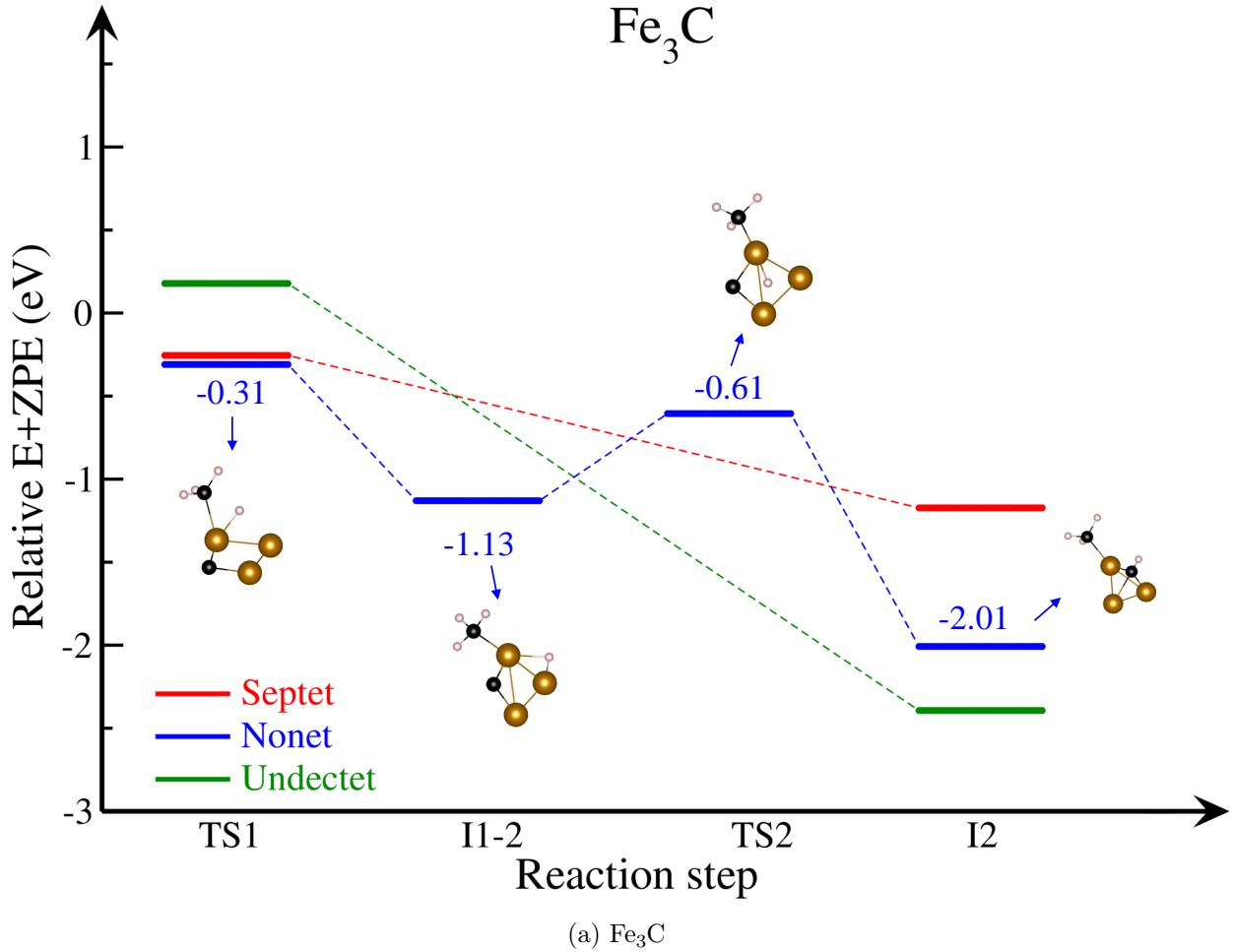


Figure S7: Elementary steps between TS1 and I2 in nonet channel of Fe₃C.

