

Electronic Supplementary Information (ESI)

A sparse modeling for small data: Case studies in controlled syntheses of 2D materials

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†**Note:** All the training and test datasets in Tables S3–S7 are available as csv file.

Characteristics of objective variables in the datasets

Table S1. Characteristics of objective variables in the datasets.

Datasets		$y_1, y_1'' / \%$	$y_2, y_2'' / -$	$y_3, y_3'' / -$
Training	Mean	34.1	0.267	0.266
	SD	21.3	0.115	0.162
	<i>n</i>	30	48	54
Test	Mean	17.4	0.298	0.210
	SD	20.7	0.256	0.167
	<i>n</i>	79	64	43
Merged ^a (Training + Test)	Mean	22.0	0.285	0.241
	SD	22.1	0.208	0.166
	<i>n</i>	109	112	97

^a The merged dataset was used for the 10-segmentalized validation in Fig. 5.

Table S2. Training dataset for y1 (yield).²⁵

No.	x1	x2	x3	x4	x5	x6	x7	x8	x9	x10	x11	x12	x13	x14	x15	x16	x17	x18	x19	x20	x21	x22	x23	x24	x25	x26	x28	x29	x30	x31	x32	x34	x36	x39	x40	y1
y1_train_1	99.1	0.531	-24.4	202	1.03	32.2	0.3	1.67	1.47	40.8	24.7	81.4	91.7	4.30	1.02E-39	18	12.3	7.2	213.4	2.80E-39	1.24	72.2	157.4	286.0	1.95	2.90	0.585	0.93	16.1	2.3	4.1	1.78E-39	3.06	47.5	11.1	13.6
y1_train_2	73.1	0.429	-60.4	153	0.94	36.7	3.7	0.80	1.43	37.1	19.9	75.8	68.1	4.37	7.23E-40	17.4	13.7	11.3	213.4	2.80E-39	1.24	72.2	157.4	286.0	1.95	2.90	0.585	0.93	16.1	2.3	4.1	2.07E-39	3.14	52.3	13.7	22.5
y1_train_3	18.0	0.149	0.0	100	1.00	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	122.2	1.46E-39	1.26	33.9	90.7	107.6	0.78	1.64	0.582	1.27	19.9	7	12.2	1.38E-39	1.17	27.9	32.6	62.1
y1_train_4	41.1	0.319	-43.8	82	0.78	35.9	88.8	0.34	1.34	31.8	10.3	60.2	30.8	3.93	3.89E-40	15.3	18	6.1	122.2	1.46E-39	1.26	33.9	90.7	107.6	0.78	1.64	0.582	1.27	19.9	7	12.2	1.07E-39	2.67	23.7	15.6	10.8
y1_train_5	99.1	0.531	-24.4	202	1.03	32.2	0.3	1.67	1.47	40.8	24.7	81.4	91.7	4.30	1.02E-39	18	12.3	7.2	122.2	1.46E-39	1.26	33.9	90.7	107.6	0.78	1.64	0.582	1.27	19.9	7	12.2	4.43E-40	3.04	9.2	8.2	12.0
y1_train_6	73.1	0.429	-60.4	153	0.94	36.7	3.7	0.80	1.43	37.1	19.9	75.8	68.1	4.37	7.23E-40	17.4	13.7	11.3	122.2	1.46E-39	1.26	33.9	90.7	107.6	0.78	1.64	0.582	1.27	19.9	7	12.2	7.40E-40	3.12	14.0	8.4	52.7
y1_train_7	78.1	0.471	18.5	189	1.10	46.5	0.6	1.99	1.48	45.7	20.1	76.5	53.0	5.16	7.93E-40	18.4	16.4	10.2	122.2	1.46E-39	1.26	33.9	90.7	107.6	0.78	1.64	0.582	1.27	19.9	7	12.2	6.69E-40	3.90	13.8	10.1	36.6
y1_train_8	18.0	0.149	0.0	100	1.00	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	121.2	1.50E-39	1.17	33.4	95.2	114.7	0.80	1.70	0.451	0.92	18.8	4.8	6.6	1.41E-39	1.26	27.4	38.0	10.0
y1_train_9	32.0	0.287	-97.7	65	0.79	32.7	127.0	0.55	1.33	24.0	8.8	56.8	34.0	2.11	2.65E-40	15.1	12.3	22.3	121.2	1.50E-39	1.17	33.4	95.2	114.7	0.80	1.70	0.451	0.92	18.8	4.8	6.6	1.23E-39	0.94	24.6	18.9	14.1
y1_train_10	32.0	0.287	-97.7	65	0.79	32.7	127.0	0.55	1.33	24.0	8.8	56.8	34.0	2.11	2.65E-40	15.1	12.3	22.3	107.2	1.28E-39	1.49	27.4	83.5	96.3	0.70	1.34	0.483	1.41	18.8	4.6	7.1	1.01E-39	0.62	18.6	18.6	21.5
y1_train_11	58.1	0.436	-94.7	58	0.78	20.6	231.1	0.30	1.36	26.2	16.6	73.8	56.0	3.23	5.90E-40	15.5	10.4	7	107.2	1.28E-39	1.49	27.4	83.5	96.3	0.70	1.34	0.483	1.41	18.8	4.6	7.1	6.89E-40	1.74	10.8	8.8	12.2
y1_train_12	99.1	0.531	-24.4	202	1.03	32.2	0.3	1.67	1.47	40.8	24.7	81.4	91.7	4.30	1.02E-39	18	12.3	7.2	125.2	1.28E-39	3.61	30.6	88.1	91.5	0.72	1.58	0.481	1.15	18.7	6.2	7.3	2.60E-40	0.69	5.9	6.3	25.3
y1_train_13	73.1	0.429	-60.4	153	0.94	36.7	3.7	0.80	1.43	37.1	19.9	75.8	68.1	4.37	7.23E-40	17.4	13.7	11.3	125.2	1.28E-39	3.61	30.6	88.1	91.5	0.72	1.58	0.481	1.15	18.7	6.2	7.3	5.56E-40	0.77	10.7	8.9	21.8
