

Convergence acceleration with low-precision data in machine learning molecular dynamics

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Table S1. Conversion of linear k-space sampling densities (Δk , top row) to equivalent sampling in both grid notation and k-points per reciprocal atom (pra) in the 1st BZ.

Δk ($\text{\AA}^{-1}$)	0.09	0.12	0.18	0.24	0.30	0.36	0.66	0.96
BCC	23 x 23 x 23	17 x 17 x 17	11 x 11 x 11	9 x 9 x 9	7 x 7 x 7	6 x 6 x 6	3 x 3 x 3	3 x 3 x 3
	25000 pra	9900 pra	2700 pra	1500 pra	700 pra	500 pra	100 pra	100 pra
Al FCC	19 x 19 x 19	13 x 13 x 13	9 x 9 x 9	7 x 7 x 7	6 x 6 x 6	5 x 5 x 5	3 x 3 x 3	2 x 2 x 2
	24000 pra	8800 pra	3000 pra	1400 pra	900 pra	500 pra	200 pra	100 pra
HCP	29 x 29 x 15	22 x 22 x 12	15 x 15 x 8	11 x 11 x 6	9 x 9 x 5	8 x 8 x 4	4 x 4 x 3	3 x 3 x 2
	26000 pra	12000 pra	3600 pra	1500 pra	900 pra	600 pra	100 pra	50 pra
BCC	25 x 25 x 25	19 x 19 x 19	13 x 13 x 13	10 x 10 x 10	8 x 8 x 8	7 x 7 x 7	4 x 4 x 4	3 x 3 x 3
	32000 pra	14000 pra	4400 pra	2000 pra	1100 pra	700 pra	200 pra	100 pra
Cu FCC	21 x 21 x 21	15 x 15 x 15	10 x 10 x 10	8 x 8 x 8	6 x 6 x 6	5 x 5 x 5	3 x 3 x 3	2 x 2 x 2
	38000 pra	14000 pra	4000 pra	2100 pra	900 pra	500 pra	200 pra	100 pra
HCP	33 x 33 x 17	26 x 26 x 14	17 x 17 x 9	13 x 13 x 7	11 x 11 x 6	9 x 9 x 5	5 x 5 x 3	4 x 4 x 2
	38000 pra	19000 pra	5300 pra	2400 pra	1500 pra	900 pra	200 pra	100 pra
BCC	21 x 21 x 21	15 x 15 x 15	10 x 10 x 10	8 x 8 x 8	6 x 6 x 6	5 x 5 x 5	3 x 3 x 3	2 x 2 x 2
	19000 pra	6800 pra	2000 pra	1100 pra	500 pra	300 pra	100 pra	50 pra
Mg FCC	17 x 17 x 17	12 x 12 x 12	8 x 8 x 8	6 x 6 x 6	5 x 5 x 5	4 x 4 x 4	3 x 3 x 3	2 x 2 x 2
	20000 pra	7000 pra	2100 pra	1000 pra	500 pra	300 pra	200 pra	50 pra
HCP	31 x 31 x 17	23 x 23 x 13	16 x 16 x 9	12 x 12 x 7	10 x 10 x 5	8 x 8 x 5	5 x 5 x 3	3 x 3 x 2
	33000 pra	14000 pra	4700 pra	2100 pra	1000 pra	700 pra	200 pra	50 pra

