Supplementary Information

MC$_2$ (M = Y, Zr, Nb, and Mo) Monolayers Containing C$_2$ Dimers:

Prediction of Anode Materials for High-performance Sodium Ion Batteries

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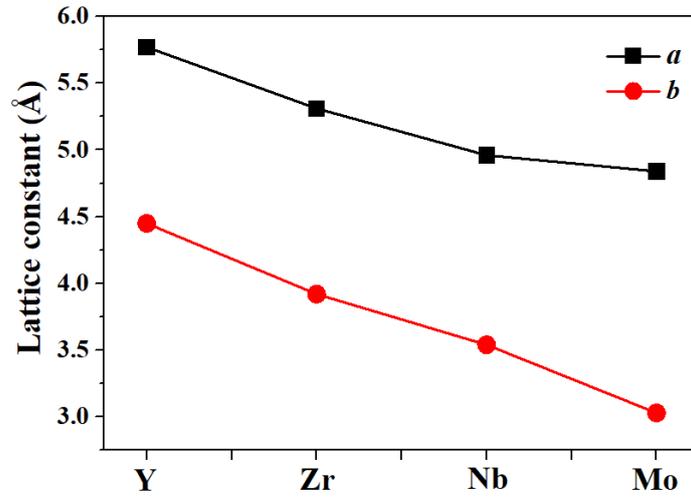
Fig. S1 Lattice constants (a, b) of the MC_2 (M = Y, Zr, Nb and Mo) monolayers.
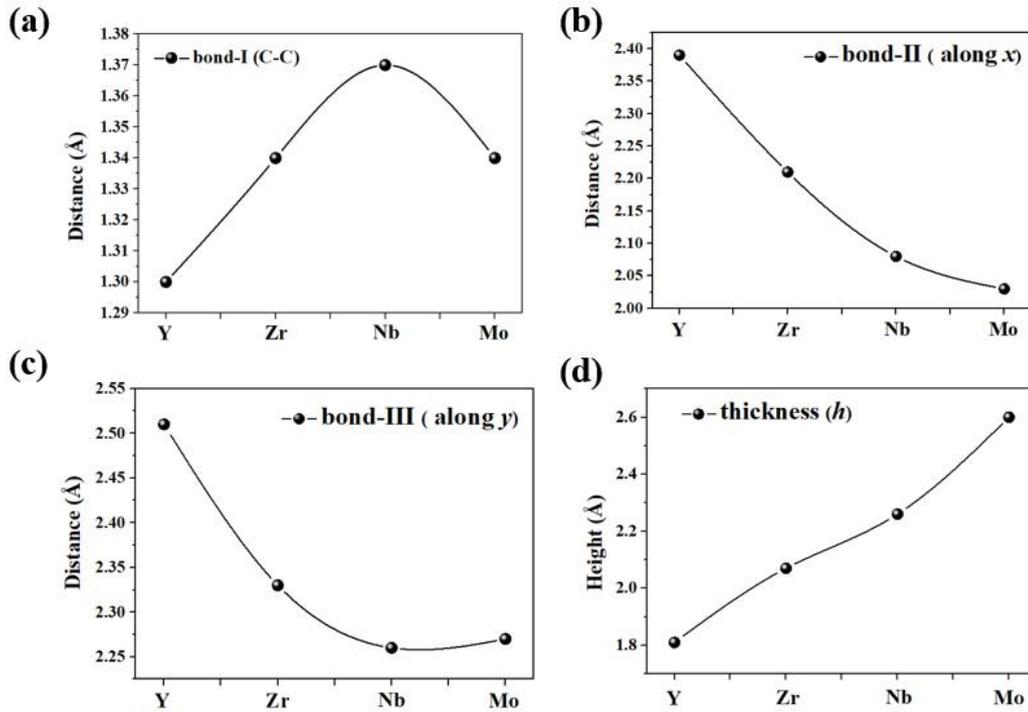
Fig. S2 Bonds length of C−C (a), M−C in the (b) (c) and thickness (d) for the MC_2 (M = Y, Zr, Nb and Mo) monolayers.