7 Free energy profile computed with TPSSh/OPBE level

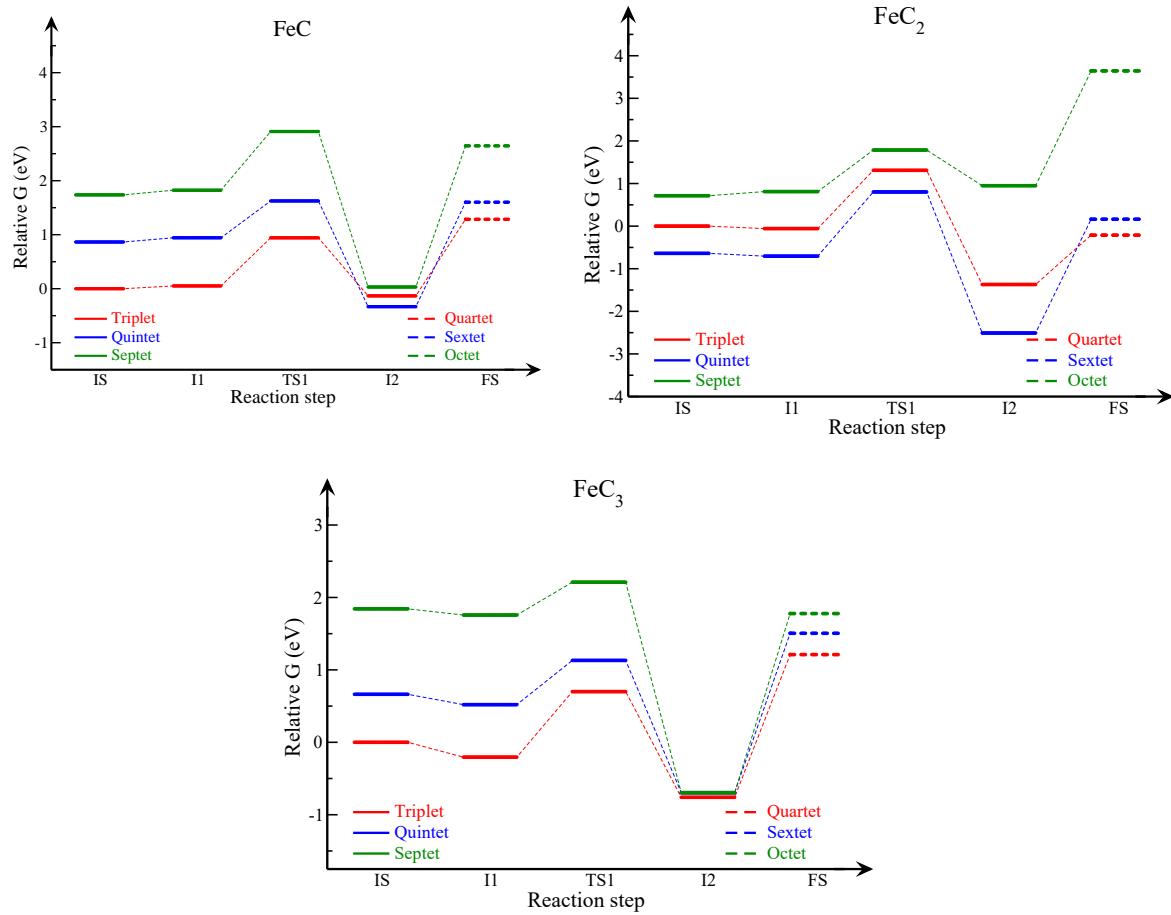
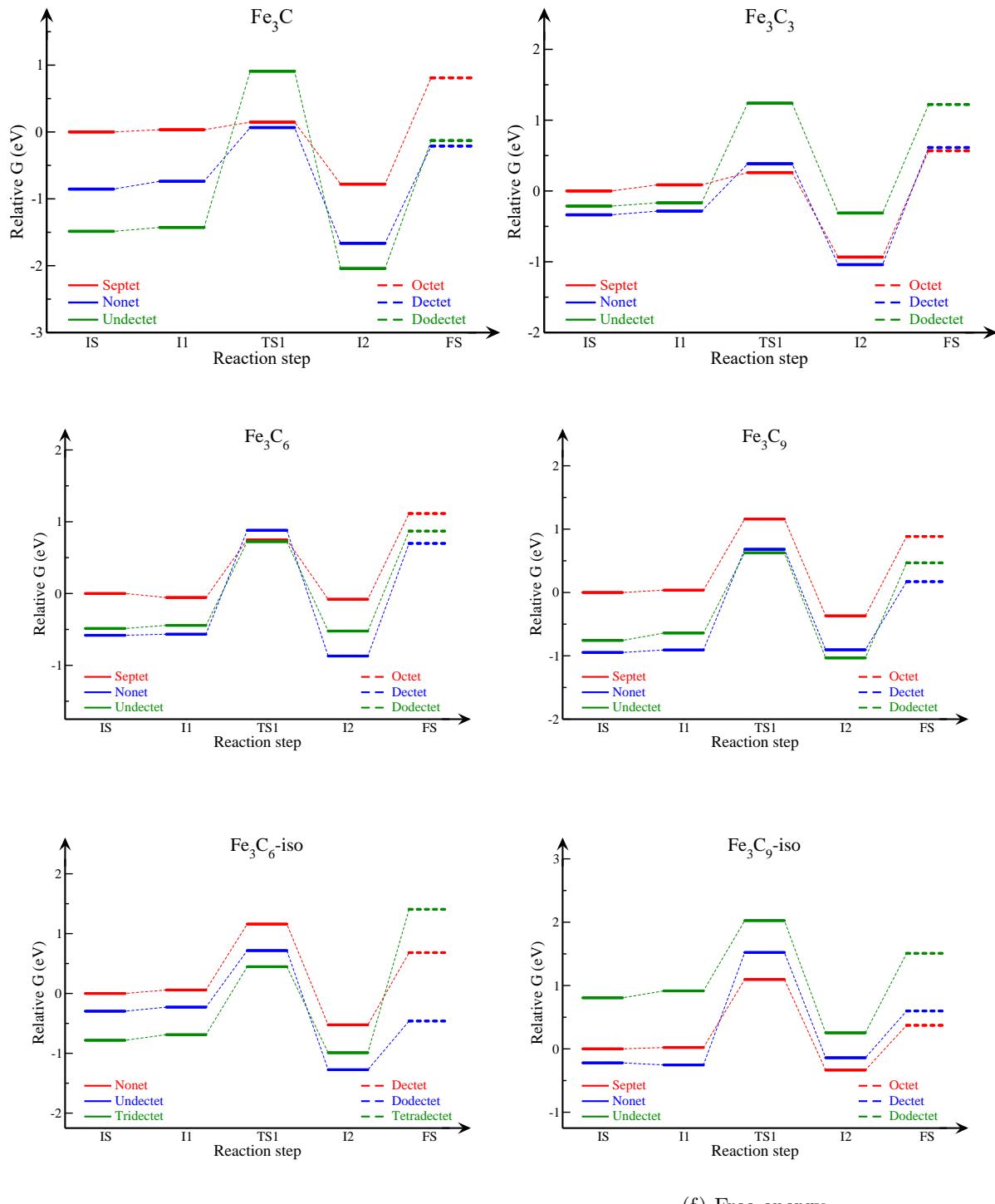