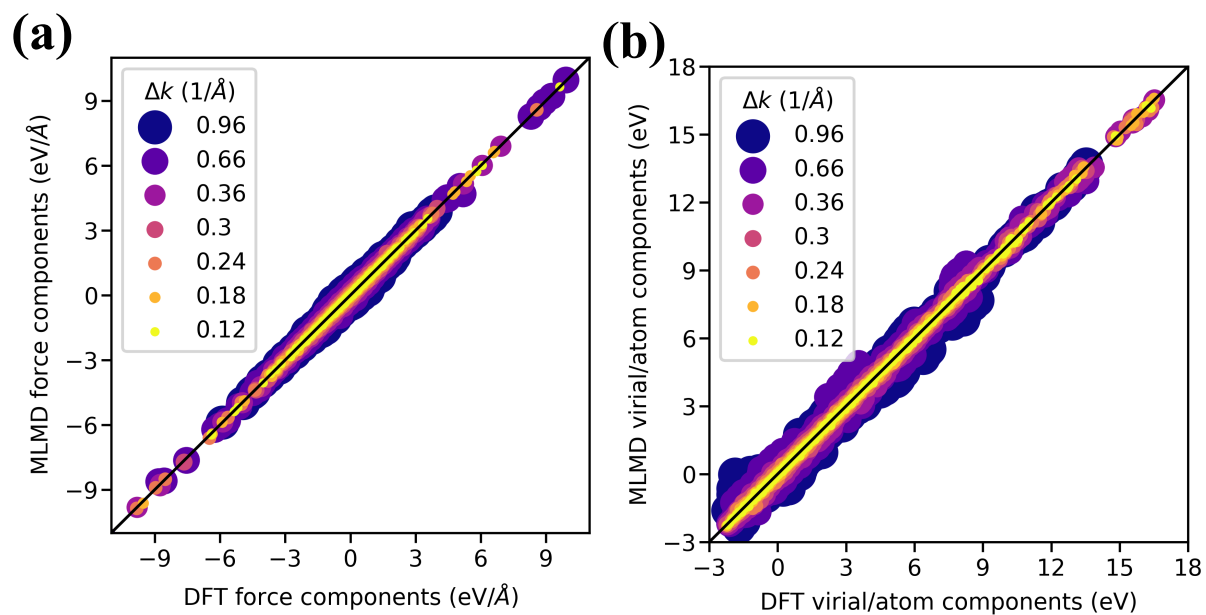


Figure S2. Parity plots of force components (a) and virial components per atom (b) for MLMD models against DFT training data. Legend indicates k-space sampling density (Δk) of the corresponding DFT training dataset.