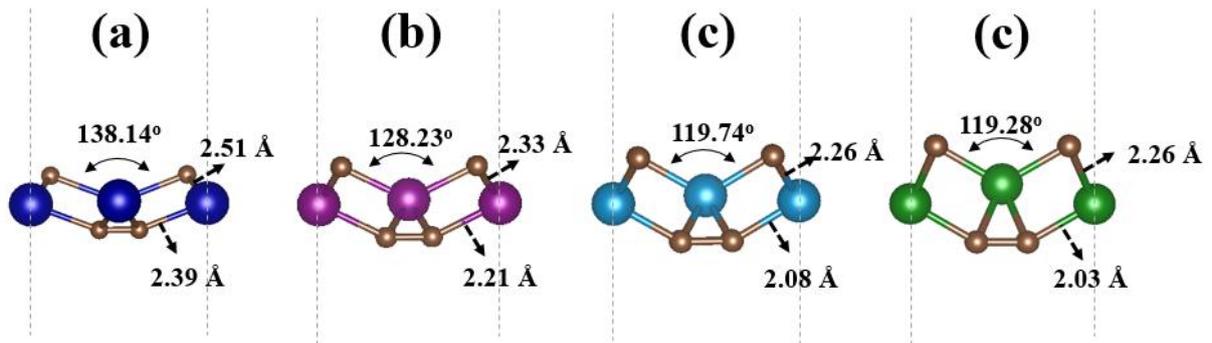
Fig. S3 Bonds length of M−C along the x (y)-direction and bond angel ($\angle$C-M-C) for the MC$_2$ (a) YC$_2$; (b) ZrC$_2$; (c) NbC$_2$ and (d) MoC$_2$ monolayers.
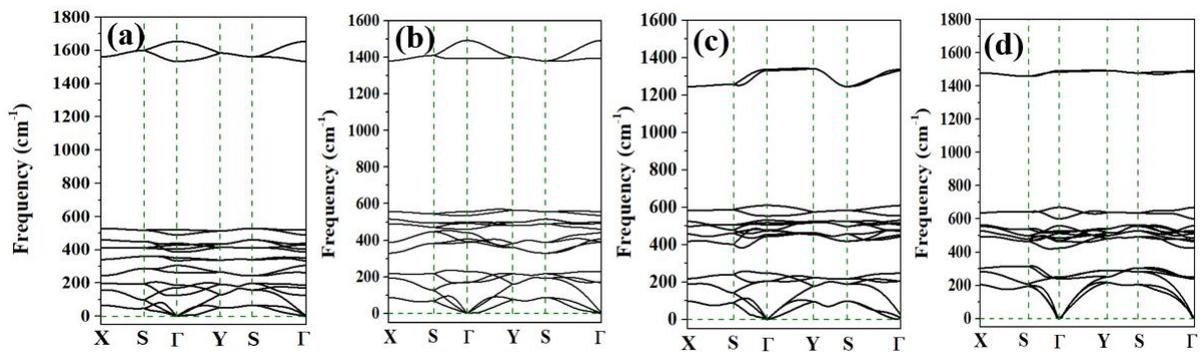
Fig. S4 The calculated phonon spectra of the YC$_2$ (a), ZrC$_2$ (b), NbC$_2$ (c), and MoC$_2$ (d) monolayers.
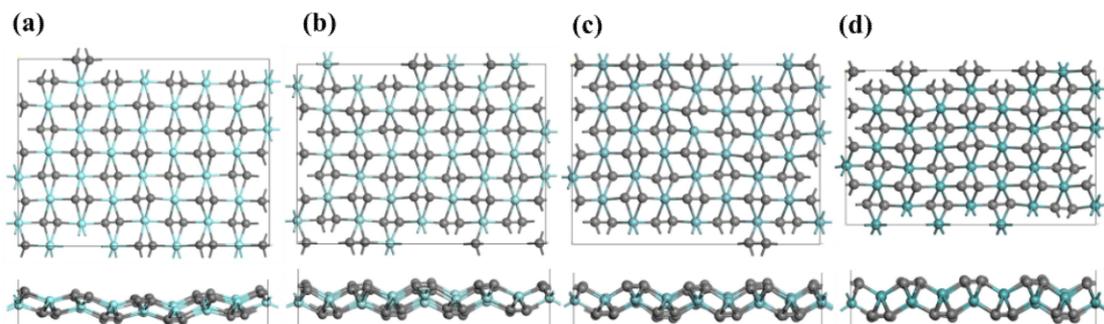
Fig. S5 The snapshots of the YC$_2$ (a), ZrC$_2$ (b), NbC$_2$ (c) and MoC$_2$ (d) monolayers at the end of 5 ps FPMD simulations at 300 K.