Figure S8: Reaction pathways for methane activation and methyl radical evolution over mononuclear clusters in three lowest energy spin multiplicity states using TPSSh/OPBE level of theory.



(f) Free energy

Figure S9: Reaction pathways for methane activation and methyl radical evolution over trinuclear clusters in three lowest energy spin multiplicity states using TPSSh/OPBE level of theory.

8 Potential energy profile and free energy profile computed with OPBE level

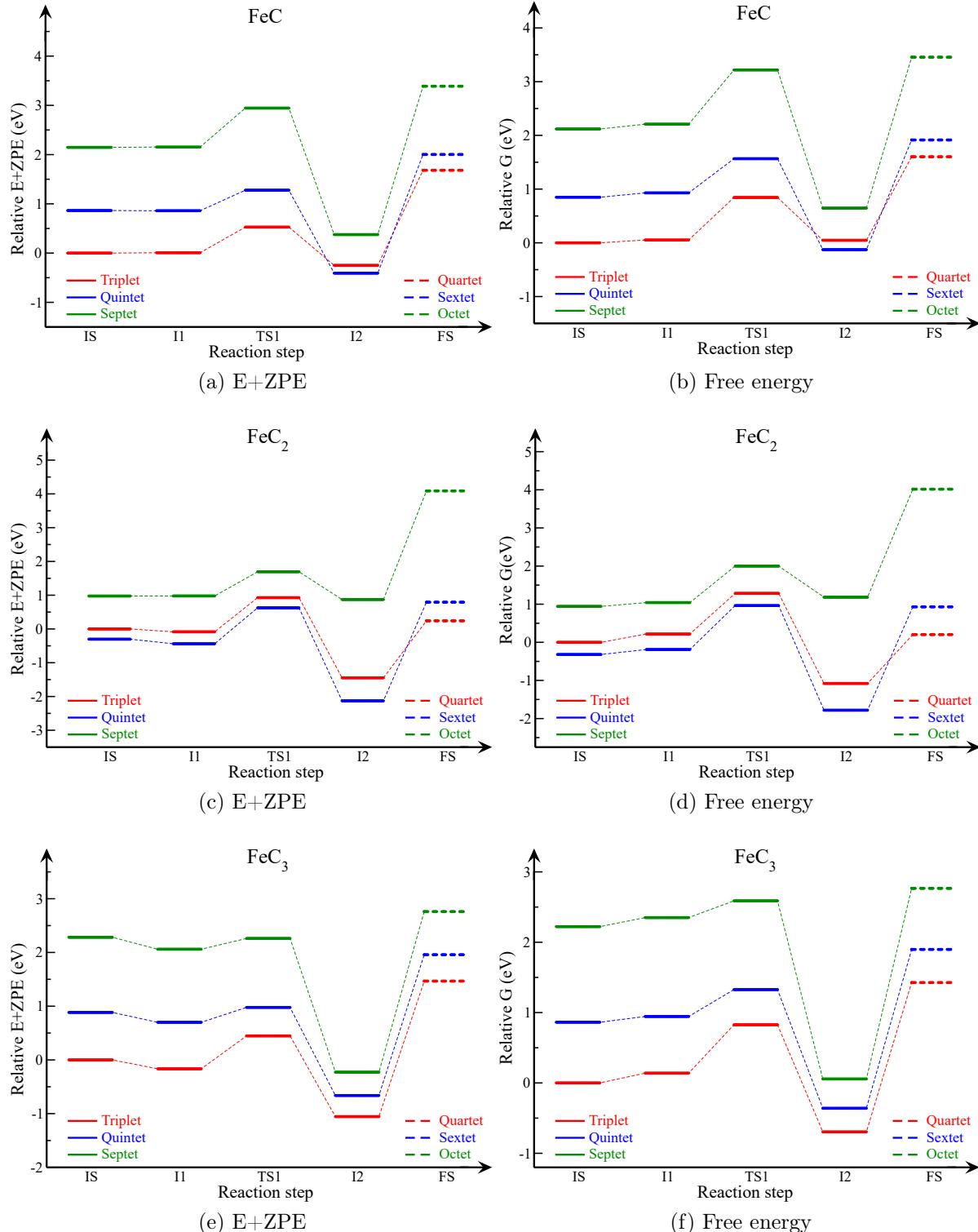


Figure S10: Reaction pathways for methane activation and methyl radical evolution over mononuclear clusters in three lowest energy spin multiplicity states using OPBE/def2TZVP level of theory.