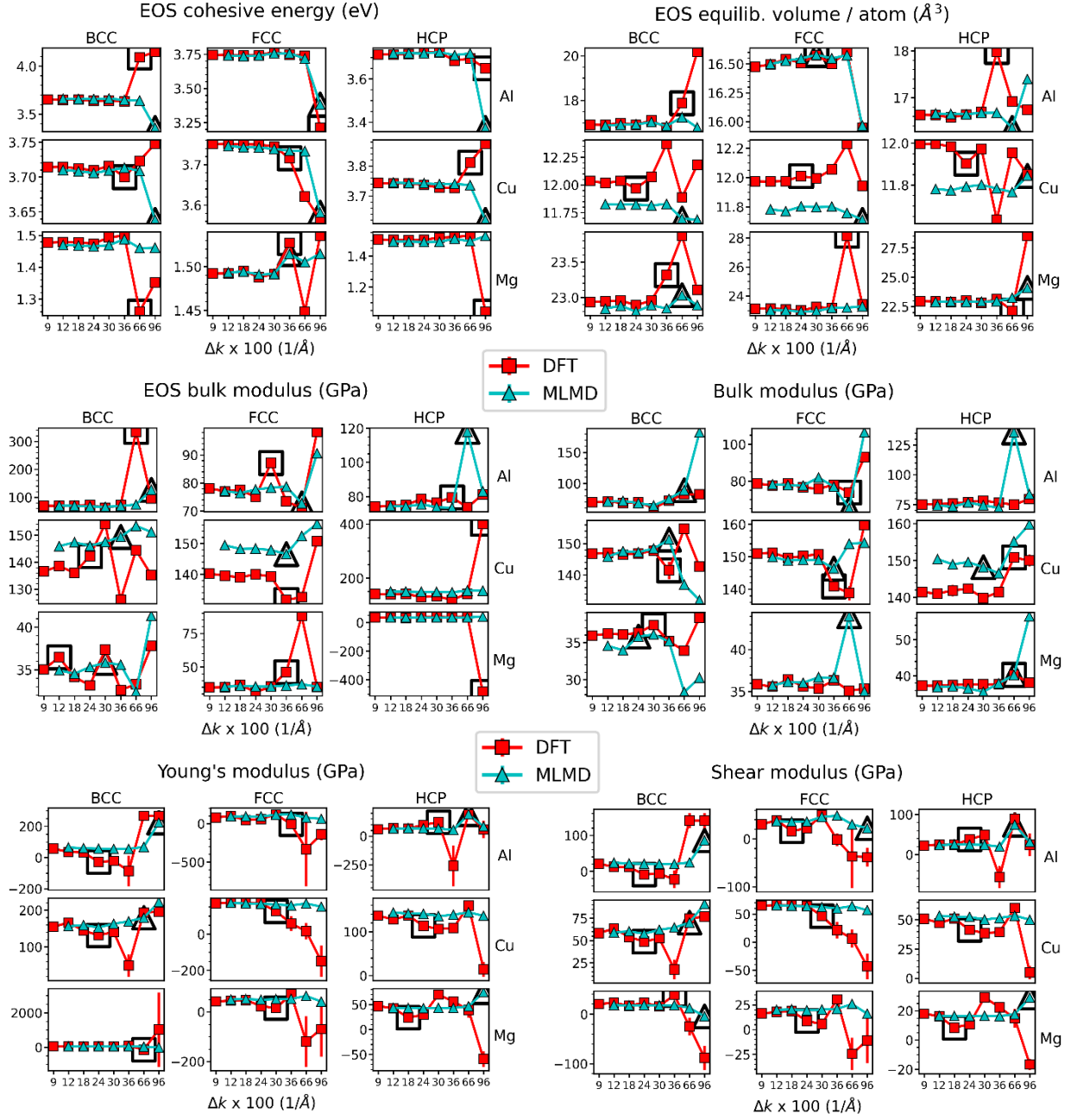


Figure S3. Material properties calculated by both DFT and MLMD plotted as a function of the k-space sampling density parameter Δk . Threshold Δk (Δk_T) where property prediction deviates from that at Δk_{min} by $\frac{1}{2} MAD_{max}$ are highlighted with large black-outlined symbols.

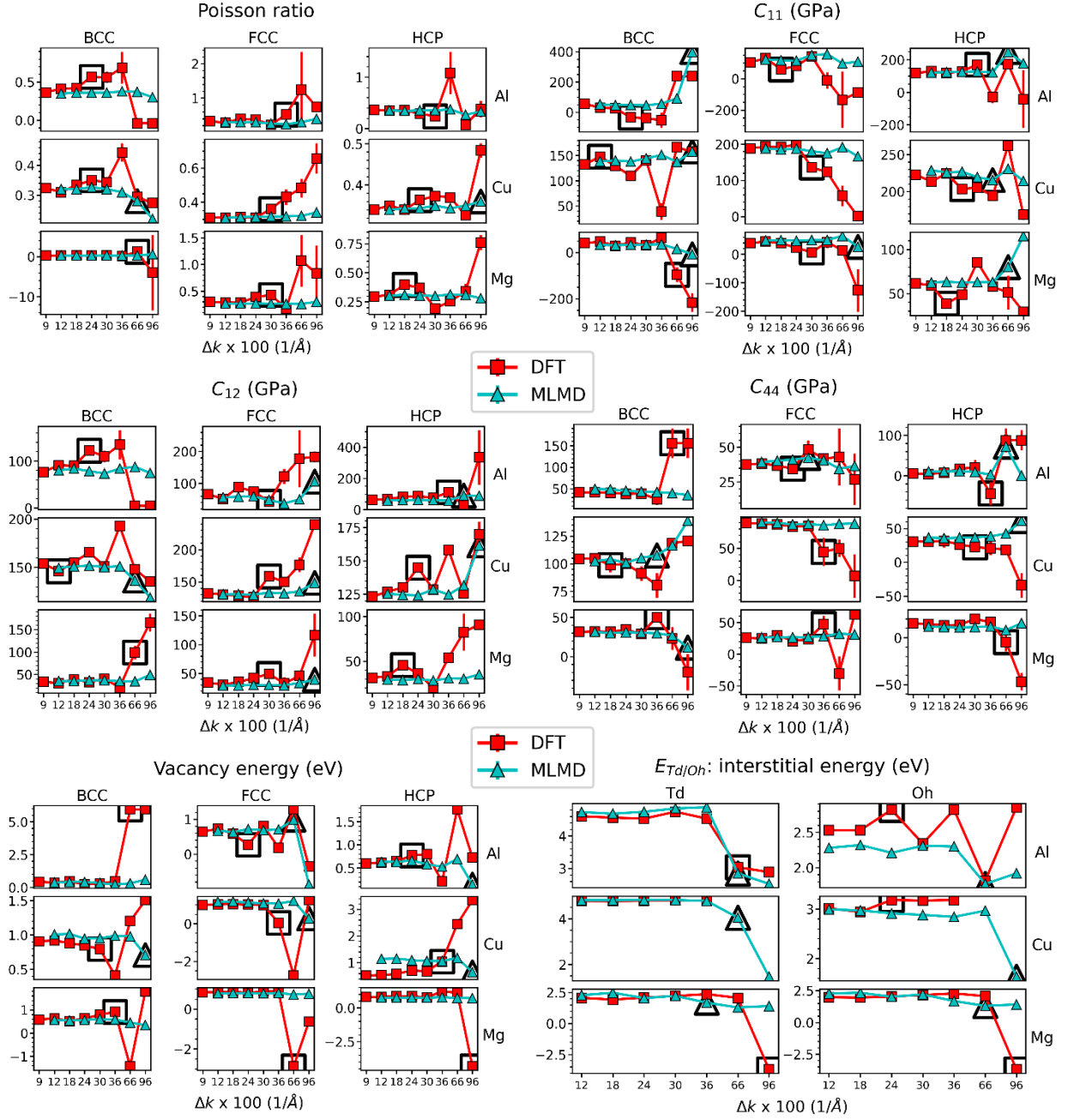


Figure S3 (continued). Additional material properties calculated by both DFT and MLMD plotted versus Δk with Δk_T highlighted by large black-outlined symbols. The interstitial energies were calculated only for equilibrium lattices (FCC-Al, FCC-Cu, HCP-Mg) for each atom type.