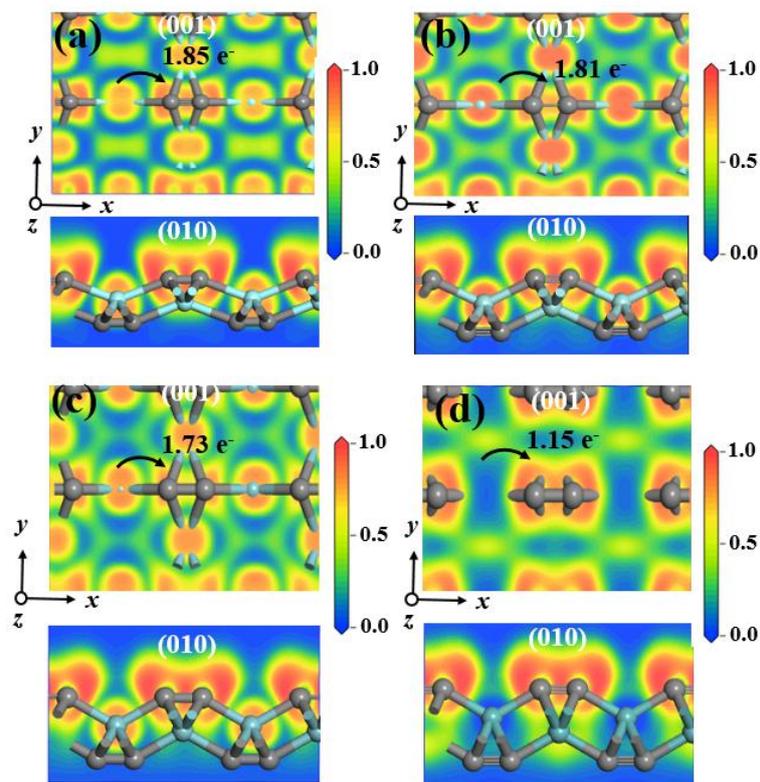
Fig. S6 The electronic localization function (ELF) of the YC$_2$ (a), ZrC$_2$ (b), NbC$_2$ (c) and MoC$_2$ (d) monolayers. In the ELF maps, the red and blue colors refer to the highest value (1.00) and the lowest value (0.00) of ELF, respectively. Corresponding to the accumulation and depletion of electrons in the two colored regions.
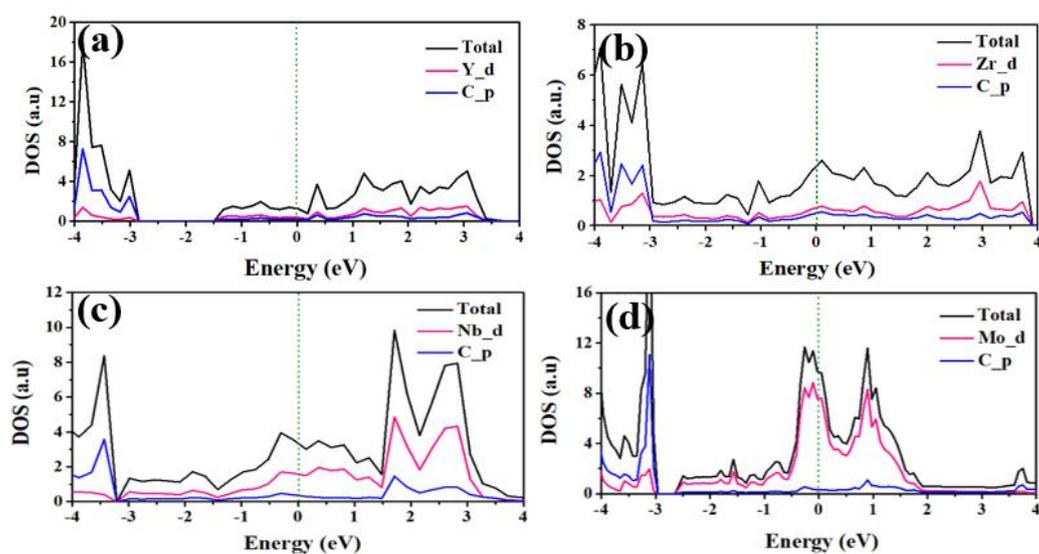
Fig. S7 The partial density of states of the YC$_2$ (a), ZrC$_2$ (b), NbC$_2$ (c), and MoC$_2$ (d) monolayers. The Fermi energy is set to 0 eV as indicated by the vertical dashed line.
