

Supplementary information

Microscale hydrodynamic confinements: shaping liquids across length scales as a toolbox in life sciences

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Most critical sections of the numerical MATLAB tool

The startup function, which is automatically called when the app is opened, plots an exemplary flow field for two apertures with given location and strength. This piece of code illustrates the entire workflow, which is also employed for later, user-defined computations. Variables shared across functions are stored in the namespace “app”. The naming and calling of variables would look a little different if everything was implemented locally. For seeing this code, open the MATLAB App Designer, choose “open” and select the “.mlapp” version of our tool, then switch to “Code View”

% Code that executes after component creation

```
function startupFcn(app)
```

```
[X, Y] = meshgrid(0:app.xdim.Value/10,...
```

```
0:1:app.ydim.Value/10);
```

```
app.plane = complex(X,Y);
```

```
app.pos.Data = [(app.xdim.Value/2-75), (app.ydim.Value/2), 1; ...
```

```
(app.xdim.Value/2+75), (app.ydim.Value/2), -3];
```

```
app.strx.Value = app.pos.Data(1,1);
```

```
app.stry.Value = app.pos.Data(1,2);
```

```
if app.first == 0
```

```
app.omega = app.potflow(1)+app.potflow(2);
```

```
Phi = real(app.omega);
```

```
Phi(~isfinite(Phi)) = 0;
```

```
contour(app.graph, Phi, 50)
```

```
app.first = 1;
```

make two 2D matrices for x and y coordinates of each point (scaling of 1/10)

combine these matrices in one complex 2D matrix

define location and strength of 2 sources

only use the velocity potential (real part)

call function “potflow” to calculate complex potential of each source and superimpose the potentials.

.. seeding for streamlines

```
[seedx, seedy] = meshgrid(app.strx.Value/10-app.strsz.Value/20  
:0.5:app.strx.Value/10+app.strsz.Value/20,...  
    app.stry.Value/10-app.strsz.Value/20 ...  
:0.5:app.stry.Value/10+app.strsz.Value/20);  
[U, V] = gradient(Phi);  
streamline(app.graph, U, V, seedx, seedy)
```

compute the local derivative for finding the flow velocity/discharge (this corresponds to the two final equations in tutorial box 2)

end

```
xlim(app.graph, [0, app.xdim.Value/10]);  
ylim(app.graph, [0, app.ydim.Value/10]);  
app.graph.XTick = linspace(0, app.xdim.Value/10, 11);  
app.graph.YTick = linspace(0, app.ydim.Value/10, 11);  
app.graph.XTickLabel = linspace(0, app.xdim.Value, 11);  
app.graph.YTickLabel = linspace(0, app.ydim.Value, 11);  
axis(app.graph, 'manual')  
disableDefaultInteractivity(app.graph)  
app.checkphi.Value = 1;  
app.checkstream.Value = 1;
```

The rest is cosmetics on the plotting.

end

```
function field = potflow(app, n)  
    source = app.pos.Data(n,:);  
    field = (1E6*source(3)/60)/(2*pi)*...  
        log(app.plane-complex(source(1)/10, source(2)/10)); % One unit  
    % in the plot = 0.01 mm, "discharge" is computed in [0.01 mm2/sec]
```

end

Computation of complex potential for each source, Q_m is converted from $\mu\text{L}/\text{min}$ to SI units, scaling of 1/10 as above.