y1_train_14	18.0	0.149	0.0	100	1.00	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.32	0.451	1.56	19.6	7.2	13.4	1.28E-39	0.60	26.2	31.3	65.8
y1_train_15	32.0	0.287	-97.7	65	0.79	32.7	127.0	0.55	1.33	24.0	8.8	56.8	34.0	2.11	2.65E-40	15.1	12.3	22.3	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.32	0.451	1.56	19.6	7.2	13.4	1.10E-39	0.27	23.4	13.6	48.8
y1_train_16	46.1	0.411	-114.5	78	0.78	24.6	59.0	1.08	1.36	24.0	13.4	64.4	52.8	1.94	4.56E-40	15.8	8.8	19.4	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.32	0.451	1.56	19.6	7.2	13.4	9.08E-40	0.11	18.8	9.8	45.4
y1_train_17	99.1	0.531	-24.4	202	1.03	32.2	0.3	1.67	1.47	40.8	24.7	81.4	91.7	4.30	1.02E-39	18	12.3	7.2	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.32	0.451	1.56	19.6	7.2	13.4	3.45E-40	2.47	7.5	8.6	57.1
y1_train_18	73.1	0.429	-60.4	153	0.94	36.7	3.7	0.80	1.43	37.1	19.9	75.8	68.1	4.37	7.23E-40	17.4	13.7	11.3	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.32	0.451	1.56	19.6	7.2	13.4	6.42E-40	2.54	12.3	8.1	67.1
y1_train_19	78.1	0.471	18.5	189	1.10	46.5	0.6	1.99	1.48	45.7	20.1	76.5	53.0	5.16	7.93E-40	18.4	16.4	10.2	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.32	0.451	1.56	19.6	7.2	13.4	5.71E-40	3.32	12.0	10.0	73.0
y1_train_20	18.0	0.149	0.0	100	1.00	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	113.2	1.19E-39	2.09	25.9	83.0	74.7	0.60	1.39	0.437	1.23	19.3	5.6	10.1	1.11E-39	0.34	19.9	34.7	59.7
y1_train_21	32.0	0.287	-97.7	65	0.79	32.7	127.0	0.55	1.33	24.0	8.8	56.8	34.0	2.11	2.65E-40	15.1	12.3	22.3	113.2	1.19E-39	2.09	25.9	83.0	74.7	0.60	1.39	0.437	1.23	19.3	5.6	10.1	9.29E-40	0.01	17.2	16.3	21.1
y1_train_22	99.1	0.531	-24.4	202	1.03	32.2	0.3	1.67	1.47	40.8	24.7	81.4	91.7	4.30	1.02E-39	18	12.3	7.2	113.2	1.19E-39	2.09	25.9	83.0	74.7	0.60	1.39	0.437	1.23	19.3	5.6	10.1	1.74E-40	2.21	1.2	7.7	14.3
y1_train_23	73.1	0.429	-60.4	153	0.94	36.7	3.7	0.80	1.43	37.1	19.9	75.8	68.1	4.37	7.23E-40	17.4	13.7	11.3	113.2	1.19E-39	2.09	25.9	83.0	74.7	0.60	1.39	0.437	1.23	19.3	5.6	10.1	4.71E-40	2.28	6.1	9.0	22.1
y1_train_24	78.1	0.471	18.5	189	1.10	46.5	0.6	1.99	1.48	45.7	20.1	76.5	53.0	5.16	7.93E-40	18.4	16.4	10.2	113.2	1.19E-39	2.09	25.9	83.0	74.7	0.60	1.39	0.437	1.23	19.3	5.6	10.1	4.00E-40	3.07	5.8	10.9	15.4
y1_train_25	18.0	0.149	0.0	100	1.00	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	171.2	2.23E-39	1.45	44.4	100.9	146.0	0.83	1.84	0.502	1.26	19.5	4	5.9	2.15E-39	0.98	38.3	39.2	10.4
y1_train_26	32.0	0.287	-97.7	65	0.79	32.7	127.0	0.55	1.33	24.0	8.8	56.8	34.0	2.11	2.65E-40	15.1	12.3	22.3	171.2	2.23E-39	1.45	44.4	100.9	146.0	0.83	1.84	0.502	1.26	19.5	4	5.9	1.97E-39	0.66	35.6	20.4	62.1
y1_train_27	46.1	0.411	-114.5	78	0.78	24.6	59.0	1.08	1.36	24.0	13.4	64.4	52.8	1.94	4.56E-40	15.8	8.8	19.4	171.2	2.23E-39	1.45	44.4	100.9	146.0	0.83	1.84	0.502	1.26	19.5	4	5.9	1.78E-39	0.49	30.9	16.1	32.0
y1_train_28	58.1	0.436	-94.7	58	0.78	20.6	231.1	0.30	1.36	26.2	16.6	73.8	56.0	3.23	5.90E-40	15.5	10.4	7	171.2	2.23E-39	1.45	44.4	100.9	146.0	0.83	1.84	0.502	1.26	19.5	4	5.9	1.64E-39	1.78	27.8	10.3	13.0
y1_train_29	119.4	0.287	-63.5	61	1.48	4.8	194.8	0.54	1.44	29.9	14.3	73.6	15.0	1.53	6.53E-40	17.8	3.1	5.7	171.2	2.23E-39	1.45	44.4	100.9	146.0	0.83	1.84	0.502	1.26	19.5	4	5.9	1.58E-39	0.08	30.1	3.5	55.3
y1_train_30	73.1	0.429	-60.4	153	0.94	36.7	3.7	0.80	1.43	37.1	19.9	75.8	68.1	4.37	7.23E-40	17.4	13.7	11.3	171.2	2.23E-39	1.45	44.4	100.9	146.0	0.83	1.84	0.502	1.26	19.5	4	5.9	1.51E-39	2.93</td			