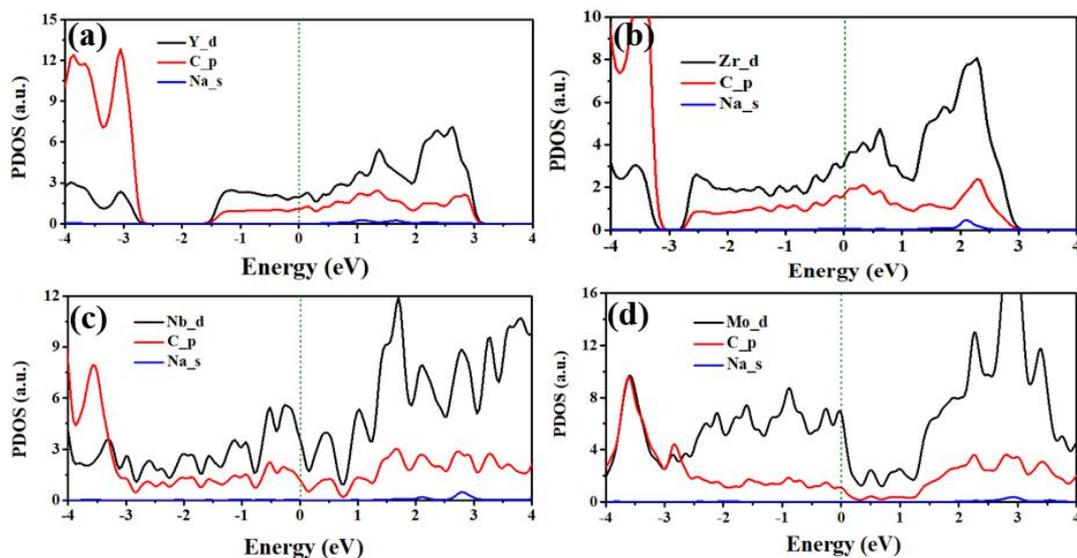
Fig. S8 The partial density of states of Na-adsorbed YC_2 (a), ZrC_2 (b), NbC_2 (c), and MoC_2 (d) monolayers. The Fermi energy is set to 0 eV as indicated by the vertical dashed line.
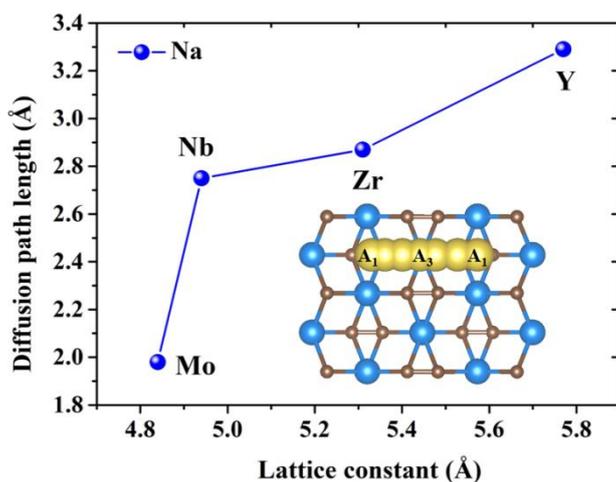
Fig. S9 The variation of Path-I diffusion lengths of Na on the MC_2 (M = Y, Zr, Nb, and Mo) monolayers with the lattice constants of MC_2.
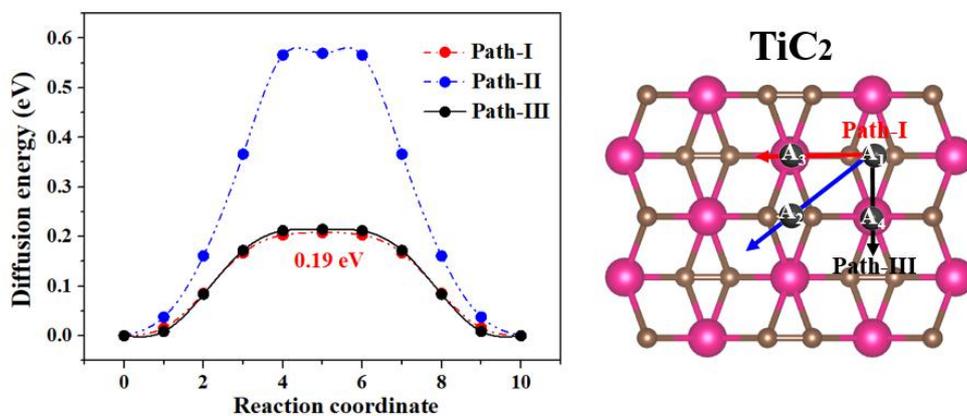
Fig. S10 The energy profile (left) and diffusion pathways (right) of Na diffusing on the TiC_2 monolayer.