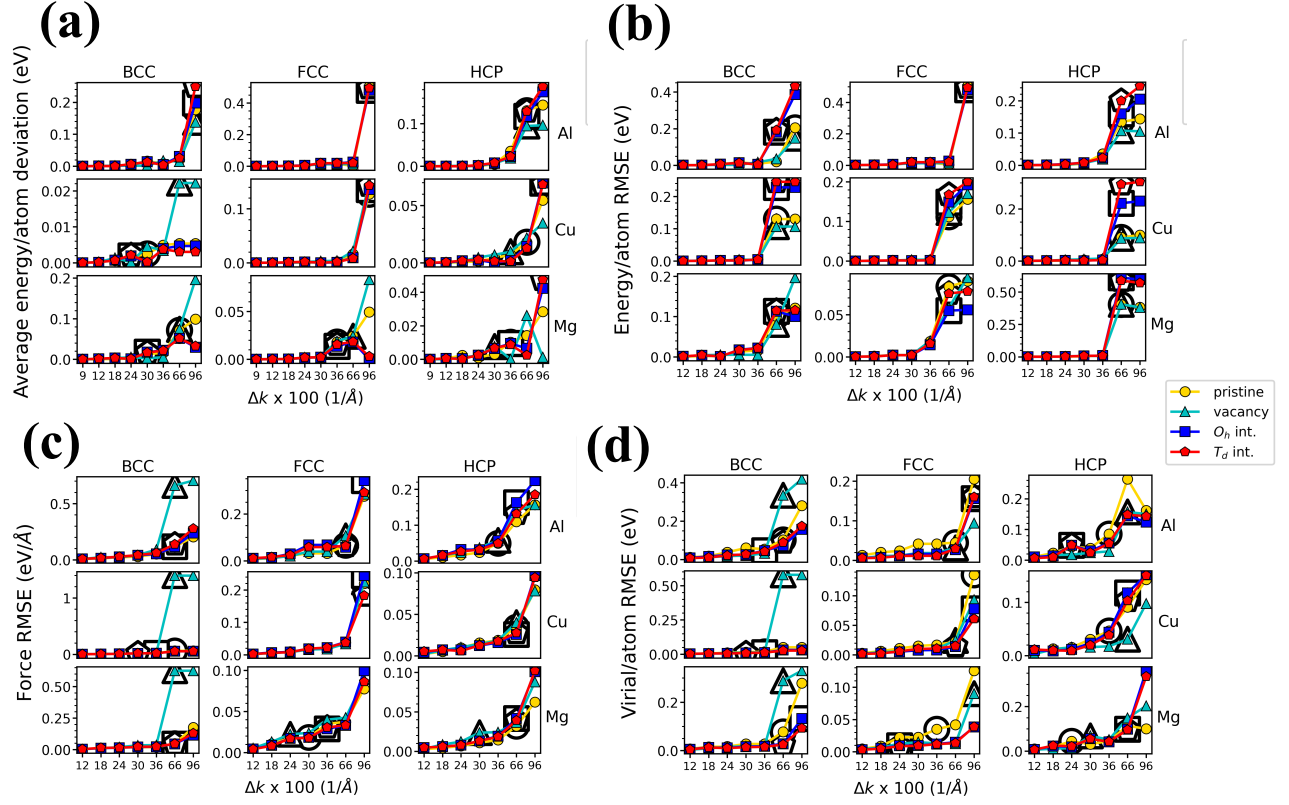


Figure S4. Statistical error metrics (SEMs) of single-point DFT calculations as a function of Δk for the 3600 configurations of the test dataset. The average energy per atom deviation (AEAD) (a), the energy per atom RMSE (E-RMSE) (b), the RMSE of interatomic force components (F-RMSE) (c), and the virial per atom RMSE (V-RMSE) (d). Threshold Δk determined by the $\frac{1}{2} MAD$ criterion is highlighted by large black-outlined symbols.