Table S3. Test dataset of for y_1'' (yield).²⁵

No.	x1	x3	x4	x5	x6	x7	x8	x9	x10	x11	x12	x13	x14	x15	x16	x17	x18	x19	x20	x21	x22	x23	x24	x26	x28	x29	x30	x31	x32	x34	x36	x39	x40	y2
y2_train_1	99.1	-24.4	202	1.03	32.2	0.3	1.67	1.47	40.8	24.7	81.4	91.7	4.30	1.02E-39	18	12.3	7.2	213.4	2.80E-39	1.24	72.2	157.4	286.0	2.90	0.585	0.93	16.1	2.3	4.1	1.78E-39	3.06	47.5	11.14	0.271
y2_train_2	73.1	-60.4	153	0.94	36.7	3.7	0.80	1.43	37.1	19.9	75.8	68.1	4.38	7.23E-40	17.4	13.7	11.3	213.4	2.80E-39	1.24	72.2	157.4	286.0	2.90	0.585	0.93	16.1	2.3	4.1	2.07E-39	3.14	52.3	13.73	0.273
y2_train_3	78.1	18.5	189	1.10	46.5	0.6	1.99	1.48	45.8	20.2	76.5	53.0	5.16	7.93E-40	18.4	16.4	10.2	213.4	2.80E-39	1.24	72.2	157.4	286.0	2.90	0.585	0.93	16.1	2.3	4.1	2.00E-39	3.92	52.0	16.04	0.241
y2_train_4	18.0	0.0	100	1.00	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	122.2	1.46E-39	1.26	33.9	90.7	107.6	1.64	0.582	1.27	19.9	7	12.2	1.38E-39	1.17	27.9	32.63	0.162
y2_train_5	41.1	-43.8	82	0.78	35.9	88.8	0.34	1.34	31.8	10.3	60.2	30.8	3.93	3.89E-40	15.3	18	6.1	122.2	1.46E-39	1.26	33.9	90.7	107.6	1.64	0.582	1.27	19.9	7	12.2	1.07E-39	2.67	23.7	15.58	0.302
y2_train_6	99.1	-24.4	202	1.03	32.2	0.3	1.67	1.47	40.8	24.7	81.4	91.7	4.30	1.02E-39	18	12.3	7.2	122.2	1.46E-39	1.26	33.9	90.7	107.6	1.64	0.582	1.27	19.9	7	12.2	4.43E-40	3.04	9.2	8.22	0.138
y2_train_7	73.1	-60.4	153	0.94	36.7	3.7	0.80	1.43	37.1	19.9	75.8	68.1	4.38	7.23E-40	17.4	13.7	11.3	122.2	1.46E-39	1.26	33.9	90.7	107.6	1.64	0.582	1.27	19.9	7	12.2	7.40E-40	3.12	14.0	8.41	0.150
y2_train_8	78.1	18.5	189	1.10	46.5	0.6	1.99	1.48	45.8	20.2	76.5	53.0	5.16	7.93E-40	18.4	16.4	10.2	122.2	1.46E-39	1.26	33.9	90.7	107.6	1.64	0.582	1.27	19.9	7	12.2	6.69E-40	3.90	13.8	10.07	0.230
y2_train_9	18.0	0.0	100	1.00	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	121.2	1.50E-39	1.17	33.4	95.2	114.7	1.70	0.451	0.92	18.8	4.8	6.6	1.41E-39	1.26	27.4	37.99	0.516
y2_train_10	41.1	-43.8	82	0.78	35.9	88.8	0.34	1.34	31.8	10.3	60.2	30.8	3.93	3.89E-40	15.3	18	6.1	121.2	1.50E-39	1.17	33.4	95.2	114.7	1.70	0.451	0.92	18.8	4.8	6.6	1.41E-39	1.26	27.4	37.99	0.212
y2_train_11	32.0	-97.7	65	0.79	32.7	127.0	0.55	1.33	24.0	8.8	56.8	34.0	2.11	2.65E-40	15.1	12.3	22.3	121.2	1.50E-39	1.17	33.4	95.2	114.7	1.70	0.451	0.92	18.8	4.8	6.6	1.23E-39	0.94	24.6	18.91	0.326
y2_train_12	99.1	-24.4	202	1.03	32.2	0.3	1.67	1.47	40.8	24.7	81.4	91.7	4.30	1.02E-39	18	12.3	7.2	121.2	1.50E-39	1.17	33.4	95.2	114.7	1.70	0.451	0.92	18.8	4.8	6.6	4.81E-40	3.13	8.7	7.69	0.216
y2_train_13	78.1	18.5	189	1.10	46.5	0.6	1.99	1.48	45.8	20.2	76.5	53.0	5.16	7.93E-40	18.4	16.4	10.2	121.2	1.50E-39	1.17	33.4	95.2	114.7	1.70	0.451	0.92	18.8	4.8	6.6	7.07E-40	3.99	13.3	12.17	0.202
y2_train_14	32.0	-97.7	65	0.79	32.7	127.0	0.55	1.33	24.0	8.8	56.8	34.0	2.11	2.65E-40	15.1	12.3	22.3	107.2	1.28E-39	1.49	27.4	83.5	96.3	1.34	0.483	1.41	18.8	4.6	7.1	1.01E-39	0.62	18.6	18.58	0.212
y2_train_15	46.1	-114.5	78	0.78	24.6	59.0	1.08	1.36	24.0	13.4	64.4	52.8	1.94	4.56E-40	15.8	8.8	19.4	107.2	1.28E-39	1.49	27.4	83.5	96.3	1.34	0.483	1.41	18.8	4.6	7.1	8.23E-40	0.45	13.9	14.32	0.453
y2_train_16	58.1	-94.7	58	0.78	20.6	231.1	0.30	1.36	26.2	16.6	73.8	56.0	3.23	5.90E-40	15.5	10.4	7	107.2	1.28E-39	1.49	27.4	83.5	96.3	1.34	0.483	1.41	18.8	4.6	7.1	6.89E-40	1.74	10.8	8.79	0.208
y2_train_17	99.1	-24.4	202	1.03	32.2	0.3	1.67	1.47	40.8	24.7	81.4	91.7	4.30	1.02E-39	18	12.3	7.2	107.2	1.28E-39	1.49	27.4	83.5	96.3	1.34	0.483	1.41	18.8	4.6	7.1	2.60E-40	2.81	2.7	7.87	0.198
y2_train_18	78.1	18.5	189	1.10	46.5	0.6	1.99	1.48	45.8	20.2	76.5	53.0	5.16	7.93E-40	18.4	16.4	10.2	107.2	1.28E-39	1.49	27.4	83.5	96.3	1.34	0.483	1.41	18.8	4.6	7.1	4.86E-40	3.67	7.2	12.23	0.482
y2_train_19	18.0	0.0	100	1.00	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	125.2	1.28E-39	3.61	30.6	88.1	91.5	1.58	0.481	1.15	18.7	6.2	7.3	1.19E-39	1.18	24.6	36.91	0.120
y2_train_20	41.1	-43.8	82	0.78	35.9	88.8	0.34	1.34	31.8	10.3	60.2	30.8	3.93	3.89E-40	15.3	18	6.1	125.2	1.28E-39	3.61	30.6	88.1	91.5	1.58	0.481	1.15	18.7	6.2	7.3	8.90E-40	0.32	20.3	13.67	0.174
y2_train_21	32.0	-97.7	65	0.79	32.7	127.0	0.55	1.33	24.0	8.8	56.8	34.0	2.11	2.65E-40	15.1	12.3	22.3	125.2	1.28E-39	3.61	30.6	88.1	91.5	1.58	0.481	1.15	18.7	6.2	7.3	1.01E-39	1.50	21.8	17.72	0.174
y2_train_22	46.1	-114.5	78	0.78	24.6	59.0	1.08	1.36	24.0	13.4	64.4	52.8	1.94	4.56E-40	15.8	8.8	19.4	125.2	1.28E-39	3.61	30.6	88.1	91.5	1.58	0.481	1.15	18.7	6.2	7.3	8.23E-40	1.67	17.1	13.67	0.300
y2_train_23	73.1	-60.4	153	0.94	36.7	3.7	0.80	1.43	37.1	19.9	75.8	68.1	4.38	7.23E-40	17.4	13.7	11.3	125.2	1.28E-39	3.61	30.6	88.1	91.5	1.58	0.481	1.15	18.7	6.2	7.3	5.56E-40	0.77	10.7	8.89	0.168
y2_train_24	78.1	18.5	189	1.10	46.5	0.6	1.99	1.48	45.8	20.2	76.5	53.0	5.16	7.93E-40	18.4	16.4	10.2	125.2	1.28E-39	3.61	30.6	88.1	91.5	1.58	0.481	1.15	18.7	6.2	7.3	5.56E-40	0.77	10.7	8.89	0.244
y2_train_25	18.0	0.0	100	1.00	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	123.2	1.36E-39	1.83	32.2	89.1	99.3	1.32	0.451	1.56	19.6	7.2	13.4	1.28E-39	0.60	26.2	31.30	0.148
y2_train_26	32.0	-97.7	65	0.79	32.7	127.0	0.55	1.33	24.0	8.8	56.8	34.0	2.11	2.65E-40	15.1	12.3	22.3	123.2	1.36E-39	1.83	32.2	89.1	99.3	1.32	0.451	1.56	19.6	7.2	13.4	1.10E-39	0.27	23.4	13.65	0.155
y2_train_27	46.1	-114.5	78	0.78	24.6	59.0	1.08	1.36	24.0	13.4	64.4	52.8	1.94	4.56E-40	15.8	8.8	19.4	123.2	1.36E-39	1.83	32.2	89.1	99.3	1.32	0.451	1.56	19.6	7.2	13.4	9.08E-40	0.11	18.8	9.81	0.198
y2_train_28	58.1	-94.7	58	0.78	20.6	231.1	0.30	1.36	26.2	16.6	73.8	56.0	3.23	5.90E-40	15.5	10.4	7	123.2	1.36E-39	1.83	32.2	89.1	99.3	1.32	0.451	1.56	19.6	7.2	13.4	7.74E-40	1.39	15.6	10.88	0.345
y2_train_29	72.1	-108.4	66	0.89	7.6	162.1	0.46	1.40	27.0	17.0	71.7	76.4	2.26	7.51E-40	16.8	5.7	8	123.2	1.36E-39	1.83	32.2	89.1	99.3	1.32	0.451	1.56	19.6	7.2	13.4	6.13E-40	0.43	15.2	7.92	0.492
y2_train_30	99.1	-24.4	202	1.03	32.2	0.3	1.67	1.47	40.8	24.7	81.4	91.7	4.30	1.02E-39	18	12.3	7.2	123.2	1.36E-39	1.83	32.2	89.1	99.3	1.32	0.451	1.56	19.6	7.2	13.4	3.45E-40	2.47	7.5	8.64	0.202
y2_train_31	73.1	-60.4	153	0.94	36.7	3.7	0.80	1.43	37.1	19.9	75.8	68.1	4.38	7.23E-40	17.4	13.7	11.3	123.2	1.36E-39	1.83	32.2	89.1	99.3	1.32	0.451	1.56	19.6	7.2	13.4	6.42E-40	2.54	12.3	8.13	0.369
y2_train_32	78.1	18.5	189	1.10	46.5	0.6	1.99	1.48	45.8	20.2	76.5	53.0	5.16	7.93E-40	18.4	16.4	10.2	1																