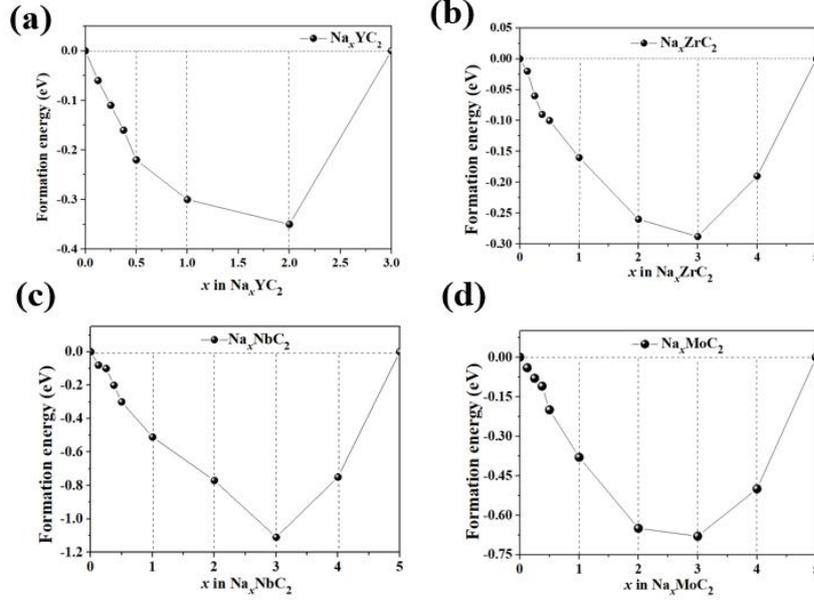
Fig. S11 The formation energy (E_f) of Na$_x$YC$_2$ (a), Na$_x$ZrC$_2$ (b), Na$_x$NbC$_2$ (c), and Na$_x$MoC$_2$ (d) with respect to MC$_2$ monolayer and Na bulk *bcc* metal. Data points located on the convex hull represents the stable adsorption without decomposition.

Here, the most stable adsorptions configuration of different Na adsorption concentrations (x) on the MC$_2$ monolayer, we calculated the based on the following equation:[S1]

$$E_f(x) = (E_{NaxMC2} \square E_{MC2} \square xE_{Na\text{-}bulk})/(x+1) \qquad (1)$$

where E_{MC2}, E_{NaxMC2}, and $E_{Na\text{-}bulk}$ are the energy of MC$_2$ monolayer, the total energy of Na-adsorbed MC$_2$, and the energy per atom in the bulk Na, respectively. We plotted the convex energy hull, the cure of formation energies of all configurations considered *vs.* the concentrations of Na (x) in the intercalated MC$_2$ systems. Located on the hull with negative formation energies, and thus thermodynamically stable, these data further confirm the stability of Na$_2$YC$_2$, Na$_3$ZrC$_2$, Na$_3$NbC$_2$, and Na$_3$MoC$_2$.

-1.19 eV   **-1.26 eV**   **-1.32 eV**   **-1.35 eV**
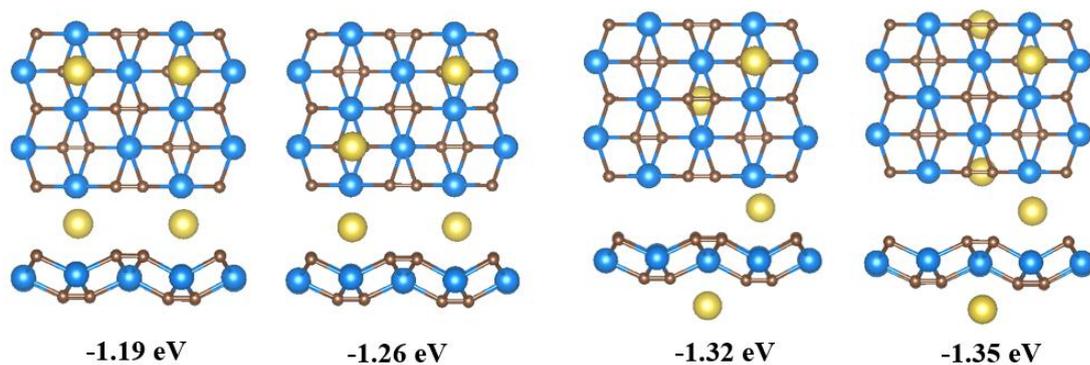
Fig. S12 The optimized configurations and the corresponding average adsorption energies of Na for $Na_{0.25}NbC_2$.