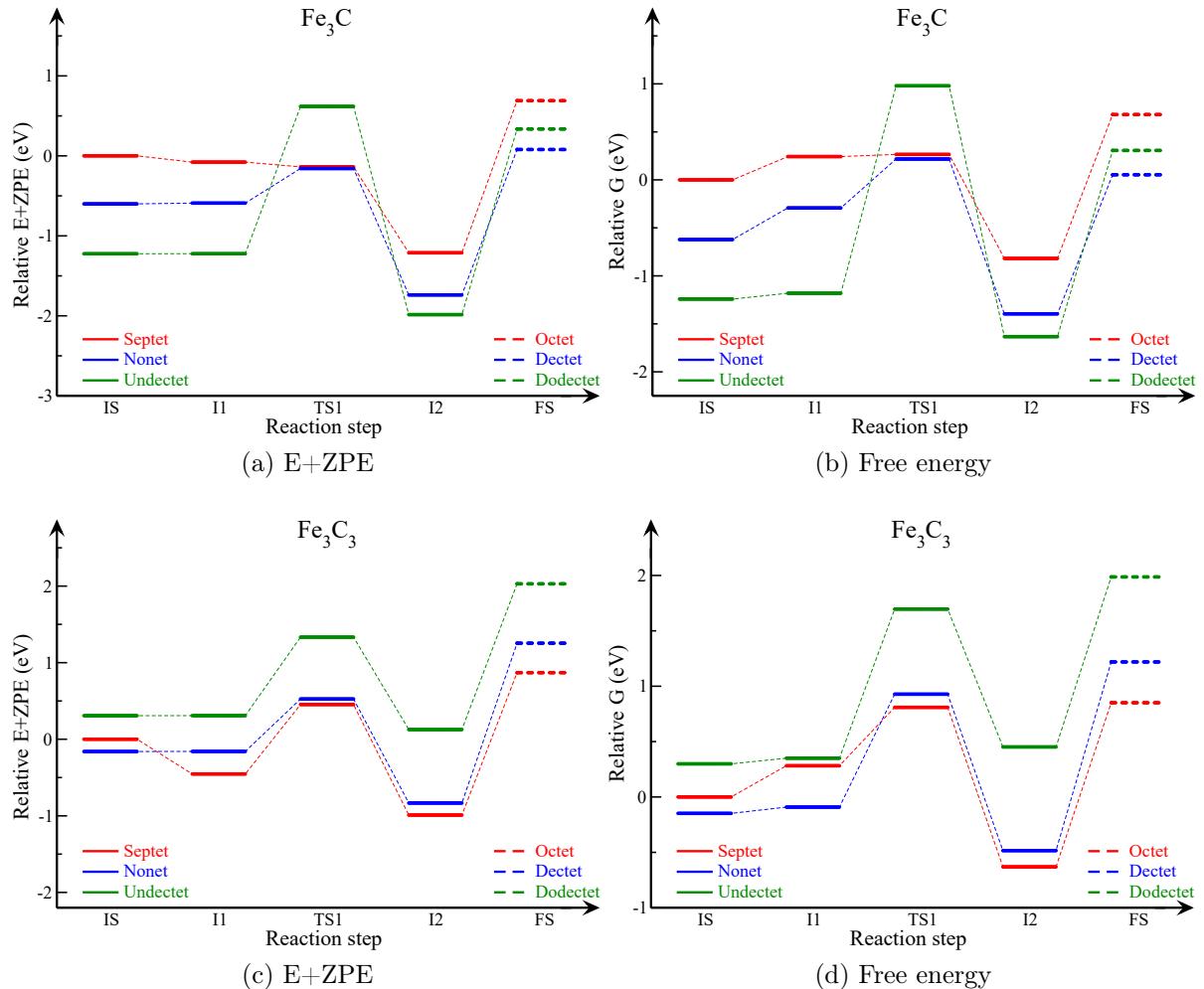


Figure S11: Reaction pathways for methane activation and methyl radical evolution over trinuclear clusters - Fe₃C and Fe₃C₃ - in three lowest energy spin multiplicity states using OPBE/def2TZVP level of theory.