Table S4. Training dataset for y2 (lateral size).²⁶

No.	x1	x3	x4	x5	x6	x7	x8	x9	x10	x11	x12	x13	x14	x15	x16	x17	x18	x19	x20	x21	x22	x23	x24	x26	x27	x30	x31	x32	x33	x34	x35	x36	x37	x38	x39	x40	x41	y3
y3_train_1	74.1	-95.0	78.0	1.06	7.1	107.2	0.6	1.40	31.2	15.8	71.3	60.8	1.49	6.23E-40	17.3	9.2	8.9	121.2	1.50E-39	1.17	33.4	95.2	114.7	2.14	1.14	18.8	4.8	6.6	-8.77E-40	8.77E-40	0.32	0.32	1.74	-17.6	17.6	5.80	2.75	0.088
y3_train_2	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	122.2	1.41E-39	2.48	31.5	92.0	107.5	1.94	0.94	18.8	7.3	8.8	-4.61E-40	4.61E-40	-0.14	0.14	5.80	-1.1	1.1	6.12	2.75	0.269
y3_train_3	106.1	-26.0	178.0	1.05	17.9	1.5	1.4	1.55	40.7	23.5	79.1	73.1	3.68	1.21E-39	18.9	8	6.2	208.3	2.33E-39	3.25	55.9	132.0	173.7	2.72	1.91	18.2	6	10.2	-1.12E-39	1.12E-39	0.43	0.43	11.97	-32.4	32.4	4.69	3.72	0.026
y3_train_4	102.1	-55.0	242.0	1.20	64.9	11.3	2.8	1.42	40.9	22.8	79.5	67.8	6.19	8.24E-40	17.4	18.6	7.4	150.2	1.63E-39	1.86	37.9	107.2	114.0	2.03	1.22	18.8	5.9	11.2	-8.04E-40	8.04E-40	4.33	4.33	11.51	-15.1	15.1	13.55	3.72	0.045
y3_train_5	41.1	-43.8	81.6	0.78	35.9	88.8	0.3	1.34	31.8	10.3	60.2	30.8	3.93	3.89E-40	15.3	18	6.1	252.2	3.20E-39	5.67	63.8	132.6	129.7	2.55	1.74	21.8	18.9	15.5	-2.81E-39	2.81E-39	-1.74	1.74	22.26	-53.6	53.6	16.07	3.72	0.112
y3_train_6	102.1	-55.0	242.0	1.20	64.9	11.3	2.8	1.42	40.9	22.8	79.5	67.8	6.19	8.24E-40	17.4	18.6	7.4	208.3	2.33E-39	3.25	55.9	132.0	173.7	2.71	1.90	18.2	6	10.2	-1.15E-39	1.15E-39	2.94	2.94	20.13	-33.0	33.0	13.01	3.72	0.265
y3_train_7	61.1	10.5	171.1	1.01	37.7	0.5	19.0	1.45	48.9	18.5	72.7	64.5	1.22	5.64E-40	17.8	10.3	21.3	154.1	1.39E-39	5.15	37.3	96.6	82.5	1.11	0.30	20.6	9.5	18.8	-8.31E-40	8.31E-40	-3.93	3.93	6.26	-18.8	18.8	6.18	3.72	0.266
y3_train_8	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	130.2	1.40E-39	1.93	38.2	106.4	135.4	2.17	1.36	16.3	5.4	11	-4.51E-40	4.51E-40	0.41	0.41	4.52	-7.8	7.8	4.38	3.72	0.286
y3_train_9	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	150.2	1.63E-39	1.86	37.9	107.2	114.0	2.12	1.31	18.8	5.9	11.2	-6.83E-40	6.83E-40	0.48	0.48	4.35	-7.5	7.5	7.18	3.72	0.288
y3_train_10	102.1	-55.0	242.0	1.20	64.9	11.3	2.8	1.42	40.9	22.8	79.5	67.8	6.19	8.24E-40	17.4	18.6	7.4	252.2	3.20E-39	5.67	63.8	132.6	129.7	2.55	1.74	21.8	18.9	15.5	-2.37E-39	2.37E-39	0.52	0.52	35.09	-41.0	41.0	11.96	3.72	0.31
y3_train_11	106.1	-26.0	178.0	1.05	17.9	1.5	1.4	1.55	40.7	23.5	79.1	73.1	3.68	1.21E-39	18.9	8	6.2	150.2	1.63E-39	1.86	37.9	107.2	114.0	2.12	1.31	18.8	5.9	11.2	-4.17E-40	4.17E-40	1.82	1.82	6.84	-14.4	14.4	5.43	3.72	0.328
y3_train_12	90.1	-70.0	135.1	0.93	29.6	0.1	1.8	1.41	28.2	26.6	87.6	93.7	0.47	8.98E-40	16.2	8.1	13.9	137.2	1.59E-39	1.33	36.8	96.6	118.1	1.75	1.04	19	6.5	8	-6.88E-40	6.88E-40	-0.87	0.87	0.63	-10.2	10.2	8.29	3.66	0.133
y3_train_13	84.2	6.5	80.7	0.78	2.0	1.3	1.0	1.43	27.6	22.6	74.6	110.7	0.00	1.07E-39	16.6	0.1	0.1	137.2	1.59E-39	1.33	36.8	96.6	118.1	1.79	1.08	19	6.5	8	-5.14E-40	5.14E-40	-1.33	1.33	0.00	-14.2	14.2	11.24	3.66	0.139
y3_train_14	88.1	-83.6	77.1	0.89	6.0	94.5	0.4	1.37	26.3	22.6	80.7	78.0	4.95	8.45E-40	15.8	5.3	7.2	269.5	3.57E-39	1.24	91.4	188.0	361.0	3.26	2.55	16	1.8	3.4	-2.72E-39	2.72E-39	3.71	3.71	6.12	-68.9	68.9	5.18	3.66	0.147
y3_train_15	106.1	-26.0	178.0	1.05	17.9	1.5	1.4	1.55	40.7	23.5	79.1	73.1	3.68	1.21E-39	18.9	8	6.2	133.2	1.77E-39	1.79	36.2	96.7	118.4	1.76	1.04	18.9	4.5	6.2	-5.59E-40	5.59E-40	1.89	1.89	6.59	-12.7	12.7	3.55	3.66	0.153
y3_train_16	76.1	-85.1	124.5	0.97	16.9	8.3	1.7	1.40	33.3	21.8	79.8	75.0	0.34	7.01E-40	16.4	9.2	15.8	125.2	1.34E-39	5.14	33.0	96.2	114.8	0.86	0.15	18.3	8.5	8.3	-6.35E-40	6.35E-40	-4.80	4.80	1.75	-11.2	11.2	8.44	3.66	0.192
y3_train_17	73.1	-60.4	153.0	0.94	36.7	3.7	0.8	1.43	37.1	19.9	75.8	68.1	4.38	7.23E-40	17.4	13.7	11.3	269.5	3.57E-39	1.24	91.4	188.0	361.0	3.26	2.55	16	1.8	3.4	-2.85E-39	2.85E-39	3.14	3.14	5.41	-71.5	71.5	14.56	3.66	0.204
y3_train_18	108.1	-15.5	205.4	1.04	11.9	0.1	5.6	1.54	38.3	24.5	78.9	87.3	2.06	1.21E-39	18.4	6.3	13.7	125.2	1.34E-39	5.14	33.0	96.2	114.8	0.86	0.15	18.3	8.5	8.3	-1.28E-40	1.28E-40	-3.08	3.08	10.62	-8.5	8.5	5.83	3.66	0.25
y3_train_19	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	121.2	1.50E-39	1.17	33.4	95.2	114.7	2.20	1.41	18.9	4.8	6.6	-5.55E-40	5.55E-40	1.17	1.17	2.74	-3.0	3.0	5.73	5.79	0.12
y3_train_20	106.1	-26.0	178.0	1.05	17.9	1.5	1.4	1.55	40.7	23.5	79.1	73.1	3.68	1.21E-39	18.9	8	6.2	121.2	1.50E-39	1.17	33.4	95.2	114.7	2.20	1.41	18.8	4.8	6.6	-2.89E-40	2.89E-40	2.51	2.51	4.30	-9.9	9.9	3.23	5.79	0.153
y3_train_21	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	125.2	1.34E-39	5.14	33.0	96.2	114.8	2.84	2.05	18.3	8.5	8.3	-3.90E-40	3.90E-40	-2.80	2.80	12.05	-2.6	2.6	5.47	5.79	0.186
y3_train_22	18.0	0.0	100.0	1.00	78.5	23.8	0.9	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	108.1	1.13E-39	8.06	29.3	89.0	51.7	0.80	0.00	19.4	20.5	14.5	-1.04E-39	1.04E-39	-5.63	5.63	19.59	-23.3	23.3	29.22	5.79	0.075
y3_train_23	60.1	97.2	80.8	20.8	19.0	1.9	1.39	25.3	18.3	72.2	71.6	1.84	6.40E-40	15.7	6.8	17.4	122.2	1.46E-39	1.26	33.9	90.7	107.6	1.60	0.67	19.9	7	12.2	-8.20E-40	8.20E-40	0.59	0.59	2.32	-15.7	15.7	9.88	1.5	0.038	
y3_train_24	74.1	-89.5	117.3	0.81	17.8	0.1	3.0	1.40	27.2	23.0	79.9	70.3	1.84	8.26E-40	16	5.7	15.8	122.2	1.46E-39	1.26	33.9	90.7	107.6	1.60	0.67	19.9	7	12.2	-6.34E-40	6.34E-40	0.62	0.62	2.36	-10.9	10.9	8.69	1.5	0.038
y3_train_25	108.1	-15.5	205.4	1.04	11.9	0.1	5.6	1.54	38.3	24.5	78.9	87.3	2.06	1.21E-39	18.4	6.3	13.7	122.2	1.46E-39	1.26	33.9	90.7	107.6	1.60	0.67	19.9	7	12.2	-2.53E-40	2.53E-40	0.81	0.81	2.59	-9.4	9.4	3.43	1.5	0.045
y3_train_26	62.1	-12.6	197.9	1.11	41.4	0.1	23.5	1.43	48.4	17.2	71.6	56.3	0.00	5.03E-40	17.8	13.5	27.4	122.2	1.46E-39	1.26	33.9	90.7	107.6	1.60	0.67	19.9	7	12.2	-9.57E-40	9.57E-40	-1.26	1.26	2.00	-16.7	16.7	17.06	1.5	0.053
y3_train_27	61.1	10.5	171.1	1.01	37.7	0.5	19.0	1.45	48.9	18.5	72.7	64.5	1.22	5.64E-40	17.8	10.3	21.3	122.2	1.46E-39	1.26	33.9	90.7	107.6	1.60	0.67	19.9	7	12.2	-8.96E-40	8.96E-40	-0.04	0.04	1.53	-15.5	15.5	10.55	1.5	0.054
y3_train_28	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	101.2	1.26E-39	1.24	33.7	96.0	136.0	1.86	0.93	16	3.9	7.5	-3.19E-40	3.19E-40	1.10	1.10	2.91	-3.4	3.4	2.25	1.5	0.078
y3_train_29	106.1	-11.5																																				