-1.12 eV   **-1.18 eV**   **-1.16 eV**   **-1.13 eV**
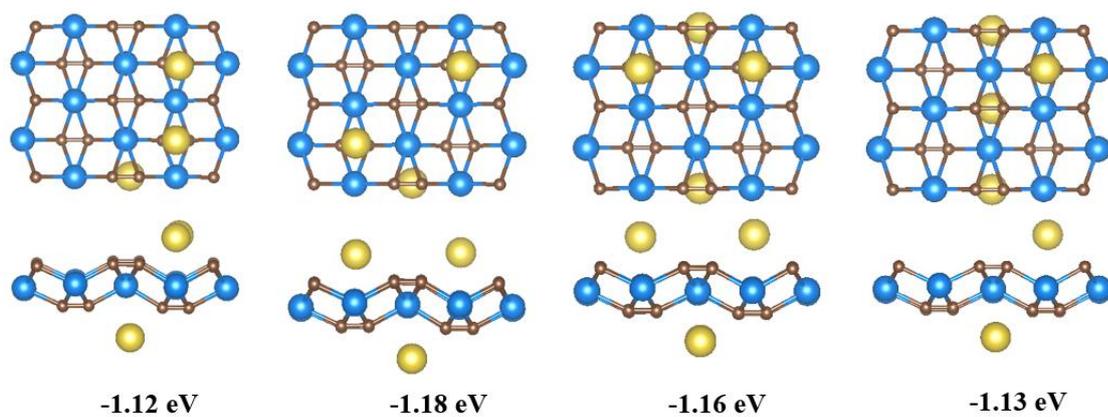
Fig. S13 The optimized configurations and the corresponding average adsorption energies of Na for $Na_{0.375}NbC_2$.

-1.09 eV   **-1.05 eV**   **-1.02 eV**   **-1.11 eV**
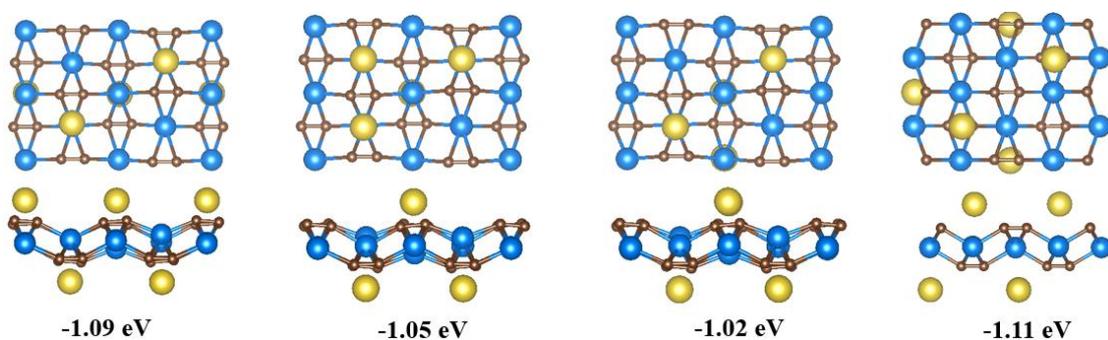
Fig. S14 The optimized configurations and the corresponding average adsorption energies of Na for $Na_{0.5}NbC_2$.