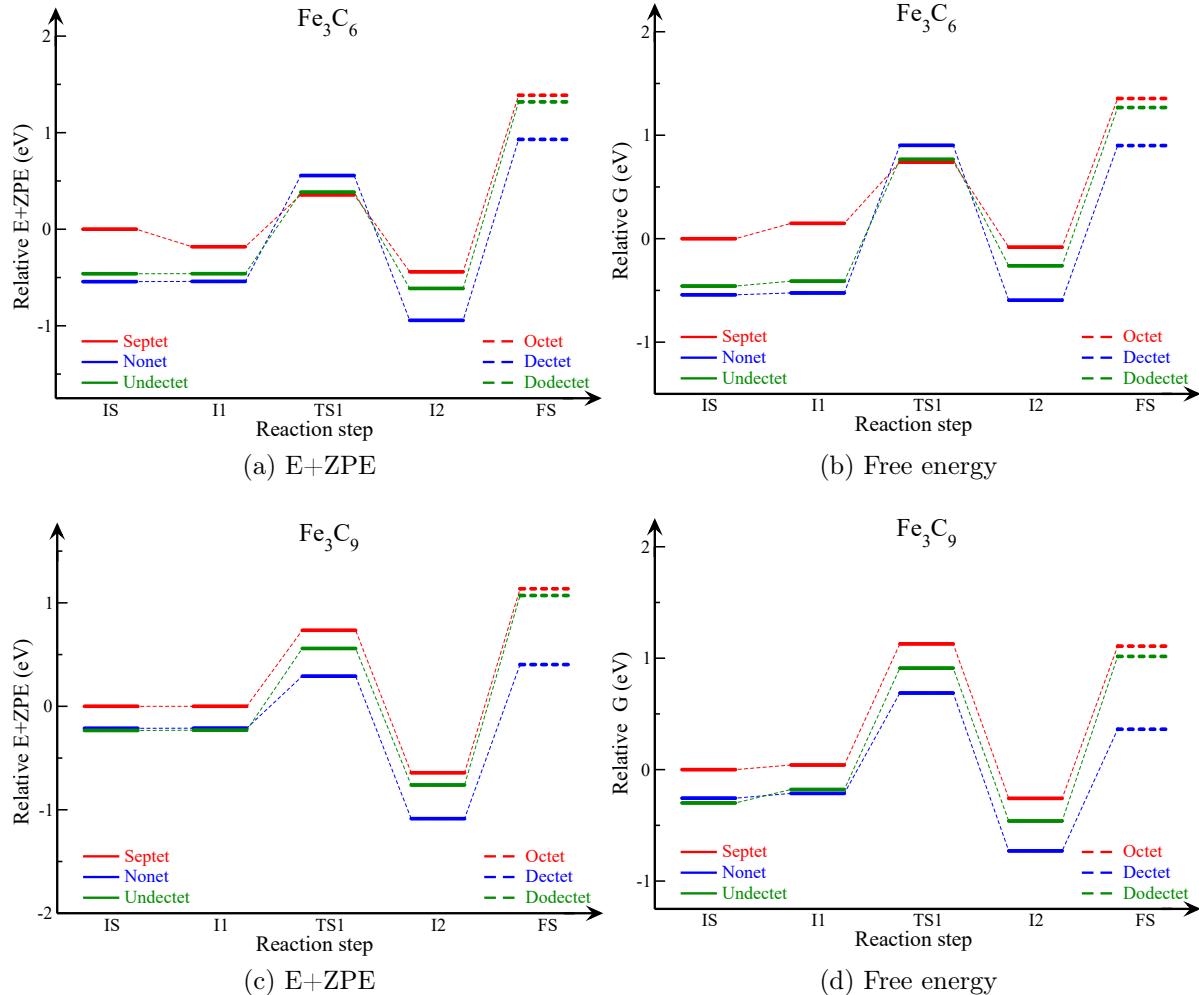


Figure S12: Reaction pathways for methane activation and methyl radical evolution over trinuclear clusters - Fe_3C and Fe_3C_3 - in three lowest energy spin multiplicity states using OPBE/def2TZVP level of theory.