Table S5. Test dataset of for y_2'' (lateral size).²⁶

Sample No.	x1	x2	x3	x4	x5	x6	x7	x8	x9	x10	x11	x12	x13	x14	x15	x16	x17	x18	x19	x20	x21	x22	x23	x24	x25	x26	x28	x29	x30	x31	x32	x34	x36	x39	x40	y1
y1,test,1	108	0.698	-15.5	205.4	1.04	11.92	0.12	5.58	1.54	38.3	24.5	78.9	87.3	2.06	1.21E-39	18.4	6.3	13.7	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.28	0.58	1.56	19.6	7.2	13.4	1.57E-40	0.23	7.67	2.58	28.12
y1,test,2	61	0.698	10.5	171.1	1.01	37.72	0.53	18.95	1.45	48.9	27.7	72.6	64.5	1.22	5.64E-40	17.8	10.3	21.3	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.28	0.58	1.56	19.6	7.2	13.4	8.00E-40	0.62	4.48	2.29	65.27
y1,test,3	108	0.698	-15.5	205.4	1.04	11.92	0.12	5.58	1.54	38.3	24.5	78.9	87.3	2.06	1.21E-39	18.4	6.3	13.7	122.2	1.46E-39	1.26	33.9	90.7	107.6	0.78	1.36	0.55	1.27	19.9	7	13.2	2.55E-40	0.81	9.41	3.43	26.46
y1,test,4	61	0.525	10.5	171.1	1.01	37.72	0.53	18.95	1.45	48.9	27.7	72.6	64.5	1.22	5.64E-40	17.8	10.3	21.3	122.2	1.46E-39	1.26	33.9	90.7	107.6	0.78	1.36	0.55	1.27	19.9	7	12.2	8.98E-40	0.04	6.23	10.55	59.92
y1,test,5	62	0.512	-12.6	197.9	1.11	41.40	0.07	23.50	1.43	48.4	17.2	71.6	56.3	0.00	5.03E-40	17.8	13.5	27.4	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.28	0.58	1.56	19.6	7.2	13.4	8.62E-40	1.83	14.94	15.77	74.18
y1,test,6	76	0.637	-85.1	124.5	0.97	16.93	8.3	1.71	1.40	33.3	21.8	79.8	75.0	0.34	7.01E-40	16.4	9.2	15.8	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.28	0.58	1.56	19.6	7.2	13.4	6.64E-40	1.49	10.43	7.12	44.17
y1,test,7	62	0.512	-12.6	197.9	1.11	41.40	0.07	23.50	1.43	48.4	17.2	71.6	56.3	0.00	5.03E-40	17.8	13.5	27.4	122.2	1.46E-39	1.26	33.9	90.7	107.6	0.78	1.36	0.55	1.27	19.9	7	12.2	9.60E-40	1.26	16.69	17.06	43.82
y1,test,8	60	0.539	-126.5	97.2	0.80	20.80	19	1.95	1.39	25.3	18.3	72.2	71.6	1.84	6.40E-40	15.7	6.8	17.4	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.28	0.58	1.56	19.6	7.2	13.4	7.25E-40	0.01	13.94	8.77	33.06
y1,test,9	108	0.698	-15.5	205.4	1.04	11.92	0.12	5.58	1.54	38.3	24.5	78.9	87.3	2.06	1.21E-39	18.4	6.3	13.7	137.2	1.59E-39	1.33	36.8	96.6	118.1	0.79	1.59	0.86	2.05	19	6.5	8	3.78E-40	0.73	12.27	5.83	18.68
y1,test,10	108	0.698	-15.5	205.4	1.04	11.92	0.12	5.58	1.54	38.3	24.5	78.9	87.3	2.06	1.21E-39	18.4	6.3	13.7	125.2	1.34E-39	5.14	33.0	96.2	114.8	0.86	1.07	0.29	1.65	18.3	8.3	1.28E-40	3.08	8.48	5.83	23.42	
y1,test,11	84	0.503	6.5	80.7	0.78	2.02	1.27	0.98	1.43	27.6	22.6	74.6	110.7	0.00	1.07E-39	16.6	0.1	0.1	137.2	1.59E-39	1.33	36.8	96.6	118.1	0.79	1.59	0.86	2.05	19	6.5	8	5.14E-40	1.33	14.22	11.24	0.32
y1,test,12	100	0.965	-90.6	98.4	0.68	1.92	46	0.42	1.38	22.1	33.8	96.2	143.0	0.06	1.34E-39	15.3	0	0	125.2	1.28E-39	6.31	30.6	88.1	91.5	0.72	1.75	0.63	1.15	18.7	6.2	7.3	5.84E-41	3.55	3.23	11.75	0.79
y1,test,13	78	0.489	5.5	80.1	0.88	2.28	133	0.65	1.50	31.5	16.8	68.8	66.1	0.00	9.43E-40	18.4	0	2	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.28	0.58	1.56	19.6	7.2	13.4	8.62E-40	1.83	15.40	13.70	1.46
y1,test,14	84	0.503	6.5	80.7	0.78	2.02	1.27	0.98	1.43	27.6	22.6	74.6	110.7	0.00	1.07E-39	16.6	0.1	0.1	125.2	1.34E-39	5.14	33.0	96.2	114.8	0.86	1.07	0.29	1.65	18.3	8.3	2.64E-40	5.14	10.43	12.22	0.9	
y1,test,15	100	0.965	-90.6	98.4	0.68	1.92	46	0.42	1.38	22.1	33.8	96.2	143.0	0.06	1.34E-39	15.3	0	0	137.2	1.59E-39	1.33	36.8	96.6	118.1	0.79	1.59	0.86	2.05	19	6.5	8	2.48E-40	1.28	2.99	12.69	0.04
y1,test,16	100	0.965	-90.6	98.4	0.68	1.92	46	0.42	1.38	22.1	33.8	96.2	143.0	0.06	1.34E-39	15.3	0	0	125.2	1.34E-39	5.14	33.0	96.2	114.8	0.86	1.07	0.29	1.65	18.3	8.3	2.13E-42	5.09	0.80	13.31	0.43	
y1,test,17	84	0.503	6.5	80.7	0.78	2.02	1.27	0.98	1.43	27.6	22.6	74.6	110.7	0.00	1.07E-39	16.6	0.1	0.1	122.2	1.46E-39	1.26	33.9	90.7	107.6	0.78	1.36	0.55	1.27	19.9	7	12.2	3.92E-40	1.26	11.36	15.41	3.12
y1,test,18	84	0.503	6.5	80.7	0.78	2.02	1.27	0.98	1.43	27.6	22.6	74.6	110.7	0.00	1.07E-39	16.6	0.1	0.1	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.28	0.58	1.56	19.6	7.2	13.4	2.94E-40	1.83	9.62	16.23	1.34
y1,test,19	100	0.965	-90.6	98.4	0.68	1.92	46	0.42	1.38	22.1	33.8	96.2	143.0	0.06	1.34E-39	15.3	0	0	122.2	1.46E-39	1.26	33.9	90.7	107.6	0.78	1.36	0.55	1.27	19.9	7	12.2	1.25E-40	1.20	0.13	16.81	1.3
y1,test,20	100	0.965	-90.6	98.4	0.68	1.92	46	0.42	1.38	22.1	33.8	96.2	143.0	0.06	1.34E-39	15.3	0	0	123.2	1.36E-39	1.83	32.2	89.1	99.3	0.77	1.28	0.58	1.56	19.6	7.2	13.4	2.72E-41	1.77	1.62	17.47	0.04
y1,test,21	108	0.698	-15.5	205.4	1.04	11.92	0.12	5.58	1.54	38.3	24.5	78.9	87.3	2.06	1.21E-39	18.4	6.3	13.7	137.2	1.59E-39	1.33	36.8	96.6	118.1	0.79	1.59	0.86	2.05	19	6.5	8	3.78E-40	0.73	12.27	5.83	28.77
y1,test,22	108	0.698	-15.5	205.4	1.04	11.92	0.12	5.58	1.54	38.3	24.5	78.9	87.3	2.06	1.21E-39	18.4	6.3	13.7	125.2	1.34E-39	5.14	33.0	96.2	114.8	0.86	1.06	0.26	1.93	18.3	8.3	1.28E-40	3.08	8.48	5.83	5.51	
y1,test,23	76	0.637	-85.1	124.5	0.97	16.93	8.3	1.71	1.40	33.3	21.8	79.8	75.0	0.34	7.01E-40	16.4	9.2	15.8	125.2	1.46E-39	5.14	33.0	96.2	114.8	0.86	1.06	0.26	1.93	18.3	8.3	6.35E-40	4.80	11.25	8.44	22.86	
y1,test,24	61	0.525	10.5	171.1	1.01	37.72	0.53	18.95	1.45	48.9	27.7	72.6	64.5	1.22	5.64E-40	17.8	10.3	21.3	125.2	1.34E-39	5.14	33.0	96.2	114.8	0.86	1.06	0.26	1.93	18.3	8.3	7.71E-40	3.93	5.30	13.16	4.58	
y1,test,25	90	0.766	-70.0	135.1	0.93	29.60	0.05	1.80	1.41	38.3	24.5	78.9	87.3	2.06	1.21E-39	18.4	12.2	31.3	213.2	1.28E-39	1.79	36.2	96.6	118.1	0.79	1.59	0.86	2.05	19	6.5	8	3.08E-40	3.35	49.40	11.13	49.08
y1,test,26	108	0.698	-15.5	205.4	1.04	11.92	0.12	5.58	1.54	38.3	24.5	78.9	87.3	2.06	1.21E-39	18.4	6.3	13.7	137.2	1.59E-39	1.33	36.8	96.6	118.1	0.79	1.59	0.86	2.05	19	6.5	8	3.92E-40	5.14	16.22	10.58	0.32
y1,test,27	84	0.489	5.5	80.1	0.88	2.28	133	0.65	1.50	31.5	16.8	68.8	66.1	0.00	9.43E-40	18.4	0	2	125.2	1.34E-39	5.14	33.0	96.2	114.8	0.86	1.06	0.26	1.93	18.3	8.3	4.38E-40	4.68	6.41	7.01	38.28	
y1,test,28	108	0.698	-15.5	205.4	1.04	11.92	0.12	5.58	1.54	38.3	24.5	78.9	87.3	2.06	1.21E-39	18.4	6.3	13.7	121.2	1.50E-39	1.71	33.4	96.2	114.7	0.86	1.06	0.26	1.93	18.3	8.3	2.93E-40	0.89	8.88	7.30	46.75	
y1,test,29	74	0.665	-89.5	117.3	0.81	17.84	0.06	3.00	1.40	27.2	23.0	79.9	90.3	1.88	8.26E-40	16	5.7	15.8	125.2	1.34E-39	5.14	33.0	96.2	114.8	0.86	1.06	0.26	1.93	18.3	8.3	5.09E-40	3.27	9.97	9.23	25.26	
y1,test,30	60	0.539	-126.5	97.2	0.80	20.80	19	1.95	1.39	25.3	18.3	72.2	71.6	1.84	6.40E-40	17.8	10.3	21.3	137.2	1.59E-39	1.33	36.8	96.6	118.1	0.79	1.59	0.86	2.05	19	6.5	8	1.02E-39	0.12	9.09	14.04	3.74