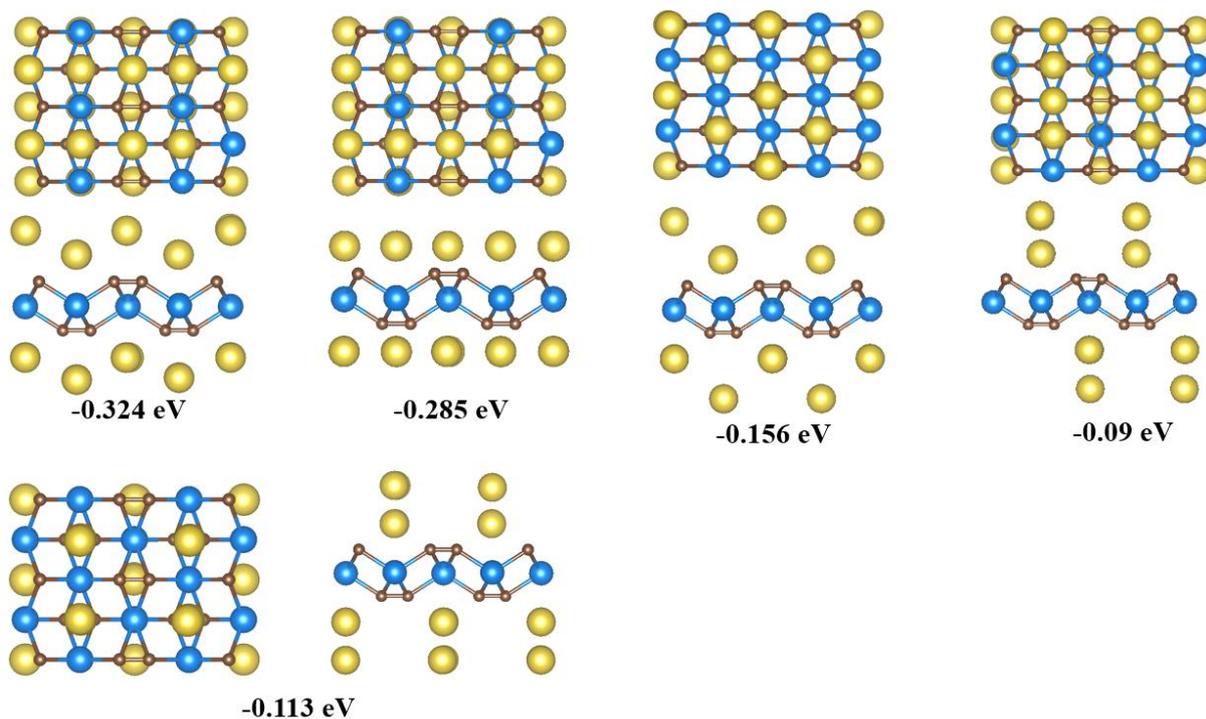
Fig. S15 The optimized configurations and the average adsorption energies of Na for Na$_2$NbC$_2$: the additional 8 Na all adsorb at the A$_3$ sites more far to the surface (E_{ave} = -0.324 eV), the additional 8 Na all adsorb at the A$_3$ sites with the same height to the surface of the preadsorbed Na at A$_1$ sites (E_{ave} = -0.285 eV), the additional 8 Na all adsorb at the A$_3$ sites more far to the surface (E_{ave} = -0.324 eV), the additional 8 Na all adsorb at the A$_1$ sites more far to the surface (E_{ave} = -0.156 eV), the additional 8 Na all adsorb at the A$_4$ sites more far to the surface (E_{ave} = -0.009 eV), the additional 8 Na all adsorb at the A$_2$ sites more far to the surface (E_{ave} = -0.113 eV).
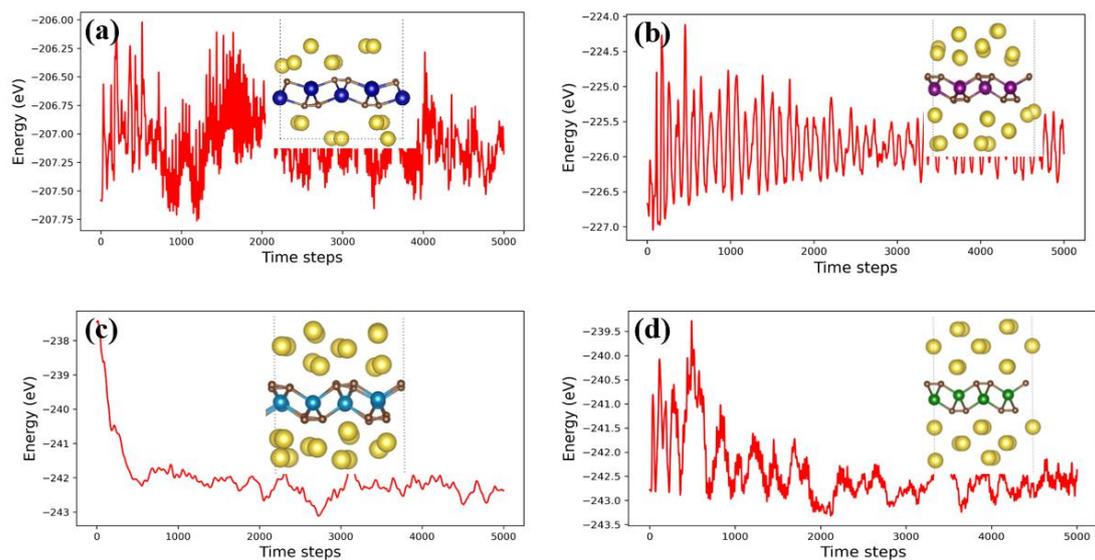
Fig. S16 The end structures (side view) of the Na-intercalated MC_2 (M = Y, Zr, Nb, and Mo) monolayers through a 5 ps FPMD simulation at 300 K.