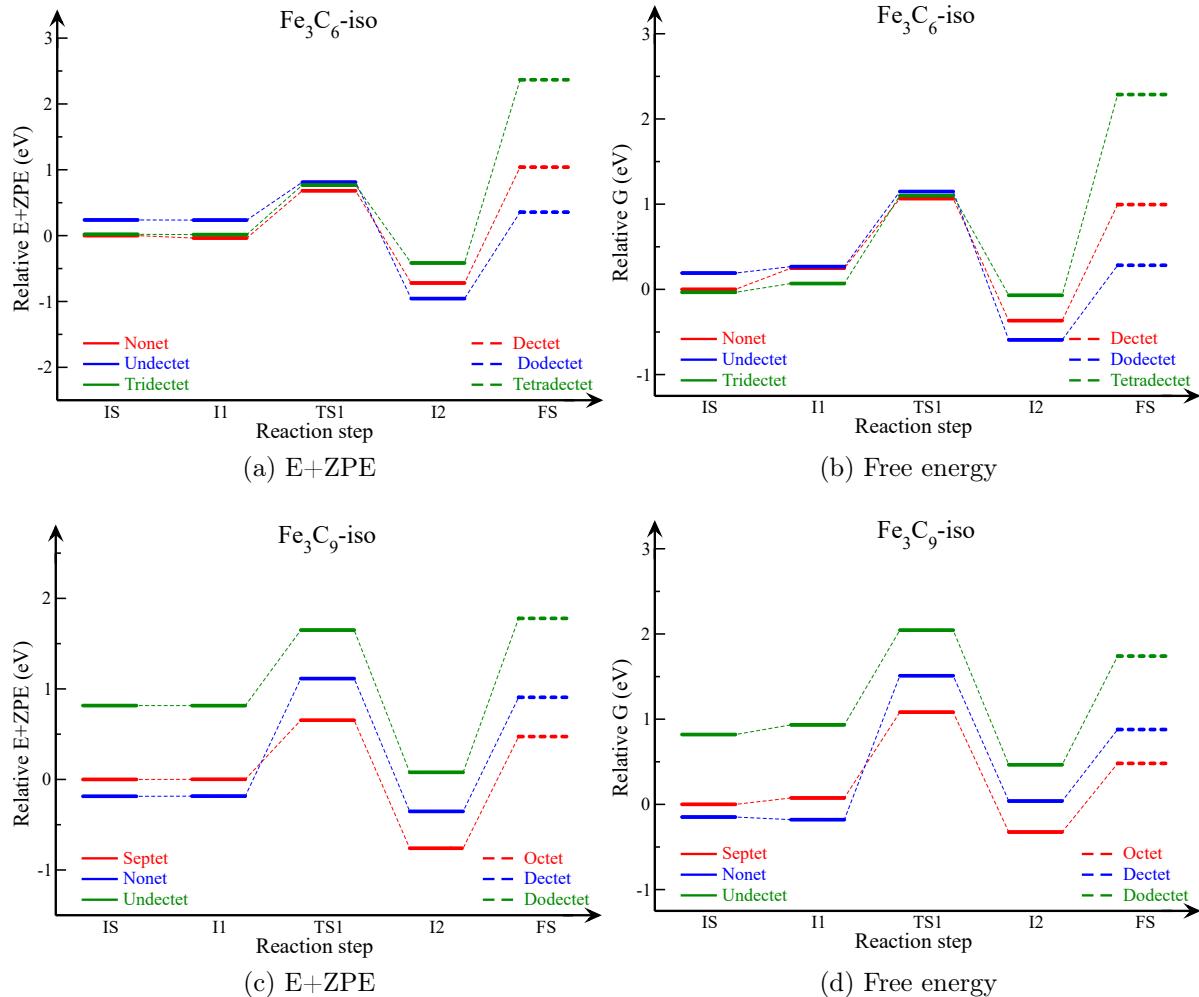


Figure S13: Reaction pathways for methane activation and methyl radical evolution over high energy isomer $\text{Fe}_3\text{C}_6\text{-iso}$ and $\text{Fe}_3\text{C}_9\text{-iso}$ triuclear clusters in three lowest energy spin multiplicity states using OPBE/def2TZVP level of theory.

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