Table S6. Training dataset for y_3 (lateral-size distribution).²⁷

No.	x1	x3	x4	x5	x6	x7	x8	x9	x10	x11	x12	x13	x14	x15	x16	x17	x18	x19	x20	x21	x22	x23	x24	x26	x28	x29	x30	x31	x32	x34	x36	x39	x40	y2
y2_test_1	72.1	-108.4	66.0	0.89	7.6	162.1	0.5	1.40	27.0	17.0	71.6	76.4	2.26	7.51E-40	16.8	5.7	8	133.2	1.77E-39	1.79	36.2	96.7	118.4	1.85	0.25	0.45	18.6	4.5	6.2	1.02E-39	0.47	19.2	4.20	1.13
y2_test_2	106.1	-26.0	178.0	1.05	17.9	1.5	1.4	1.55	40.7	23.5	79.1	73.1	3.68	1.21E-39	18.9	8	6.2	107.2	1.28E-39	1.49	27.4	83.5	96.3	1.70	0.55	0.90	18.8	4.6	7.1	6.82E-41	2.19	3.9	3.52	0.182
y2_test_3	106.2	-95.0	136.2	0.87	2.5	9.0	0.6	1.50	29.2	25.5	79.2	102.8	0.48	1.34E-39	17.6	2.3	3	133.2	1.77E-39	1.79	36.2	96.7	118.4	1.85	0.25	0.45	18.6	4.5	6.2	4.27E-40	1.32	10.7	4.37	0.233
y2_test_4	74.1	-95.0	78.0	1.06	7.1	107.2	0.6	1.40	31.2	15.8	71.3	60.8	1.49	6.23E-40	17.3	9.2	8.9	171.2	2.23E-39	1.45	44.4	100.9	146.0	1.81	0.49	1.15	19.5	4	5.9	1.61E-39	0.04	28.5	7.44	0.308
y2_test_5	72.1	-108.4	66.0	0.89	7.6	162.1	0.5	1.40	27.0	17.0	71.6	76.4	2.26	7.51E-40	16.8	5.7	8	127.2	1.38E-39	2.15	33.0	92.5	93.6	1.53	0.44	1.06	18.9	5.3	9.9	6.34E-40	0.11	13.8	4.63	0.352
y2_test_6	106.1	-26.0	178.0	1.05	17.9	1.5	1.4	1.55	40.7	23.5	79.1	73.1	3.68	1.21E-39	18.9	8	6.2	113.2	1.19E-39	2.09	25.9	83.0	74.7	1.46	0.46	1.08	19.3	5.6	10.1	1.70E-41	1.59	2.5	4.65	0.434
y2_test_7	106.1	-26.0	178.0	1.05	17.9	1.5	1.4	1.55	40.7	23.5	79.1	73.1	3.68	1.21E-39	18.9	8	6.2	121.2	1.50E-39	1.17	33.4	95.2	114.7	1.87	0.40	0.62	18.8	4.8	6.6	2.89E-40	2.51	9.9	3.23	0.334
y2_test_8	72.1	-108.4	66.0	0.89	7.6	162.1	0.5	1.40	27.0	17.0	71.6	76.4	2.26	7.51E-40	16.8	5.7	8	241.5	3.35E-39	1.18	36.2	84.0	22.0	0.27	0.65	16.1	1.5	3	2.60E-39	1.08	70.2	6.68	0.264	
y2_test_9	74.1	-95.0	78.0	1.06	7.1	107.2	0.6	1.40	31.2	15.8	71.3	60.8	1.49	6.23E-40	17.3	9.2	8.9	107.2	1.28E-39	1.49	27.4	83.5	96.3	1.70	0.55	0.90	18.8	4.6	7.1	6.56E-40	0.00	11.5	5.78	0.354
y2_test_10	74.1	-95.0	78.0	1.06	7.1	107.2	0.6	1.40	31.2	15.8	71.3	60.8	1.49	6.23E-40	17.3	9.2	8.9	122.2	1.46E-39	1.26	33.9	90.7	107.6	1.60	0.57	1.18	19.9	7	12.2	8.40E-40	0.23	18.1	6.54	0.592
y2_test_11	45.0	2.6	210.0	1.14	111.0	0.1	2.9	1.45	58.2	10.1	60.2	31.1	4.24	3.43E-40	17.3	18.7	19.3	108.1	8.06	29.3	89.0	57.1	0.92	0.07	0.66	20.5	14.5	7.87E-40	3.83	19.2	6.63	0.179		
y2_test_12	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	125.2	1.34E-39	5.14	33.0	96.2	114.8	1.06	0.20	1.18	18.3	8.5	8.3	3.90E-40	2.80	2.6	5.47	0.163
y2_test_13	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	131.2	1.19E-39	2.18	42.0	114.4	158.2	1.94	0.45	0.72	16.1	5.1	7	5.91E-40	0.16	11.6	0.97	0.31
y2_test_14	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	269.5	3.57E-39	1.24	91.4	188.0	361.0	3.43	0.58	0.85	16	1.8	3.4	2.62E-39	1.10	61.1	5.34	0.312
y2_test_15	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	101.2	1.26E-39	1.24	33.7	96.0	136.0	1.85	0.44	0.58	16	3.9	7.5	3.19E-40	1.10	3.4	2.25	0.189
y2_test_16	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	137.2	1.59E-39	1.33	36.8	96.6	118.1	1.53	0.46	1.17	19	6.5	8	6.40E-40	1.01	6.4	6.16	0.194
y2_test_17	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	125.2	1.28E-39	3.61	30.6	88.1	91.5	1.77	0.49	0.88	18.7	6.2	7.3	3.34E-40	1.27	0.2	5.44	0.117
y2_test_18	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	241.5	3.35E-39	1.18	87.3	178.6	342.0	2.20	0.27	0.65	16.1	1.5	3	2.40E-39	1.16	56.9	5.83	0.2
y2_test_19	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	127.2	1.38E-39	2.15	30.9	92.5	93.6	1.53	0.44	1.06	18.9	5.3	9.9	4.40E-40	0.19	0.5	6.66	0.118
y2_test_20	45.0	2.6	210.0	1.14	111.0	0.1	2.9	1.45	58.2	10.1	60.2	31.1	4.24	3.43E-40	17.3	18.7	19.3	105.1	1.01E-39	3.20	31.1	94.9	105.4	1.01	0.07	0.19	17.6	10.6	20.9	6.65E-40	1.04	21.0	8.28	0.292
y2_test_21	106.1	-26.0	178.0	1.05	17.9	1.5	1.4	1.55	40.7	23.5	79.1	73.1	3.68	1.21E-39	18.9	8	6.2	171.2	2.23E-39	1.45	44.4	100.9	146.0	1.90	0.35	1.51	19.5	4	5.9	1.02E-39	2.23	20.9	4.19	0.53
y2_test_22	72.1	-108.4	66.0	0.89	7.6	162.1	0.5	1.40	27.0	17.0	71.6	76.4	2.26	7.51E-40	16.8	5.7	8	133.2	1.77E-39	1.79	36.2	96.7	118.4	1.76	0.37	1.38	18.6	4.5	6.2	1.02E-39	0.47	19.2	4.20	0.5
y2_test_23	106.2	-95.0	136.2	0.87	2.5	9.0	0.6	1.50	29.2	25.5	79.2	102.8	0.48	1.34E-39	17.6	2.3	3	133.2	1.77E-39	1.79	36.2	96.7	118.4	1.76	0.37	1.38	18.6	4.5	6.2	4.27E-40	1.32	10.7	4.37	0.284
y2_test_24	74.1	-95.0	78.0	1.06	7.1	107.2	0.6	1.40	31.2	15.8	71.3	60.8	1.49	6.23E-40	17.3	9.2	8.9	171.2	2.23E-39	1.45	44.4	100.9	146.0	1.90	0.35	1.51	19.5	4	5.9	1.61E-39	0.04	28.5	7.44	0.817
y2_test_25	106.1	-26.0	178.0	1.05	17.9	1.5	1.4	1.55	40.7	23.5	79.1	73.1	3.68	1.21E-39	18.9	8	6.2	133.2	1.77E-39	1.79	36.2	96.7	118.4	1.76	0.37	1.38	18.6	4.5	6.2	5.59E-40	1.89	12.7	3.55	0.153
y2_test_26	74.1	-95.0	78.0	1.06	7.1	107.2	0.6	1.40	31.2	15.8	71.3	60.8	1.49	6.23E-40	17.3	9.2	8.9	133.2	1.77E-39	1.79	36.2	96.7	118.4	1.76	0.37	1.38	18.6	4.5	6.2	1.15E-39	0.31	20.4	6.01	0.175
y2_test_27	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	122.2	1.41E-39	2.48	31.5	92.0	107.5	0.99	0.17	1.42	18.8	7.3	8.8	4.61E-40	0.14	1.1	6.12	0.046
y2_test_28	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	101.2	1.26E-39	1.24	33.7	96.0	136.0	1.00	0.14	0.97	16	3.9	7.5	3.19E-40	1.10	3.4	2.25	0.023
y2_test_29	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	213.4	2.80E-39	1.24	72.2	157.4	286.0	2.81	0.64	2.14	16.1	2.3	4.1	1.85E-39	1.10	41.8	4.53	0.092
y2_test_30	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	101.2	1.26E-39	1.24	33.7	96.0	136.0	1.00	0.14	0.97	16	3.9	7.5	3.19E-39	1.10	41.8	4.53	0.092
y2_test_31	106.1	-11.5	245.0	1.11	31.1	0.0	32.0	1.45	47.0	30.4	94.9	97.3	2.34	9.45E-40	16	6	6.7	133.2	1.77E-39	1.79	36.2	96.7	118.4	1.76	0.37	1.38	18.6	4.5	6.2	8.25E-40	0.55	5.8	5.44	0.221
y2_test_32	45.0	2.6	210.0	1.14	111.0	0.1	2.9	1.45	58.2	10.1	60.2	31.1	4.24	3.43E-40	17.3	18.7	19.3	106.1	3.57E-39	1.24	6.7	131.2	1.54E-39	2.18	42.0	114.4	158.2	0.65	0.34	0.3				