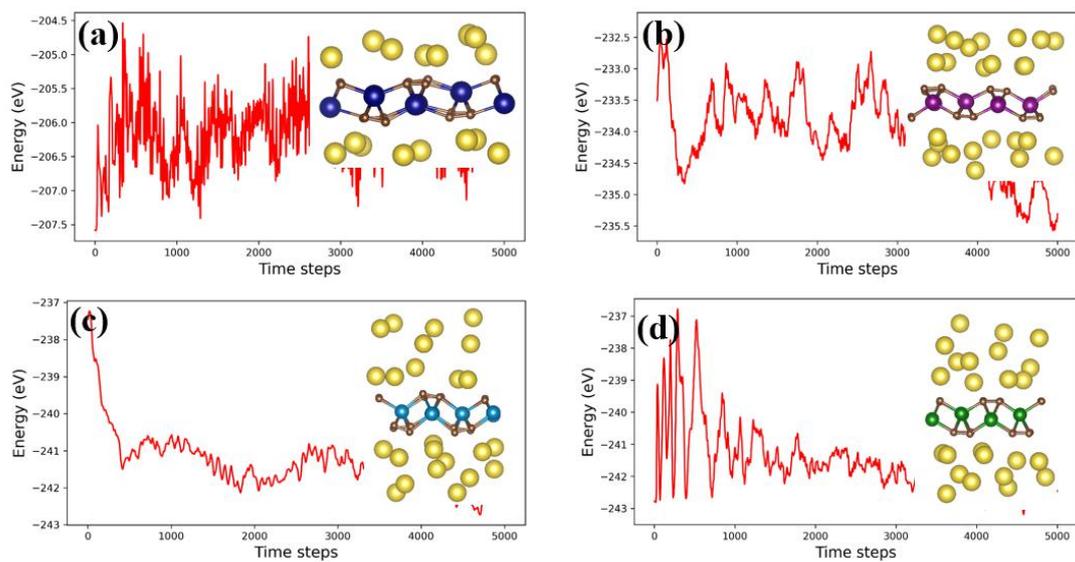
Fig. S17 The end structures (side view) of the Na-intercalated MC_2 (M = Y, Zr, Nb, and Mo) monolayers through a 5 ps FPMD simulation at 500 K.

Table S1. The calculated lattice constant (a, b, Å), lattice and volume change of MC_2 (M = Y, Zr, Nb, and Mo) nanosheets without and with adsorbed Na atoms.

	a (Å)	b (Å)	Lattice variation (%)		Volume variation (%)
YC_2	11.60	8.56			
Na_2YC_2	11.84	8.10	2.1	-5.3	9.8
ZrC_2	10.67	7.78			
Na_3ZrC_2	10.73	7.19	0.5	-7.5	0.8
NbC_2	9.95	7.10			
Na_3NbC_2	9.77	6.70	-1.8	-5.6	6.9
MoC_2	9.68	6.02			
Na_3MoC_2	9.56	6.18	-1.2	2.6	6.05

[S1] (a) T. Bo, P. F. Liu, J. Xu, J. R. Zhong, Y. B. Chen, O. Eriksson, F. W. Wang and B. T. Wang, *Phys. Chem. Chem. Phys*., 2018, **20**, 22168–22178; (b) T. Bo, P. F. Liu, J. Xu, J. R. Zhong, F. W. Wang and B. T. Wang, *Phys. Chem. Chem. Phys*., 2019, **21**, 5178–5188.