Table S7. Test dataset of for y_3'' (lateral-size distribution).²⁷

No.	x1	x3	x4	x5	x6	x7	x8	x9	x10	x11	x12	x13	x14	x15	x16	x17	x18	x19	x20	x21	x22	x23	x24	x26	x27	x30	x31	x32	x33	x34	x35	x36	x37	x38	x39	x40	x41	y3	
y3_test_1	60.1	-89.5	82.4	0.786	20.2	44.0	2.04	1.38	22.9	18.9	71.2	71.1	1.93	6.46E-40	15.5	7.2	12.8	105.1	1.01E-39	3.20	31.1	94.9	105.4	1.01	0.08	17.6	10.6	20.9	-3.62E-40	3.62E-40	-1.27	1.27	6.2	-12.2	12.2	9.7	1.5	0.033	
y3_test_2	74.1	114.7	98.5	0.803	17.3	0.2	4.20	1.40	24.5	23.7	78.6	89.9	1.85	8.25E-40	15.7	5.8	12.3	105.1	1.01E-39	3.20	31.1	94.9	105.4	1.01	0.08	17.6	10.6	20.9	-1.83E-40	1.83E-40	-1.34	1.34	5.9	-7.4	7.4	10.6	1.5	0.044	
y3_test_3	46.1	-114.5	78.3	0.785	24.6	59.0	1.08	1.36	24.0	13.4	64.4	52.8	1.94	4.56E-40	15.8	8.8	19.4	105.1	1.01E-39	3.20	31.1	94.9	105.4	1.01	0.08	17.6	10.6	20.9	-5.52E-40	5.52E-40	-1.25	1.25	6.2	-17.7	17.7	4.3	1.5	0.027	
y3_test_4	32.0	-97.7	64.6	0.786	32.7	127.0	0.55	1.33	24.0	8.8	56.8	34.0	2.11	2.65E-40	15.1	12.3	22.3	105.1	1.01E-39	3.20	31.1	94.9	105.4	1.01	0.08	17.6	10.6	20.9	-7.43E-40	7.43E-40	-1.09	1.09	6.7	-22.3	22.3	5.5	1.5	0.071	
y3_test_5	60.1	-126.5	97.2	0.804	20.8	19.0	1.95	1.39	25.3	18.3	72.2	71.6	1.84	6.40E-40	15.7	6.8	17.4	105.1	1.01E-39	3.20	31.1	94.9	105.4	1.01	0.08	17.6	10.6	20.9	-3.68E-40	3.68E-40	-1.35	1.35	5.9	-12.9	12.9	6.4	1.5	0.05	
y3_test_6	18.0	0.0	100.0	0.997	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	108.1	1.13E-39	8.06	29.3	89.0	57.1	0.93	0.00	19.4	20.5	14.5	-1.04E-39	1.04E-39	-5.63	5.63	19.6	-23.3	23.3	29.2	1.5	0.36	
y3_test_7	18.0	0.0	100.0	0.997	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	125.2	1.34E-39	5.14	33.0	96.2	114.8	1.10	0.16	18.3	8.5	8.3	-1.25E-39	1.25E-39	-2.72	2.72	12.5	-27.0	27.0	35.3	1.5	0.281	
y3_test_8	18.0	0.0	100.0	0.997	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	125.2	1.28E-39	3.61	30.6	88.1	91.5	1.78	0.85	18.7	6.2	7.3	-1.19E-39	1.19E-39	-1.18	1.18	8.8	-24.6	24.6	36.9	1.5	0.281	
y3_test_9	18.0	0.0	100.0	0.997	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	131.2	1.54E-39	2.18	42.0	111.4	158.2	1.94	1.01	16.1	5.1	7	-1.45E-39	1.45E-39	0.25	0.25	5.3	-36.0	36.0	37.0	1.5	0.342	
y3_test_10	18.0	0.0	100.0	0.997	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	70.1	6.96E-40	4.52	20.0	76.6	61.3	0.93	0.00	17.2	14	12.2	-6.09E-40	6.09E-40	-2.09	2.09	11.0	-14.0	14.0	30.4	1.5	0.282	
y3_test_11	45.0	2.6	210.0	1.135	111.0	0.1	2.93	1.45	58.2	10.1	60.2	31.1	4.24	3.43E-40	17.3	18.7	19.3	108.1	1.13E-39	8.06	29.3	89.0	57.1	0.93	0.00	19.4	20.5	14.5	-7.87E-40	7.87E-40	-3.83	3.83	34.2	-19.2	19.2	6.6	1.5	0.271	
y3_test_12	60.1	-89.5	82.4	0.786	20.2	44.0	2.04	1.38	22.9	18.9	71.2	71.1	1.93	6.46E-40	15.5	7.2	12.8	137.2	1.59E-39	1.33	36.8	96.6	118.1	1.75	1.03	19	6.5	8	-9.39E-40	9.39E-40	0.59	0.59	2.6	-17.9	17.9	8.5	3.66	0.107	
y3_test_13	74.1	114.7	98.5	0.803	17.3	0.2	4.20	1.40	24.5	23.7	78.6	89.9	1.85	8.25E-40	15.7	5.8	12.3	137.2	1.59E-39	1.33	36.8	96.6	118.1	1.75	1.03	19	6.5	8	-7.60E-40	7.60E-40	0.52	0.52	2.5	-13.1	13.1	7.9	3.66	0.046	
y3_test_14	74.1	114.7	98.5	0.803	17.3	0.2	4.20	1.40	24.5	23.7	78.6	89.9	1.85	8.25E-40	15.7	5.8	12.3	101.2	1.26E-39	1.24	33.7	96.0	136.0	1.80	1.09	16	3.9	7.5	-4.39E-40	4.39E-40	0.61	0.61	2.3	-10.0	10.0	5.2	3.66	0.06	
y3_test_15	46.1	-114.5	78.3	0.785	24.6	59.0	1.08	1.36	24.0	13.4	64.4	52.8	1.94	4.56E-40	15.8	8.8	19.4	137.2	1.59E-39	1.33	36.8	96.6	118.1	1.75	1.03	19	6.5	8	-1.13E-39	1.13E-39	0.61	0.61	2.6	-23.4	23.4	13.3	3.66	0.111	
y3_test_16	18.0	0.0	100.0	0.997	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	168.6	1.57E-39	6.36	33.5	92.9	96.5	1.42	0.71	19.6	10.2	6.7	-1.25E-39	1.25E-39	-3.93	3.93	15.4	-27.4	27.4	37.0	3.66	0.746	
y3_test_17	18.0	0.0	100.0	0.997	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	125.2	1.34E-39	5.14	33.0	96.2	114.8	0.82	0.11	18.3	8.5	8.3	-1.25E-39	1.25E-39	-2.72	2.72	12.5	-27.0	27.0	35.3	3.66	0.37	
y3_test_18	45.0	2.6	210.0	1.135	111.0	0.1	2.93	1.45	58.2	10.1	60.2	31.1	4.24	3.43E-40	17.3	18.7	19.3	168.6	1.57E-39	6.36	33.5	92.9	96.5	1.42	0.71	19.6	10.2	6.7	-1.23E-39	1.23E-39	-2.12	2.12	26.9	-23.4	23.4	15.9	3.66	0.284	
y3_test_19	18.0	0.0	100.0	0.997	78.5	23.8	0.89	1.33	72.6	6.0	46.5	14.7	2.43	8.64E-41	15.5	16	42.3	122.2	1.41E-39	2.48	31.5	92.0	107.5	0.72	0.01	18.8	7.3	8.8	-1.32E-39	1.32E-39	-0.05	0.05	6.0	-25.5	25.5	35.2	3.66	0.283	
y3_test_20	45.0	2.6	210.0	1.135	111.0	0.1	2.93	1.45	58.2	10.1	60.2	31.1	4.24	3.43E-40	17.3	18.7	19.3	125.2	1.34E-39	5.14	33.0	96.2	114.8	0.82	0.11	18.3	8.5	8.3	-9.92E-40	9.92E-40	-0.91	0.91	21.8	-22.9	22.9	15.1	3.66	0.683	
y3_test_21	60.1	-89.5	82.4	0.786	20.2	44.0	2.04	1.38	22.9	18.9	71.2	71.1	1.93	6.46E-40	15.5	7.2	12.8	105.1	1.01E-39	3.20	31.1	94.9	105.4	2.03	0.23	1.21	17.6	10.6	20.9	-3.62E-40	3.62E-40	-1.27	1.27	6.2	-12.2	12.2	9.7	5.79	0.099
y3_test_22	74.1	114.7	98.5	0.803	17.3	0.2	4.20	1.40	24.5	23.7	78.6	89.9	1.85	8.25E-40	15.7	5.8	12.3	105.1	1.01E-39	3.20	31.1	94.9	105.4	2.03	0.23	1.21	17.6	10.6	20.9	-1.83E-40	1.83E-40	-1.34	1.34	5.9	-7.4	7.4	10.6	5.79	0.057
y3_test_23	46.1	-114.5	78.3	0.785	24.6	59.0	1.08	1.36	24.0	13.4	64.4	52.8	1.94	4.56E-40	15.8	8.8	19.4	105.1	1.01E-39	3.20	31.1	94.9	105.4	2.03	0.23	1.21	17.6	10.6	20.9	-5.52E-40	5.52E-40	-1.25	1.25	6.2	-17.7	17.7	4.3	5.79	0.118
y3_test_24	32.0	-97.7	64.6	0.786	32.7	127.0	0.55	1.33	24.0	8.8	56.8	34.0	2.11	2.65E-40	15.1	12.3	22.3	105.1	1.01E-39	3.20	31.1	94.9	105.4	2.03	0.23	1.21	17.6	10.6	20.9	-7.43E-40	7.43E-40	-1.09	1.09	6.7	-22.3	22.3	5.5	5.79	0.247
y3_test_25	60.1	-126.5	97.2	0.804	20.8	19.0	1.95	1.39	25.3	18.3	72.2	71.6	1.84	6.40E-40	15.7	6.8	17.4	105.1	1.01E-39	3.20	31.1	94.9	105.4	2.03	0.23	1.21	17.6	10.6	20.9	-3.68E-40	3.68E-40	-1.35	1.35	5.9	-12.9	12.9	6.4	5.79	0.113
y3_test_26	74.1	114.7	98.5	0.803	17.3	0.2	4.20	1.40	24.5	23.7	78.6	89.9	1.85	8.25E-40	15.7	5.8	12.3	105.1	1.01E-39	3.20	31.1	94.9	105.4	2.03	0.23	1.21	17.6	10.6	20.9	-1.83E-40	1.83E-40	-1.34	1.34	5.9	-7.4	7.4	10.6	5.79	0.075
y3_test_27	90.1	-70.0	135.1	0.930	29.6	0.1	1.84	1.41	28.2	26.6	87.6	93.7	0.47	8.98E-40	16.2	8.1	13.9	105.1	1.01E-39	3.20	31.1	94.9	105.4	2.03	0.23	1.21	17.6	10.6	20.9	-1.10E-40	1.10E-40	-2.73	2.73	1.5	-4.5	4.5	7.9	5.79	0.162
y3_test_28	76.1	-85.1	124.5	0.965	16.9	8.3	1.71	1.40	33.3	21.8	79.8	75.0	0.34	7.01E-40	16.4	9.2	15.8	105.1	1.01E-39	3.20	31.1	94.9	105.4	2.03	0.23	1.21	17.6	10.6	20.9										